



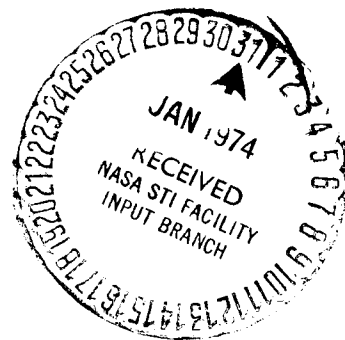
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# DESCRIPTION OF APOLLO GUIDANCE ANALYSIS STATISTICAL TRIALS PROGRAM



Orbital Mission Analysis Branch

## MISSION PLANNING AND ANALYSIS DIVISION

MANNED SPACECRAFT CENTER  
HOUSTON, TEXAS

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STATISTICAL TRIALS PROGRAM

By Elric N. McHenry, Dennis M. Braley,  
Ernest M. Fridge, and Robert N. Hinson  
Orbital Mission Analysis Branch

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NATIONAL AERONAUTICS AND SPACE ADMINISTRATION  
MANNED SPACECRAFT CENTER  
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## DESCRIPTION OF APOLLO GUIDANCE ANALYSIS

### STATISTICAL TRIALS PROGRAM

By Elric N. McHenry, Dennis M. Braley,  
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#### 1.0 SUMMARY

The purpose of this report is to describe the techniques, capabilities, and formulations of the Apollo Guidance Analysis Statistical Trials Program. The Apollo Guidance Analysis Statistical Trials Program (AGAST) is an error analysis computer program designed to aid studies of Apollo rendezvous mission plans. The AGAST simulates targeting, guidance, and navigation computations specified for the Apollo rendezvous missions. Error analyses may be performed by AGAST for both lunar and earth missions. The error analysis technique used is that of statistical trials, that is, the Monte Carlo method (ref. 1).

#### 2.0 INTRODUCTION

A collection of FORTRAN language simulations of routines in the lunar module (LM) and command/service module (CSM) onboard computers form the core of the program. Modeled are the onboard guidance and navigation systems of the command module computer (CMC), the LM primary guidance and navigation control system (PGNCS), and the LM abort guidance system (AGS) as documented in references 2, 3, and 4, respectively. The maneuver targeting and guidance equations for LM descent to the lunar surface, LM ascent into lunar orbit, and the concentric sequence rendezvous are programmed into AGAST. Other onboard routines coded into AGAST are the state vector integrators and the navigation equations. The program has the capability to simulate both AGS and PGNCS computations and maneuver control. Also modeled are some of the Real-Time Computer Complex (RTCC) rendezvous maneuver targeting computations and Manned Space Flight Network (MSFN) state vector updates. To perform an error analysis of a mission profile, the program may model any or all of the four computers: CMC, PGNCS, AGS, and RTCC.

The program simulates a mission by performance of maneuver computations (targeting and guidance) and integration of the state vectors

between maneuvers. The update of the state vector estimates by either onboard sensors or ground based tracking (MSFN) is also simulated. The mission plan profile is defined by input packages to the program. Each individual input package is called an event package and defines a specific set of computations to be performed. Program computations are actuated by the reading of the event packages on computer cards (ref. 5). The program user may have the program simulate events of the following kinds.

- a. Maneuver events
- b. Vehicle-to-vehicle transferral of maneuver information
- c. Platform alinement
- d. AGS-to-PGNCS alinement
- e. Vehicle-to-vehicle update of state vector estimates
- f. MSFN update of state vector estimates
- g. Update of onboard state vector estimates with onboard sensors (rendezvous radar, etc.)

There are few program restrictions on the order or number of events which define the mission profile; the program is very flexible and requires little or no modification for the different Apollo missions.

Although AGAST has been developed to be used primarily to perform the integrating Monte Carlo trajectory error analysis, it need not necessarily be used for that purpose; it may be used to perform deterministic (error free) studies of a variety of mission plans. It may also be used to perform studies of the effects of particular error sources; for instance, the program user may specify certain engine performance discrepancies and may obtain the deterministic effects of those discrepancies on the mission.

Documentation may be found in the references mentioned in appendix A for all subroutines which are used in AGAST but not represented by a flow chart in appendix B. Symbols used in appendices A and B are defined in appendix C. The authors wish to express their appreciation for the help rendered by the ITT-FEC engineering aides in the preparation of the figures and flow charts in this document.

## 3.0 DEFINITIONS

## 3.1 Abbreviations

AGAST	Apollo Guidance Analysis Statistical Trials program
AGS	abort guidance system
APS	ascent propulsion system
BR	basic reference coordinate system
CMC	command module computer
CSM	command/service module
DPS	descent propulsion system
IMU	inertial measurement unit
LGC	lunar module guidance computer
LM	lunar module
LOS	line-of-sight coordinate system
LS	landing site
LV	local vertical coordinate system
MSFN	Manned Space Flight Network
NA	nominal alinement
PA	preferred alinement
PGNCS	primary guidance and navigation control system
RCS	reaction control system
REFSMMAT	rotation matrix which defines the IMU orientation in basic reference coordinates
RR	rendezvous radar
RTCC	Real-Time Computer Complex

SCT	scanning telescope
SXT	sextant
VHF	relative range measuring device on the CSM

### 3.2 Algebraic Symbol Definition

[A]	rotation matrix maintained by the AGS which relates the AGS strapped down platform to the AGS reference frame
[B]	rotation matrix that represents the bias misalignment of the accelerometers with respect to the platform
[I]	the n by n identity matrix
$R_A$	actual relative range between two vehicles
$R_M$	measured relative range between two vehicles
$\dot{R}_A$	actual relative range rate between two vehicles
$\dot{R}_M$	measured relative range rate between two vehicles
[P(t)]	IMU platform orientation error matrix; rotates from ideal IMU orientation to the true orientation of the IMU
[P <sub>T</sub> ]	value of [P(t)] at the time of an AGS-to-PGNCS alinement
[S]	diagonal matrix with the accelerometer scale factors of each accelerometer axis on the diagonal
[T]	REFSMMAT; rotation matrix from basic reference coordinates to the ideal orientation of the platform
t	current time
$\bar{u}_T$	unit vector along the thrust direction
$\bar{u}_{TA}$	unit vector of the actual thrust direction
$\bar{u}_{TD}$	unit vector of the desired thrust direction

$\bar{V}_G$	velocity-to-be-gained for burn
$X$	six-dimensional state vector of a vehicle's position and velocity in BR coordinates
$X_A$	actual (environmental) state vector
$X_E$	estimated (onboard or MSFN) state vector
$X_E^*$	value of the onboard state being updated which results in no estimated relative state errors in a local sense
$X_R$	reference (nominal) state vector
$\bar{x}$	n-dimensional vector subject to random Gaussian dispersions
$\{\bar{x}_i\}_{i=1}^N$	array of N random samples of the random vector $\bar{x}$
$\beta_A$	actual RR or SXT shaft angle
$\beta_M$	measured RR or SXT shaft angle
$\Delta\bar{V}_A$	actual incremental velocity change added during a guidance cycle
$\Delta\bar{V}_B$	accelerometer $\Delta\bar{V}$ read bias
$\Delta\bar{V}_{co}$	burn error due to pilot cutoff error
$\Delta\bar{V}_E$	measured $\Delta\bar{V}$ rotated into BR coordinates
$\Delta\bar{V}_M$	accelerometer measured $\Delta\bar{V}$ in platform coordinates
$\Delta\bar{V}_P$	burn error due to initial thrust vector misalignment
$\Delta X$	six-dimensional relative state vector between two vehicles; for instance, the nominal relative state vector is:

$$\Delta X_R = X_{R,I} - X_{R,J}$$

where the relative position vector is directed from vehicle J to vehicle I

$\Delta X_A$	actual relative state vector
$\Delta X_E$	estimated relative state vector
$\Delta X_E^*$	estimated relative state which the onboard tracking must produce to have no errors in a local vertical sense
$\delta R$	measurement bias in $R_M$
$\dot{\delta R}$	measurement bias in $\dot{R}_M$
$\delta X_A$	difference between $X_A$ and $X_R$
$\delta X_E$	difference between $X_E$ and $X_A$
$\delta X_{REL}$	error in the estimated relative state vector
$\bar{\delta x}$	n-dimensional random dispersion of $\bar{x}$ whose components have zero mean; i.e., $\bar{x} = \bar{\mu} + \bar{\delta x}$
$\delta \beta$	measurement bias in $\beta_M$
$\delta \theta$	measurement bias in $\theta_M$
$\bar{\eta}$	n-dimensional random vector whose components individually have zero mean and unity variance; i.e., a normalized random vector
$\theta_A$	actual RR or SXT trunnion angle
$\theta_M$	measured RR or SXT trunnion angle
$\bar{\mu}$	mean of the random vector $\bar{x}$
$\Sigma$	n x n covariance matrix of an n-dimensional random vector
$\Sigma_A$	covariance matrix of an actual state vector $X_A$
$\Sigma_{REL}$	covariance matrix of an estimated relative state vector (from onboard tracking)

$\Sigma_T$	MSFN tracking covariance matrix
$\Sigma_{\delta \bar{x}}$	$n \times n$ covariance matrix of $\delta \bar{x}$
$\Sigma_{\bar{\eta}}$	$n \times n$ covariance matrix of $\bar{\eta}$
$\sigma$	standard deviation of a random variable with normal distribution
$\sigma_{ij}$	element of the $i$ th row and $j$ th column of $\Sigma$
$\sigma_{N_R}$	standard deviation for the noise on the range measurement
$\sigma_{N_R^{\cdot}}$	standard deviation for the noise on the range rate measurement
$\sigma_{N_{\beta}}$	standard deviation for the noise on the shaft angle measurement
$\sigma_{N_{\theta}}$	standard deviation for the noise on the trunnion angle measurement
$\bar{\omega}_A$	actually turning rate vector for the thrust direction
$\bar{\omega}_D$	desired turning rate vector for the thrust direction

## 4.0 COORDINATE SYSTEMS

The coordinate system in which AGAST does most of its computations is called the basic reference frame. The AGAST basic reference frame corresponds to that of the CMC and the LM PGNCs. For earth missions, the reference coordinate system is the Besselian inertial frame; for moon reference, it is the selenocentric coordinate system. The AGS computer actually uses as its basic reference computing frame the definition of the PGNCs platform orientation at AGS-to-PGNCs alinement; but in AGAST, the AGS basic reference system is the same as that of the PGNCs. The following sections define some of the other coordinate systems used in AGAST.

### 4.1 Apollo Local Vertical Frame

The Apollo local vertical frame is defined for a given vehicle at a given time. Where  $X_{LV}$ ,  $Y_{LV}$ , and  $Z_{LV}$  represent the axes of that coordinate system, the directions are defined as follows.

- $X_{LV}$  along the local horizontal in the direction of orbital motion
- $Y_{LV}$  along the negative of the angular momentum vector
- $Z_{LV}$  along the negative of the radius vector

### 4.2 The UVW Coordinate System

Another local vertical system used in AGAST is the UVW coordinate system. Where U, V, and W represent the axes of that coordinate system, the directions are defined as follows.

- U along the radius vector
- V along the local horizontal in the direction of orbital motion
- W along the angular momentum vector

### 4.3 Line-of-sight Coordinate System

The line-of-sight coordinate system is useful for some output purposes. A part of the onboard tracking simulation output is in that coordinate system. For the definition of the LOS system, the following notations are used: the indices  $i$  and  $j$  refer to either the LM or the CSM but not to both. Where  $X_{LOS}$ ,  $Y_{LOS}$ , and  $Z_{LOS}$  represent the axes of the LOS coordinate system, the directions are defined as follows.



- $X_{LOS}$  along the line of sight from the  $i$ th vehicle to the  $j$ th vehicle
- $Y_{LOS}$  along the vector defined by the cross product of the line-of-sight vector with the  $i$ th vehicle's radius vector
- $Z_{LOS}$  along the vector which forms a right-handed system with  $X_{LOS}$  and  $Y_{LOS}$

#### 4.4 Nominal Platform Alinement Coordinate System

The CMC and PGNCs platform orientations denoted nominal are local vertical frames. The CMC nominal alinement system is the same as the Apollo local vertical defined in section 4.1. The PGNCs nominal platform alinement has a different definition. Where  $X_{NA}$ ,  $Y_{NA}$ , and  $Z_{NA}$  represent the axes of the PGNCs nominal alinement coordinates, the directions are defined as follows.

- $X_{NA}$  along the positive radius vector
- $Y_{NA}$  along the negative angular momentum vector
- $Z_{NA}$  along the local horizontal in the direction of orbital motion

#### 4.5 Preferred Platform Alinement Coordinate System

The inertial platforms of the CSM and the LM are usually put into the preferred maneuver orientation before a maneuver is executed. Where  $X_{PA}$ ,  $Y_{PA}$ , and  $Z_{PA}$  represent the axes of the preferred platform coordinate system, the directions are defined as follows.

- $X_{PA}$  along the initial thrust direction
- $Y_{PA}$  along the vector formed by crossing the thrust vector into the radius vector
- $Z_{PA}$  along the vector which forms a right-handed system with  $X_{PA}$  and  $Y_{PA}$

#### 4.6 Landing Site Platform Alinement Coordinate System

During LM descent to the lunar surface and ascent into lunar orbit, the LM platform will be alined to the landing site alinement. That alinement is defined by the following definition of axes.

- $X_{LS}$  along the landing site radius vector
- $Y_{LS}$  along the direction which forms a right-handed system with  $X_{LS}$  and  $Z_{LS}$
- $Z_{LS}$  along the vector formed by the cross product of the CSM angular momentum with the radius vector of the landing site

## 5.0 TRAJECTORY ERROR ANALYSIS TECHNIQUE

The following two sections describe the general Monte Carlo error analysis technique and its specific use in AGAST.

### 5.1 Statistical Trials Technique

Before a mission is flown, it is desirable to know the statistical characteristics of certain important trajectory parameters, for example, the covariance matrix of state vector uncertainties at some point in a rendezvous mission plan. The classical way to determine statistical information about an occurrence (or event) subject to random perturbation is to perform that event enough times experimentally to develop sufficient empirical data on its behavior. Obviously, that method is not appropriate for trajectory error analysis. Another method that can be used is that of statistical trials, in which the basic idea is substitution of a mathematical model for experimentation. That method requires a mathematical model of the occurrence under investigation (such as the flight of a spacecraft) and a model of the random perturbations that affect the occurrence. The computational procedure of the statistical trials method of error analysis is to perform the computations which model the occurrence (with the random perturbations) enough times to generate sufficient data to determine its statistical characteristics. Each time that those computations which model the event are made, a mathematical model of the perturbations introduces into the computations random values for the perturbations. There are standard formulations used to determine the number of times that a model must be cycled to produce a given confidence level in the validity of the computation of statistical characteristics based on the sample results (ref. 1).

Whenever the occurrence to be investigated is the trajectory of a spacecraft, it is desirable to determine the statistical characteristics of the trajectory when subject to specified perturbations with random distributions. For example, it may be desired to randomly perturb spacecraft engine performance and to determine the effects upon the trajectory. Each perturbed trajectory produced by the model is referred to as a sample actual trajectory. Whenever a mission is really flown, estimates of the actual trajectory are maintained in onboard and ground

computers. A trajectory error analysis model also may simulate the computation of such estimates for each sample actual trajectory produced. An estimate of a sample actual trajectory which simulates the computations of an onboard or ground computer is referred to as a sample estimated trajectory.

## 5.2 AGAST Trajectory Simulation

The way in which the concept of statistical trials is used in AGAST to perform trajectory error analysis is described in this section. A nominal or reference trajectory is first produced by AGAST for both the LM and CSM; computations of the reference trajectory precedes the generation of perturbed Monte Carlo sample trajectories. To generate the nominal trajectory, the events of the input-defined mission plan are simulated with no navigation or guidance errors introduced into the computations.

The basic trajectory error analysis scheme of the program is to simulate for two vehicles an actual trajectory and to simulate estimated trajectories for the onboard and RTCC computers. The actual (environmental) state vectors are initialized as random dispersions of the initial reference state vectors. The estimated (onboard and RTCC) trajectories are dispersions of the actual trajectory. That is, the program maintains a true trajectory and onboard and RTCC estimates of that trajectory.

Discrepancies between the actual trajectory and the onboard estimates are assumed to occur because of error sources which include onboard integrator inaccuracies, measurement errors in the onboard sensors, engine performance discrepancies, and MSFN tracking uncertainties. A pseudorandom number generator is used in the introduction of random errors to the simulation of onboard and RTCC computations. The actual state vectors are propagated with an analytic ephemeris predictor which is assumed to be error free. The estimated state vectors are propagated with routines which simulate the onboard integrators.

After the program generates the reference trajectory, the computational sequence is cycled to produce (with error sources randomly sampled) several simulations of the mission profile. Each simulation consists of the initialization and maintenance of actual trajectories and, for each monitored computer, estimated trajectories. When a given mission plan is entered as input to the program, one of the input parameters is an integer  $N$  that represents the number of statistical trials (simulations) of the mission which the program user desires to have produced. The program will automatically cycle  $N$  times to generate  $N$  sets of actual and estimated trajectories for the mission plan defined by the input event packages. Because the error sources are randomly sampled, no trajectory in the set of  $N$  simulations will

be duplicated. A summary of the trajectories produced by AGAST is as follows.

- a. A reference mission trajectory  $X_R$  is produced for both vehicles.
- b. For each Monte Carlo cycle, an actual mission trajectory  $X_A$  is computed for both vehicles.
- c. For each Monte Carlo cycle, an estimated mission trajectory  $X_E$  is computed for both vehicles for each monitored computer.

The collection of actual and estimated trajectories produced is then processed to determine its statistical characteristics. Included in the statistical analysis are some of the burn parameters of the maneuvers. That is, after the required number of Monte Carlo simulations are produced, the statistical characteristics of the trajectory dispersions and the dispersions of maneuver parameters are computed. The statistics include maneuver  $\Delta V$  means and standard deviations; covariance matrices that represent uncertainties in state vectors also are produced.

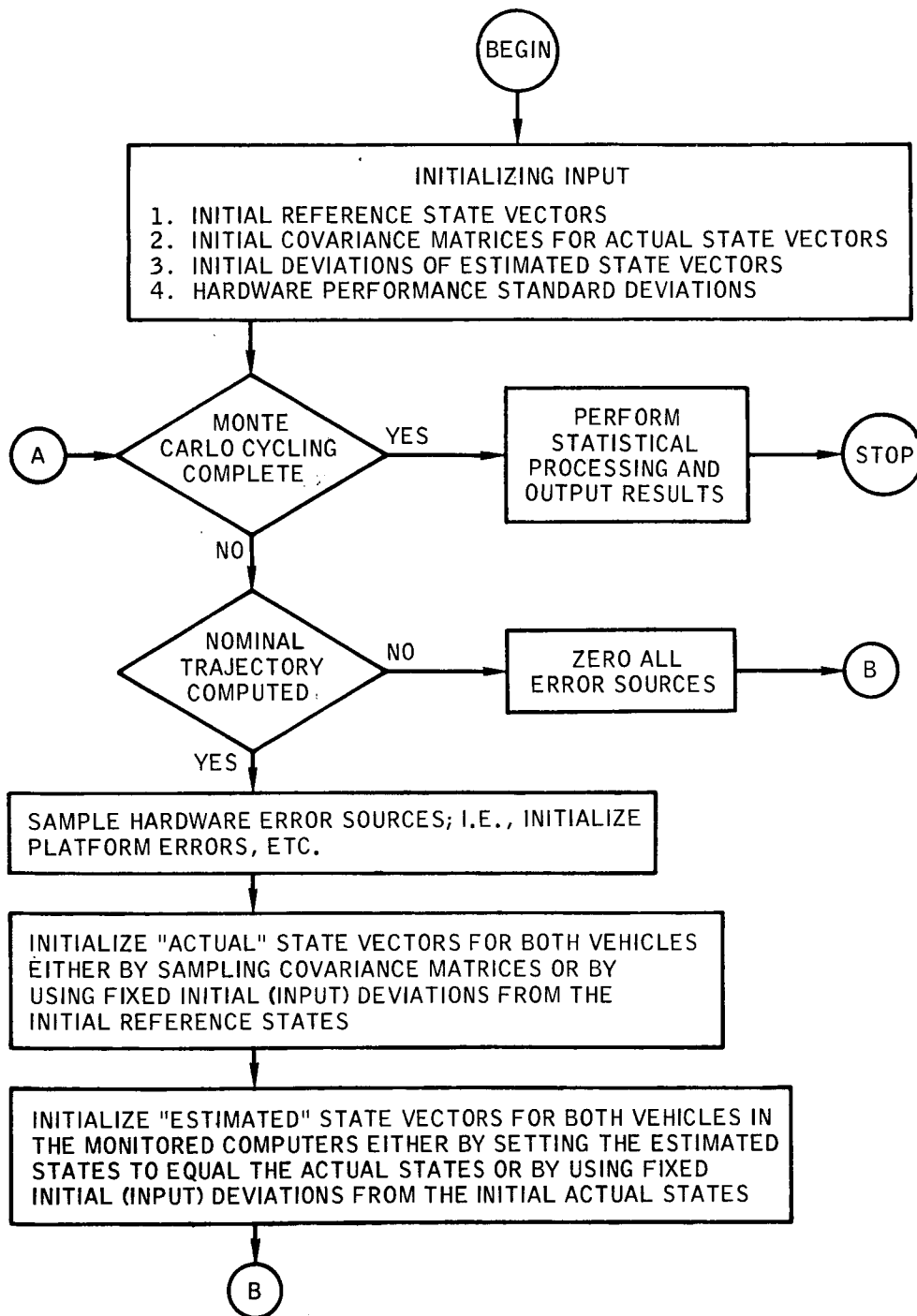


Figure 1.- AGAST schematic flow chart.

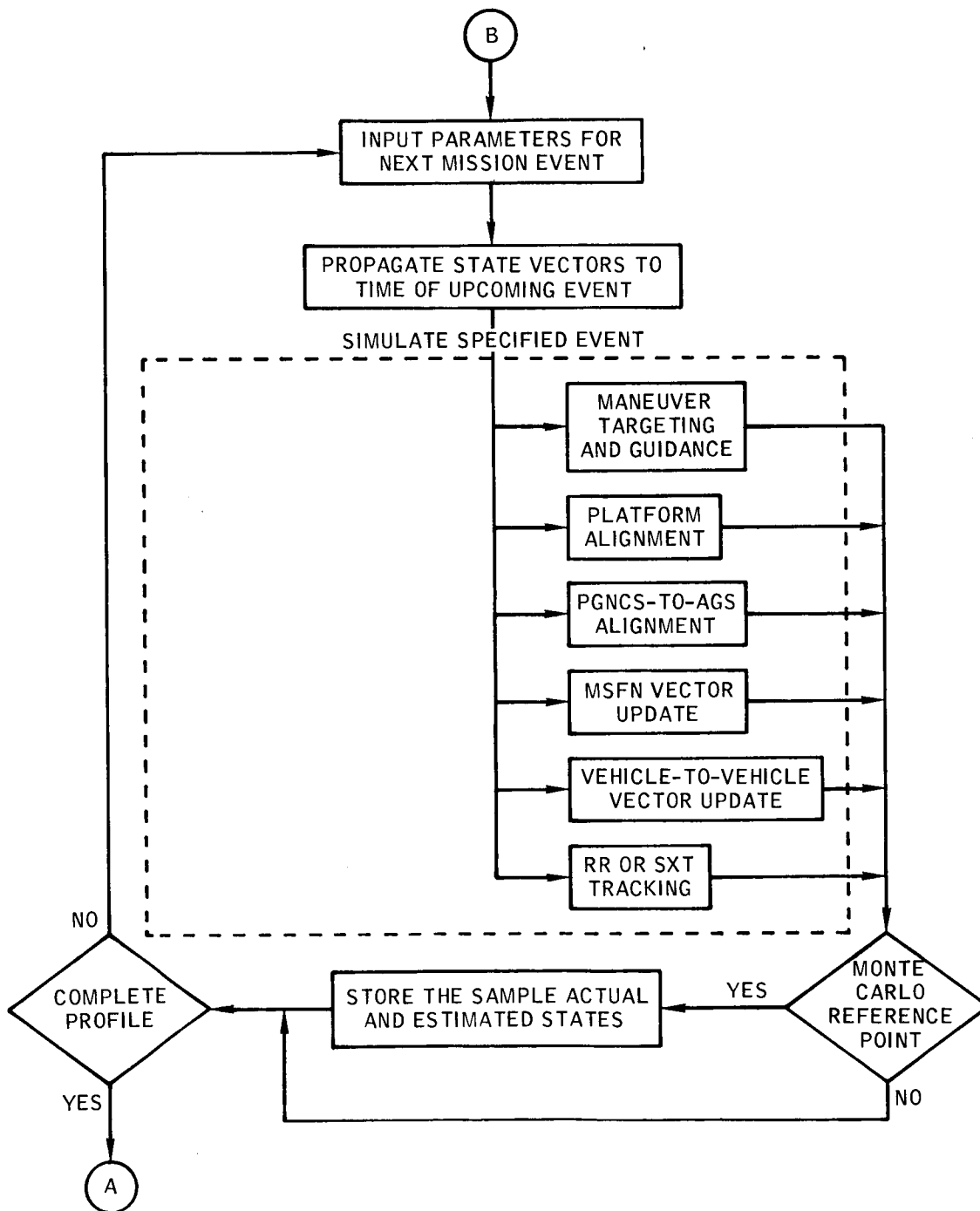


Figure 1.- Concluded.

## 6.0 PROGRAM CAPABILITIES

The capabilities and options of AGAST are presented in this section. Subroutine names are capitalized. Further information is presented in the section on methods, in the individual routine descriptions, and in the user's manual (ref. 5). The reader is referred to section 3.2 of this document for definition of symbols used in the following discussion.

### 6.1 Computer Monitoring

The program user may have the program monitor any combination of CMC, PGNCS, AGS, and RTCC computers. When a computer is monitored, AGAST simulates the computations of that computer and maintains estimated state vectors for it.

An option exists in AGAST to have the AGS monitor a PGNCS controlled burn and vice versa. When one LM computer monitors a burn controlled by the other, the first computer accepts accelerometer sensed  $\Delta V$  increments and accordingly integrates its estimate of the LM state vector.

### 6.2 Error Sources Modeled

Discrepancies arise between the reference and actual trajectories and the actual and estimated trajectories because of the following error sources.

- a. Onboard integrator inaccuracies
- b. MSFN tracking uncertainties
- c. Platform misalignment and drift
- d. Accelerometer misalignment, bias, and scale factors
- e. Rendezvous radar noise and bias on range, range rate, shaft, and trunnion measurements
- f. Sextant noise and bias on the angle measurements
- g. VHF ranger noise and bias on range measurement
- h. Engine thrust profile discrepancies
- i. Thrust misalignment

The introduction of these error sources into the computations is described in the section on methods used and in the subroutine descriptions in the appendix.

### 6.3 Integrators and Central Body Options

The user may specify that either the earth potential model or lunar potential model be used. This capability permits error analyses to be performed for earth rendezvous missions and for lunar rendezvous missions.

The program maintains an actual trajectory, denoted by  $X_A$ , for both the LM and the CSM. Propagation of the actual trajectory during coasting flight is achieved by an analytic ephemeris predictor (AEG) and during powered flight by a modified average-g integrator (RUNGA). The perturbation models of the AEG and the powered flight integrator have more terms than the corresponding onboard integrators. Numerical values of the perturbation constants used in the reference integrators are periodically updated to correspond to the findings of the most recent potential studies.

The CMC and PGNCs estimates of the LM and CSM state vectors are propagated during coasting flight by the onboard coasting integrator (ENCKE). The onboard coasting integrator does not model atmospheric drag in near-earth orbits. Powered flight state vector integration is accomplished in those computers by the onboard average-g integrator (AVEG). A nonperturbed central body potential model is used in the AGS computer for both coasting and powered flight integration of AGS estimated state vectors. The AGS coasting integrator and powered flight integrator as modeled in AGAST are, respectively, AGSKEP and AGSAG.

### 6.4 Program Initialization

Initialization of AGAST is accomplished by specification of the following.

- a. Computers to be monitored (i.e., CMC, PGNCs, AGS, RTCC)
- b. Appropriate central body (earth or moon)
- c. Desired number of Monte Carlo trajectory simulations
- d. Initial reference state vectors for the CSM and LM, denoted by  $X_R$



- e. Engine characteristics
- f. Numerical hardware error models

Several options exist in the initialization process. Numerical models of the Apollo hardware performance are programed into AGAST, but the program user may specify changes to any of those models. The prestored constants are listed in the appendix as defined in reference 6 and include the following.

- a. Nominal engine thrust profiles
- b. Nominal lunar landmarks for optical tracking
- c. One-sigma engine performance discrepancies
- d. One-sigma platform and accelerometer errors
- e. One-sigma RR, SXT, VHF, and SCT measurement errors

Each time that the program is cycled by the Monte Carlo logic, all the random Gaussian errors are reinitialized; the model is resampled.

The initial dispersions of the actual state vectors  $X_A$  are also reinitialized for each Monte Carlo cycle. The initial actual state vectors may be initialized as follows.

- a. For either vehicle,  $X_A$  may be defined as a random dispersion  $\delta X_A$  from  $X_R$  computed by sampling an input covariance matrix of actual state vector uncertainties, denoted by  $\Sigma_A$ .

- b. For either vehicle,  $X_A$  may be defined by input to be a specified deviation  $\delta X_A$  from  $X_R$ . In this way, the user may, if he wishes, have  $X_A = X_R$ .

The initial estimated state vectors  $X_E$  for any monitored computer are always initialized to be a specified (input) deviation from  $X_A$ . There exists no option to obtain the initial estimated states by the process of sampling a tracking covariance matrix because that capability exists as a mission event option (MSFN update). That is, if a user wishes to model MSFN tracking uncertainties, he may specify the first mission event to be a MSFN update and enter as input a matrix of tracking uncertainties,  $\Sigma_T$ . This method is the one most often used.

The covariance matrix  $\Sigma_A$  represents uncertainties of the dispersions of the initial actual state vector from the initial nominal  $X_R$ . For instance,  $\Sigma_A$  may represent the uncertainties of launching the LM into a nominal lunar orbit from the lunar surface.

The initialization of  $X_A$  (for one vehicle) from a covariance matrix of uncertainties about  $X_R$  is presented in figure 2. Also presented is the subsequent modeling of the MSFN determination of the estimated state  $X_E$ . The sequential process followed by AGAST which is schematized in figure 2 is as follows.

- a.  $X_R$  is defined by input
- b.  $\Sigma_A$  is defined by input
- c.  $\delta X_A$  is computed as a random sampling of  $\Sigma_A$
- d.  $X_A = X_R + \delta X_A$
- e. Input specifies a MSFN update mission event:  $\Sigma_T$  is input.
- f.  $\delta X_E$  is computed as a random sampling of  $\Sigma_T$ .
- g.  $X_E = X_A + \delta X_E$

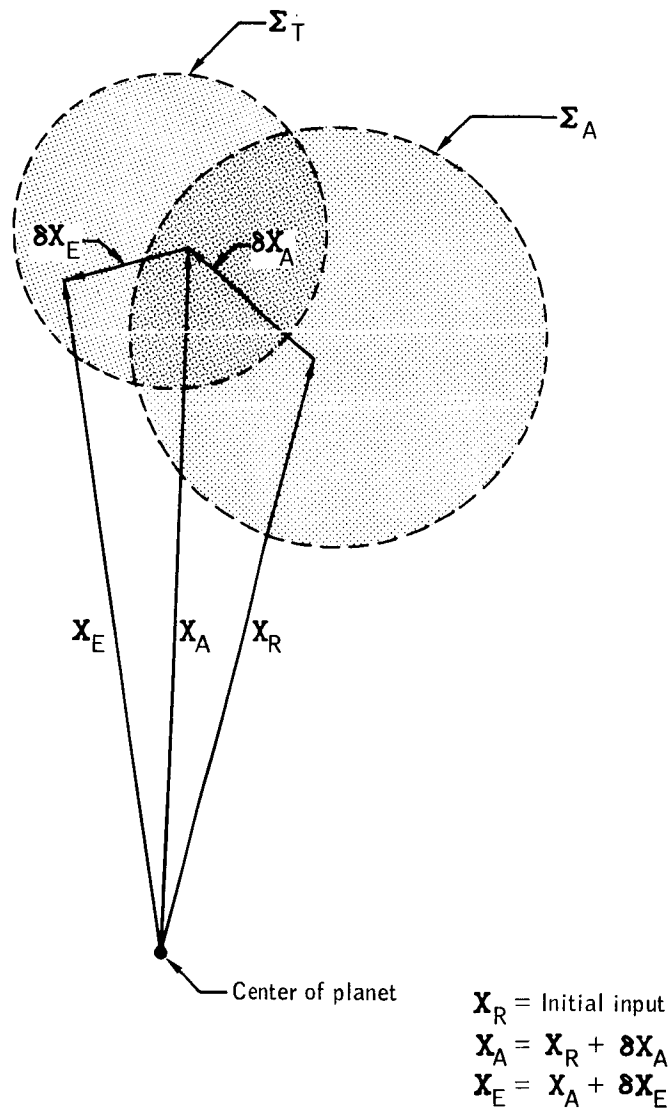


Figure 2.- Initialization of AGAST state vectors.

## 6.5 Maneuver Computations

The discussion of maneuver computations in AGAST is divided into a section on maneuver simulation and a section on special targeting computations for comparative studies. The associated logic is presented in more detail in the flow charts of AGAST subroutines MANEUV and TARGET.

6.5.1 Maneuver simulation.- A variety of options exist in AGAST for the computation of maneuver targeting and for simulation of guidance. One of those options is that the numerical thrust model of any engine may be changed at any point in the simulation of the mission plan. The program user may use one of the following options on any maneuver event which he schedules.

- a. Targeting is computed, but the  $\Delta V$  is not applied to the state vector.
- b. The targeted  $\Delta V$  is impulsively applied to the state vector (with no maneuver execution errors modeled).
- c. The burn is controlled by onboard guidance equations
  1. With system errors not modeled
  2. With system errors modeled

The following lists present all the maneuver events which may be simulated in AGAST.

- a. Target  $\Delta V$ : updates the CSM(LM) state in the PGNCs (CMC) by impulsive simulation of a maneuver which has been performed by the CSM(LM)
- b. External  $\Delta V$  guidance
- c. SOI: stable orbit initiation
- d. SOM: stable orbit midcourse
- e. SOR: stable orbit rendezvous
- f. CSI: coelliptic sequence initiation
- g. CDH: constant delta height
- h. TPI: terminal phase initiation
- i. TPM: terminal phase midcourse

- j. Direct intercept
- k. Direct transfer to input target
- l. TPF: braking
- m. NCC: corrective combination
- n. NSR: coelliptization
- o.  $N_{Cl}$  DKI phasing maneuver
- p.  $N_H$  height maneuver
- q. Staging
- r. Plane change
- s. DOI: descent orbit injection
- t. Descent: powered descent to the lunar surface
- u. Ascent: powered ascent into lunar orbit
- v. Abort: abort from a powered descent to a powered ascent into lunar orbit

The following list is a summary of the capabilities of the AGAST models of the different computers.

- a. The RTCC model can generate targeting for any maneuver in the above list.
- b. The PGNCs can handle all the computations indicated by the above list except for DOI and the ground (RTCC) computed maneuver sequences that involve NCC, NSR,  $N_{Cl}$ , and  $N_H$ .
- c. The CMC can perform all the maneuver computations except DOI, lunar descent, lunar ascent, and ground computed maneuvers NCC, NSR,  $N_{Cl}$ , and  $N_H$ .
- d. AGAST currently has AGS capability only for CSI, CDH, TPI, TPM, and external  $\Delta V$  guidance, ascent guidance, and abort guidance.

6.5.2 Special maneuver targeting computations.— Often it is desirable to determine for a given maneuver the targeting parameters

which the different computers will produce. Such information is useful in analyzing and setting up computational procedures for the mission plan under study.

For a given maneuver, AGAST has the capability to generate targeting based on the estimated states of any or all of the four computers (with the computer restrictions noted in section 6.5.1) and also to compute the targeting based on the actual state vectors. Subsequent to those computations, AGAST will produce the following.

- a. Targeting discrepancies between the different computers
- b. Targeting discrepancies between the solution based on the actual state vectors and the solutions based on the estimated states of the computers

The burn simulation is controlled by the targeting computed for the controlling computer.

Because the different computers will produce different maneuver times for some maneuvers, the targeting based on the actual states is computed for each of those different times. The program user may command AGAST to compute the following solutions for any given maneuver in a mission.

- a. The CMC  $\Delta V$  solution at CMC predicted maneuver time: CMC/CMC
- b. The PGNCS  $\Delta V$  solution at PGNCS predicted maneuver time: PGNCS/PGNCS
- c. The AGS  $\Delta V$  solution at AGS predicted maneuver time: AGS/AGS
- d. The RTCC  $\Delta V$  solution at RTCC predicted maneuver time: RTCC/RTCC
- e. The  $\Delta V$  solution based on the actual state vectors but computed at the CMC predicted maneuver time: ACT/CMC
- f. The  $\Delta V$  solution based on the actual state vectors but computed at the PGNCS predicted maneuver time: ACT/PGNCS
- g. The  $\Delta V$  solution based on the actual state vectors but computed at the AGS predicted maneuver time: ACT/AGS
- h. The  $\Delta V$  solution based on the actual state vectors and computed at the predicted maneuver time based also on the actual state vectors: ACT/ACT

Coincident with the computation of special maneuver targeting is the generation of the resultant target differences. Depending upon which targeting solutions are computed, some or all of the following  $\Delta V$  target differences are formed by AGAST, and their statistical characteristics are produced.

- a. CMC/CMC - ACT/CMC
- b. PGNCS/PGNCS - ACT/PGNCS
- c. AGS/AGS - ACT/AGS
- d. RTCC/RTCC - ACT/ACT
- e. PGNCS/PGNCS - CMC/CMC
- f. PGNCS/PGNCS - AGS/AGS
- g. PGNCS/PGNCS - RTCC/RTCC
- h. RTCC/RTCC - CMC/CMC
- i. RTCC/RTCC - AGS/AGS
- j. CMC/CMC - AGS/AGS

## 6.6 Platform Alinements

Platform alinements for the CMC and for the PGNCS are simulated by computation of a platform orientation matrix REFSMMAT for each computer. The platform orientation matrix is the rotation matrix from the basic reference coordinate system to the coordinate system of the inertial platform. The REFSMMAT matrix is used in many onboard computations; for instance, during a burn the sensed  $\Delta V$  increments are measured in the coordinate system of the inertial platform but must be transformed into the basic reference coordinate system which the guidance uses. In AGAST, the computation of the REFSMMAT at a given time in the mission is an implicit definition of a platform alinement. The REFSMMAT may be computed for the following types of alinement.

- a. Nominal alinement is defined to be the alining of the platform gyros to a local vertical coordinate system defined at the alinement time.
- b. Preferred maneuver alinement is based on the desired thrust direction of a given maneuver.

c. Lunar surface alinement is used during lunar landing and lunar launch and is based on the radius vector of the landing site.

The specific REFSMMAT formulations associated with those three types of alinements are detailed in the flow charts of the AGAST subroutines ALIGN, PMATRIX, PALIGN, and LSALGN.

Platform errors are reinitialized with each alinement. The errors are modeled as initial platform misalignment at the alinement time and platform gyro drift after alinement. These errors are represented in AGAST as a coordinate system rotation error in the definition of REFSMMAT. The associated rotation error matrix is introduced into the guidance computations and in the incorporation of onboard tracking measurements.

### 6.7 AGS-to-PGNCS Alinement

One procedure by which the AGS computer is initialized is as follows.

- a. Define the AGS reference coordinate system to be that of the PGNCS inertial platform.
- b. Load into the AGS the PGNCS estimated state vectors rotated into the AGS reference coordinate system.

This procedure is called AGS-to-PGNCS alinement. The AGS may be initialized in AGAST in this manner as a mission event. The required operations are modeled in subroutine ALIGN, but AGAST AGS computations are made in the basic reference frame to facilitate comparison of AGS with the other computers. However, AGS platform errors which are caused by PGNCS misalignment at the AGS-to-PGNCS alinement time are accounted for.

### 6.8 State Vector Updates

Several options exist in AGAST for the modeling of updates of the estimated state vectors maintained in the monitored computers. Updates during a mission may be accomplished by transferral of state vector information from one computer to another, by MSFN orbit determinations, and by the use of onboard tracking devices.

6.8.1 Vehicle-to-vehicle transferral.-- The estimated state vectors of one computer may be used to replace those of one of the other computers. This mission event models the procedure by which the CMC update of the PGNCS (or vice versa) is accomplished by the voicing of state vector information between the two vehicles.

6.8.2 MSFN updates.-- MSFN orbit determination and the subsequent update of the estimated states in the computers are modeled in AGAST by



the method of randomly sampling a covariance matrix of MSFN tracking uncertainties. Whenever the program user specifies that a mission event is a MSFN update of one of the computers, he must also enter as input to AGAST a matrix of state vector tracking uncertainties  $\sum_T$ .

That matrix implicitly correlates the MSFN CSM state vector uncertainties with the MSFN LM state vector uncertainties. Both estimated states in the specified computer are updated by sampling  $\sum_T$  and determining new estimated states at the mission event time.

The random sampling method is discussed in section 7.1. The update logic which models the MSFN is to be found in AGAST subroutine REPLAC.

6.8.3 Onboard tracking.-- Onboard tracking is modeled in AGAST in two ways.

- a.. Random sampling of an input onboard tracking covariance matrix
- b. Explicit modeling of the onboard Kalman filters and the associated navigation equations

Updates for both CSM and LM tracking devices can be simulated.

A rendezvous radar (RR) is attached to the LM. The RR measures the range and range rate between the LM and CSM by the pulsing of signals to a beacon on the CSM and the sensing of the pulse returned by that beacon. Also measured are the radar disk shaft and trunnion angles which relate the line-of-sight direction and the LM body attitude. The PGNCS is interfaced with the RR; and when the PGNCS is in the tracking incorporation mode, it samples the output of the RR approximately once a minute. The PGNCS uses a modified Kalman filter to incorporate the tracking parameters into the estimate of the state vector of either the CSM or the LM.

The AGS computer may accept range and range rate information manually keyed into the computer by a crewman. The crewman may read the RR tracking data from a display. The AGS RR filter incorporates the tracking data into the LM state vector estimate.

Two optical tracking devices are part of the equipment of the CSM. One of the instruments is a sextant (SXT), and the other is called a scanning telescope (SCT). Also attached to the CSM is a VHF ranger, a device used to measure the range between the CSM and LM. The SXT and VHF tracking data are passed through the same filter. In this document, the symbol SXT will refer to both SXT and VHF tracking.

These CSM optical instruments may be directed by a crewman toward either the LM or a lunar landmark. When the operator depresses the MARK button on a CSM console, the time and measured line-of-sight angles are stored in the CMC. When the VHF range measuring device is being used, the measured relative range is automatically stored in the CMC, and that computer picks up the VHF output approximately once a minute. Through the use of a modified Kalman filter, the measured relative information is incorporated into the CMC estimate of the CSM state vector if the CMC is in the lunar landmark tracking mode or either the CSM or LM estimated state if the CMC is in the LM tracking mode.

6.8.3.1 Covariance matrix modeling of onboard tracking: Except for lunar landmark tracking, the effect of the state vector updates accomplished with the onboard tracking devices and filters is to reduce the errors in the estimated relative state between the two vehicles. The onboard computer logic which handles such updates is based on the assumption that the estimate of one of the vehicles' state vector is error free. Both RR tracking of the CSM and SXT tracking of the LM can be modeled in AGAST by the sampling of a corresponding covariance matrix of tracking uncertainties  $\sum_{REL}$  for the relative state vector. In that way, a random estimate of the relative state vector is formed; and, in turn, an estimate of one of the vehicles' state vector is made. That method of modeling entails no explicit use of onboard filters. The input matrix  $\sum_{REL}$  must be generated external to AGAST. The relevant AGAST logic is in subroutine REPLAC, and the details of the formulation are presented in section 7.4.

6.8.3.2 Explicit modeling of onboard tracking: The Kalman filters for CMC incorporation of SXT and SCT data, for PGNCs incorporation of RR data, and for AGS incorporation of RR data are programed into AGAST. The program user may specify any number of tracking events for a mission. The program will simulate the operation of the tracking devices by the production of tracking data for each mark followed by the performance of the computations of the filter and subsequent updates of one of the estimated state vectors. The AGAST subroutines UPDATV and AGSRR are the program entry points for tracking logic and formulation.

## 7.0 METHODS AND FORMULATIONS

Detailed discussions of some of the more important modeling methods and formulations used in AGAST are presented in this section. Much of the formulation used in AGAST originated in the referenced documents and is adequately discussed in those reports.

### 7.1 Random Sampling Technique

The modeling method of statistical trials is based upon the technique of generation of random dispersions for certain parameters considered to have random distributions. All AGAST parameters with random dispersions are assumed to have normal (Gaussian) distributions.

Several references have been made in the preceding text to the process of sampling error sources. For example, each time that the program is cycled, a new set of initial state vector dispersions are generated by randomly sampling a covariance matrix of the uncertainties of the state vector. An explanation of that process will be presented in this section.

To validly perform the generation of dispersions for a given random variable, the following are required.

- a. An input set that defines the statistical properties of the variable, that is, the variance for a scalar variable or the covariance matrix for a vector variable
- b. A random number generator

There exist standard computer routines for the generation of random numbers. AGAST uses a UNIVAC 1108 math-pack routine RANDN which produces random arrays for which the components have a mean of zero and a variance of 1. The use of RANDN is discussed in the description of AGAST subroutine RANNO. In the following discussion, assume that the normalized random vector  $\bar{\eta}$  is generated by a random number generator such as RANDN.

Consider the random vector  $\bar{\eta}$  to be a normalization of the random vector  $\delta\bar{x}$ . That is, assume  $\delta\bar{x} = C\bar{\eta}$  where  $C$  is an  $n \times n$  constant matrix that relates  $\delta\bar{x}$  to  $\bar{\eta}$ . The problem is to determine the multiplier  $C$ .

By definition,

$$\sum_{\bar{\eta}} \bar{\eta} = E [\bar{\eta} \cdot \bar{\eta}^T] = I \quad (1)$$

where  $E$  is the statistical expectation operator.

Also, note that

$$\sum_{\delta \bar{x}} = E [\delta \bar{x} \cdot (\delta \bar{x})^T] \quad (2)$$

If  $\delta \bar{x}$  is set equal to  $C \bar{\eta}$  and is substituted into equation (2), equation (3) results.

$$\begin{aligned} \sum_{\delta \bar{x}} &= E [C \bar{\eta} \cdot (C \bar{\eta})^T] \\ &= E [C \bar{\eta} \cdot \bar{\eta}^T C^T] \\ &= C \cdot E [\bar{\eta} \cdot \bar{\eta}^T] \cdot C^T \\ &= C \cdot C^T \end{aligned} \quad (3)$$

Therefore, the matrix  $C$  is a factor in a decomposition of  $\sum_{\delta \bar{x}}$ . However, the decomposition  $CC^T$  of a square matrix is not unique. Assume that  $C$  will be lower left triangular and therefore unique.

Let  $\sigma_{ij}$  and  $c_{ij}$  represent, respectively, the element of  $\sum_{\delta \bar{x}}$  and  $C$  in the  $i$ th row and  $j$ th column. The matrix can be written as follows.

$$C \cdot C^T = \begin{bmatrix} c_{11}^2 & c_{11}c_{21} & \dots & c_{11}c_{n1} \\ c_{21}c_{11} & c_{21}^2 + c_{22}^2 & \dots & c_{21}c_{n1} + c_{22}c_{n2} \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot \\ c_{n1}c_{11} & c_{n1}c_{21} + c_{n1}c_{22} & \dots & \sum_{k=1}^n c_{nk}^2 \end{bmatrix}$$

When the elements of  $\sum_{\delta\bar{x}}$  and  $CC^T$  are equated and when  $c_{ij}$  is solved for, equation (4) results.

$$c_{ij} = 0$$

where  $j > i$ .

$$c_{11} = \sqrt{\sigma_{11}}$$

$$c_{ii} = \sqrt{\sigma_{ii} - \sum_{k=1}^{i-1} c_{ik}^2}$$

$$c_{ij} = \frac{\sigma_{ji} - \sum_{k=1}^{i-1} c_{jk}c_{ik}}{c_{ii}} \quad (4)$$

where  $j < i$ .

Compute the matrix  $C$  when  $\sum_{\delta\bar{x}}$  is given as input and by use of the algorithm indicated by the above formulation. Each time that it is desired to sample the matrix  $\sum_{\delta\bar{x}}$ , it will only be necessary to generate an  $n$ -dimensional array of random numbers symbolized by  $\bar{\eta}$  and then set the random dispersion  $\delta\bar{x}$  to be  $C\bar{\eta}$ .

Note that when the variable  $\bar{x}$  is a scalar the multiplier  $C$  also reduces to a scalar. The sampling technique described above is used in AGAST to produce dispersions for all variables  $\bar{x}$  which are subject to random variation  $\delta\bar{x}$ . Variables which are dispersed randomly include state vectors, platform alinements, engine parameters, and onboard tracking measurements. Sampling of covariance matrices is performed in subroutine SAMPLE.

## 7.2 Maneuver Execution Error Model

Nonnominal execution of maneuvers is modeled in AGAST in three ways.

- a. Nonnominal engine performance (thrust levels, etc.)

b. Introduction of platform and accelerometer errors into the computation of guidance commands and the simulation of sensed  $\Delta \bar{V}$

c. At the end of a burn, approximation of the burn error caused by an initial thrust pointing discrepancy

Nonnominal engine performance is simulated by dispersion of the thrust profile from the nominal. Thrust dispersions are generated in each thrust phase either as a percentage of the nominal thrust magnitude for that phase or by randomly sampling the standard deviation of the thrust magnitude for that phase.

7.2.1 Platform and accelerometer error models for CMC and LGC maneuver simulation.— The guidance logic and equations used by subroutine MANEUV (fig. B-55) generate either a desired thrust direction  $\bar{u}_{TD}$  or a desired thrust vector turning rate  $\bar{\omega}_D$  in basic reference coordinates.

Those commands are transformed into IMU coordinates and then into body referenced coordinates. The digital autopilot (DAP) accepts the steering commands in body referenced coordinates and attempts to execute them. Because the inertial platform's alignment is not perfect, the transformation matrix REFSMMAT is in error by the amount of rotation of the platform from its desired orientation. Therefore, the transformation of basic reference frame guidance commands with REFSMMAT does not produce the correct transformation to the true orientation of the platform so that the steering commands which the DAP receives do not have the correct orientation. The error in the steering commands is modeled in AGAST by determination of the true orientation of the platform and subsequent determination of the basic reference orientation of the guidance command executed by the DAP.

AGAST does not contain a model of the DAP. When the guidance command is  $\bar{u}_{TD}$ , the burn simulator (RUNGA) generates a turning rate vector similar to  $\bar{\omega}_D$  which rotates the thrust direction at a constant rate from the old thrust direction to the new  $\bar{u}_{TD}$ . Whether the thrust command is generated as  $\bar{u}_{TD}$  or  $\bar{\omega}_D$ , the turning rate is limited to be less than or equal to 10 deg/sec. Both  $\bar{u}_{TD}$  and  $\bar{\omega}_D$  are rotated to reflect the REFSMMAT error before they are processed by RUNGA.

The object of the platform error model is to apply the effects of the platform errors to an output of the guidance equations in such a way that the burn simulation will reflect the true reaction of the steering system. Both the guidance equations and the burn simulator compute in basic reference coordinates. Therefore, the error model formulation must convert the guidance command into IMU coordinates, apply the platform

errors, and then reconvert to basic reference coordinates. The platform errors consist of initial misalignment in each of the three gyros at the alinement time and of gyro drift since alinement time. At alinement time, the platform errors are determined either by setting them to input specifications or by sampling the numerical model of platform statistics. The platform errors are the three rotation angles that define platform misalignment about the three axes of the REFSMMAT coordinate system. Let  $[P(t)]$  represent the platform error matrix at the time  $t$ , and let  $[T]$  represent the REFSMMAT matrix. Then if  $\bar{u}_{TD}$  or  $\bar{\omega}_D$  is produced as output from the guidance equations, the values  $\bar{u}_{TA}$  and  $\bar{\omega}_A$  are entered as input to the burn simulator, where

$$\bar{u}_{TA} = [T]^{-1} \cdot [P(t)] \cdot [T] \cdot \bar{u}_{TD} \quad (5)$$

$$\bar{\omega}_A = [T]^{-1} \cdot [P(t)] \cdot [T] \cdot \bar{\omega}_D \quad (6)$$

The burn simulator accepts the guidance command and performs the burn computations which include the following.

- a. The  $\Delta\bar{V}$  added during the guidance
- b. New thrust direction (in basic reference frame) at the end of the guidance cycle
- c. Integration of the actual trajectory to the end of the guidance cycle

The  $\Delta\bar{V}$  output from the burn simulator is considered to be the actual and is symbolized by  $\Delta\bar{V}_A$ ; the value of  $\bar{u}_{TA}$  is updated in the burn simulator and represents the new actual thrust direction.

In actual flight, the accelerometers attached to the platform sense the burn and feed to the computer the measured incremental velocity. The measured  $\Delta\bar{V}$  is transformed from IMU coordinates to basic reference coordinates and is used in the onboard average-g state vector integrator to integrate the estimated state vector forward one guidance cycle. The AGAST modeling of accelerometer and platform errors on the measured  $\Delta\bar{V}$  fed to the onboard computer is as follows.

$$\Delta\bar{V}_E = [T]^{-1} \left\{ [S] \cdot [B] \cdot [P(t)] \cdot [T] \cdot \Delta\bar{V}_A + \Delta\bar{V}_B \right\} \quad (7)$$

Integration of  $X_E$  is performed in AVEG, which accepts  $\Delta\bar{V}_E$  as an input.

The new thrust direction  $\bar{u}_{TA}$  which is produced as output from the burn simulator is also perturbed with platform errors before being passed on to the guidance equation.

$$u_T = [T]^{-1} \cdot [P(t)] \cdot [T] \cdot \bar{u}_{TA} \quad (8)$$

where  $\bar{u}_T$  is the AGAST representation of the onboard estimate of the new thrust direction.

7.2.2 Platform and accelerometer error models for AGS maneuver simulation.— The AGS error models differ in formulation from those of the PGNCS because the AGS reference frame is defined to be the orientation of the PGNCS platform at the time of AGS-to-PGNCS alinement. Therefore, PGNCS platform errors at the time of AGS alinement affect the AGS guidance computations. For an AGS controlled burn, the thrust vector sent to the burn simulator in AGAST is

$$\bar{u}_{TA} = [T]^{-1} \cdot [A(t)]^{-1} \cdot [P_A(t)] \cdot [A(t)] \cdot [P_T] \cdot [T] \cdot \bar{u}_{TD} \quad (9)$$

where  $\bar{u}_{TD}$  is generated in basic reference coordinates and  $[A(t)]$  relates the AGS strapped down platform to the AGS reference computing frame (not used in AGAST). The burn simulator routine RUNGA outputs a new  $\bar{u}_{TA}$  at the end of the 2-second guidance cycle, and the new estimated thrust vector passed on to the AGS guidance equations is

$$\bar{u}_T = [T]^{-1} \cdot [A(t)]^{-1} \cdot [P_A(t)] \cdot [A(t)] \cdot [P_T] \cdot [T] \cdot \bar{u}_{TA} \quad (10)$$

The actual incremental velocity of a guidance cycle  $\Delta \bar{V}_A$  is output from RUNGA. Formulation in AGAST for computation of the incremental velocity sensed by the AGS accelerometer over a guidance cycle is as follows.

$$\Delta \bar{V}_M = [S_A] \cdot [B_A] \cdot [P_A(t)] \cdot [A(t)] \cdot [P_T] \cdot [T] \cdot \Delta \bar{V}_A \quad (11)$$

$$\Delta \bar{V}_E = [T]^{-1} \cdot [A(t)]^{-1} \cdot \Delta \bar{V}_M \quad (12)$$

The value  $\Delta \bar{V}_E$  is used by the AGS average-g integrator AGSAG to advance the AGS estimated LM state one guidance cycle.



7.2.3 Pointing error model and burn trim.- The effects of thrust pointing errors, accelerometer quantization, or manual maneuver cutoff errors are accounted for in AGAST subroutine TRIM by the introduction of random velocity perturbations into the states at burn cutoff. Thrust pointing error is caused by insufficient knowledge in the onboard guidance computer of the spacecraft center of gravity. During attempts to correct for the center of gravity error, the guidance computer introduces cross-axis errors into the burn. Cross-axis errors are in the plane normal to the thrust direction. The pointing error velocity is simulated in AGAST when a normal distribution is assumed for the error and a random sampling is used based upon a standard deviation value taken from the cross-axis velocity curves in reference 6.

RCS burns are manually controlled, and for such maneuvers, the vehicle usually is placed in an attitude which places the desired  $\Delta \bar{V}$  along one of the body thrusting axes. Because no steering is involved in RCS burns, pointing errors are not considered. The RCS burn error considered in AGAST is based on the crewman's inability to release the throttle at exactly the proper time. A random velocity error is computed in the direction of the thrust to account for RCS cutoff error.

Quantization error results because the accelerometers measure  $\Delta \bar{V}$  applied during a burn as an integral number of PIPA pulses so that some partial pulse is applied but not included in the accelerometer readout. AGAST accounts for this effect by addition to the actual state of random  $\Delta \bar{V}$  which is uniformly distributed over the quantization interval of the accelerometer.

The use in AGAST of the pointing error  $\Delta \bar{V}_P$  and the manual cutoff error  $\Delta \bar{V}_{CO}$  depends upon the trim option desired. If no trim is desired, then  $\Delta \bar{V}_P$  and  $\Delta \bar{V}_{CO}$  must be added to the actual and estimated states to account for the errors that would result in a burn with no trim. For a burn which is to be trimmed, AGAST does not model pointing errors or manual cutoff errors; that is, it is assumed that those errors will be taken out by trimming the residuals. Trims are simulated by impulsive applications to both the actual and estimated states of part or all of the  $\bar{V}_G$  residual that results from guidance errors. If the program user specifies the perfect trim option, then the trim  $\Delta \bar{V}$  applied is equal to the  $\bar{V}_G$  residual; otherwise, the residual in each axis is trimmed to a preset value.

### 7.3 Onboard Tracking Error Models

The onboard tracking devices are subject to bias and noise errors in their measurements. Numerical models of the bias and noise are programed into AGAST. Each time that the program starts another Monte Carlo cycle of a given mission plan, all biases are fixed by randomly sampling the numerical models. For example, there is a standard deviation value stored in AGAST for the bias in the RR measurement of the dish shaft angle. AGAST simulates that bias by randomly sampling that standard deviation each new cycle of the program. Other biases are similarly modeled.

For each mark of an onboard tracking schedule, the tracking logic of AGAST simulates the measured parameters as follows.

$$\text{Measured} = \text{Actual} + \text{Bias} + \text{Noise}$$

The measured relative range, range rate, shaft and trunnion angles are computed as follows.

$$R_M = R_A + \delta R + (\sigma_{N_R}) \cdot \eta_1 \quad (13)$$

$$\dot{R}_M = \dot{R}_A + \delta \dot{R} + (\sigma_{N_{\dot{R}}}) \cdot \eta_2 \quad (14)$$

$$\beta_M = \beta_A + \delta \beta + (\sigma_{N_\beta}) \cdot \eta_3 \quad (15)$$

$$\theta_M = \theta_A + \delta \theta + (\sigma_{N_\theta}) \cdot \eta_4 \quad (16)$$

where the  $\delta$ -values are the biases, the  $\sigma_N$ -values are the standard deviations of the noise, and the  $\eta_i$  are normalized random numbers which are generated for each mark. Similarly, the optical and VHF data measured onboard the CSM are simulated by computation of the actual parameters and addition of bias and noise values. For the SXT and SCT, the AGAST error model takes the form of rotation bias and noise in the unit vector along the measured line of sight. The VHF relative range measurement is formulated exactly as that for the RR. The standard deviation values for RR and VHF measurement bias and noise are functions of the range (ref. 6). These standard deviation functions are modeled in the programed tracking logic.

#### 7.4 Covariance Matrix of Onboard Tracking Uncertainties

As previously explained, AGAST may model the effects of onboard vehicle-to-vehicle tracking by sampling an input matrix of relative state vector uncertainties. The assumptions and logic formulations of that option are presented in this section.

The vehicle-to-vehicle onboard tracking measurements are of relative state vector parameters. For the RR, these parameters are range, range rate, and the radar dish orientation angles shaft and trunnion. The SXT produces a unit vector directed from the CSM to the LM, and the VHF device produces range data. The measurement incorporation algorithm updates the estimated state vector of one of the vehicles in such a manner that the error in the measurement parameters tends to converge to zero. This method of updating does not account for the fact that the estimated state vector of the other vehicle may also be in error.

The computation sequence in AGAST which uses a covariance matrix of relative state vector uncertainties to model onboard tracking is as follows.

- a. Compute  $\Delta X_A$  in the local vertical coordinate system of  $X_{A,J}$ .
- b. Define  $\Delta X_E^* = \Delta X_A$ .
- c.  $\Delta X_E^*$  is assumed to be a vector centered at  $X_{E,J}$  and is rotated from the local vertical of  $X_{E,J}$  to the basic reference coordinate system.
- d. Define  $X_{E,I}^* = X_{E,J} + \Delta X_E^*$ .
- e. Compute  $\delta x_{REL}$  by sampling  $\Sigma_{REL}$ .
- f. Rotate  $\delta x_{REL}$  from the local vertical coordinate system of  $X_{E,I}^*$  to the basic reference frame.
- g. Define  $X_{E,I} = X_{E,I}^* + \delta X_{REL}$ .

When the dispersion  $\delta x_{REL}$  is zero, the new estimated relative state vector is  $\Delta X_E^*$ , which produces the same relative range, range rate, and local vertical line-of-sight angles as does  $\Delta X_A$ . Note that  $\Delta X_E^*$  is the best relative state vector that the onboard tracking may produce;

that is, the relative state directed from  $X_{E,J}$  corresponds in a local sense to  $\Delta X_A$ .

The computer logic of this option is formulated in the description of AGAST subroutine REPLAC. A schematic of the geometrical relationships of the above computational sequence is presented in figure 3. In this figure, the angle  $\beta$  is the actual line-of-sight angle from the local horizontal.

### 7.5 Computation of Sample Statistics

When a program user defines a mission plan to AGAST, he may specify that certain events be reference points. Such reference points are those events of the mission plan for which the program operator desires to produce sample state vector statistics and sample  $\Delta V$  statistics. For each cycle of the program by the Monte Carlo logic, sample actual state vectors and sample estimated state vectors of the reference points are saved on magnetic tape. If the reference point is a maneuver event, targeting and burn parameters are also stored.

After the requested number of statistical trials of a trajectory has been computed, AGAST then reads the sample state vectors and maneuver parameters from the tape and performs statistical processing of that sample data. For each reference point, the AGAST statistical processing logic computes the array of dispersions of the sample actual state vectors from the corresponding nominal state vector at that point. Also computed is the array of dispersions of sample estimated state vectors from the corresponding sample actual state vectors. These arrays of dispersions are processed by the logic of subroutine PROCES. The following statistics are produced.

- a. Sample means and sample standard deviations for the total  $\Delta V$  required to fly the mission plan
- b. Cumulative distribution of dispersions to the nominal total  $\Delta V$  required
- c. Sample means and sample standard deviations for the components of the  $\Delta V$  targeting solutions for the maneuver events
- d. Sample means and sample covariance matrices for state vector dispersions

The specific logic used and parametric output are discussed in detail in the description of subroutine PROCES. The formulation by which

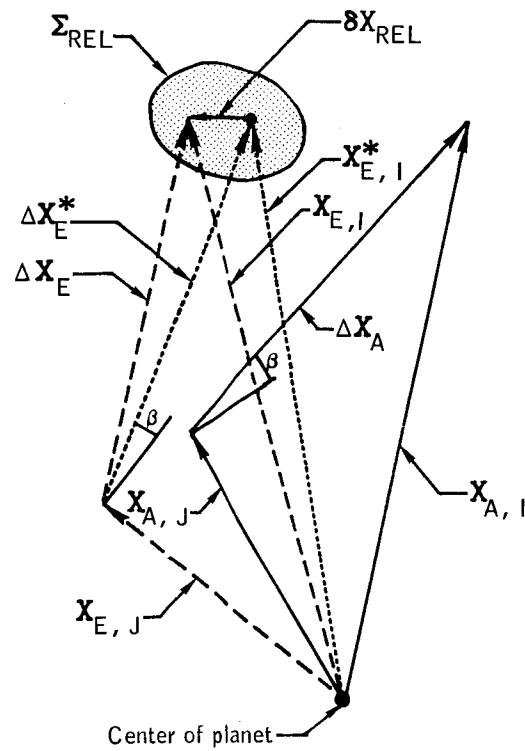


Figure 3.- Using relative state vector covariance matrix to simulate onboard tracking.

AGAST computes sample statistics is presented below and is based on derivations in reference 7.

If the following symbols are defined as shown,

$X$  a random vector

$\left\{ X_i \right\}_{i=1}^N$  an array of random samples of  $X$

$\bar{\mu}$  mean of  $X$

$\sigma$  standard deviation of  $|X|$

$\Sigma$  covariance matrix of  $X$

then the formulation used in AGAST is

$$\bar{\mu} = \frac{1}{N} \sum_{i=1}^N X_i \quad (17)$$

$$\sigma = \sqrt{\frac{1}{N-1} \left[ \sum_{i=1}^N X_i^2 - \frac{1}{N} \left( \sum_{i=1}^N X_i \right)^2 \right]} \quad (18)$$

$$\Sigma = \frac{1}{N-1} \left\{ \sum_{i=1}^N X_i X_i^T - \frac{1}{N} \left( \sum_{i=1}^N X_i \right) \cdot \left( \sum_{i=1}^N X_i \right)^T \right\} \quad (19)$$

APPENDIX A  
DESCRIPTIONS OF THE SUBROUTINES OF AGAST

## APPENDIX A

DESCRIPTIONS OF THE SUBROUTINES OF AGAST<sup>a</sup>

## AEG (Analytic Ephemeris Generator)

Purpose: To propagate analytically state vectors to a specified time

Called by: AFLPN, AGSRR, AMAIN, BUTTON, CFAEG5, COEDH, COMDKI, DELTAV, ENCKE, FILTER, INPUT, JOCDH, LOPC, MANEUV, ONR, PCA, PMISS, PROPAG, REPLAC, RTCCSI, TARGET, TAUAL, TCONE, TILL, TIMAL, TIMFAL, TPASS, UPDATV

Input: ELE, CART, SPHERE,  $T_{SEC}$ ,  $K_{REF}$ ,  $L_1$ ,  $L_2$ , KORIN, KOROUT,  $I_{SET}$ ,  $I_{WRAP}$ ,  $K_1$

Output: ELE, CART, SPHERE

Comments: Subroutine AEG in AGAST is a driver which advances state vectors by use of the earth analytic ephemeris generator (ref. 8) or the lunar analytic ephemeris generator (ref. 9). The  $K_{REF}$  flag indicates whether the earth or lunar potential is to be used.

## AFLPN (Ascent Flight Plan Routine)

Purpose: To compute the desired lift-off time, the ascent targets, and the inertial position and velocity of the actual and estimated landing sites at lift-off time

Called by: AMAIN, INPUT2

Input:  $H_A$ ,  $H_P$ ,  $\theta_{INS}$ ,  $L_{SA}$ ,  $L_{SE}$ ,  $\Sigma_{LSA}$ ,  $\Sigma_{LSE}$ ,  $\delta\chi_{LSA}$ ,  $\delta\chi_{LSE}$ ,  $\phi_D$ ,  $T_{EVENT}$

Output:  $X_A$ ,  $X_E$ ,  $T_{LO}$ ,  $R_{DD}$ ,  $V_R$ ,  $V_H$

---

<sup>a</sup>Symbols used in this appendix are defined in appendix C.



# AGS (Abort Guidance System)

Purpose: To simulate the onboard AGS guidance routines

Called by: MANEUV, TARGET

Input: See maneuver input defined in reference 5

Output: Either maneuver targets, if used by TARGET for targeting, or thrust direction and magnitude, if used by MANEUV for guidance

Comments: See sections 6.3.7 and 7.19 to 7.30 of reference 4

## AGSAG

Purpose: To simulate 2-second integration step of the AGS average-g method of propagation of LM state (either powered or coasting flight)

Called by: AGSKEP, MANEUV

Input:  $\bar{r}(t)$ ,  $\bar{v}(t)$ ,  $\bar{\Delta v}$

Output:  $\bar{r}(t+2)$ ,  $\bar{v}(t+2)$

Comments: See sections 6.3.4 and 7.13 of reference 4

## AGSKEP

Purpose: To propagate AGS LM and CSM state vectors during coasting flight

Called by: FILTER, MANEUV, PROPAG, TARGET

Input:  $\bar{r}(t)$ ,  $v(t)$ ,  $\bar{r}_c(t)$ ,  $\bar{v}_c(t)$ ,  $\Delta t$

Output:  $\bar{r}(t+\Delta t)$ ,  $\bar{v}(t+\Delta t)$ ,  $\bar{r}_c(t+\Delta t)$ ,  $\bar{v}_c(t + \Delta t)$

## AGSRR

Purpose: To simulate AGS rendezvous radar tracking and updating of AGS LM state vector

Called by: AMAIN

Comments: Present program uses G-mission tracking schedule

## ALDENS

Purpose: To compute atmospheric density for use in subroutine DRAG

Called by: DRAG

Comments: See reference 8

## ALIGN

Purpose: To compute the REFSMMAT [T] for the desired alinement and initialize the platform errors associated with the alinement

Called by: AMAIN

Input:  $T_{EVENT}$ ,  $L_{EN}$ ,  $I_{COM}$ ,  $I_{VEH}$ ,  $I_{PE}$ , alinement option flag

Output: [T]

Comments: See references 2 and 3 for a discussion of the different types of IMU alinement

## AMAIN

Purpose: This routine is the main driver for the AGAST program

Comments: The logic of AMAIN calls the input routines, the routines which initialize the state vectors for the monitored computers, and the routines which simulate the mission events. The Monte Carlo loop is controlled from the main program. State vectors and

other pertinent data for the reference points are written on tape unit 13 by AMAIN. When the Monte Carlo simulation is complete, AMAIN calls up the statistical processor PROCES to generate sample means, standard deviations, and covariance matrices for state vectors and maneuver parameters of the reference points.

#### AMATRX

Purpose: To compute  $[A]$ , the rotation matrix from the Besselian reference system to Greenwich true of date coordinates

Called by: INPUT

Input:  $B_{\text{YEAR}}$ ,  $B_{\text{MONTH}}$ ,  $B_{\text{DAY}}$

Output:  $[A]$

Comments: The subroutine first computes the Julian date of the nearest Besselian year as described in reference 10; then subroutines MANGLE, NUTE, and PRESS are used to compute the data needed to obtain  $[A]$ .

#### ANOM

Purpose: To compute mean anomaly from true anomaly

Called by: AEG, CONVRT

Input:  $e$ ,  $\theta$

Output:  $M$

#### APSIDE

Purpose: To compute the apocynthion and pericynthion radii and the eccentricity of an orbit defined by input

Called by: CFP

Input:  $\bar{R}_1$ ,  $\bar{V}_1$

Output:  $R_A, R_P, e$

Comments: See section 5.5.14 of reference 3

#### ASCENT

Purpose: On each guidance cycle, to update the thrust direction which will insert the LM into the desired orbit. This program is used for ascent from the lunar surface or for aborts from powered descent.

Called by: MANEUV

Input:  $X_E, \Delta T_{TO}, X_A, A_{TM}, \tau, V_E, R_{DD}, Y_{DD}, \bar{X}_{DD}, I_{FPC}, I_{FLUP}$

Output:  $\bar{U}_T, T_{GO}, \Delta \bar{V}_G$

Comments: This subroutine is an engineering simulation of the logic described in section 5.3.5 of reference 3

#### AVEG (Onboard Powered Flight Integrator)

Purpose: To propagate estimated state during powered flight

Called by: MANEUV

Input:  $\bar{R}(T), \bar{V}(T), \Delta T$

Output:  $\bar{R}(T+\Delta T), \bar{V}(T+\Delta T)$

Comments: See section 5.3.2 of reference 3

#### AVGOBL

Purpose: To compute the gravity vectors used by subroutine AVEG

Called by: AVEG, MANEUV

Input:  $\bar{R}$

Output:  $\bar{g}, \bar{g}_b$

Comments: See section 5.3.2 of reference 3

#### BUTTON

Purpose: To control logic for the targeting computations for the  $N_{CC}$  and  $N_{SR}$  maneuvers

Called by: TARGET

Comments: See reference 11 for a discussion of the logic of BUTTON

#### CATIME

Purpose: Driver logic for the computation of a table of times of CSM closest approach to the landmarks to be tracked

Called by: UPDATV

Input:  $N_{LM}, \{\phi_i, \lambda_i\}_{i=1}^{N_{LM}}$

Output:  $N_{TOTAL}, T_{TRK}$  - Table

#### CBA

Purpose: To compute the accelerometer misalignment matrix for the indicated computer

Called by: ALIGN

Input:  $I_{COM}$ , accelerometer  $\epsilon$ -array

Output:  $[B]$  for the indicated computer

## CDFUNC

Purpose: To compute a cumulative distribution function table for a sample array of a random variable (such as total fuel consumed)

Called by: PROCES

Input:  $K, N, \{X_j\}_{j=1}^N$

Output:  $\{p_i\}_{i=1}^K$

Comments: The output array is computed as follows.

$p_i = \text{probability that } X < X_{\min} + i \cdot \Delta X$

## CFAEG5

Purpose: Logic required to compute conic fit two-impulse rendezvous solutions based on the analytic ephemeris generator and a Lambert targeting routine

Called by: BUTTON, TURNUP

Comments: See reference 9

## CFP (Concentric Flight Plane Routine)

Purpose: To compute the CSI and CDH maneuvers by use of the onboard targeting logic

Called by: TARGET

Input for CSI:  $T_{\text{CSI}}, T_{\text{TPI}}, E_L, N_{\text{CDH}}, I_{\text{VEH}}$ ; for CDH:  $T_{\text{CDH}}, T_{\text{TPI}}, E_L, I_{\text{VEH}}$

Output:  $\bar{A}V_{\text{CSI}} \text{ (LV)}, \bar{A}V_{\text{CDH}} \text{ (LV)}, T_{\text{CDH}}$

Comments: See programs P32 and P33 described in section 5.4.2 of reference 3

## COE

Purpose: This routine consists of the coelliptic orbit equations which compute the orbital parameters of an orbit that is coelliptic to an input orbit and separated from the input orbit by  $\Delta H_{CDH}$ .

Called by: SOR

Input:  $\Delta H_{CDH}$ ,  $a_J$ ,  $V_{V,J}$ ,  $\bar{R}_J$ ,  $\bar{V}_J$

Output:  $\bar{R}_I$ ,  $\bar{V}_I$

## COEDH

Purpose: To compute the targeting for the  $N_{SR}$  maneuver:  $\Delta \bar{V}$  required and coelliptic orbital elements

Called by: RTCCSI, TARGET

Comments: See reference 13

## COMDKI

Purpose: To use modified CSI/CDH targeting logic to compute DK I maneuvers for the following four sequences:  $N_{C1-N_{SR}}$ ;  $N_{C1-N_H-N_{SR}}$ ;  $N_H-N_{C1-N_{SR}}$ ;  $N_H-N_{SR}$ .

Called by: TARGET

Input:  $K_{TARG}$ ,  $I_{TEV}$ ,  $TH_{CL}$ ,  $\Delta T_{CL}$ ,  $N_1$ ,  $N_2$ ,  $N_3$ ,  $T_{N1}$ ,  $T_{N2}$ ,  $T_{N3}$ ,  $L_{EN}$ ,  $X_{E,I}$ ,  $X_{E,J}$ ,  $X_{A,I}$ ,  $X_{A,J}$

Output:  $\Delta \bar{V}_1$ ,  $\Delta \bar{V}_2$ ,  $\Delta \bar{V}_3$ ,  $T_{N1}$ ,  $T_{N2}$ ,  $T_{N3}$

Comments: A general discussion of the four maneuver sequences targeted by COMDKI is presented in reference 14

## COMMPT

Purpose: To load and display the mission plan table

Called by: AMAIN

Input:  $T_{EX}$ ,  $\overline{\Delta V}_{EX}$ , SAVMAN array

Output: Mission plan table display

## CONIC

Purpose: To propagate state vectors by use of the universal variable formulation of Kepler's equation

Called by: CFP, DESCNT, ENCKE, MIDCRS, PRETPI, TRITPM

Comments: Conic is equivalent to the Kepler subroutine of section 5.5.5 of reference 2

## CONVRT

Purpose: To convert input vectors to a form suitable for use by the AEG

Called by: INPUT

Input:  $X$ ,  $I_{SET}$ ,  $I_{CON}$

Output: ELE, CART, SPHERE

## COVTAB

Purpose: Initially to store input covariance matrices and subsequently reset those matrices when commanded by the logic of the program

Called by: INCOV, REPLAC



Input:  $I_{TYPE}$ ,  $K_D$ ,  $I_{COV}$ ,  $I_{ROT}$ ,  $\Sigma$

Output:  $\Sigma$

#### CPEM

Purpose: To compute the platform misalignment rotation matrix for the indicated computer

Called by: AGSRR, ALIGN, MANEUV, PERRO, UPDATV

Input:  $I_C$ ,  $T_A$ ,  $\theta_{x,o}$ ,  $\theta_{y,o}$ ,  $\theta_{z,o}$ ,  $\dot{\theta}_x$ ,  $\dot{\theta}_y$ ,  $\dot{\theta}_z$

Output:  $[P(t)]$

#### CROSP (Onboard Cross Product Steering Routine)

Purpose: To compute the burn  $T_{GO}$  and compute the commanded turning rate for each guidance cycle

Called by: MANEUV

Input:  $\bar{V}_G$ ,  $\bar{U}_{TA}$ ,  $K_{STEER}$ ,  $I_{VEH}$ ,  $\bar{\Delta V}$ ,  $\Delta T_{TAIL-OFF}$

Output:  $\bar{U}_{TD}$ ,  $\bar{W}_C$ ,  $T_{GO}$ ,  $K_{STEER}$

Comments: Section 5.3.3 of reference 3 contains a discussion of cross-product guidance

#### CROSS

Purpose: To cross two input vectors  $\bar{a}$  and  $\bar{b}$  and output the product  $\bar{c}$ .

## DELTAV

Purpose: To perform impulsive simulation of a maneuver

Called by: MANEUV

Input:  $I_{PASS}$ ,  $T_{DV}$ ,  $X_{E,I}$ ,  $\Delta \bar{V}_{LV}$ ,  $L_{EN}$ ,  $I_{COM}$ ,  $X_{A,I}$

Output:  $X_{E,I}$ ,  $X_{A,I}$

Comments: This routine is used both to simulate a burn impulsively and to perform the target  $\Delta V$  operations of the onboard computers

## DESCNT

Purpose: To update the thrust magnitude and thrust direction every 2 seconds which will guide the LM to a desired landing site. This is the powered descent guidance program.

Called by: MANEUV

Input:  $X_E$ ,  $W_T$ ,  $I_{phase}$ ,  $[T]$ ,  $\bar{R}_{LS}$

Output:  $\bar{U}_T$ ,  $T_{GO}$ ,  $PDI$ ,  $F_c$ ,  $I_{sp}$

Comment: This subroutine is an engineering simulation of part of the logic in section 5.3.4 of reference 3. It does not include a simulation of the landing radar or of any body oriented displays.

## DINCP1

Purpose: To compute the navigational Kalman filter parameters and compute the correction to be made to the state vector

Called by: DMESIP

Input:  $J_D$ ,  $\bar{\alpha}^2$ ,  $\bar{b}_1$ ,  $\bar{b}_2$ ,  $\bar{b}_3$ ,  $[W]$

Output:  $a$ ,  $[Z]$ ,  $[\Omega]$ ,  $[\delta X]$

Comments: This subroutine corresponds to INCORP1 as described in section 5.2.3 of reference 3.

In the DINCP1 flow chart of appendix B, the W-matrix is partitioned as follows.

$$[W] = \begin{pmatrix} W_1 & \vdots & W_2 & \vdots & W_3 \\ \hline W_4 & \vdots & W_5 & \vdots & W_6 \\ \hline W_7 & \vdots & W_8 & \vdots & W_9 \end{pmatrix}$$

DINCP2

Purpose: To update the W-matrix

Called by: DMESIP

Input:  $\bar{\alpha}^2$ ,  $J_D$ ,  $[Z]$ ,  $[W]$

Output:  $[W]$

Comments: This subroutine corresponds to INCORP2 as described in section 5.2.3 of reference 3.

The W-matrix of the DINCP2 flow chart of appendix B is partitioned as follows.

$$[W] = \begin{pmatrix} \bar{W}_1 & \bar{W}_2 & \dots & \bar{W}_9 \\ \bar{W}_{10} & \bar{W}_{11} & \dots & \bar{W}_{18} \\ \bar{W}_{19} & \bar{W}_{20} & \dots & \bar{W}_{27} \end{pmatrix}$$

DMESIP

Purpose: Utility routine which calls DINCP1 and DINCP2 to compute the correction to the state vector and subsequently update the state vector

Called by: ONR, RNR, RR

Input:  $LM_{UP}, X_{E,1}, X_{E,2}, \bar{\delta}_1, \bar{\delta}_2, \bar{v}_1, \bar{v}_2, \delta\beta_E, \delta\theta_E$

Output:  $X_{E,1}, X_{E,2}, \bar{\delta}_1, \bar{\delta}_2, \bar{v}_1, \bar{v}_2, \delta\beta_E, \delta\theta_E$

#### DMTMPY

Purpose: To compute the double precision product [C] of the double precisioned m by n matrix [A] and the double precisioned n by p matrix [B]

Called by: AMATRX

Input: [A], [B], m, n, p

Output: [C]

Comments: [C] is computed by

$$C_{ij} = \sum_{k=1}^n a_{ik} b_{kj}$$

#### DOI (Descent Orbit Insertion Routine)

Purpose: To compute the descent orbit insertion maneuver

Called by: TARGET

Input:  $T_{EVENT}, \bar{X}_{LS}$

Output:  $T_{EX}, \bar{\Delta V}_{EX}$

Comments: See subroutine LLTPR of reference 15

#### DOT

Purpose: To compute the dot product of two vectors

## DRAG

Purpose: To compute the effects of atmospheric drag on a state vector propagated through a given time interval by the earth AEG

Called by: ESAEG

Comments: See reference 8

## ELPRE

Purpose: To propagate AGS state vectors in AGS guidance routine by use of Keplerian motion

Called by: AGS, AGSKEP

Comments: See figure 7.33 of reference 4

## ENCKE (Onboard Coasting Integrator)

Purpose: To propagate estimated state vectors during coasting flight

Called by: CFP, DOI, INITV, LAMAIM, MANEUV, MIDCRS, ONR, PRETPI, PROPAG, QRDTP1, RNR, RR, SOR, SPLIT, TARGET, UPDATV

Input: ELE, CART, SPHERE,  $T_{SEC}$ ,  $L_1$ ,  $L_2$ ,  $I_{SET}$ , KORIN, KOROUT,  $K_1$

Output: ELE, CART, SPHERE

Comments: Subroutine ENCKE is the AGAST simulation of the onboard coasting integrator for the CMC and the LGC (section 5.2.2 of ref. 3)

## EPERT

Purpose: To compute the perturbing acceleration caused by planetary oblateness

Called by: RUNGA

Input:  $x, y, z, \mu, J_2, J_3, J_4, J_{22}, J_{31}, K_{REF}$

Output:  $x, y, z$

#### ERRSXT

Purpose: To compute the error matrix for the unit vector that represents the sextant alinement to a landmark and then rotate the true unit vector through the error matrix to obtain an errored unit vector

Called by: UPDATV

Input:  $\bar{U}_{SXT}, \delta_{SXT_x}, \delta_{SXT_y}, \delta_{SXT_z}, \sigma_{SXT_x}, \sigma_{SXT_y}, \sigma_{SXT_z}$

Output:  $\bar{U}$

#### ESAEG (Earth AEG)

Purpose: To propagate a state vector in earth orbit

Called by: AEG

Comments: See reference 8

#### ETOXYZ

Purpose: To convert Keplerian orbit elements to Cartesian elements

Called by: AEG, ENCKE

Input:  $a, e, i, g, h, M$

Output:  $\bar{R}, \bar{V}$

## EXDV

Purpose: To compute the initial velocity-to-be-gained vector for an external  $\Delta V$  guided maneuver

Called by: MANEUV

Input:  $\bar{R}$ ,  $\bar{V}$ ,  $\bar{\Delta V}_{LV}$ ,  $F$ ,  $W_E$

Output:  $\bar{V}_G$

Comments: See section 5.3.3.3.1 of reference 3 for a discussion of external  $\Delta V$  prethrust computations

## FILTER

Purpose: To simulate the onboard AGS rendezvous radar filter which updates the LM state vector

Called by: AGSRR

Comments: See figures 7.16 through 7.19 of reference 4

## GEOMET (Geometric Parameters Routine)

Purpose: To compute various parameters defined from two input vectors

Called by: LAMBRT, PARAM

Input:  $\bar{n}_1$ ,  $\bar{n}_2$

Output:  $n_1, n_2$ ,  $\bar{U}_{n_1}$ ,  $\bar{U}_{n_2}$ ,  $\cos \phi$ ,  $\sin \phi$ ,  $\bar{N}$ ,  $\bar{U}_N$

Comments: This subroutine is documented in section 5.5.10 of reference 3

## GMATRX

Purpose: To compute the product [C] of the m by n matrix [A] and the n by p matrix [B]

Called by: (General utility routine)

Input: [A], [B], m, n, p

Output: [C]

Comments: [C] is computed by

$$C_{ij} = \sum_{k=1}^n a_{ik} b_{kj}$$

## GMTIME

Purpose: To convert days, hours, minutes, and seconds to seconds and vice versa

Called by: COMMPT, DESCNT, INPUT1, OUTPUT

## GUESS

Purpose: To compute an optimum solution for the  $N_{CC} - N_{SR}$  sequence

Called by: TURNUP

Comments: The iterative technique used in GUESS is documented in reference 16. There is no detailed flow chart for this routine.

## INCOV

Purpose: Input routine for those matrices whose dimension is a multiple of six

Called by: INPUT1, INPUT2

Input:  $K_D$



## INITV (Initial Velocity Routine)

Purpose: To compute the velocity required to intercept a specified point in space at a specified time

Called by: LAMAIM, MIDCRS, PRETPI, SOR, VTBG

Input:  $\bar{R}$ ,  $\bar{V}$ ,  $\bar{R}_T$ ,  $T_2$ ,  $E$ ,  $N_1$

Output:  $\bar{V}_T$ ,  $\bar{R}_{T_2}$

Comments: This subroutine is discussed in section 5.5.11 of reference 3

## INPUT

Purpose: Routine for the reading of the base date and reference state(s) into the program and the computation of the A-matrix or initialization of the ephemeris tape

Called by: INPUT1

Input:  $K_{REF}$ ,  $L_1$ ,  $L_2$

Output:  $T_R$ ,  $\bar{X}_R$ , Base Date

## INPUT1

Purpose: Routine for the reading of program initialization data

Called by: AMAIN

Comments: See reference 5 for a detailed description of the initialization input

## INPUT2

Purpose: Routine for the reading of the event package input for each event to be performed

Called by: AMAIN

Comments: See reference 5 for a detailed discussion of the event package input

## INRTCC

Purpose: To read the RTCC vector package

Called by: INPUT

Input:  $I_{VEH}$

Output:  $\bar{X}_R, T_R$

## ITRATE

Purpose: To determine the zero of a monotonically increasing function or the minimum of a function whose first derivative is single valued in the desired range

Called by: CONIC, LAMBRT

Comments: See section 5.5.10 and figure 5.10-3 of reference 2

## JDATE

Purpose: To compute the Julian date corresponding to the base date

Called by: PRESS

Input:  $B_{YEAR}, B_{MONTH}, B_{DAY}$

Output:  $T_{JC}, T_{JD}$

## JOC DH

Purpose: To compute the CDH time slip required to hold TPI time fixed

Called by: TARGET

Input:  $K_{NSR}$ ,  $T_{NSR}$ ,  $T_{TPI}$ ,  $\epsilon_D$

Output:  $K_{NSR}$ ,  $T_{SAVE}$

## JP LE PH

Purpose: To compute the lunar libration matrix [PNL] and the positions of the sun and moon with respect to the earth

Called by: PWVCON, TAPEUP, TCONE, TILL, TRANCO

Comments: See reference 17

## KEP (Kepler Equation Routine)

Purpose: To compute the transfer time in a Keplerian orbit for a given value of the universal variable  $\chi$

Called by: CONIC, LAMBRT, TIMEP

Input:  $C_1$ ,  $C_2$ ,  $\chi$ ,  $\zeta$ ,  $\bar{R}$

Output:  $T_{21}$ ,  $C(\zeta)$ ,  $S(\zeta)$

Comments: See reference 2, pages 5.5-42 and 5.5-47

## LAMA IM

Purpose: To compute the initial  $\bar{V}_G$  for a Lambert guided maneuver

Called by: MANEUV

Input:  $T_1$ ,  $T_2$ ,  $T_{IG}$ ,  $\bar{R}_T$ ,  $\bar{R}$ ,  $\bar{V}$

Output:  $\bar{V}_G$

Comments: See reference 2, pages 5.3-23 to 5.5-26

#### LAMB

Purpose: To solve for the two-body initial velocity given the initial and final position vectors and a transfer time between the two

Called by: CFAEG5

Comments: LAMB is essentially equivalent to the LAMBERT subroutine of section 5.5.6 of reference 2 with the exception that multiple revolution transfer trajectory capability has been added.

#### LAMBRT

Purpose: To simulate the onboard Lambert program which computes the targeting for a two-impulse rendezvous solution

Called by: INITV

Comments: This subroutine is discussed fully in section 5.5.6 of reference 3

#### LOPC (CSM Lunar Orbit Plane Change Routine)

Purpose: To compute a maneuver to place the landing site in the CSM orbital plane at lift-off time

Called by: TARGET

Input:  $T_{EVENT}$ ,  $\bar{X}_{LS}$

Output:  $T_{EX}$ ,  $\bar{\Delta V}_{EX}$

Comments: See reference 18.

## LSAEG (Lunar AEG)

Purpose: To propagate analytically the state vector of a vehicle in lunar orbit

Called by: AEG

Comments: Two versions of the LSAEG are used in AGAST. See reference 9 for the triaxial version and reference 19 for the generalized version.

## LSALGN (Lunar Surface and Landing Site Alinement Routine)

Purpose: To compute the REFSMMAT [T] for a lunar surface alinement

Called by: ALIGN

Input:  $\bar{R}_{LS}$ ,  $\bar{H}$

Output: [T]

Comments: See reference 2, page 5.6-54

## LVLHDX

Purpose: One route converts a state vector increment from LV coordinates to BR coordinates and adds the increment to the input state vector; the other route converts a state vector increment from BR to LV coordinates

Called by: REPLAC, SAMPLE

Input:  $\bar{R}_O$ ,  $\bar{V}_O$ ,  $\Delta\bar{R}$ ,  $\Delta\bar{V}$

Output:  $\bar{R}$ ,  $\bar{V}$

## MANEUV

Purpose: To perform powered flight maneuvers

Called by: AMAIN

Input: See reference 5 for maneuver event input

Output: Actual and estimated state vectors after the maneuver

Comments: See section 5.3 of references 2 and 3

## MANGLE

Purpose: To calculate various parameters relating to the orbits of the sun and moon which are used by subroutines AMATRX, NUTE AND PRESS

Called by: AMATRX

Comments: See reference 20

## MATRIX

Purpose: To multiply a three dimensioned vector  $\bar{B}$  by a 3 by 3 matrix  $[A]$

Called by: (General utility routine)

Input:  $[A]$ ,  $\bar{B}$

Output:  $\bar{C}$

## MDOT

Purpose: To compute the velocity of a point on the moon caused by lunar rotation

Called by: TRANCO

Comments: See reference 21

## MIDCRS

Purpose: To compute the terminal phase midcourse maneuver and the direct intercept maneuver

Called by: TARGET

Input:  $T$ ,  $T_2$ , active vehicle number

Output:  $\bar{\Delta V}_{EX}$

Comments: See program P35 of reference 2 or 3 (section 5.4.25)

## MTRP

Purpose: To transpose an  $m$  by  $n$  matrix  $[A]$

Called by: (General utility routine)

Input:  $[A]$ ,  $m$ ,  $n$

Output:  $[A]^T$

## NEWT

Purpose: To perform a fifth-order Newton interpolation on the data from the JPL ephemeris

Called by: JPLEPH

Comments: See reference 17

## NUTE

Purpose: To compute the earth nutation terms needed in subroutine AMATRX

Called by: AMATRX

Comments: See reference 20

## OBS

Purpose: To produce tracking data that simulates the observations of the RR and SXT; to incorporate the tracking equipment error models into the computations of measurements

Called by: UPDATV

Input:  $\bar{R}_{REL}$ ,  $\bar{V}_{REL}$ ,  $[T_A]$ ,  $[SMNB]$ ,  $\sigma_{N_R}$ ,  $\sigma_{N_{\dot{R}}}$ ,  $\sigma_{N_\beta}$ ,  $\sigma_{N_\theta}$ ,  $R_{BIAS}$ ,  $\delta R$ ,  $\delta \dot{R}$ ,  $\delta \beta$ ,  $\delta \theta$ ,  $\sigma_{N_{VHF}}$ ,  $VHF_{BIAS}$ ,  $\delta R_{VHF}$ ,  $\delta_{SXT_x}$ ,  $\delta_{SXT_y}$ ,  $\delta_{SXT_z}$ ,  $\sigma_{SXT_x}$ ,  $\sigma_{SXT_y}$ ,  $\sigma_{SXT_z}$

Output:  $R_A$ ,  $\dot{R}_A$ ,  $\beta_A$ ,  $\theta_A$ ,  $R_M$ ,  $\dot{R}_M$ ,  $\beta_M$ ,  $\theta_M$ ,  $\bar{U}_{REL}$ ,  $\bar{U}_{SXT}$

## ONR

Purpose: To accept simulated optics data and perform navigational updates to the CSM vector and the landmark radius vector

Called by: UPDATV

Input:  $X_E$ ,  $I_{known}$ ,  $L$ ,  $K_{RNDFG}$ ,  $N$ ,  $\bar{U}_{NB}$ ,  $[T]$ ,  $[NBSM]$ ,  $\phi$ ,  $\lambda$ ,  $h_{LS}$ ,  $[W_{LRV}]$ ,  $[W_{UNL}]$ ,  $\bar{X}_{KL}$ ,  $VAR_{IMU}$ ,  $VAR_{SCT}$ ,  $VAR_{INT}$ ,  $[W]$

Output:  $X_E$ ,  $[W]$

Comments: Subroutine ONR is an engineering simulation of the logic described in section 5.2.5.2 of reference 2.

The W-Matrix of the ONR flowchart of appendix B is partitioned as follows.

$$[W] = \begin{pmatrix} W_1 & \vdots & W_2 & \vdots & W_3 \\ \text{---} & \vdots & \text{---} & \vdots & \text{---} \\ W_4 & \vdots & W_5 & \vdots & W_6 \\ \text{---} & \vdots & \text{---} & \vdots & \text{---} \\ W_7 & \vdots & W_8 & \vdots & W_9 \end{pmatrix}$$



## OPS

Purpose: To compute orbital parameters  $r$ ,  $\alpha$ ,  $n$ ,  $c$ ,  $s$  for use by subroutine ELPRE

Called by: AGS, AGSKEP

Comments: See figure 7.33 of reference 4

## ORD

Purpose: To order the table  $T_{TRK}$  in an ascending sequence

Called by: CATIME

Input:  $N_{TOTAL}$ ,  $T_{TRK}$ -Table,  $K_{TRK}$ -Table

Output:  $T_{TRK}$ -Table,  $K_{TRK}$ -Table

## OUTPUT

Purpose: Display routine for the orbital parameters of the reference state vector

Called by: INPUT1

Input: Reference state vector

Output: Printed display

## PALIGN (Preferred Alinement Routine)

Purpose: To calculate the desired alinement for powered flight maneuvers

Called by: ALIGN, TRIM, ULLDIR

Input:  $\bar{R}$ ,  $\bar{V}$ ,  $\bar{U}_{TD}$

Output: [T]

Comments: See reference 2, pages 5.6-53

#### PARAM

Purpose: To compute various orbital parameters for use in other routines

Called by: APSIDE, TIMEP

Input:  $\bar{R}$ ,  $\bar{V}$

Output:  $\cot \gamma$ ,  $C_3$ ,  $\alpha_N$ ,  $P_N$

Comments: See reference 2, pages 5.5-43

#### PCA

Purpose: To compute the time and distance of closest approach between two vehicles

Called by: MANEUV

Input: vehicle state vectors

Output:  $T_{CA}$ ,  $D_{CA}$

#### PERRO

Purpose: To simulate the effects of platform and accelerometer errors on the  $\Delta \bar{V}$  sensed by the systems

Called by: MANEUV

Input:  $L$ ,  $I_{COM}$ ,  $\Delta \bar{V}_A$ ,  $[B_C]$ ,  $[B_P]$ ,  $[B_A]$ , REFSMMAT,  $[A(t)]$ , scale factors, accelerometer read biases

Output:  $\Delta \bar{V}_E$ ,  $[P(t)]$

## PMATRIX

Purpose: To compute the rotation matrix from basic reference coordinates to the vehicle platform for various platform alinements

Called by: AFLPN, ALIGN, COMDKI, DELTAV, LOPC, LVLHDX, MANEUV, REPLAC, RNRPRT, SANDIF, TPITPM

Input:  $\bar{R}$ ,  $\bar{V}$  option flag

Output: [T]

## PMISS

Purpose: To advance the LM and CSM AEG states to  $T_{TPI}$  and to compute the phase angle discrepancy

Called by: COMDKI

Input:  $\epsilon_D$ ,  $T_{TPI}$

Output:  $\Delta\theta$

Comments: The desired phase angle at TPI is defined as that phase angle which produces an elevation angle  $\epsilon_D$ . The phase angle discrepancy  $\Delta\theta$  is then the difference between the desired phase angle  $\theta_D$  and the phase angle  $\theta_{TPI}$ .

## PRESS

Purpose: To compute the earth precession term required by AMATRIX

Called by: AMATRIX

Comments: See reference 20

## PRETPI

Purpose: To compute the terminal phase initiation maneuver

Called by: CFP, TARGET

Input:  $T_{TPI}$ ,  $E_L$ ,  $\omega t$ , active vehicle number

Output:  $T_{TPI}$ ,  $\bar{\Delta V}_{EX}$

Comments: See program P34 of reference 2, pages 5.4-22 to 5.4-27

## PROCES

Purpose: To read the Monte Carlo data on the output tape and process those data to generate sample means, standard deviations, and covariance matrices

Called by: AMAIN, XMAIN

Input:  $I_{SAVE}$ ,  $N_{SAM}$ ; for each reference point, the following parameters are read from the data tape (maneuver parameters are not read for nonmaneuver events)

- a. Reference state vectors and time
- b. Reference maneuver  $\Delta V$  burned
- c. Sample state vectors and times
- d. Sample maneuver  $\Delta \bar{V}$  targeted
- e. Sample maneuver  $\Delta V$  burned
- f. Sample maneuver burn time  $\Delta T_B$
- g. Sample maneuver residual  $\Delta V$
- h. Sample maneuver trimmed  $\Delta V$
- i. The XTRA array
- j. The SAVMAN array

Output: Statistics are printed

## PROPAG

Purpose: To propagate actual and estimated state vectors to a given time

Called by: AMAIN, DELTAV, SPLIT, TARGET, UPDATV

Input:  $I_{COM}$ ,  $I_{NOMT}$ ,  $I_{PASS}$ ,  $L_{EC}$ ,  $L_{EN}$ ,  $T_{EVENT}$ ,  $T_{START}$ ,  $T_{STOP}$ ,  $I_{WMATRIX}$

Output: Advanced state vectors

#### PWVCON

Purpose: To perform various vector transformations needed by LSAEG

Called by: LSAEG

Comments: See reference 9

#### QRDTPI

Purpose: To compute the desired phase angle at TPI which corresponds to the desired elevation angle E

Called by: SOR

Input: E,  $\Delta H_{CDH}$ ,  $X_{E,J}$

Output:  $\theta_i$ ,  $\bar{R}'_J$ ,  $\bar{V}'_J$

#### RANDN

Purpose: UNIVAC MATH-PACK routine which generates an array of random numbers that has Gaussian distribution and has a mean and standard deviation approximating a desired input

Called by: RANNO

Input: n,  $x_1$ ,  $\sigma$ ,  $\mu$

Output:  $\{X_i\}_{i=1}^n$

Comments: RANDN accepts an input number  $X_1$  and outputs an array  $\{X_i\}_{i=1}^n$  which approximates a normal distribution with mean  $\mu$  and standard deviation  $\sigma$ . The method of generation is a recursive congruence scheme; that is

$$X_{i+1} = f(X_i) \text{MOD } 2^{27}$$

On each call to RANDN, the first number generated replaces the input  $X_1$ . A detailed explanation of the generating function may be found in references 22 and 23.

#### RANDU

Purpose: UNIVAC MATH-PACK routine that generates an array of random numbers uniformly distributed on the interval  $[0,1]$

Called by: RANNO, TRIM

Input:  $n, y_1$

Output:  $\{y_i\}_{i=1}^n$

Comments: See reference 23 for a description of the equations used in RANDU

#### RANNO

Purpose: To produce an array of pseudorandom numbers

Called by: AMAIN, ERRSXT, OBS, SAMPLE, SETPLT, SETRBS, SETTHR, TRIM

Input:  $n, I_{\text{RAN}}$

Output:  $\{X_i\}_{i=1}^n$

Comments: The UNIVAC MATH-PACK routines RANDN and RANDU are used to generate the random numbers used by the components of the AGAST program. On the first call to RANNO, the UNIVAC 1108 computer clock routine is called upon to obtain the time, which is then

operated on to produce the first input to RANDN. That routine accepts  $X_i$  as the initializing parameter of the random number generation scheme. To decrease the correlation of the initializing parameter on successive calls to RANNO, the current call to that routine operates on the current output array  $\{X_i\}_{i=1}^n$  to produce  $X_{\text{RAN}}$ , which will be the next input to RANDN.

#### RARP

Purpose: To compute the radius of apogee and radius of perigee of an orbit

Called by: MANEUV, OUTPUT

Comments: See reference 24

#### REGFAL (Regula-Falsi Iteration Routine)

Purpose: To obtain a guess at the value of the independent variable in a function that will drive the dependent variable to zero

Called by: PCA, TCONE

Input:  $x$ ,  $f(x)$ ,  $I_{\text{COVNT}}$ ,  $I_{\text{GUESS}}$

Output:  $\Delta x$

Comments: By use of the guess at the independent variable to recompute the dependent variable, REGFAL is recalled for a new guess. This process is continued until convergence is obtained.

#### REPLAC

Purpose: To compute the state vectors which start each cycle through the program and perform vector replacement events

Called by: AMAIN

Input: Initial state vector perturbation data (block B, ref. 5)  
and vector replacement data (blocks EVENT and LEC3, ref. 5)

Output: The desired state vectors

## RNR

Purpose: To accept simulated sextant and VHF observational data and to perform navigational updates to the CMC estimated state vectors

Called by: UPDATV

Input:  $X_{E,I}$ ,  $X_{E,J}$ ,  $\bar{W}_D$ ,  $[W]$ ,  $[T]$ ,  $[NBSM]$ ,  $\Delta R_M$ ,  $\bar{U}_M$ ,  $VAR_{VHF}$ ,  $VAR_{VHFmin}$ ,  
 $VAR_{SXT}$ ,  $VAR_{IMU}$ ,  $VAR_{INT}$ ,  $LM_{UP}$ ,  $I_{PRINT}$ ,  $KRNDFG$

Output:  $X_{E,I}$ ,  $[W]$

Comments: Subroutine RNR is an engineering simulation of the VHF and optical navigational logic described in section 5.2.5.2 of reference 2.

The W-matrix in the RNR flow chart of appendix B is partitioned as follows.

$$[W] = \begin{pmatrix} W_1 & W_2 & W_3 \\ W_4 & W_5 & W_6 \\ W_7 & W_8 & W_9 \end{pmatrix}$$

## RNRPRT

Purpose: To print rendezvous tracking information: actual state vectors, estimated state vectors, tracking observations, filter parameters, and state vector corrections.

Called by: AGSRR, FILTER, ONR, RNR, RR, UPDATV

Input:  $J_F$ ,  $I_P$ ,  $N$ ,  $I_{COM}$

Output: Prints as indicated in the flow chart of RNRPRT in appendix B.



## ROTXYZ

Purpose: To compute a rotation matrix  $[M]$  for the angles  $\theta_x$ ,  $\theta_y$  and  $\theta_z$ ; the rotation is in the x-y-z order

Called by: CPFM, ERRSXT, OBS

Input:  $\theta_x$ ,  $\theta_y$ , and  $\theta_z$

Output:  $[M]$

Comments: The rotation matrix  $[M] = (M_{ij})$  is computed as follows.

$$\begin{aligned} M_{11} &= \cos \theta_z \cos \theta_y \\ M_{12} &= \sin \theta_z \cos \theta_x + \cos \theta_z \sin \theta_y \sin \theta_x \\ M_{13} &= \sin \theta_z \sin \theta_x - \cos \theta_z \sin \theta_y \cos \theta_x \\ M_{21} &= -\sin \theta_z \cos \theta_y \\ M_{22} &= \cos \theta_z \cos \theta_x - \sin \theta_z \sin \theta_y \sin \theta_x \\ M_{23} &= \cos \theta_z \sin \theta_x + \sin \theta_z \sin \theta_y \cos \theta_x \\ M_{31} &= \sin \theta_y \\ M_{32} &= -\cos \theta_y \sin \theta_x \\ M_{33} &= \cos \theta_y \cos \theta_x \end{aligned}$$

## RR

Purpose: To accept simulated rendezvous radar observational data and to perform navigational updates to LGC estimated state vectors

Called by: UPDATV

Input:  $X_{E,I}$ ,  $X_{E,J}$ ,  $\bar{W}_D$ ,  $[W]$ ,  $[T]$ ,  $[SMNB]$ ,  $\Delta R_M$ ,  $\Delta \dot{R}_M$ ,  $\beta_M$ ,  $\theta_M$ ,  $VAR_R$ ,  $VAR_{RMIN}$ ,  $VAR_V$ ,  $VAR_{VMIN}$ ,  $VAR_\beta$ ,  $VAR_{IMU}$ ,  $\delta\beta_E$ ,  $\delta\theta_E$ ,  $LM_{UP}$ ,  $I_{PRINT}$ ,  $I_{ANGLE}$ ,  $KRNDG$

Output:  $x_{E,I}$ ,  $[W]$ ,  $\delta\beta_E$ ,  $\delta\theta_E$

Comments: Subroutine RR is an engineering simulation of the logic described in section 5.2.4.2.2 of reference 3.

The W-matrix of the RR flow chart of appendix B is partitioned as follows.

$$[W] = \begin{pmatrix} w_1 & w_2 & w_3 \\ w_4 & w_5 & w_6 \\ w_7 & w_8 & w_9 \end{pmatrix}$$

RRSMNB

Purpose: To compute the stable member to navigation base rotation matrix for the LM

Called by: AGSRR, UPDATV

Input:  $\Delta\bar{R}$ ,  $\bar{P}$ ,  $[T_A]$

Output:  $[SMNB]$

Comments: The matrix  $[T_A]$  is a transformation from basic reference coordinates to the true platform orientation. The output matrix  $[SMNB]$  represents an orientation of the LM with the z-body axis directed along the relative line of sight to the CSM, the y-body axis directed perpendicular to the plane defined by the LM position vector and the line of sight vector, and with the x-body axis completing a right-handed system.

RTCCSI

Purpose: To compute the concentric sequence initiation maneuver based on the RTCC logic, and to compute the NCl - NH sequence in the DKI maneuver sequences

Called by: COMDKI, TARGET

Input:  $T_{CSI}$ ,  $T_{CDH}$ ,  $T_{TPI}$ ,  $E_L$ ,  $N_{CDH}$ ,  $I_{VEH}$ ,  $L_{EN}$ ,  $\Delta h_D$

Output:  $\bar{\Delta V}_{CSI}$  (LV),  $T_{CDH}$ ,  $\bar{\Delta V}_{CDH}$  (LV)

Comments: The logic of RTCCSI is a combination of the CSI/CDH logic of references 2 and 25

#### RUNGA

Purpose: To integrate the actual state vector through each guidance cycle of a burn and to compute the thrust model used during each guidance cycle of the burn

Called by: MANEUV

Input:  $\bar{R}$ ,  $\bar{V}$ ,  $T_{GO}$ ,  $\bar{U}_{TD}$ ,  $T$ ,  $I$ ,  $I_{ENG}$ ,  $I_{PH}$ ,  $\delta t$ ,  $E_{NO}$ ,  $W$ ,  $L_{EN}$ ,  $K_{TOFF}$ ,  $I_{MDC}$ ,  $V_{FLAG}$ ,  $N_{THROT}$ ,  $K_{UL}$ ,  $F_D$ ,  $I_{SP_D}$ ,  $\bar{\Delta V}_{TOTAL}$ ,  $C_K$ ,  $\theta_{CANT}$ ,  $F_A^*$ ,  $I_{SP_A}^*$ ,  $I_{ME}$ ,  $I_{THRC}^*$ ,  $\Delta T_{BP}^*$

Output:  $\bar{R}$ ,  $\bar{V}$ ,  $\bar{\Delta V}$ ,  $\bar{U}_{TA}$ ,  $T$ ,  $\Delta T_{BURN}$ ,  $I_{PH}$ ,  $W$ ,  $K_{TOFF}$ ,  $K_{UL}$ ,  $\dot{W}$ ,  $\Delta V_{TOTAL}$ ,  $C_K$

#### SAMCOV

Purpose: To accept an array of random dispersions to a state vector and to compute a sample covariance matrix, correlation coefficients, standard deviations of the individual components of the state vector, and standard deviations for the position and velocity

Called by: PROCES

Input:  $\delta X_S$

Output:  $\Sigma$ ,  $\{\sigma_i\}_{i=1}^6$ ,  $\sigma_R$ ,  $\sigma_V$

Comments: The output  $\Sigma$  has in its lower left triangular part the correlation coefficients

## SAMDIF

Purpose: To compute for a reference point the differences between sample arrays of state vectors produced for that reference point. The entries in the table of state vector differences are output in a local vertical coordinate system

Called by: PROCES

Input:  $N, I_{DIF}, X_{R,I_V}, X_{A,1}, X_{A,2}, X_{E,1}, X_{E,2}$

Output:  $\{\delta X_k\}_{k=1}^n$

## SAMPLE

Purpose: To sample a covariance matrix to produce a sample random dispersion of the vector for which the covariance matrix is defined

Called by: AFLPN, REPLAC

Input:  $K_D, \Sigma, X_R$

Output:  $X, \delta X$

Comments: See section 7.1 of this document for a detailed explanation of the sampling technique used in SAMPLE

## SAMSIG

Purpose: To compute sample means and standard deviations for an array of random variables

Called by: PROCES

Input:  $K, N, I_{SIG}, \{ \{X_{ji}\}_{j=1}^n \}_{i=1}^k$

Output:  $\{\delta \mu_i\}_{i=1}^k, \{\sigma_i\}_{i=1}^k$

Comments: The formulation used in SAMSIG is based on derivations in reference 7

## SAVIP2

Purpose: To read the saved data from unit 15 back into the program needed to initialize each cycle and to perform each event

Called by: AMAIN

Input:  $L_{EC}$

Output: The saved INPUT1 data or the saved event package input

## SCTXYZ

Purpose: To convert a position vector in spherical coordinates to Cartesian coordinates

Called by: INPUT1

Input:  $R, \lambda, \phi$

Output:  $x, y, z$

Comments: The conversion is computed as follows

$$x = R \cos \lambda \cos \phi$$

$$y = R \sin \lambda \cos \phi$$

$$z = R \sin \phi$$

## SENSOR

Purpose: To obtain the sensed  $\Delta V$  during each guidance cycle of a maneuver

Called by: RUNGA

Input:  $\bar{R}$ ,  $\bar{U}_{TD}$ ,  $\bar{\omega}_C$ ,  $W$ ,  $\dot{W}$ ,  $F_A$

Output:  $\Delta\bar{V}$ ,  $\bar{U}_{TA}$

Comments: See reference 26

#### SETPC

Purpose: To load the constant array with the proper data depending upon which central body is being considered

Called by: INPUT

Input:  $K_{REF}$

Output:  $\pi$ ,  $R_{REF}$ ,  $\mu$ ,  $J_2$ ,  $J_2$ ,  $J_3$ ,  $J_4$ ,  $J_{22}$ ,  $J_{31}$

#### SETPLT

Purpose: To set the initial platform misalignment angles, gyro drift rates, accelerometer misalignment angles, accelerometer read biases, and accelerometer scale factors

Called by: ALIGN, AMAIN

Input:  $I_{PE}$ ,  $I_{PLTSG}$ ,  $I_{PLTN}$ ,  $\sigma_{ALN}$ ,  $\sigma_{DFT}$ ,  $\sigma_{AAL}$ ,  $\sigma_{DVB}$ ,  $\sigma_S$

Output:  $\theta_{x,o}$ ,  $\theta_{y,o}$ ,  $\theta_{z,o}$ ,  $\dot{\theta}_x$ ,  $\dot{\theta}_y$ ,  $\dot{\theta}_z$ ,  $\epsilon$ -array,  $\Delta\bar{V}_B$ ,  $S$ -array

#### SETRBS

Purpose: To set RR and SXT bias values

Called by: AMAIN

Input:  $\sigma_{\delta R}$ ,  $\sigma_{\delta \dot{R}}$ ,  $\sigma_{\delta \beta}$ ,  $\sigma_{\delta \theta}$ ,  $\sigma_{SXT_x}^B$ ,  $\sigma_{SXT_y}^B$ ,  $\sigma_{SXT_z}^B$ ,  $\sigma_{VHF}^B$

Output:  $\delta R$ ,  $\delta \dot{R}$ ,  $\delta \beta$ ,  $\delta \theta$ ,  $\delta_{SXT_x}$ ,  $\delta_{SXT_y}$ ,  $\delta_{SXT_z}$ ,  $VHF_{BIAS}$ ,  $RBIAS$

### SETTHR

Purpose: To set for each thrust phase of each engine the thrust level and specific impulse which model the actual engine performance

Called by: AMAIN

Input:  $J_1$ ,  $J_2$ ,  $K_1$ ,  $K_2$ ,  $I_{NOMT}$ ,  $I_{THR}$ ,  $F_A^*$ ,  $I_{SPA}^*$

Output:  $F_A$ ,  $I_{SPA}$

### SHORTB

Purpose: To compute an estimated burn time to determine if steering and in the case of the DPS engine if throttling is allowed

Called by: MANEUV

Input:  $I_{VEH}$ ,  $I_{ENG}$ ,  $|\bar{V}_G|$ ,  $ENO$ ,  $W_E$ ,  $\dot{W}_E$

Output:  $K_{STBURN}$ ,  $N_{THROT}$ ,  $T_{GO}$

Comments: See the time-to-go predictor routine in references 2 and 3

### SMEAN

Purpose: To accept an array of state vectors to compute the mean vector of the array, and to compute the magnitude of the mean position vector and the mean velocity vector

Called by: PROCES

Input:  $N$ ,  $\{\delta X_k\}_{k=1}^n$

Output:  $\bar{\mu}$ ,  $\mu_R$ ,  $\mu_V$

## SOR

Purpose: This routine contains the Stable Orbit Rendezvous logic of section 5.4.2.6 of reference 3: targeting for the SOI, SOR, and SOM maneuvers. Also contained in SOR is logic to compute for the active vehicle desired offsets from the passive vehicle at CDH time, and to subsequently compute the SOI and SOR maneuvers to achieve those offsets at CDH and to maneuver into a coelliptic orbit

Called by: TARGET

Input:  $L_{EN}$ ,  $K_{TARG}$ ,  $\delta r$ ,  $\Delta H_D$ ,  $\omega t$ ,  $T$ ,  $X_{E,I}$ ,  $X_{E,J}$ ,  $T_{TPI}$ ,  $\epsilon_D$ ,  $\epsilon_A$

Output:  $\bar{\Delta V}_1$ ,  $\bar{\Delta V}_2$ ,  $T_1$ ,  $T_2$

## SPHELE

Purpose: To compute spherical orbit elements from Cartesian elements and vice versa

Called by: AEG, ENCKE, LSAEG

Comments: See subroutine CONV of reference 17

## SPLIT

Purpose: To call subroutine START to compute the burn time for an external  $\Delta V$  maneuver, then to compute the time of ignition and bias the external  $\bar{\Delta V}$  by one half the finite burn arc

Called by: MANEUV

Input:  $I_{ENG}$ ,  $T_{EX}$ ,  $\bar{\Delta V}_{EX}$ ,  $X_{E,I}$ ,  $E_{NO}$ ,  $F_A^*$ ,  $I_{SP_A}^*$ ,  $\Delta T_{BP_A}^*$

Output:  $\bar{\Delta V}_{EX}$



## START

Purpose: To calculate the thrust ignition time, the burn duration, and the thrust attitude required of the actual maneuver which duplicates the results obtained by a given impulsive maneuver

Called by: SPLIT

Input:  $\Delta V$ ,  $W_T$ ,  $\Delta T_{TO}$ ,  $F$ ,  $\dot{W}$ ,  $\Delta T_{BP}$ ,  $I_{ENG}$

Output:  $\Delta T_{TI}$ ,  $\Delta T_B$ ,  $P$ ,  $Y$

## STAYT

Purpose: To propagate a vector through the time interval  $T_{21}$  by use of Keplerian motion

Called by: CONIC, TIMEP

Input:  $\bar{R}(T_1)$ ,  $\bar{V}(T_1)$ ,  $\chi$ ,  $\xi$ ,  $C(\xi)$ ,  $S(\xi)$ ,  $T_{21}$

Output:  $\bar{R}(T_2)$ ,  $\bar{V}(T_2)$

Comments: See reference 2, pages 5.5-42 and 5.5-48

## TA

Purpose: To compute true anomaly when eccentricity and mean anomaly are given

Called: AEG, ENCKE, ETOXYZ, MANEUV, OUTPUT, RARP

Input:  $e$ ,  $M$

Output:  $\theta$

## TAPEUP

Purpose: To initialize the JPL ephemeris tape

Called by: INPUT

Input: Base date

## TARGET

Purpose: To target all desired maneuvers

Called by: MANEUV

Input: Block EVENT and Block LECI data (see ref. 5)

Output:  $T_{IG}$ ,  $\bar{\Delta V}_{EX}$ ,  $I_{FLAG}$ ,  $I_{SPLIT}$

Comments: The routine has the capability to target the maneuver on the primary computer states and to target each maneuver based on the actual states and on the estimated states of other computers. All the solutions requested for a given maneuver are stored in the SAVMAN array to be used as described in section 6.5.2 of this document.

## TAUAL

Purpose: To compute the time lag and  $\Delta H$  between two orbiting vehicles

Called by: PMISS

Comments: See reference 27 for a discussion of the formulation of subroutine TAUAL

## TCONE

Purpose: To compute the time of closest approach of the CSM to the landing site

Called by: AFLPN

Input: T, vehicle number

Output:  $T_1$

#### THETR

Purpose: To compute the phase angle between two orbiting vehicles

Called by: CFAEG5, JOCDH, MANEUV, PMISS, RTCCSI, TARGET, TAUAL

Input: Orbital elements i, h, and u for both vehicles

Output:  $\theta_R$

Comments: For an explanation of the formulation of THETR, see  
reference 27

#### THRFIL

Purpose: To accept the simulated accelerometer readings and to output  
the acceleration magnitude and  $\tau$

Called by: MANEUV

Input:  $\Delta T$ ,  $\Delta V$ ,  $\tau$ ,  $V_E$

Output:  $a_m$ ,  $\tau$

#### TILL

Purpose: To compute the time of intersection of a spacecraft's  
trajectory with a right circular cone whose vertex is centered in  
the planet

Called by: TCONE

Comments: See reference 28

## TIMAL

Purpose: To determine the arrival time of a spacecraft at a designated counter line

Called by: COMDKI, PMISS, RTCCSI

Comments: A discussion of the formulation of TIMAL occurs in reference 27

## TIMEB

Purpose: To compute the burn time for a maneuver

Called by: START

Input:  $\Delta V$ ,  $W_o$ ,  $\dot{W}$ ,  $g$ ,  $I_{SP}$

Output:  $\Delta T_B$

Comments: The burn time is computed as follows.

$$\Delta T_B = \frac{W_o}{\dot{W}} \left[ 1 - \frac{1}{\text{EXP} \left( \frac{|\Delta V|}{g I_{SP}} \right)} \right]$$

TIMEP (Time-Theta Routine)

Purpose: To compute the time required for a vehicle to pass through an angle  $\theta$  using Keplerian motion

Called by: CFP, LOPC, PRETPI, QRDTPPI, SOR

Input:  $\bar{R}(T_1)$ ,  $\bar{V}(T_1)$ ,  $\theta$

Output:  $T_{21}$

Comments: See the Time-Theta Routine of reference 2, page 5.5-34

## TIMFAL

**Purpose:** To compute the time of arrival of a spacecraft at an upcoming apsis

**Called by:** COMDKI, RTCCSI

**Comment:** This routine is documented in reference 27

## TPASS

**Purpose:** To compute a table of times for which an orbiting vehicle passes within sight of a lunar landmark

**Called by:** CATIME

**Input:**  $T$ ,  $T_{\text{START}}$ ,  $T_{\text{STOP}}$ ,  $\phi_{R,0}$ ,  $\lambda_{R,0}$ ,  $\phi_R$ ,  $\lambda_R$ ,  $H$ ,  $R_{\text{REF}}$ ,  $\bar{R}_{\text{LSA}}$ ,  $X_{A,I}$ ,  $\epsilon_{\text{MIN}}$ ,  $\Delta T_{\text{PASS}}$

**Output:**  $\{T_{\text{SAVE}}(i)\}_{i=1}^N$ ,  $\{\Delta T_{\text{SAVE}}(i)\}_{i=1}^N$

**Comments:** The iterative scheme used in TPASS to compute the closest approach times is documented in reference 29

## TPITPM

**Purpose:** To display the maneuver  $\Delta V$ 's associated with maneuvers that use the onboard Lambert targeting

**Called by:** AGS, MIDCRS, PRETPI, SOR

**Input:**  $T_1$ ,  $T_2$ ,  $\bar{\Delta V}_1$ ,  $\bar{\Delta V}_2$ ,  $R_I$ ,  $V_I$ ,  $R_J$ ,  $V_J$ ,  $I_{\text{PC}}$

**Output:** The Lambert targeting display

## TRANCO

Purpose: To perform transformations of vectors from planetary coordinates to inertial coordinates and vice versa

Called by: AFLPN, ALIGN, DESCNT, DOI, ENCKE, EPERT, LOPC, MANEUV, ONR, TPASS, UPDATV

Input:  $T$ ,  $\bar{X}$ ,  $\bar{V}$ ,  $K_{REF}$ , option flag

Output:  $\bar{X}_R$ ,  $\bar{V}_R$

## TRIM

Purpose: To compute and trim the  $V_G$  residuals caused by initial thrust misalignment and center of gravity offset errors

Called by: MANEUV

Input:  $X_A$ ,  $X_E$ ,  $X_M$ ,  $\bar{U}_{TA}$ ,  $\bar{V}_G$ ,  $I_{EX}$

Output:  $X_A$ ,  $X_E$ ,  $X_M$ ,  $\bar{V}_G$

## TURNUP

Purpose: To compute an optimum  $\Delta V$  two-impulse solution based on the interpolation technique of subroutine GUESS

Called by: BUTTON

Comments: No documentation is available

## ULLDIR

Purpose: Based on its knowledge of the center of gravity location this subroutine calculates the thrust direction during ullage and the initial thrust direction of the main engine after ullage

Called by: MANEUV, RUNGA

Input:  $\bar{U}_{TD}$ ,  $\bar{U}_{TA}$ ,  $X_E$ ,  $W_T$ ,  $I_{VEH}$

Output:  $\bar{U}_{TD}$ ,  $\bar{U}_{TA}$

#### UNIT

Purpose: To compute the unit vector  $\bar{U}$  which corresponds to an input vector  $\bar{a}$

#### UNIVAR

Purpose: To compute the universal parameter  $x$  used by subroutine LAMBRT and TIMEP

Called by: LAMBRT, TIMEP

Comments: See section 5.5.10 of reference 2

#### UPDATV

Purpose: Driver logic for the onboard tracking programs

Called by: AMAIN

Input:  $I_{MARK}$ ,  $L_{EN}$ ,  $\Delta T_{MARK}$ ,  $T_{START}$ ,  $T_{STOP}$ ,  $IVUP$ ,  $[T]$ ,  $I_{PE}$ ,  $I_{GIM}$ ,  $\epsilon_T$ ,  
landing site array,  $X_{E,1}$ ,  $X_{E,2}$ ,  $X_{A,1}$ ,  $X_{A,2}$

Output:  $X_{E,IVUP}$

#### VECMG

Purpose: To compute the magnitude of an input vector  $\bar{a}$

## VTBG (Velocity-To-Be-Gained Routine)

Purpose: To obtain  $\bar{V}_G$  for each guidance cycle of a Lambert guided burn

Called by: MANEUV

Input:  $\bar{R}$ ,  $\bar{V}$ ,  $N$ ,  $N_{MAX}$ ,  $\bar{g}$ ,  $\bar{g}_b$ ,  $\bar{\Delta V}_E$ ,  $T_{IG}$ ,  $\bar{b}\bar{\Delta T}$ ,  $T_2$ ,  $\bar{R}_T$

Output:  $\bar{V}_G$

Comments: See reference 3, section 5.3.3.5

## WMATCN

Purpose: To transform the  $[W]$  used by ONR into a triangular matrix;  
this form is required to propagate  $[W]$  to the next landmark

Called by: ONR

Input:  $[W]$

Output:  $[W]$

## WMT

Purpose: To print the W-matrix, the E-matrix, and the square roots of  
the diagonal of the E-matrix

Called by: RNRPRT

Input:  $\bar{W}_C$ ,  $[BRLOS]$ ,  $I_{PRINT}$

Output: None

Comments: The W-matrix is input to WMT as a column vector with 81 entries,  
 $\bar{W}_C$ . That vector is loaded into the W-matrix array  $[W]$ . The  
E-matrix is computed as  $WW^T$  in LOS coordinates.



## XESTAB

Purpose: To maintain a table of current state vectors for each vehicle of each computer

Called by: AFLPN, AGSRR, ALIGN, AMAIN, COMDKI, DELTAV, MANEUV, PROPAG, REPLAC, TARGET, UPDATV

Input:  $X_E$ ,  $I_{COM}$ ,  $I_{VEH}$

Output:  $X_E$

## XMAIN

Purpose: A driver program which calls subroutine PROCES to process a data tape generated by AGAST on a previous computer run

Input:  $N_{SAM}$ ,  $N_{REF}$

Output: Same as subroutine PROCES

## XYZTOE

Purpose: To convert Cartesian orbit elements to Keplerian orbit elements

Called by: AEG, AGSKEP, CFP, ENCKE, LSAEG, MANEUV

Input:  $\bar{R}$ ,  $\bar{V}$

Output:  $a$ ,  $e$ ,  $i$ ,  $g$ ,  $h$ ,  $M$

## XYZTSC

Purpose: To convert a position vector to spherical coordinates

Called by: AFLPN

Input:  $x, y, z$

Output:  $R, \lambda, \phi$

Comments: The conversion is computed as follows.

$$R = \sqrt{x^2 + y^2 + z^2}$$

$$\lambda = \tan^{-1}\left(\frac{y}{x}\right)$$

$$\phi = \cos^{-1}\left(\frac{z}{\sqrt{x^2 + y^2}}\right)$$

APPENDIX B

FLOW CHARTS OF THE SUBROUTINE OF AGAST

## APPENDIX B - FLOW CHARTS OF THE SUBROUTINE OF AGAST

The following figures are in alphabetical order according to the subroutine names. The driver program is the routine AMAIN. Not all routines used in AGAST have flow charts in this appendix; however, documentation of the larger routines not flow-charted here occurs in the references noted in the subroutine descriptions of appendix A. Symbols used in these flow charts are defined in appendix C.

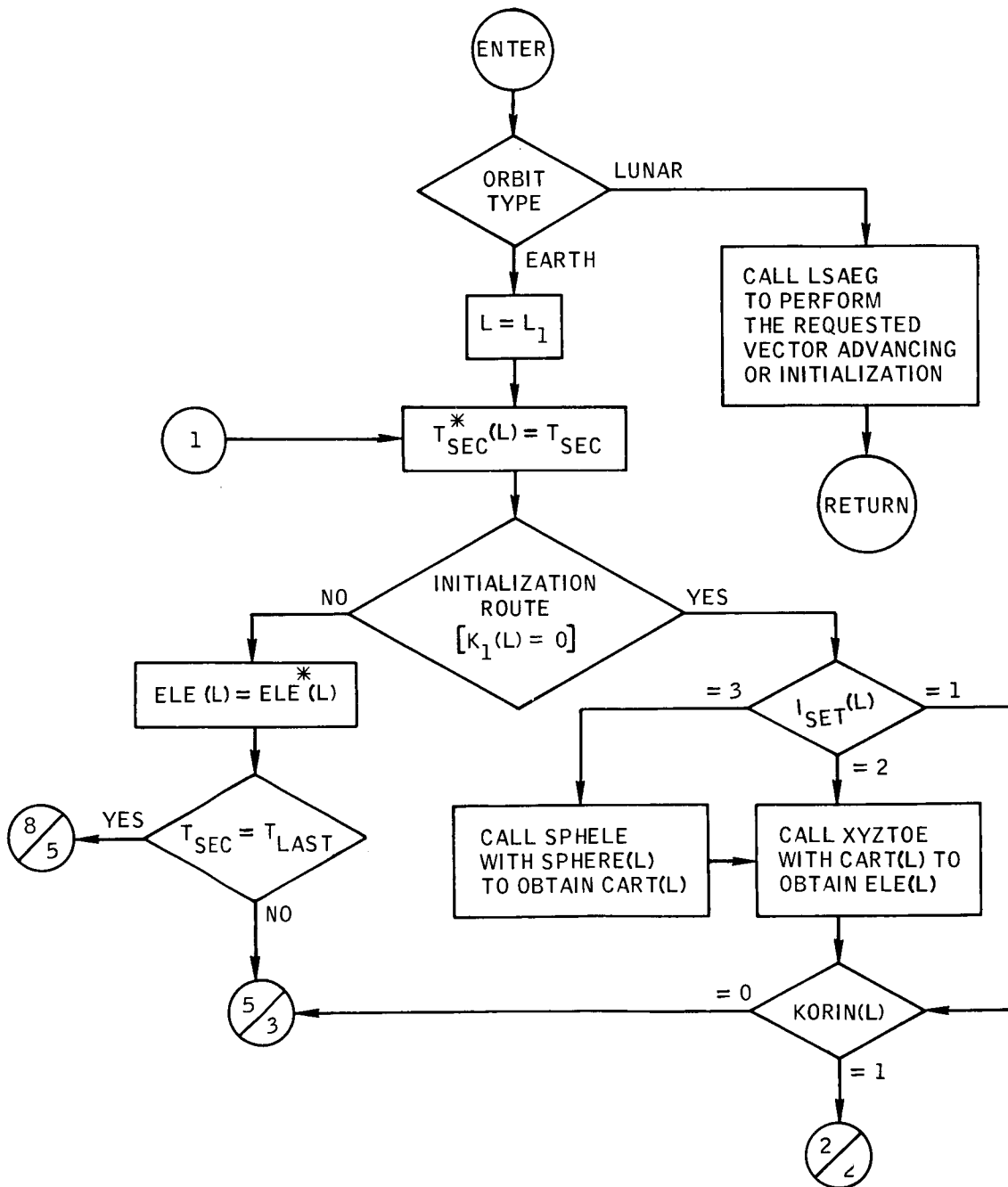


Figure B-1.- Flow chart of subroutine AEG.

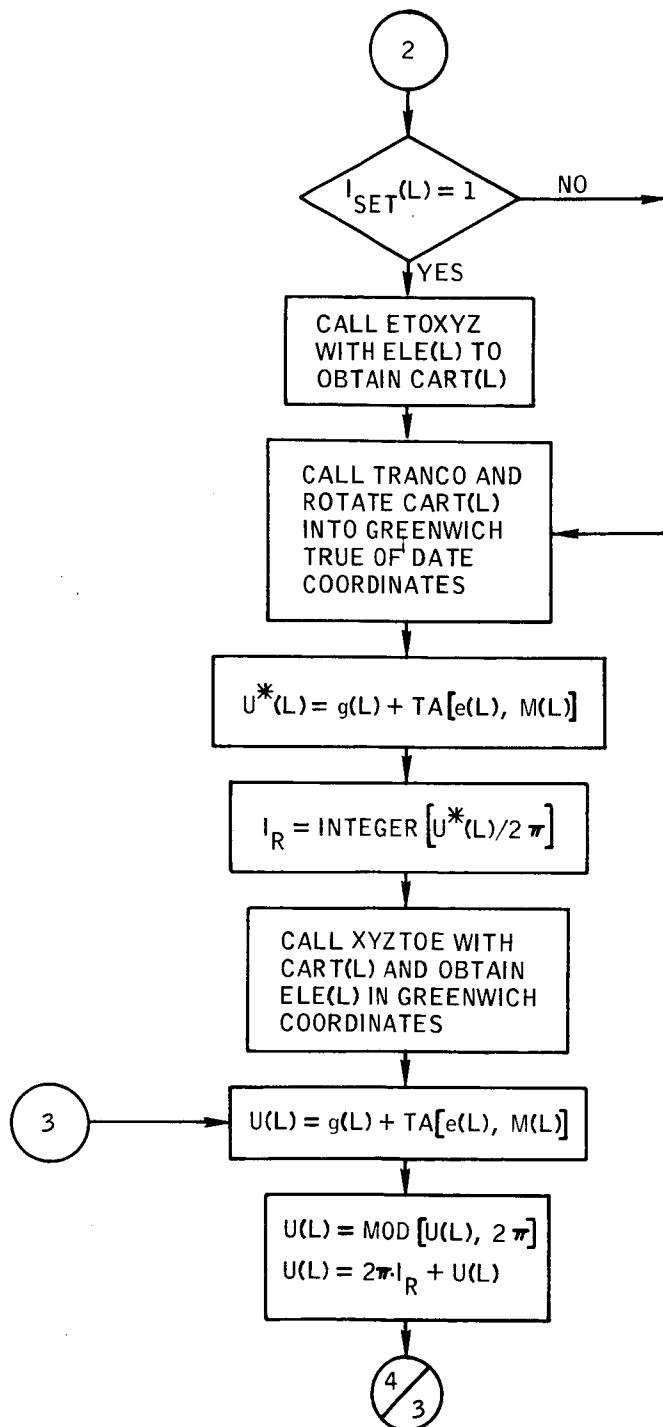


Figure B-1.- Continued.

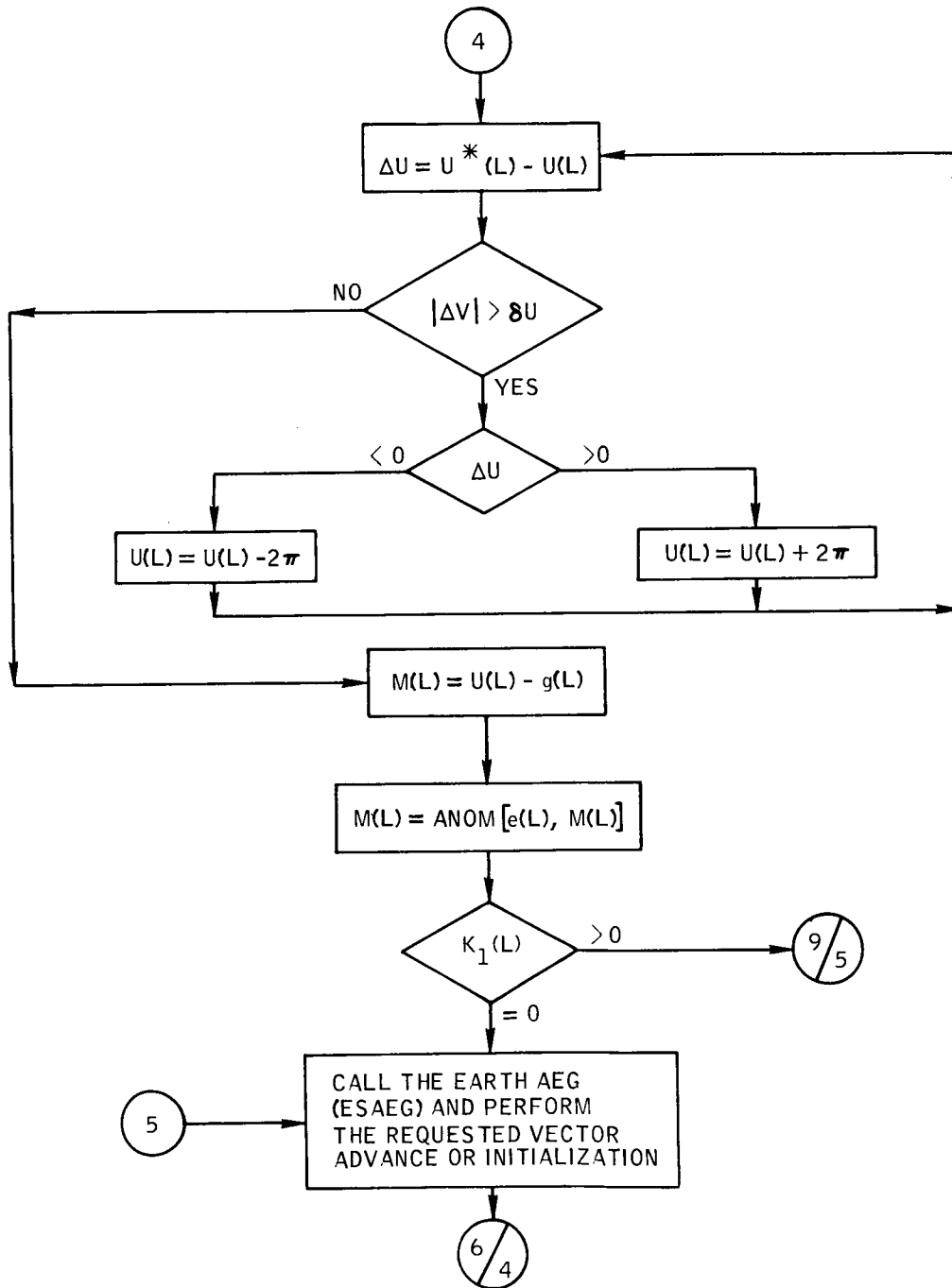


Figure B-1.- Continued.

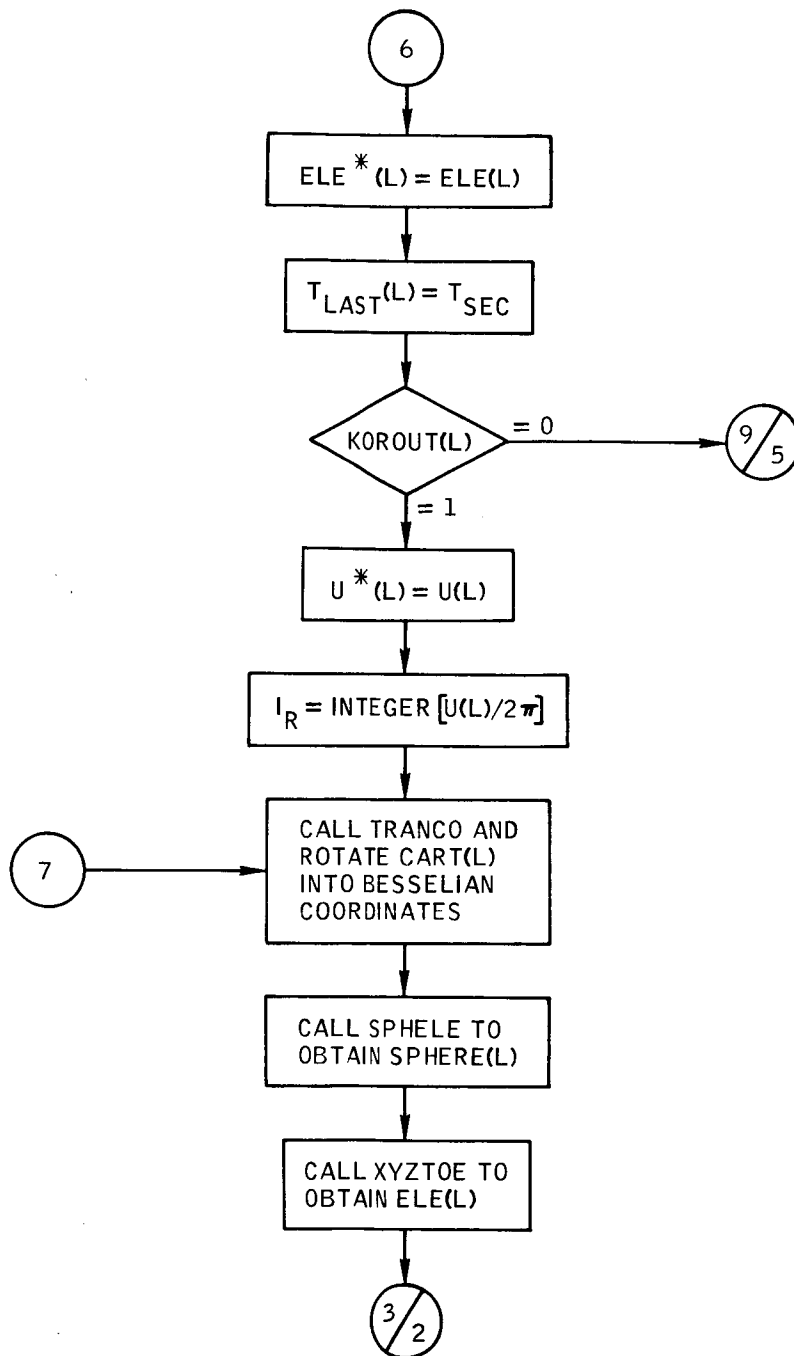


Figure B-1.- Continued.



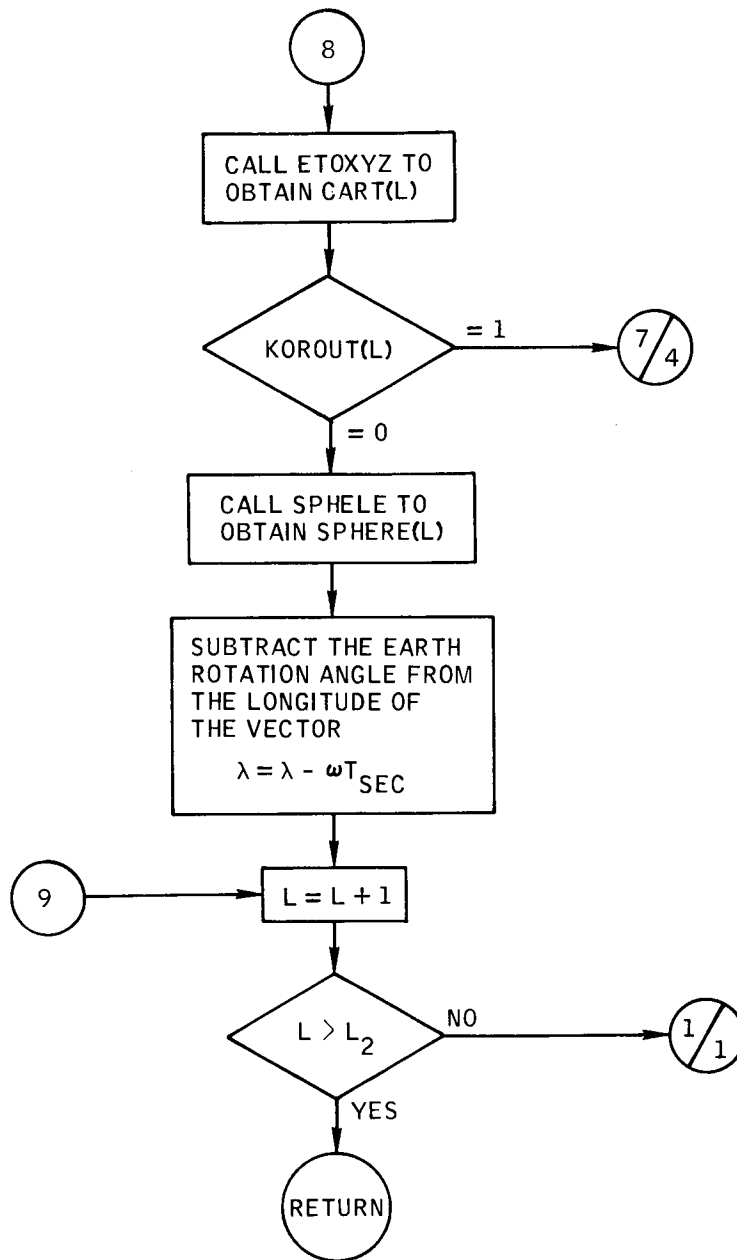


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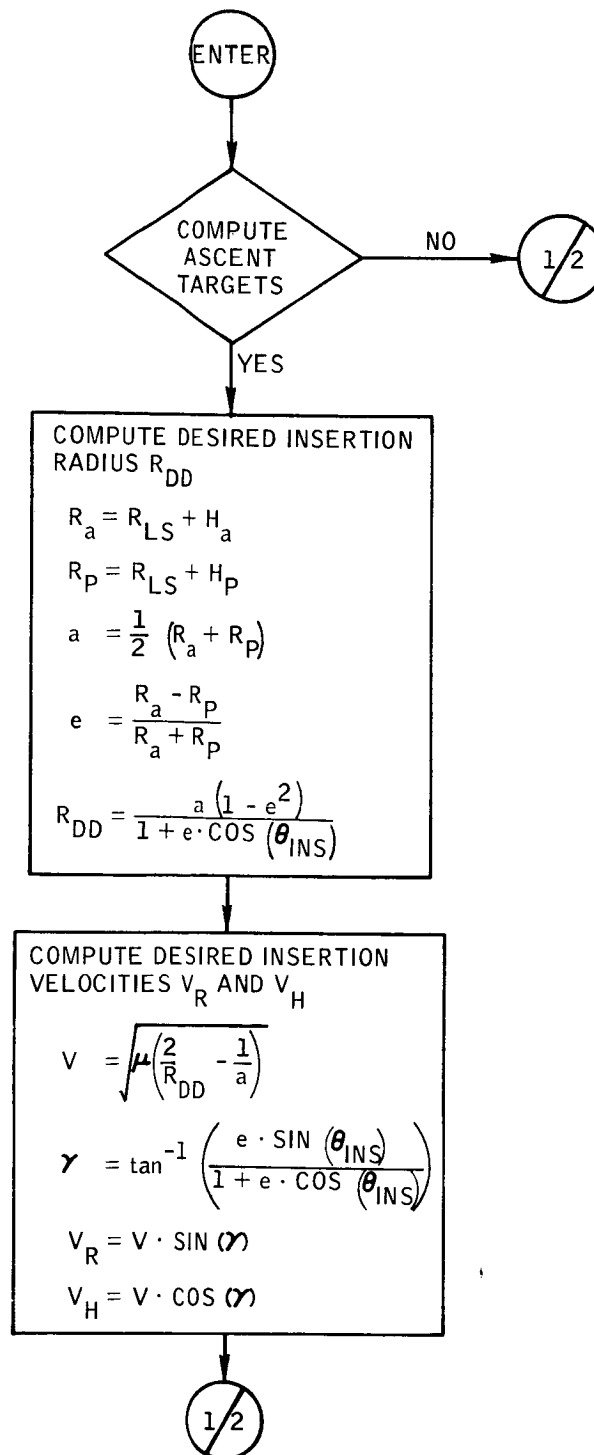


Figure B-2.- Flow chart of subroutine AFLPN.



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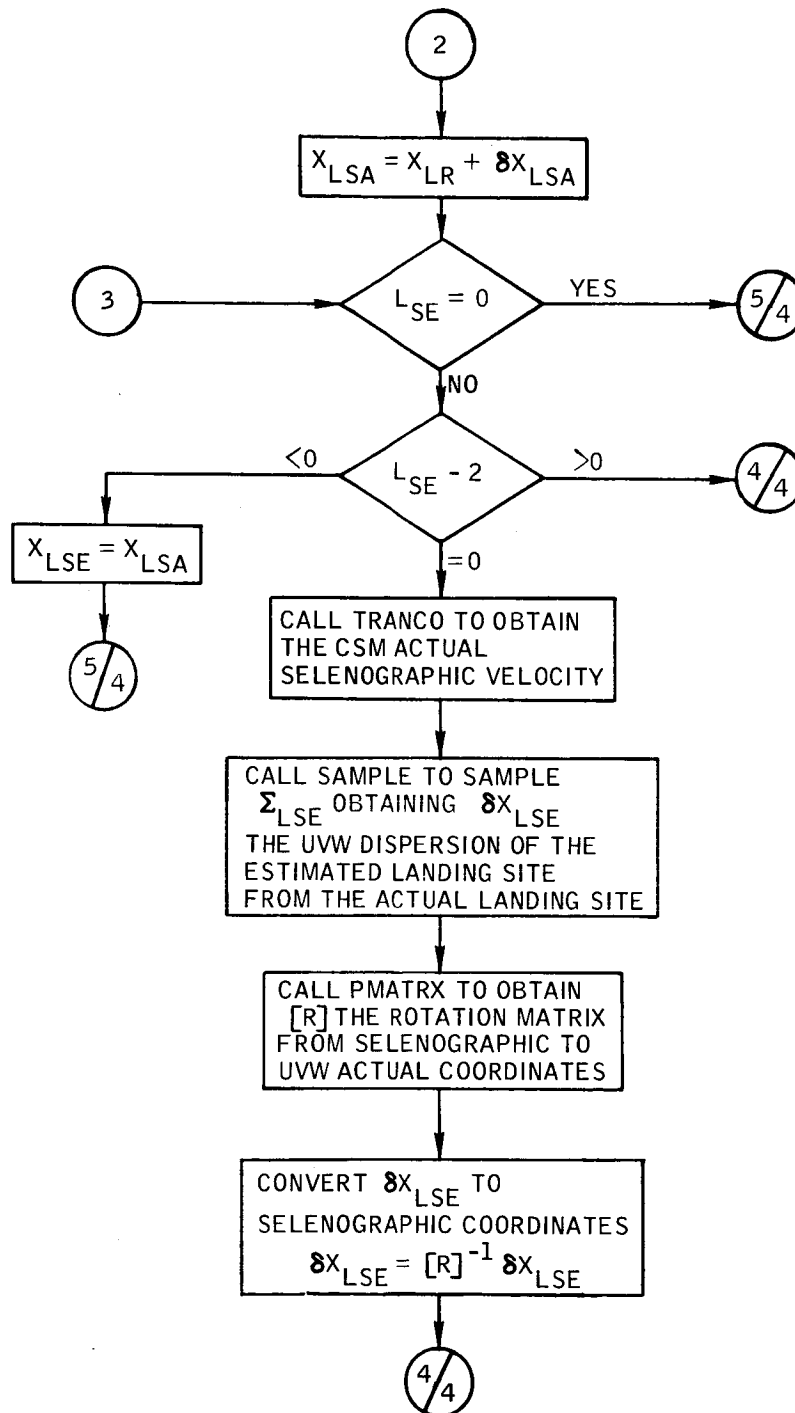


Figure B-2.- Continued.

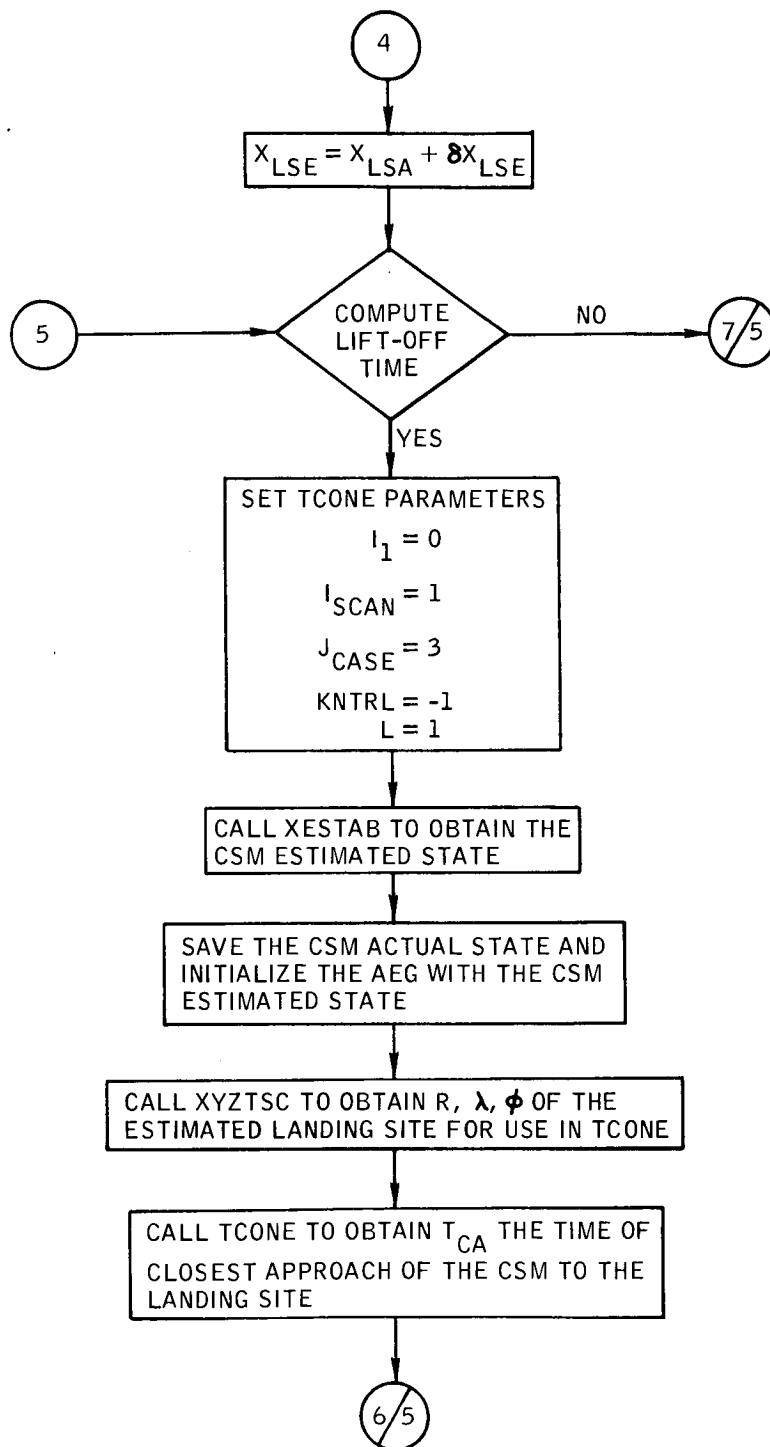


Figure B-2.- Continued.

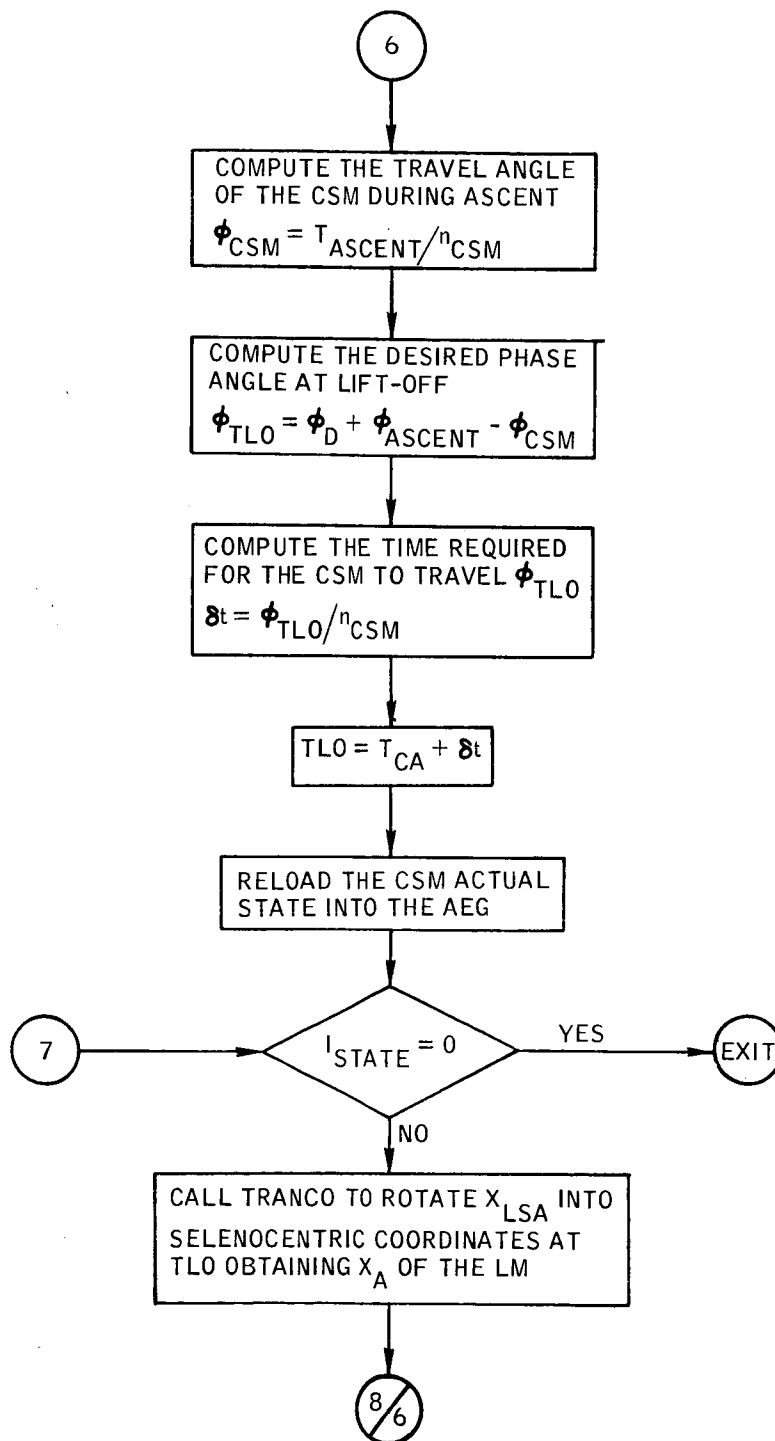


Figure B-2.- Continued.

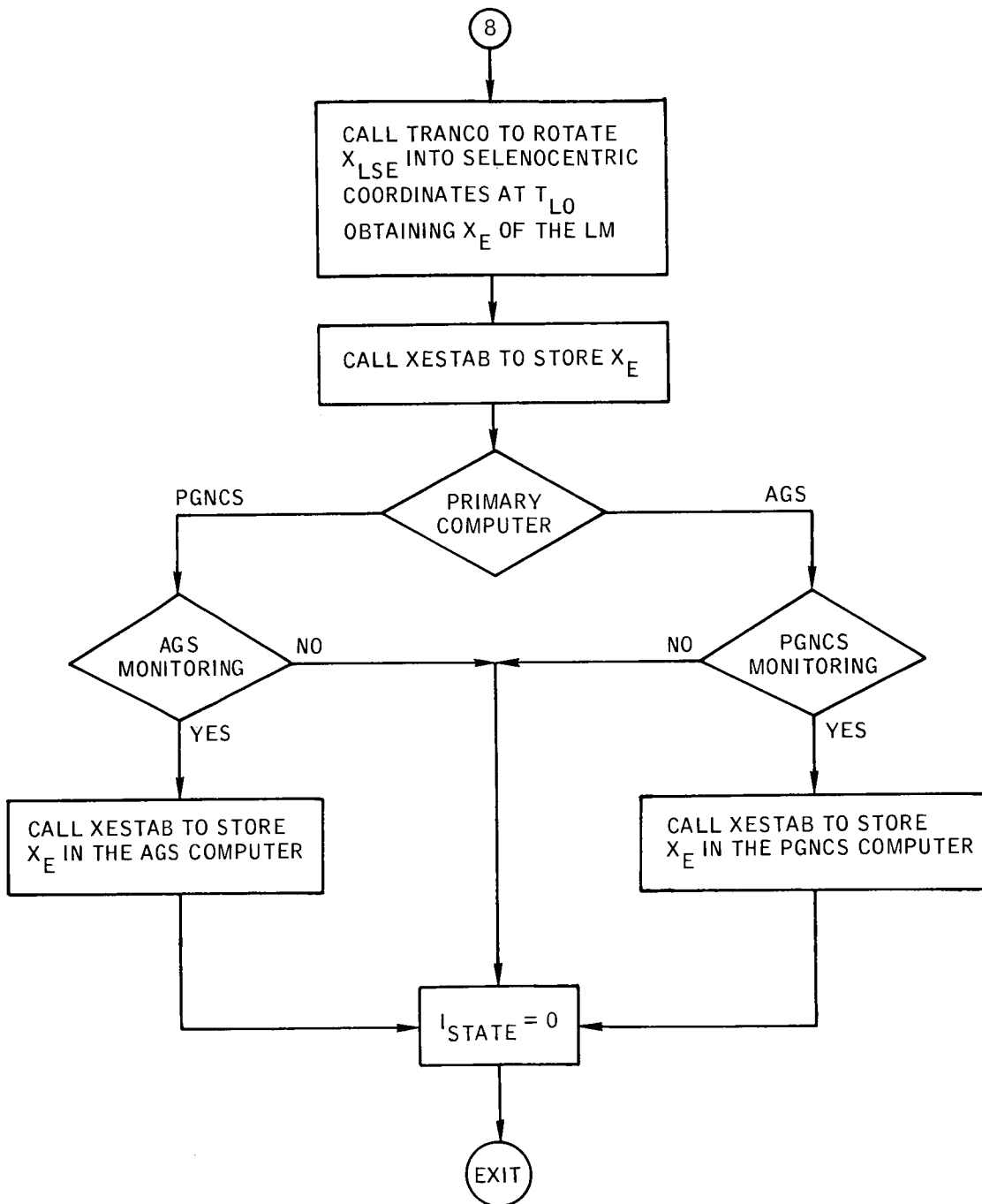


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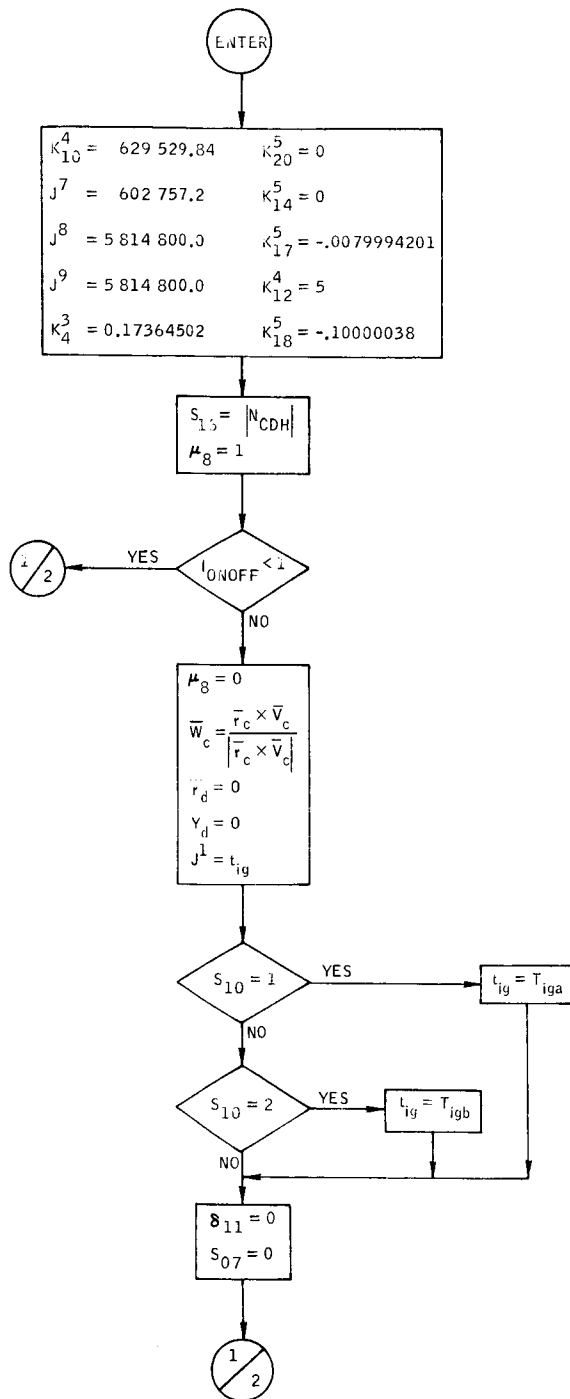


Figure B-3. - Flow chart of subroutine AGS.



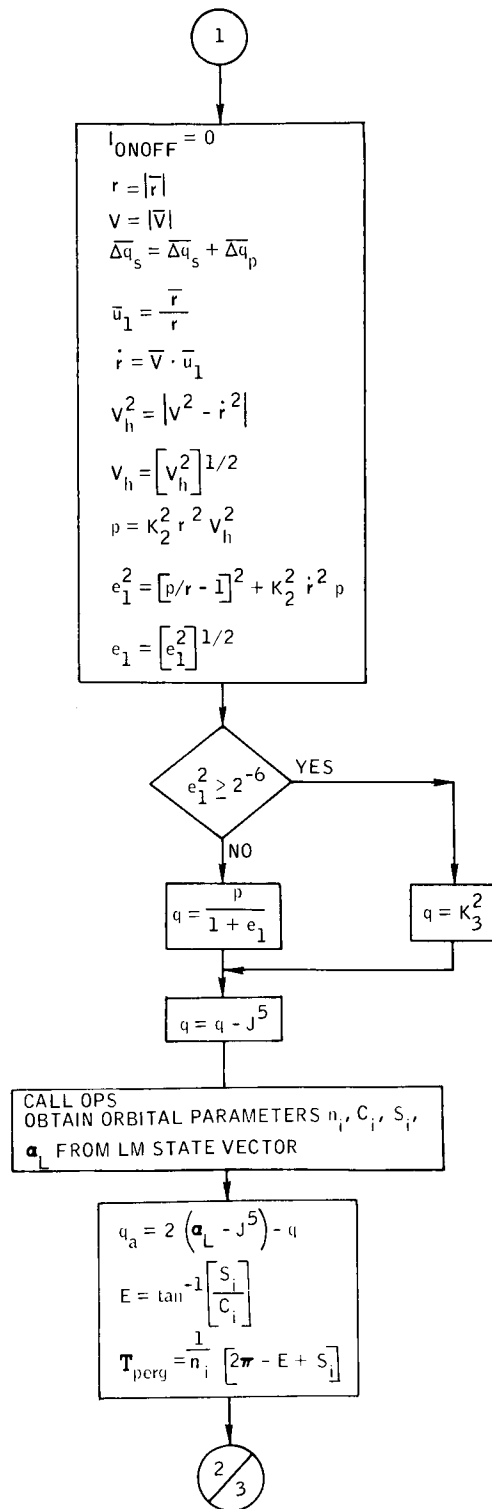


Figure B-3. - Continued.

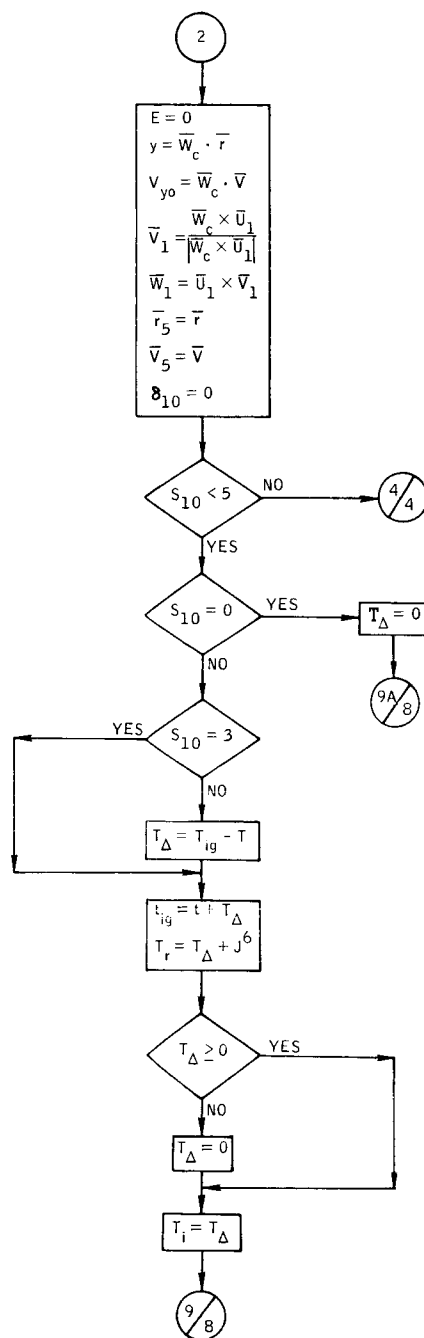
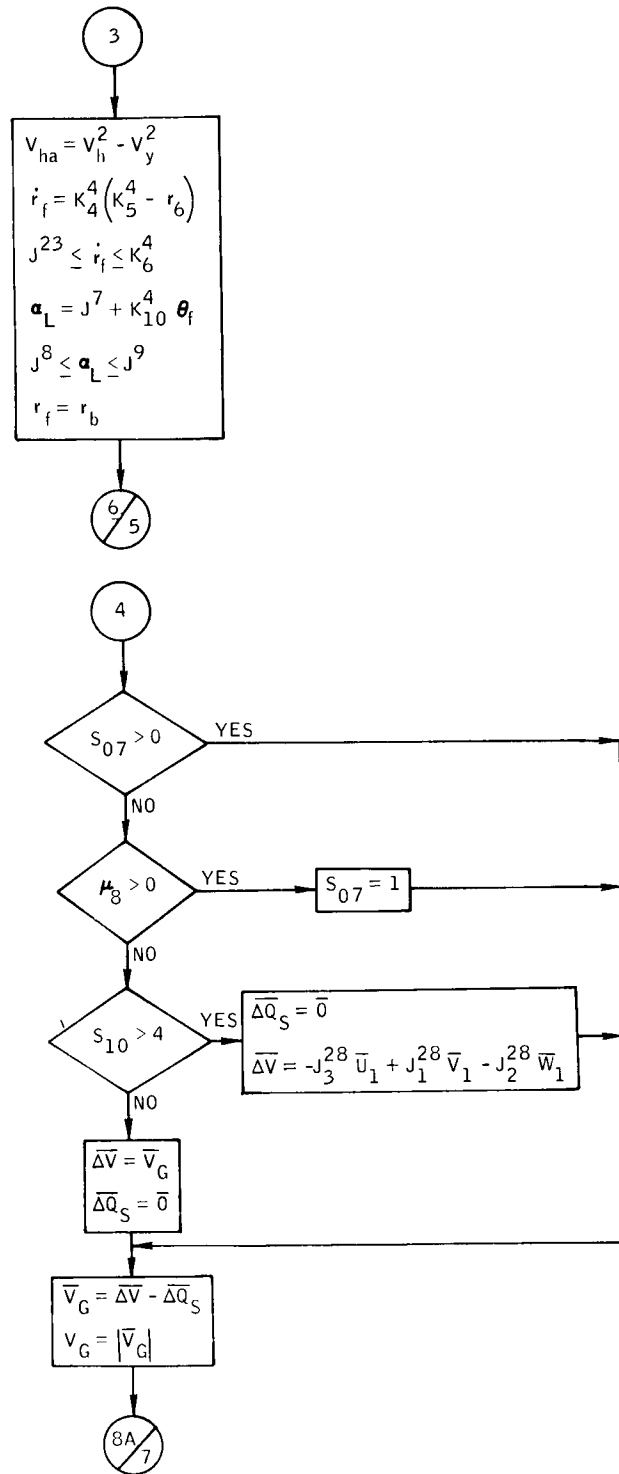


Figure B-3. - Continued.



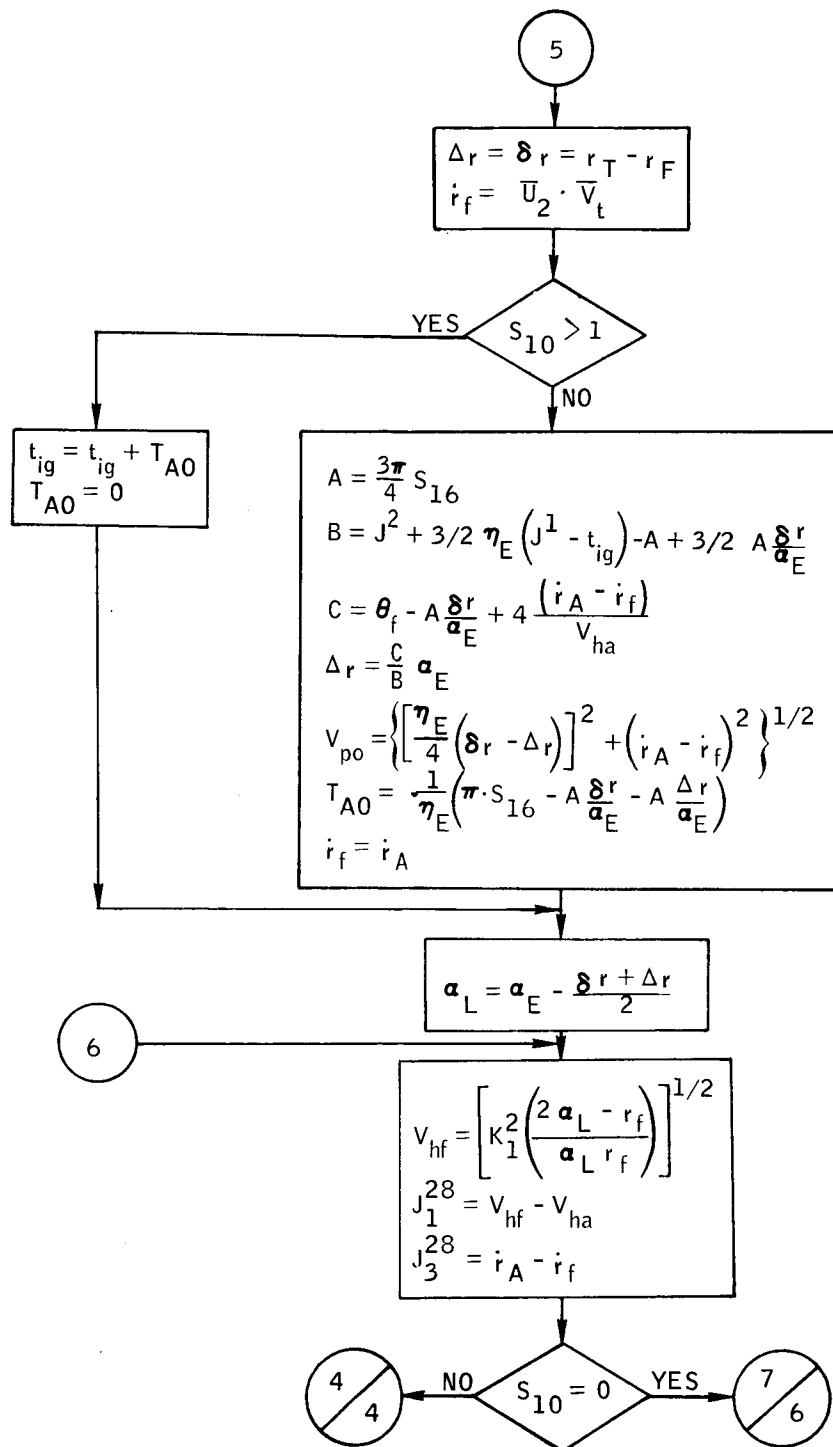


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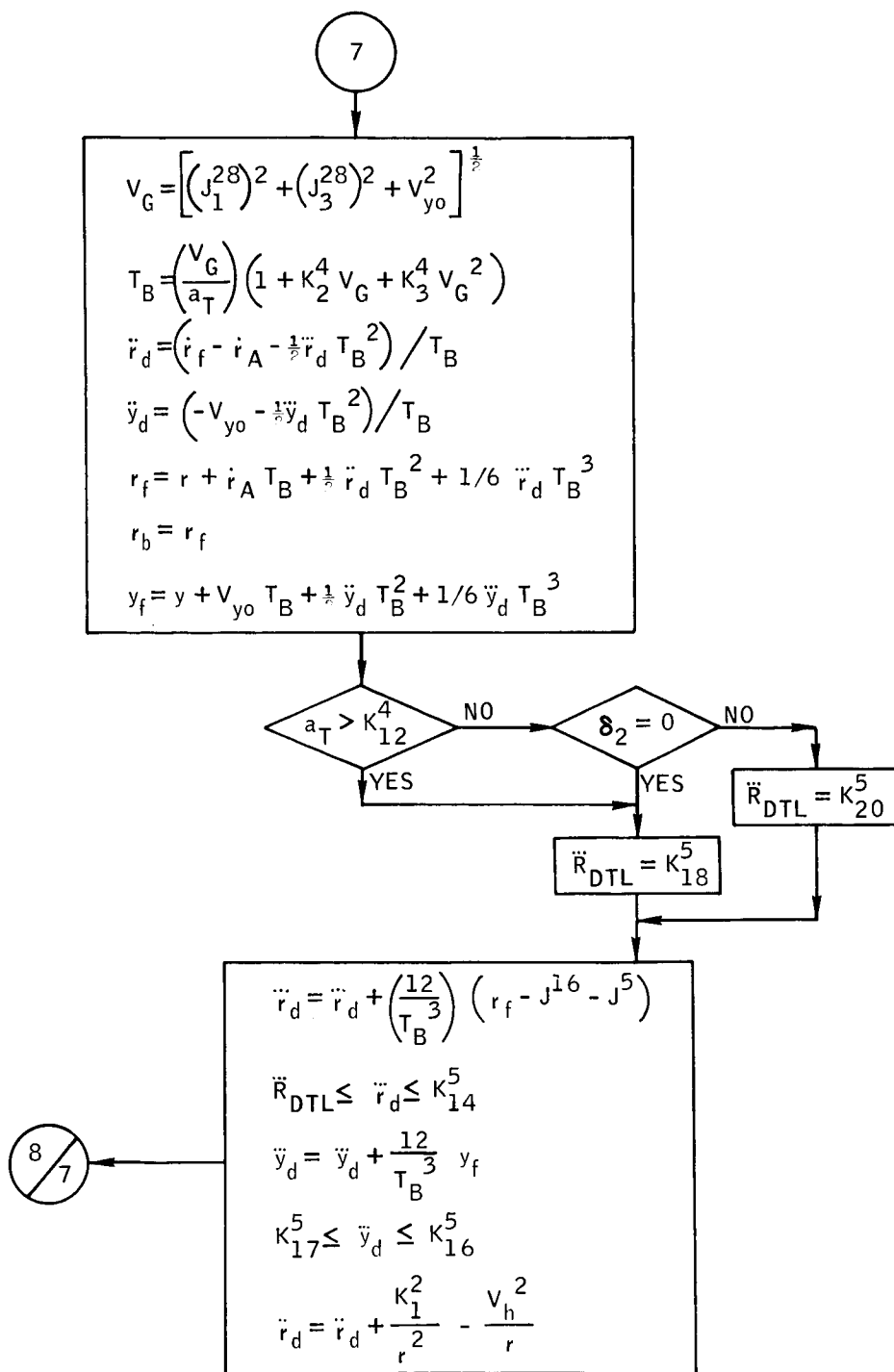
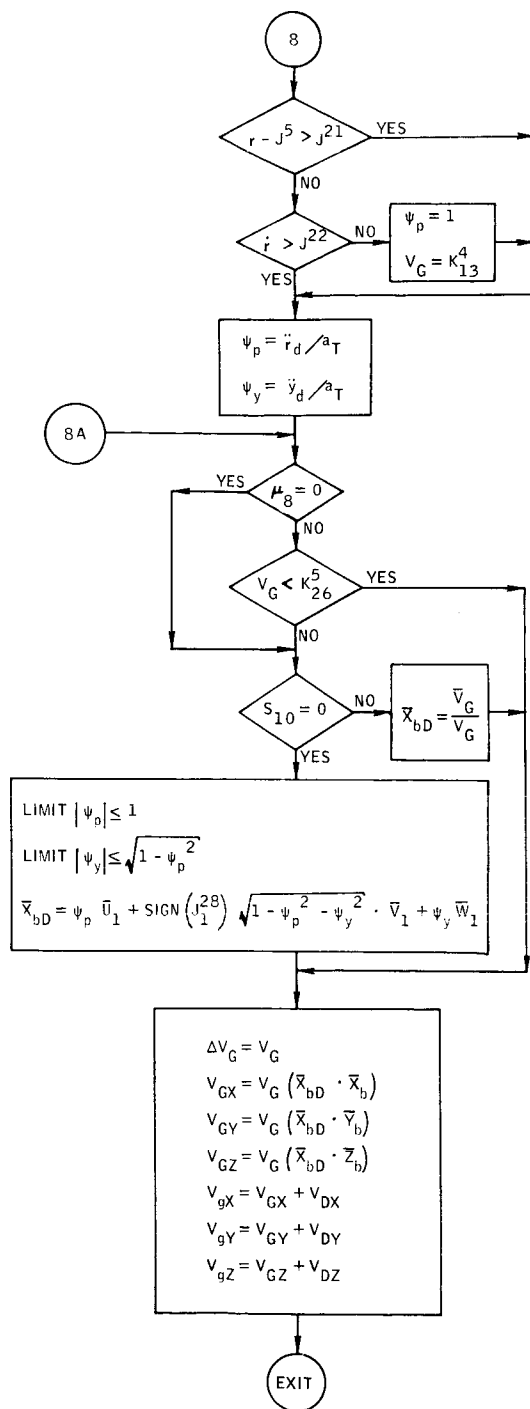


Figure B-3. - Continued.



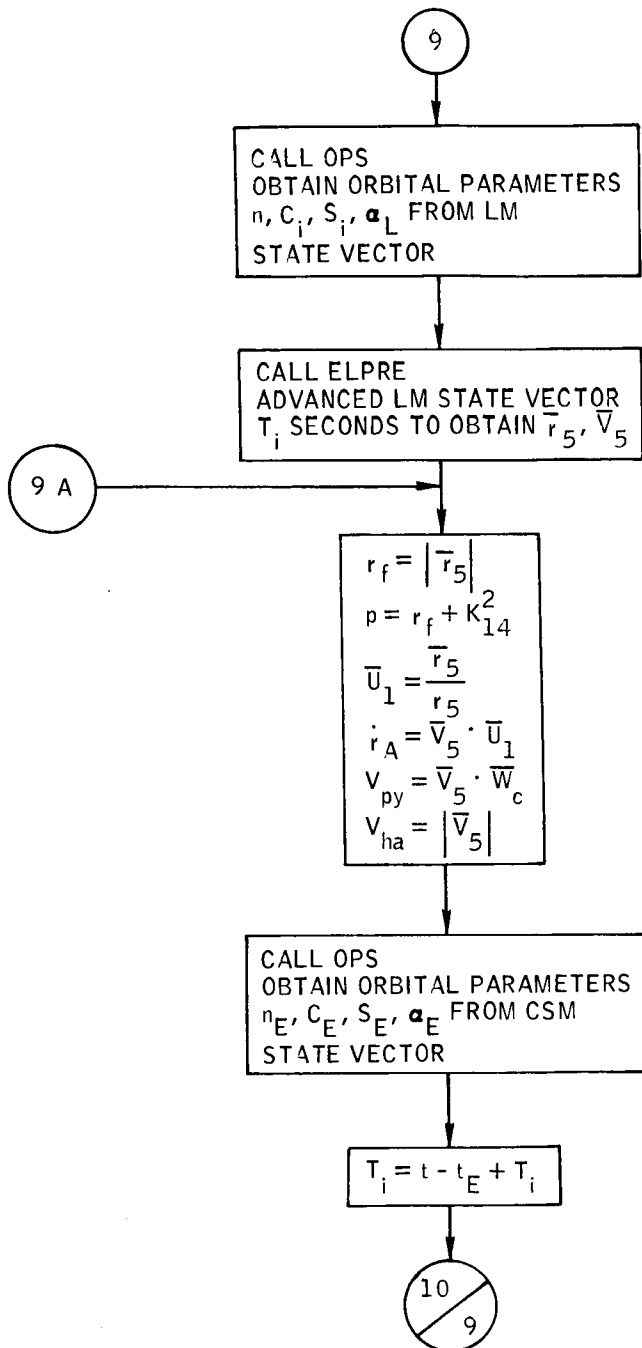


Figure B-3.- Continued.

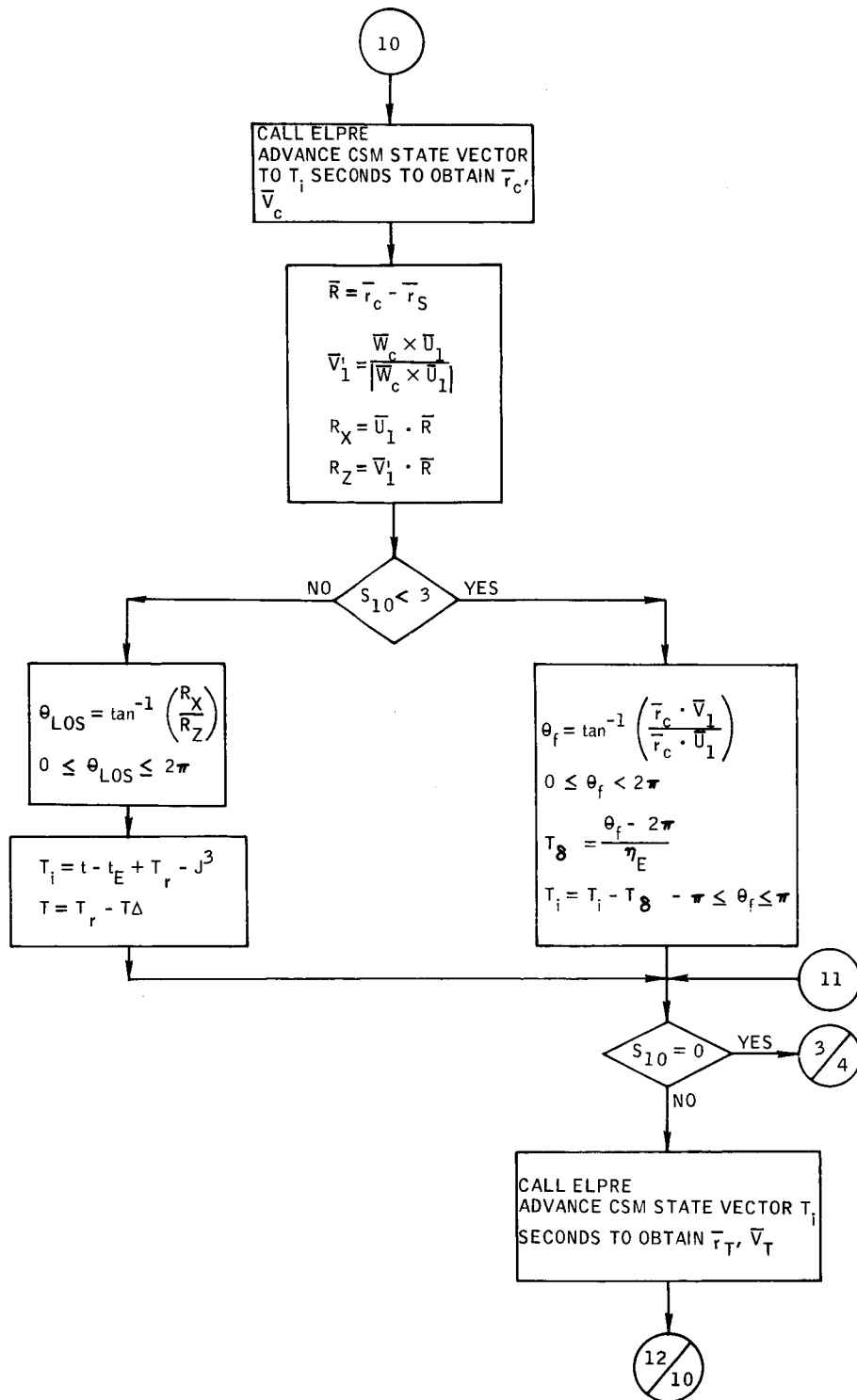


Figure B-3. - Continued.



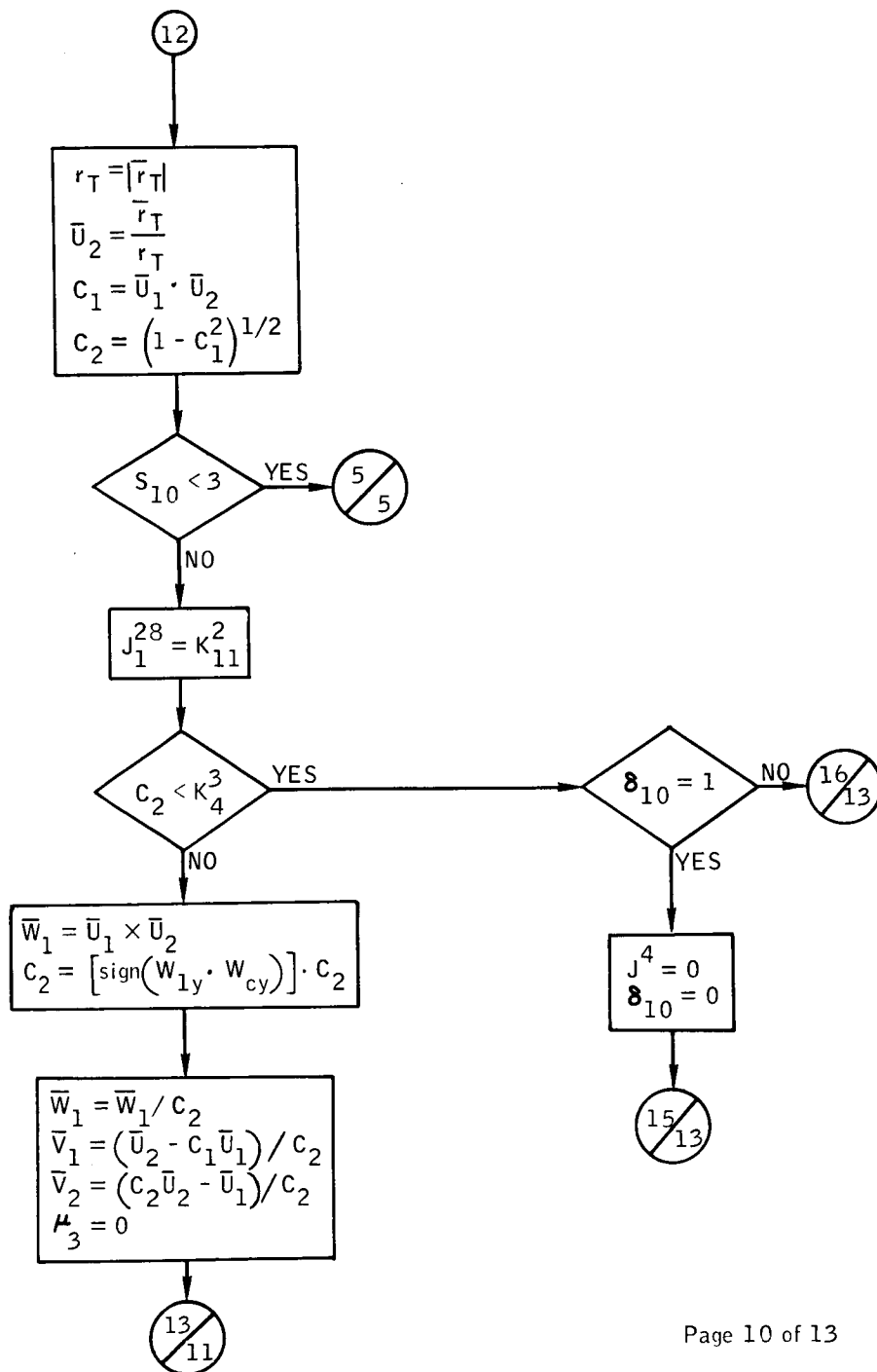


Figure B-3.- Continued.

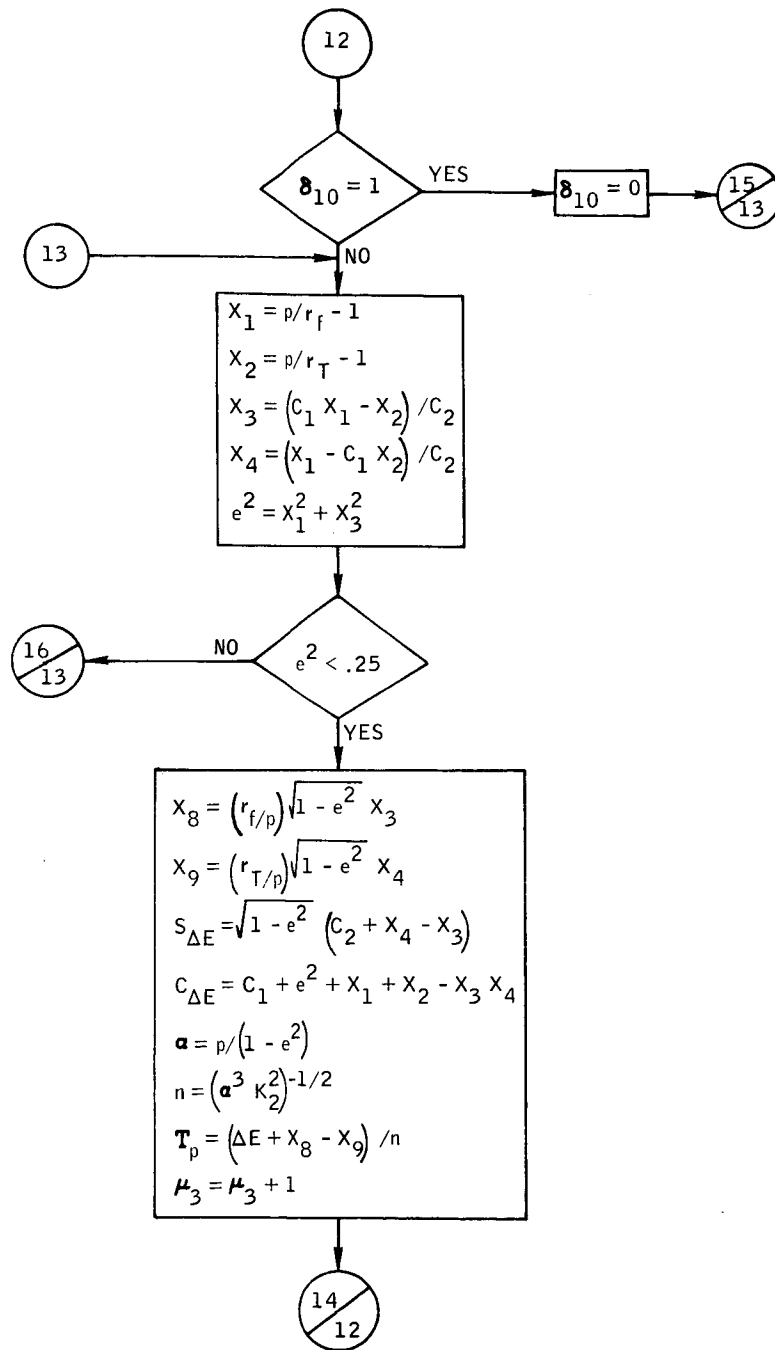


Figure .- Continued.

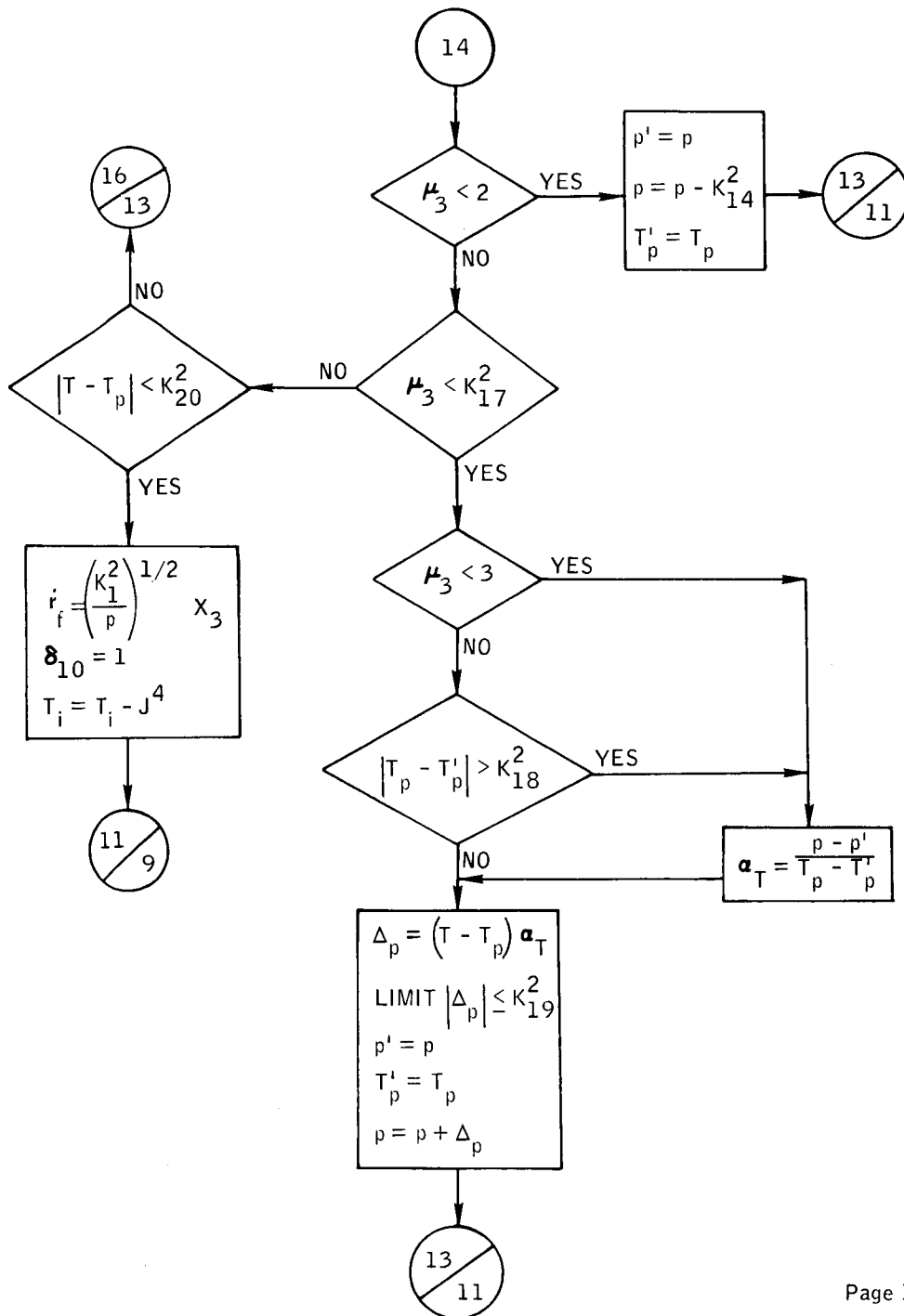


Figure B-3. - Continued.

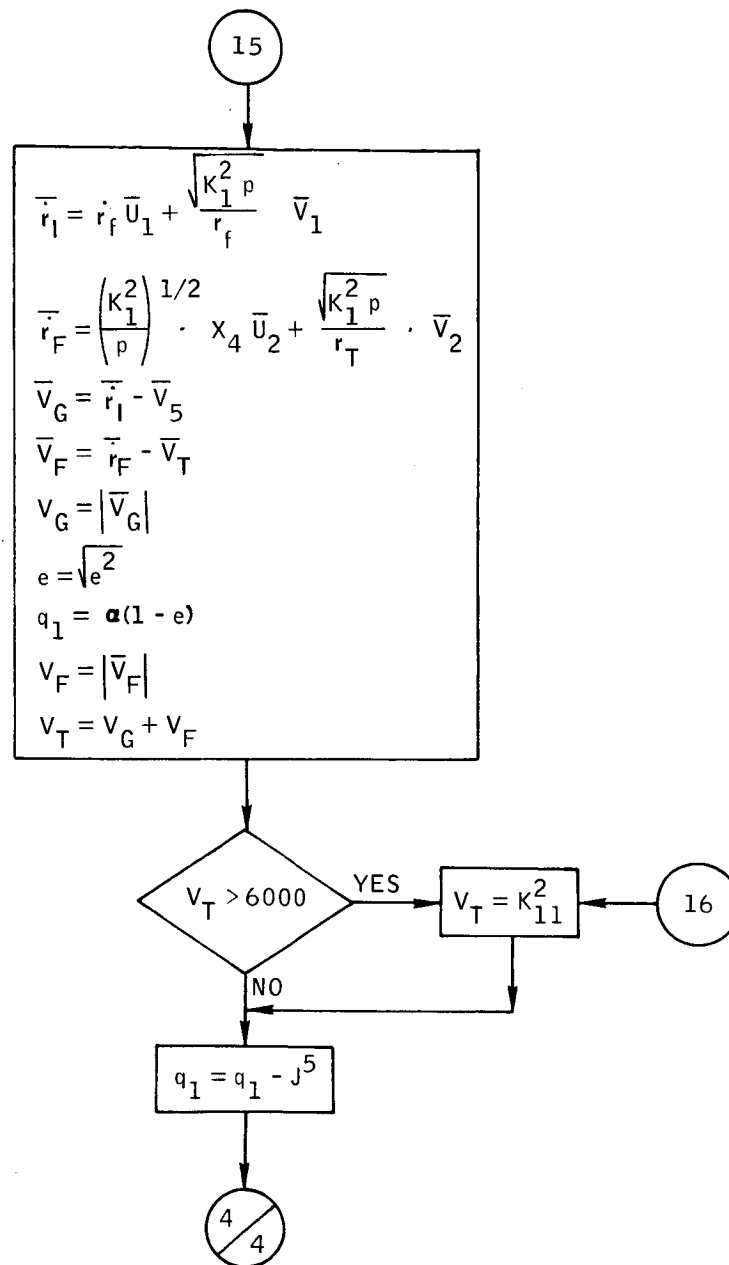


Figure B-3.- Concluded.

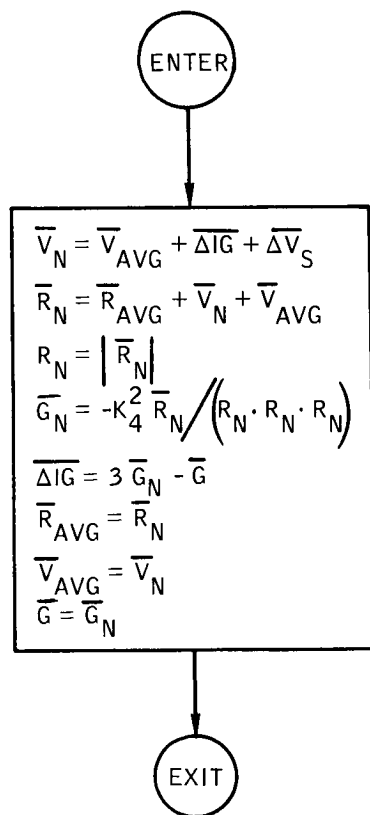


Figure B-4. - Flow chart of subroutine AGSAG.

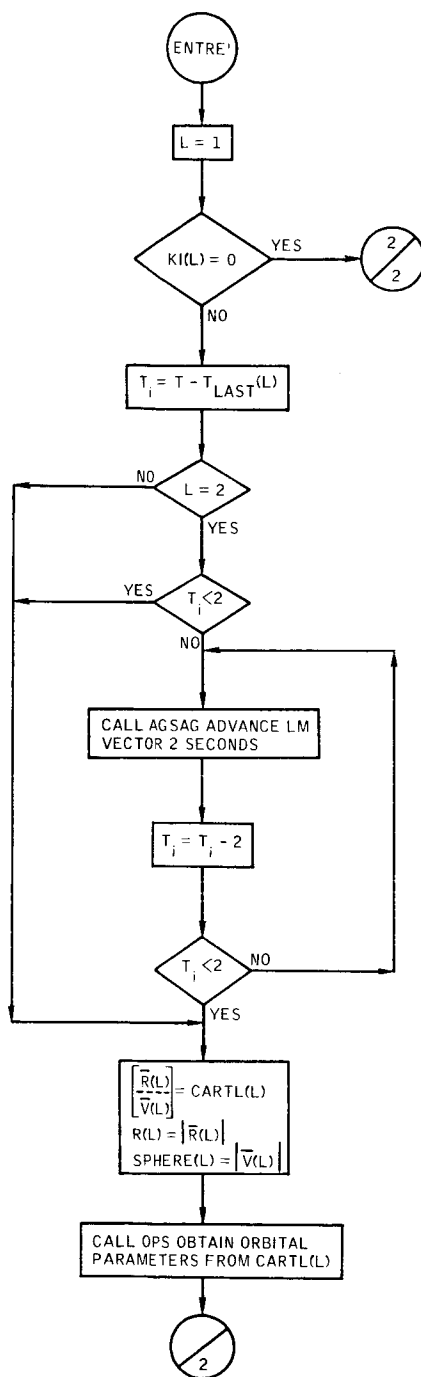
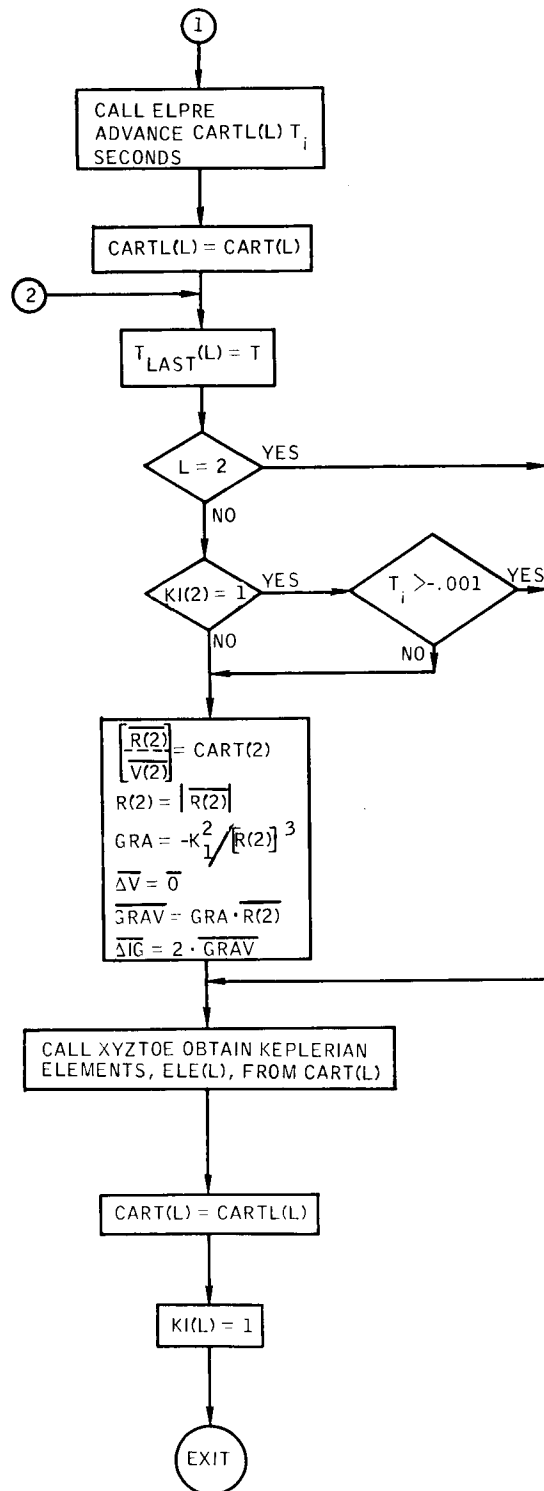


Figure B-5.- Flow chart of subroutine AGSKEP.



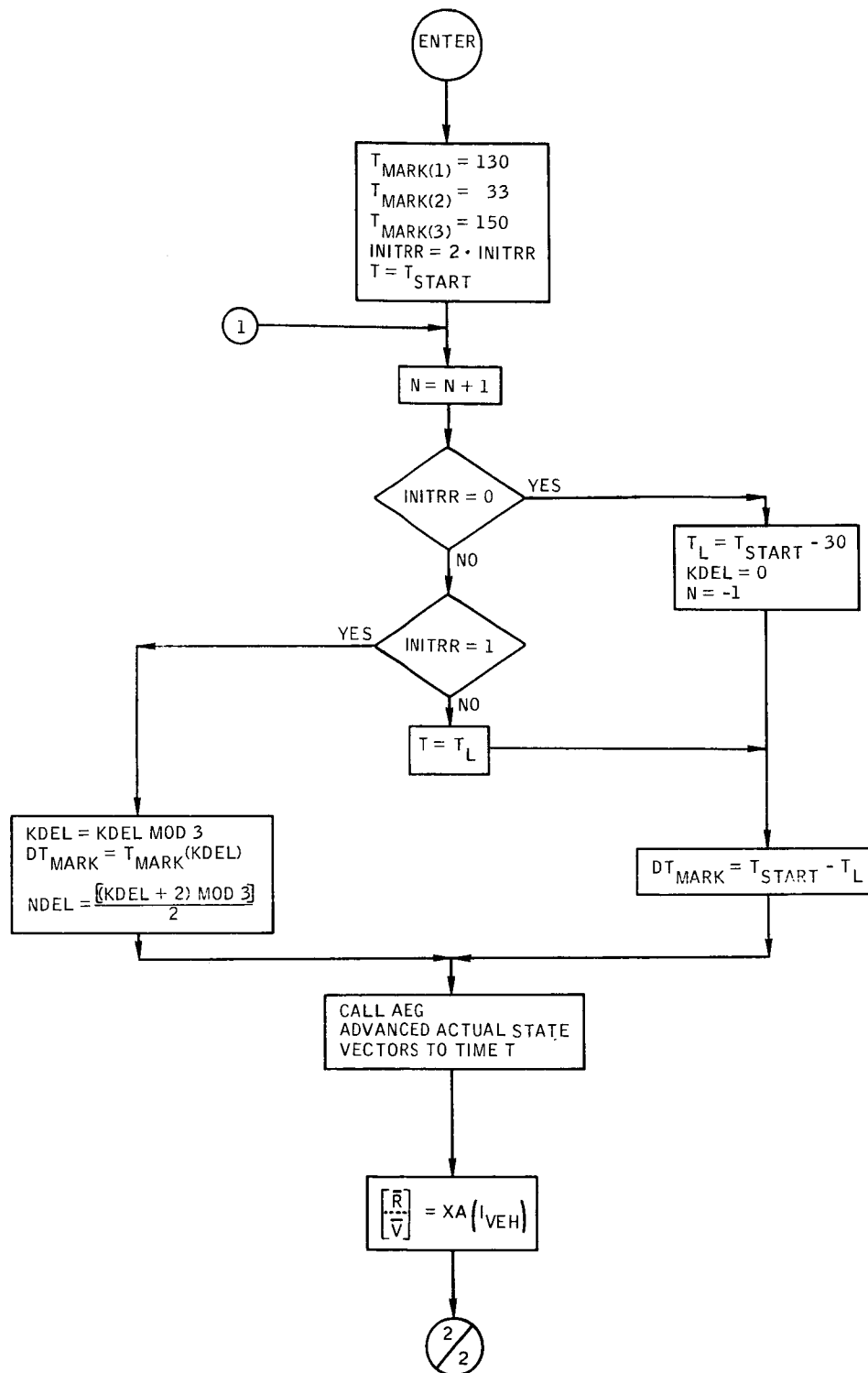
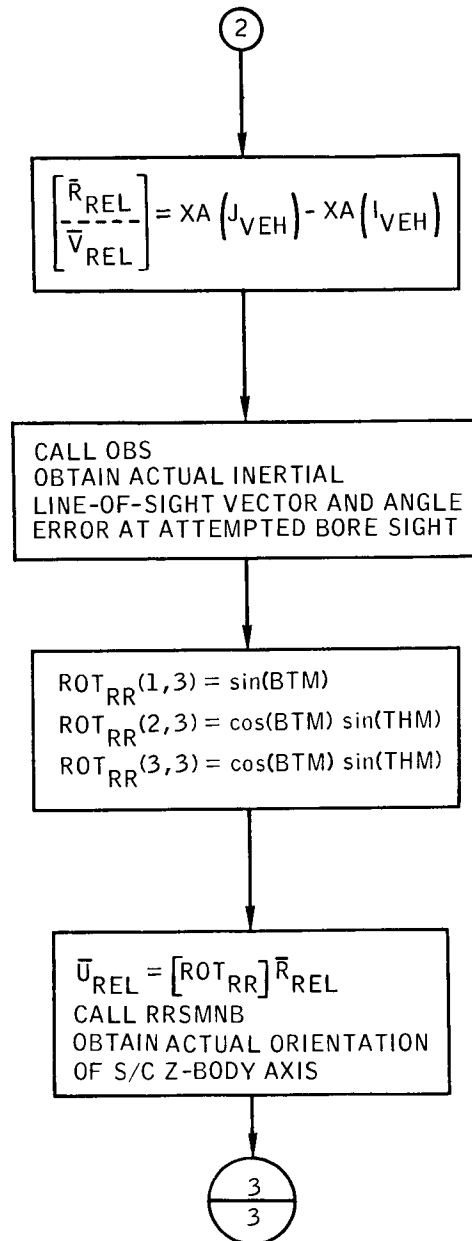


Figure B-6.- Flow chart of subroutine AGSRR.





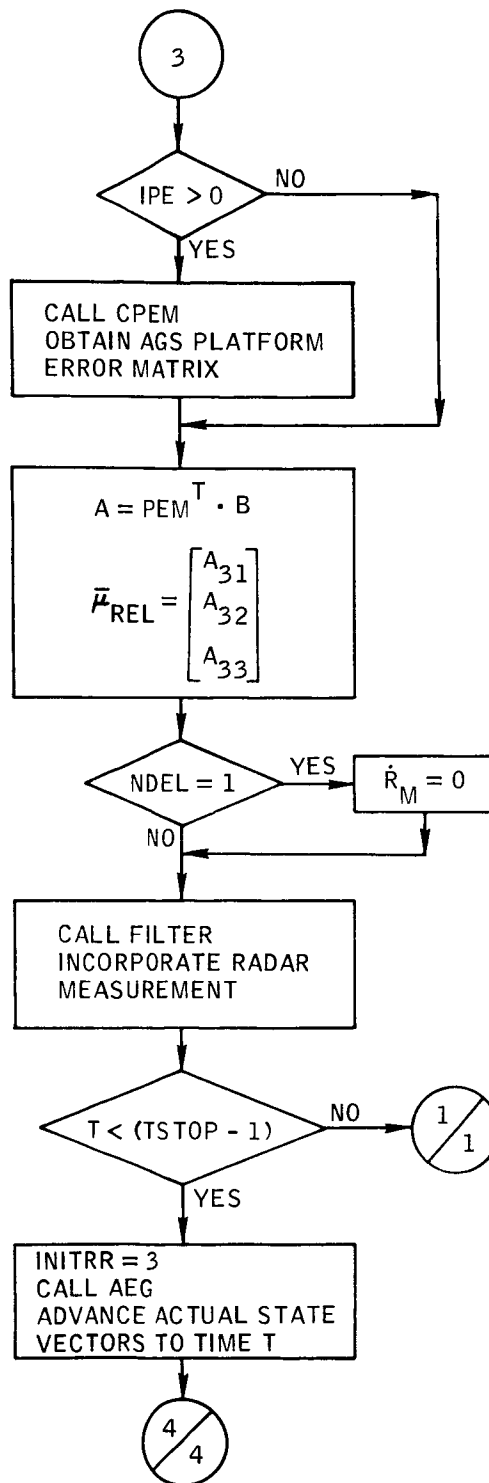
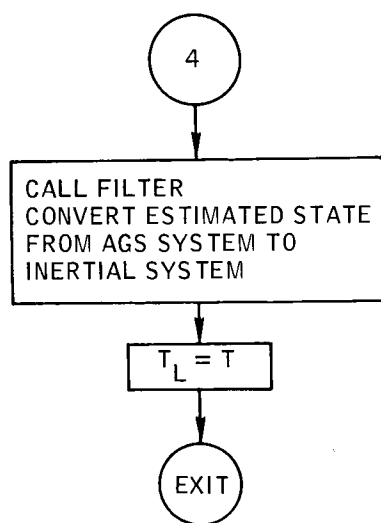


Figure B-6.- Continued.



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Figure B-6.- Concluded.

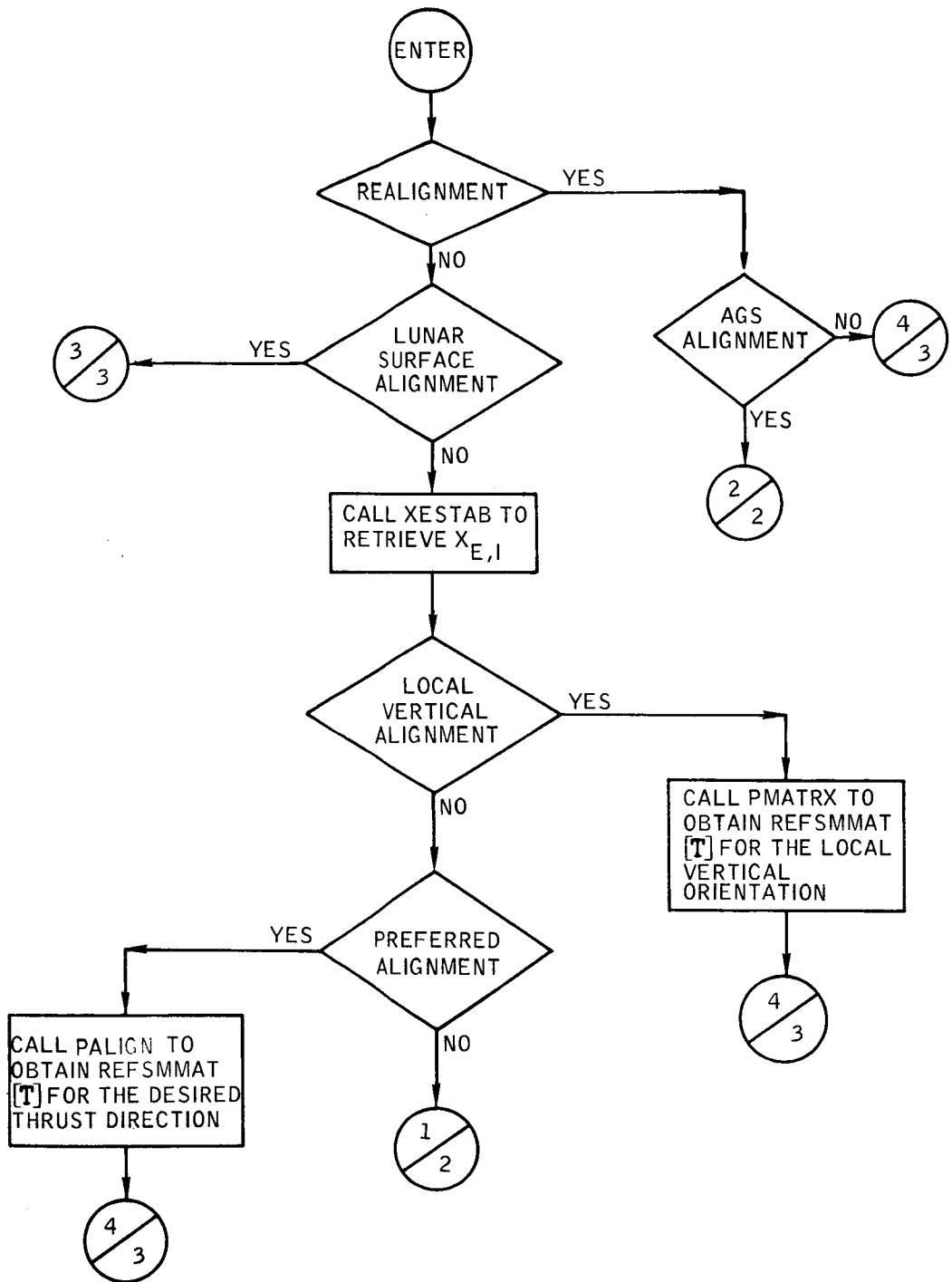


Figure B-7.- Flow chart of subroutine ALIGN.

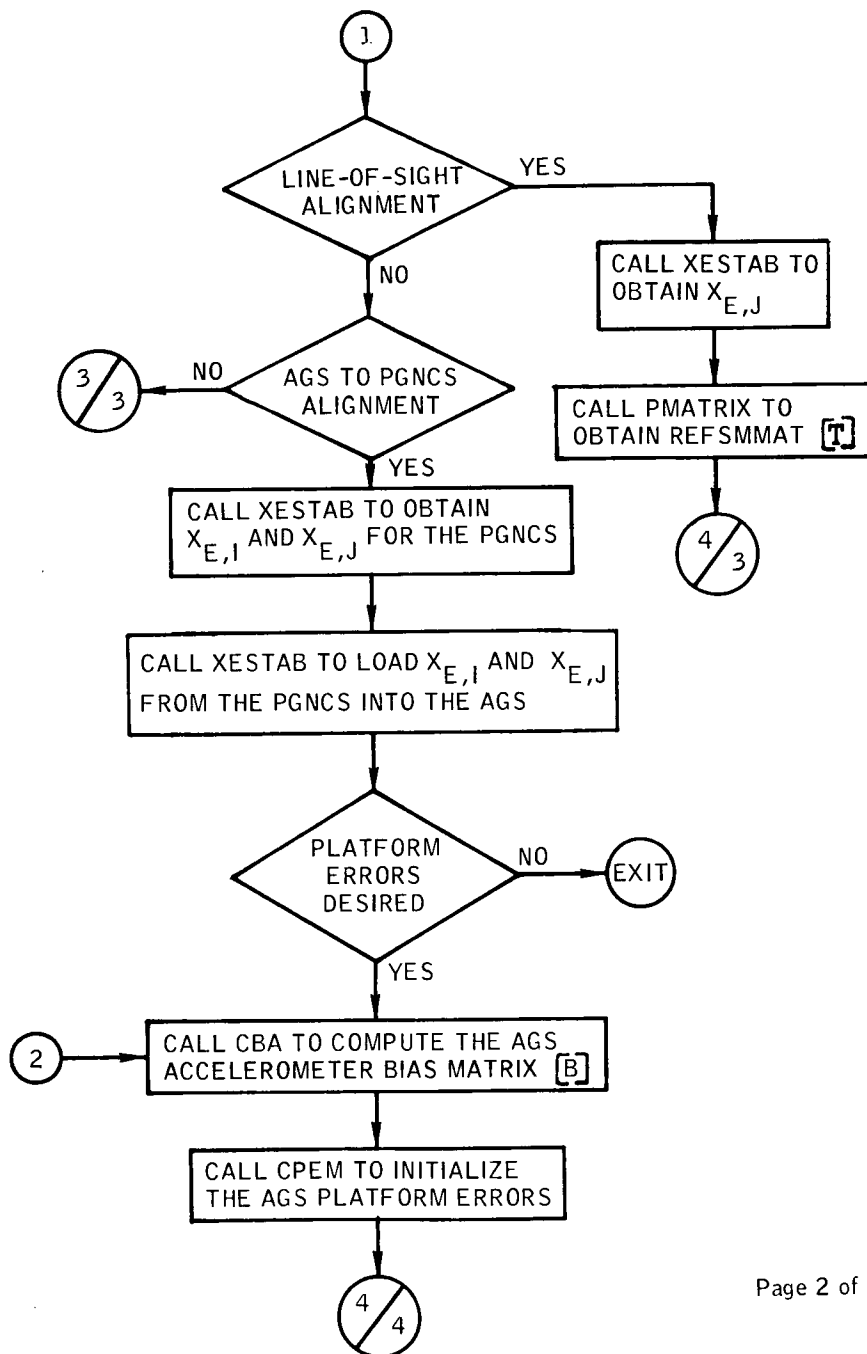


Figure B-7. - Continued.

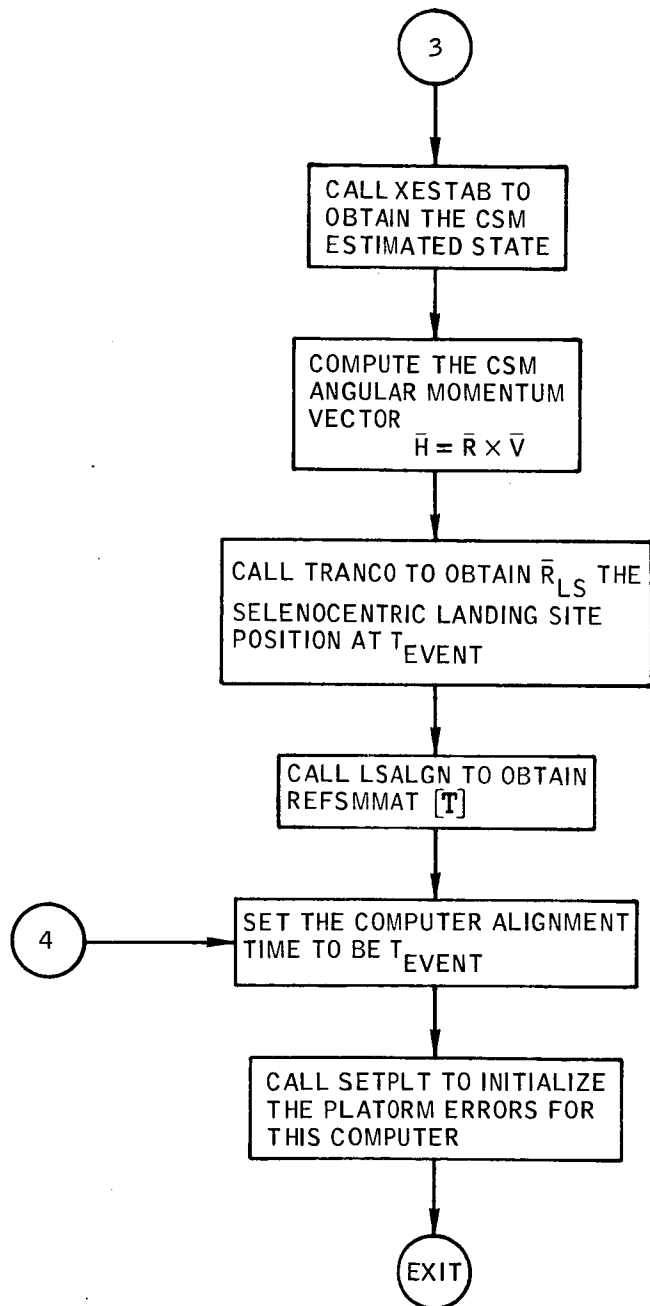


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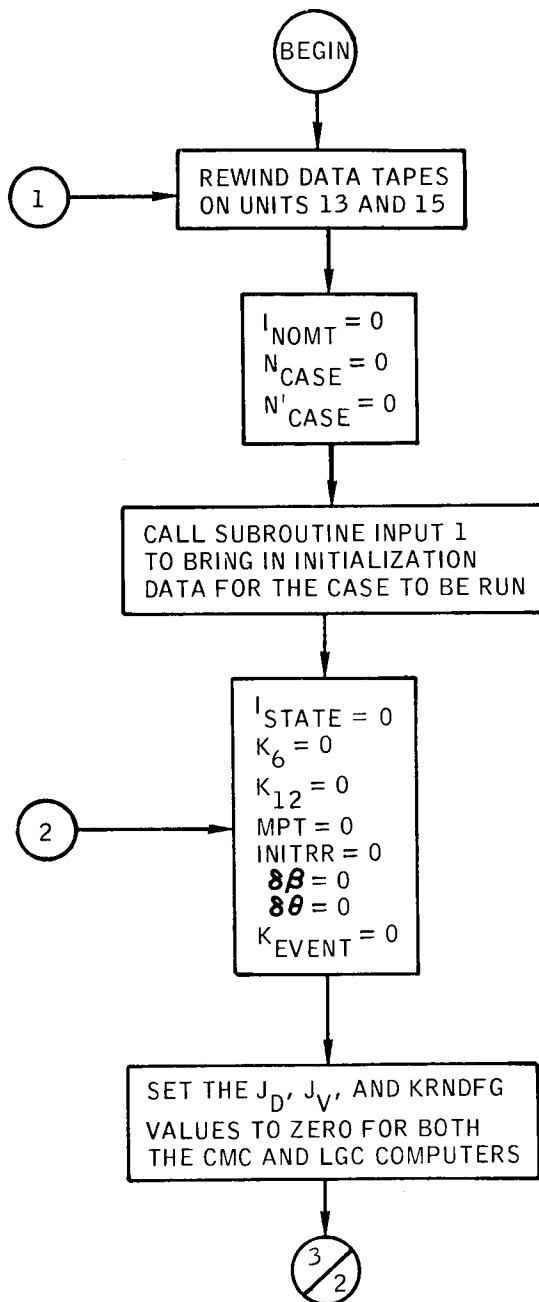


Figure B-8.- Flow chart of AGAST driver AMAIN.

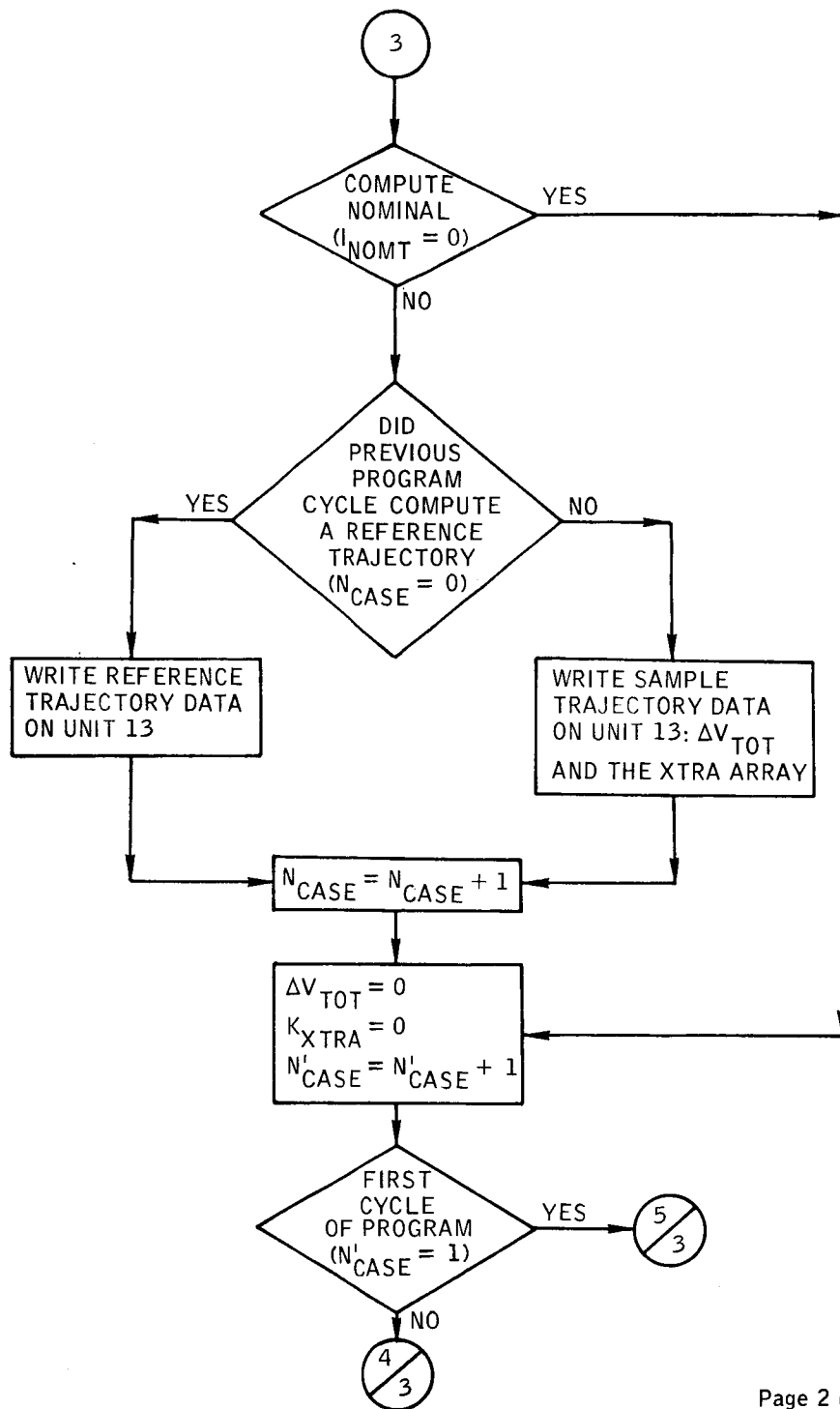


Figure B-8. - Continued.



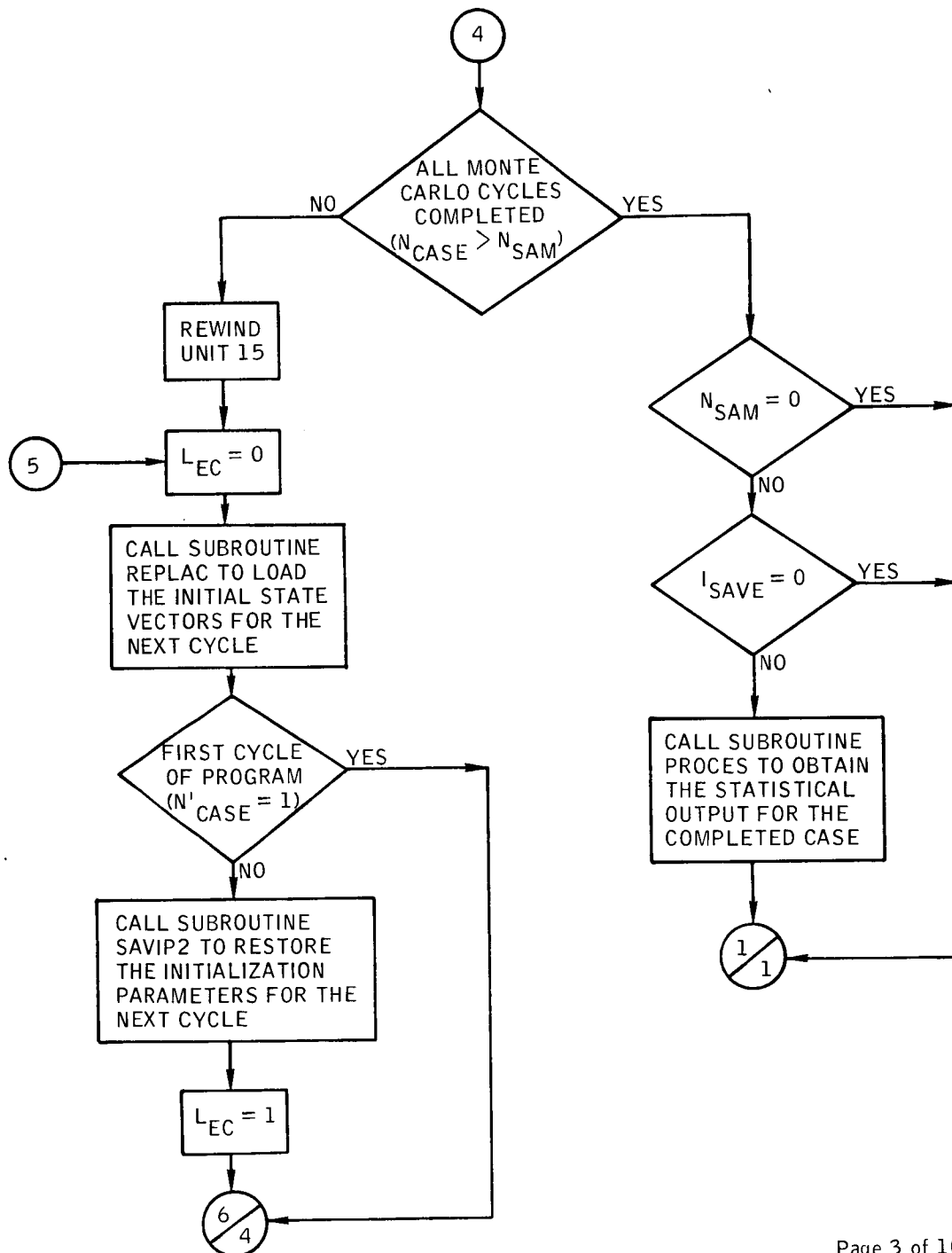


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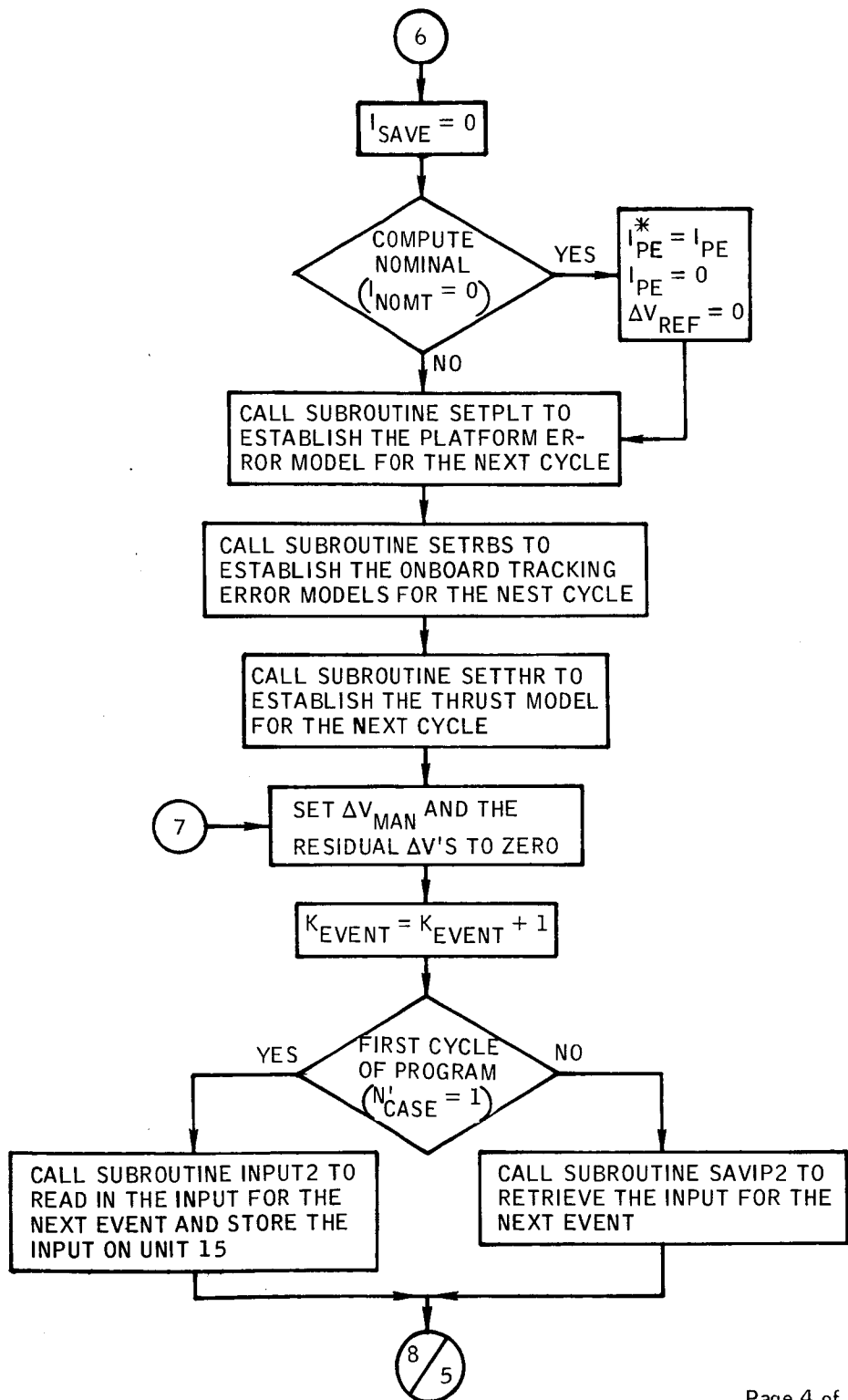


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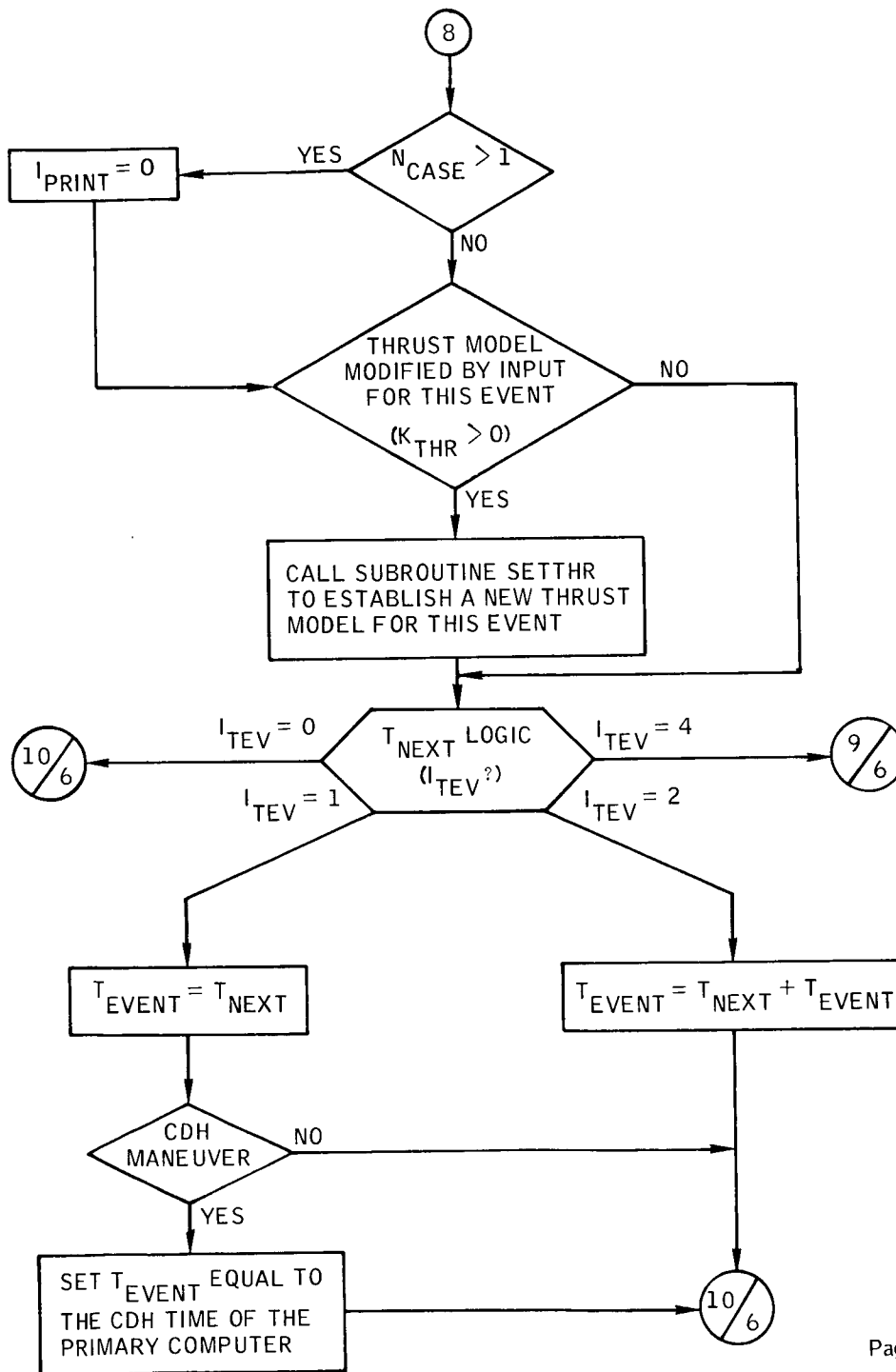


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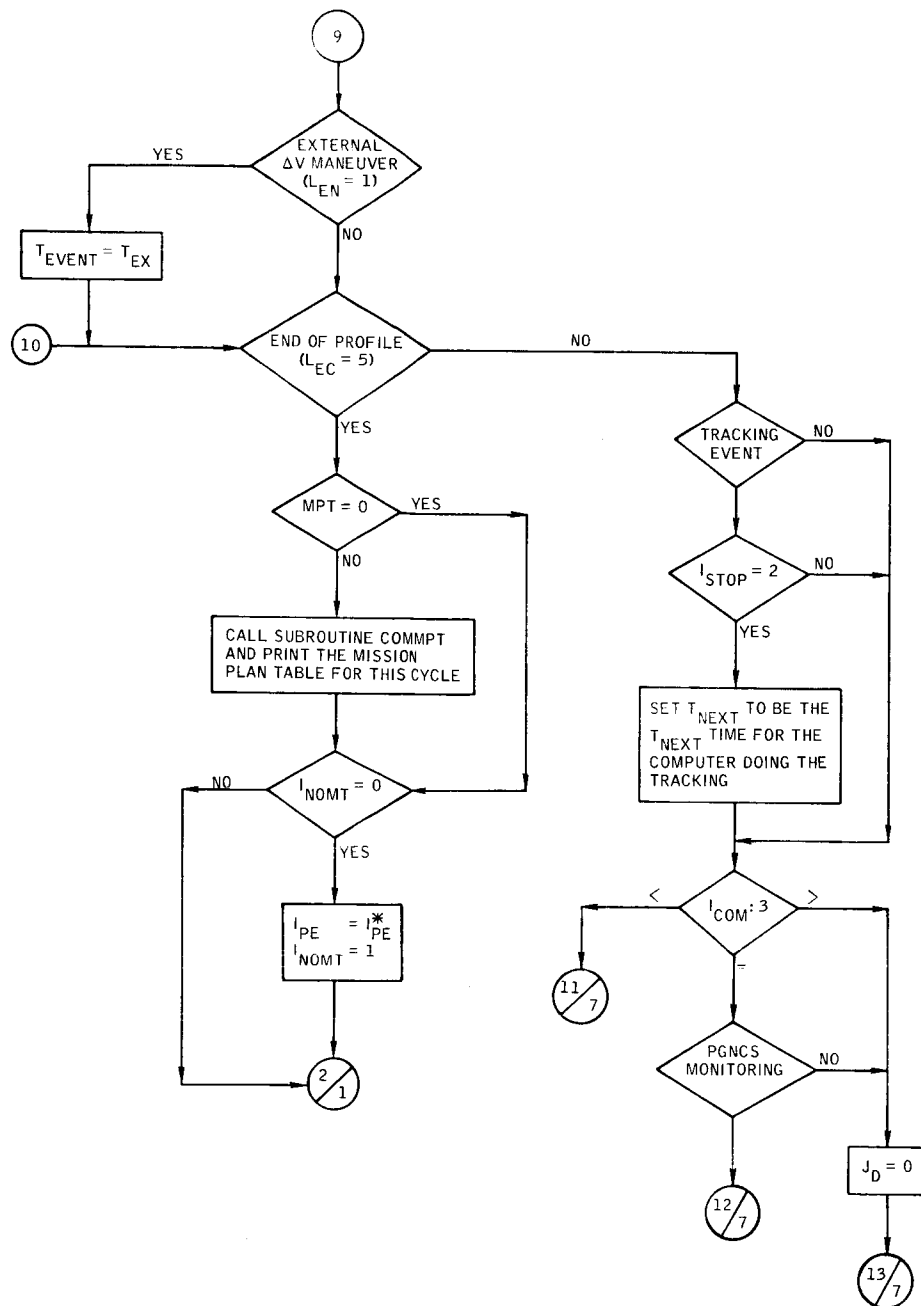


Figure B-8. - Continued.

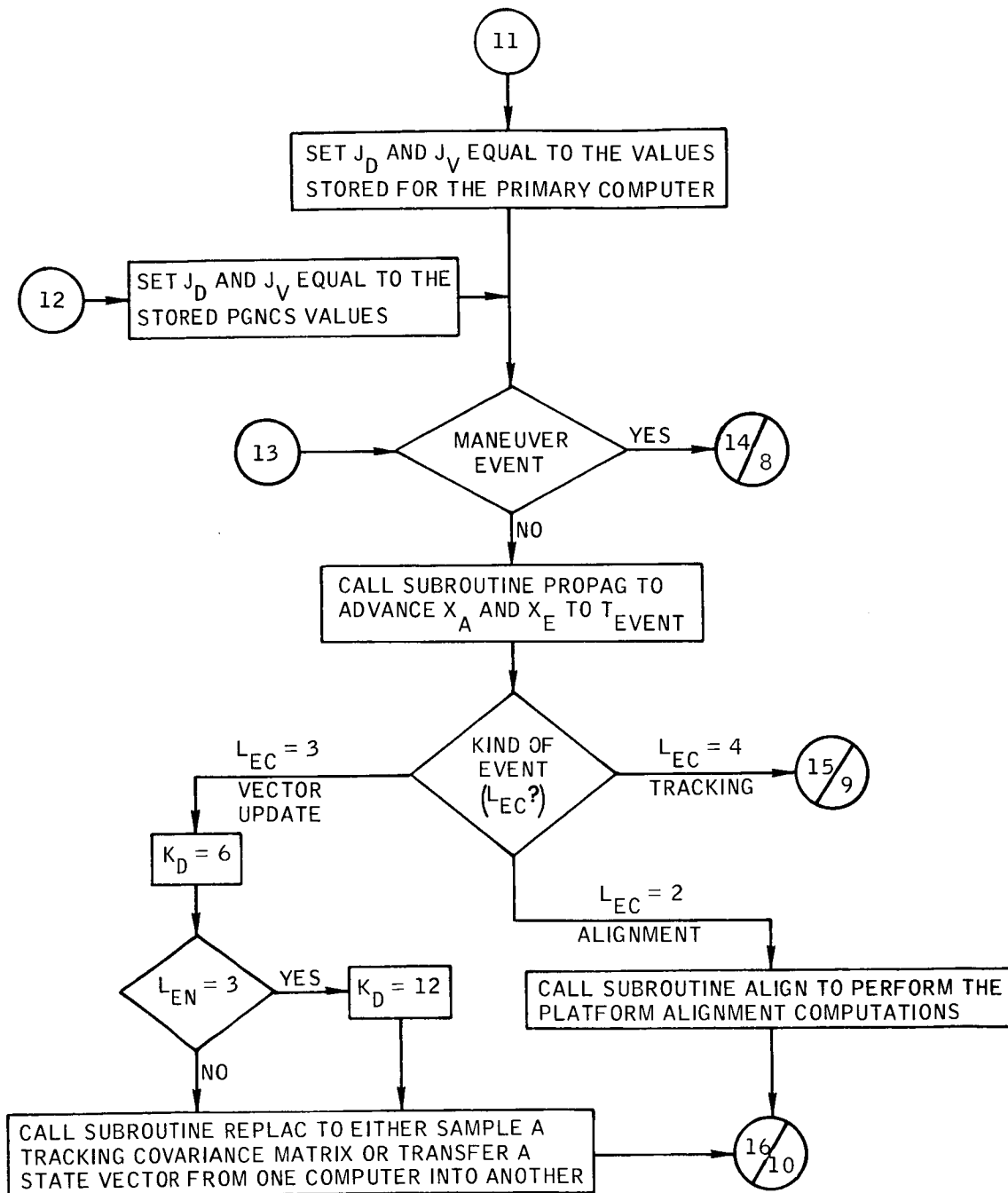


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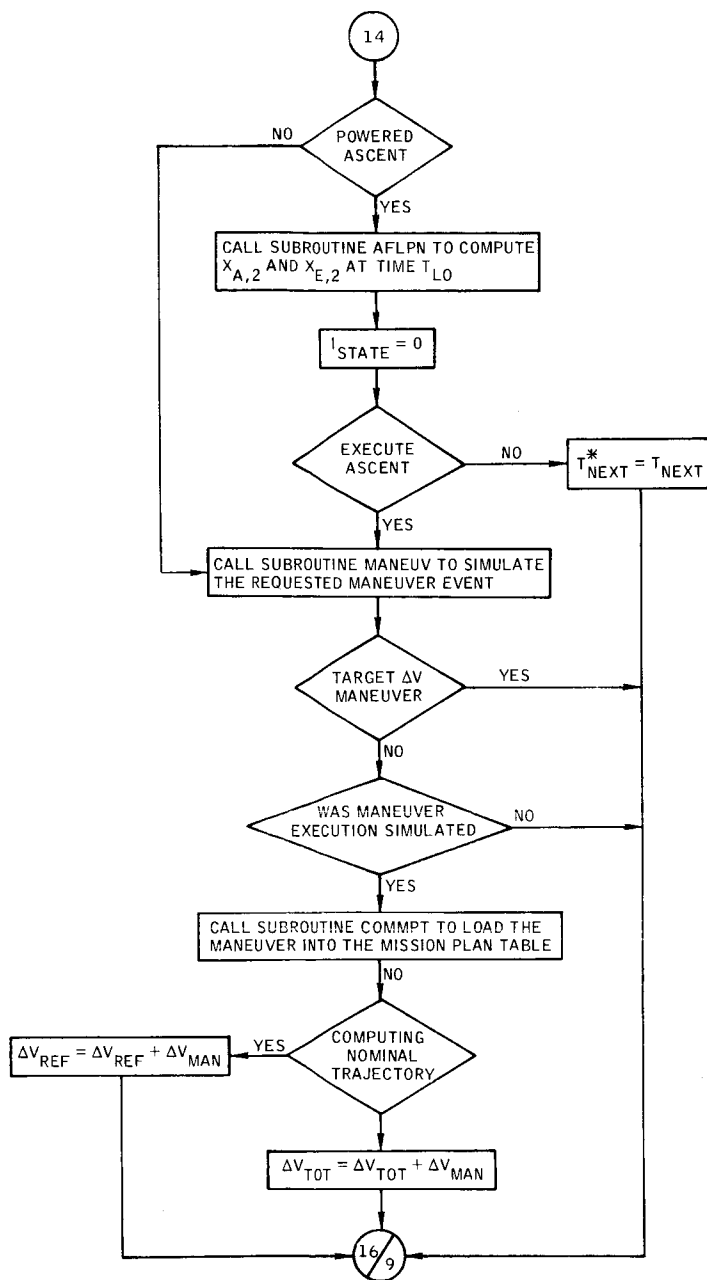


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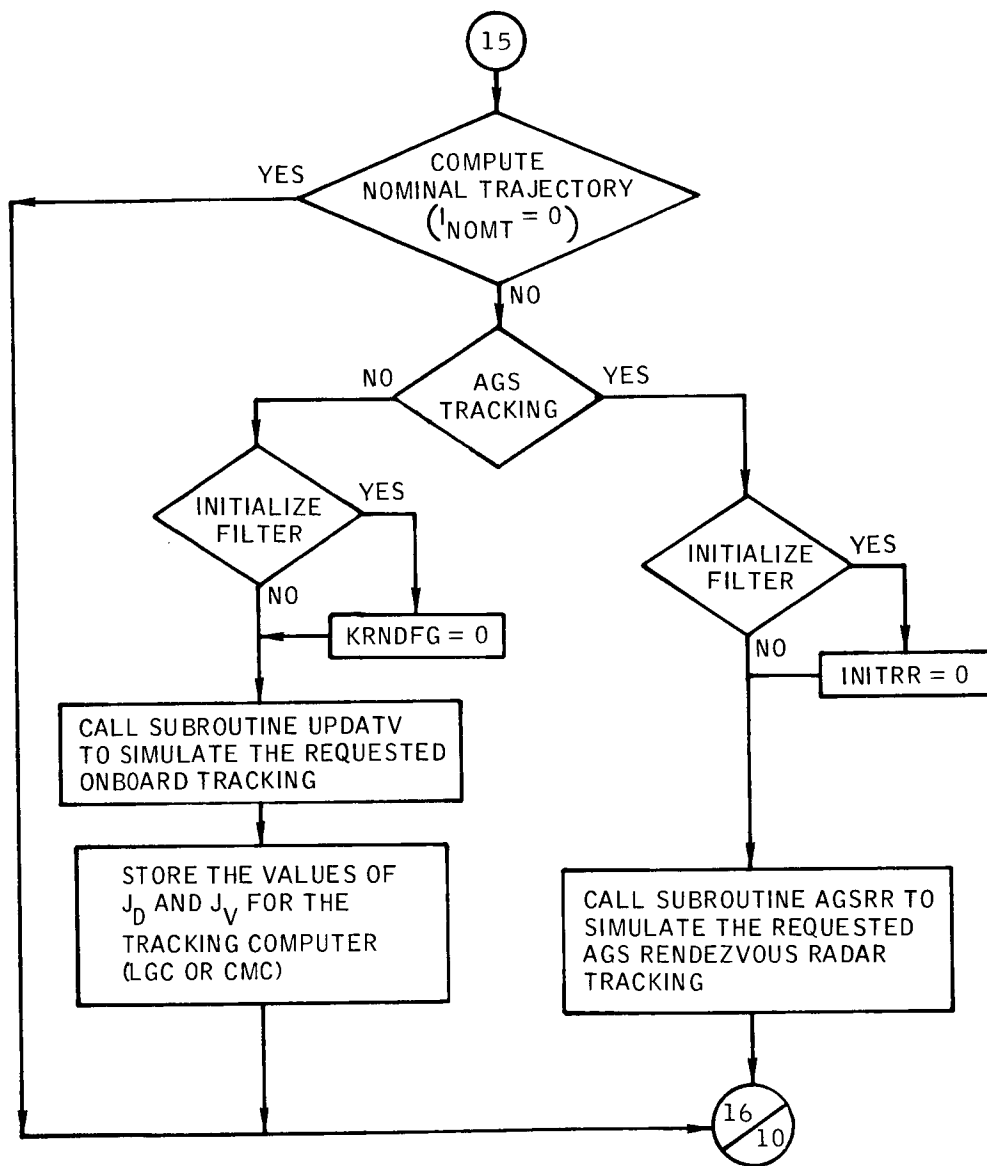


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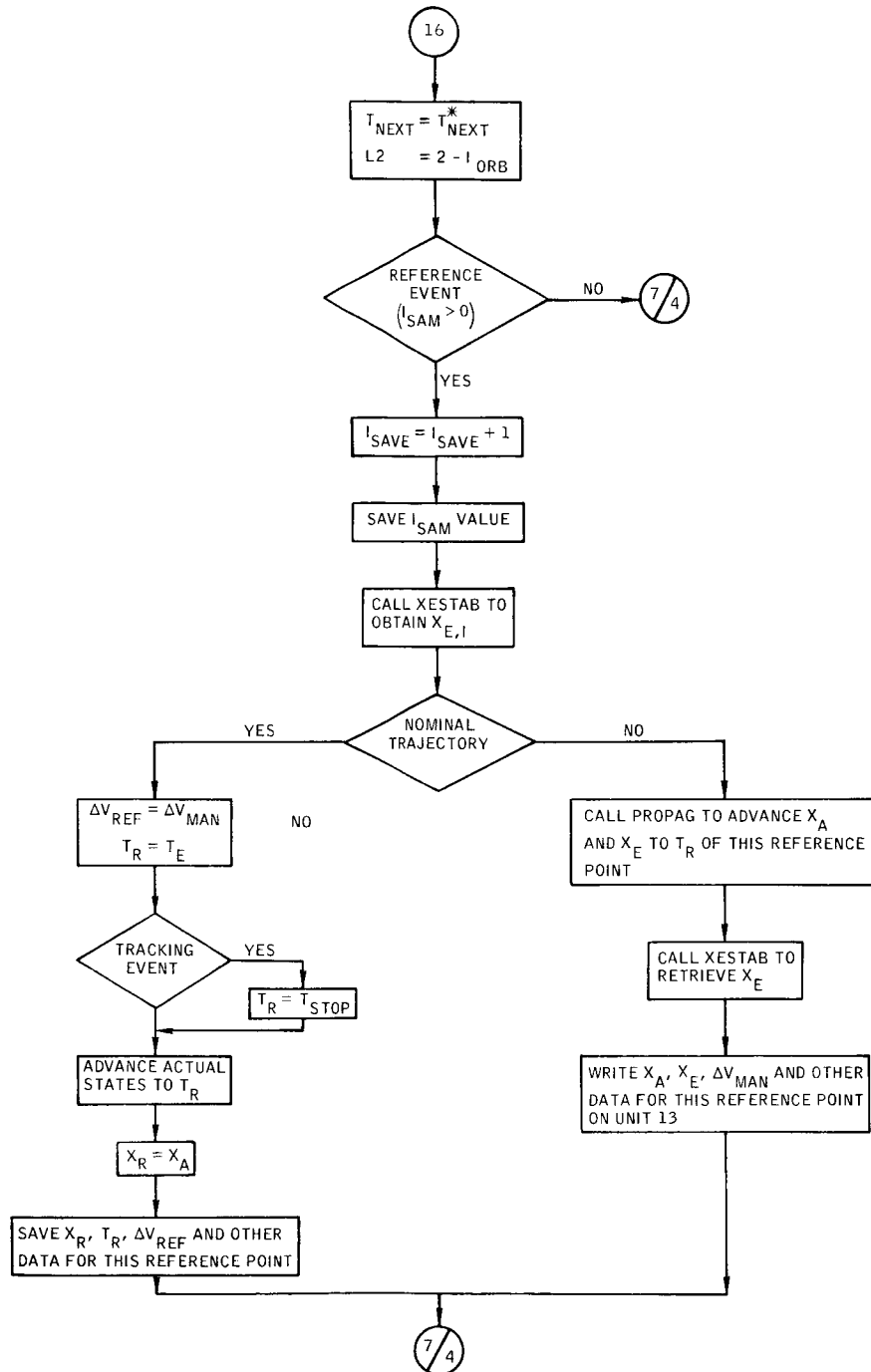


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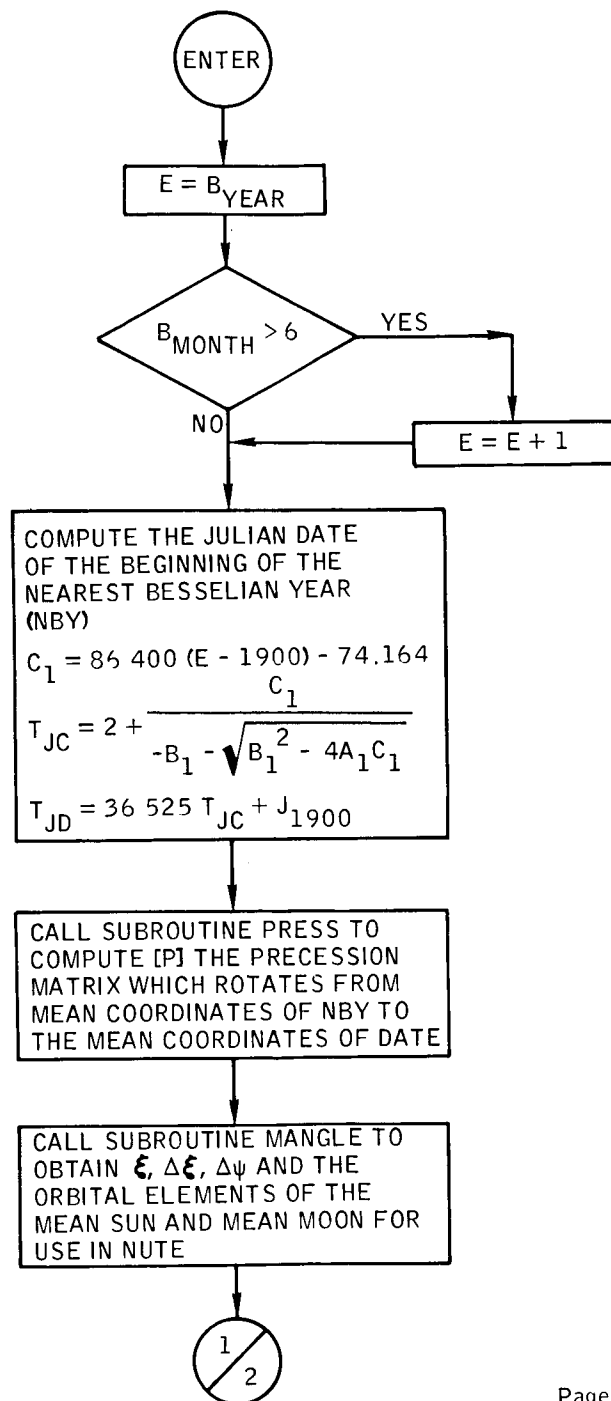


Figure B-9.- Flow chart of subroutine AMATRIX.

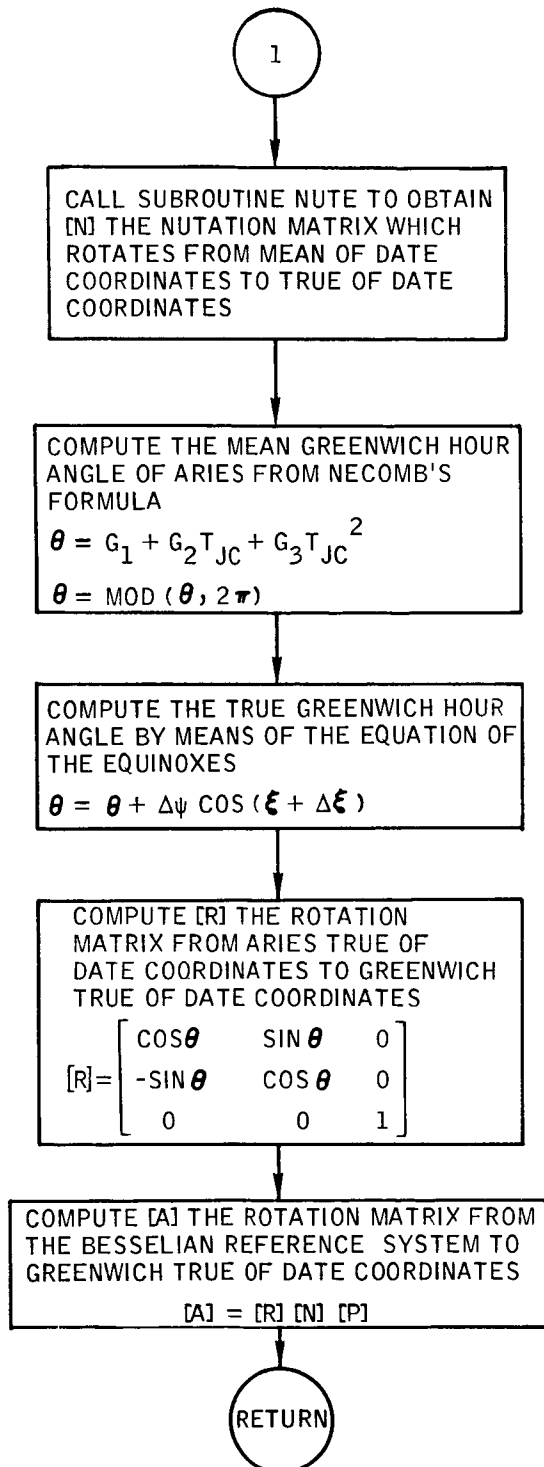


Figure B-9.- Concluded.

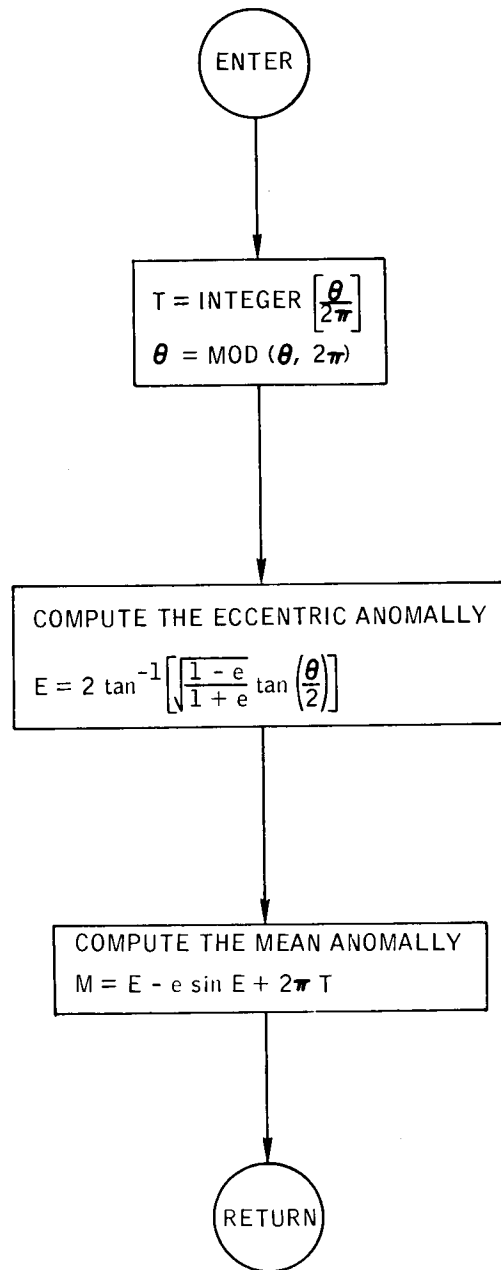


Figure B-10.- Flow chart of subroutine ANOM.

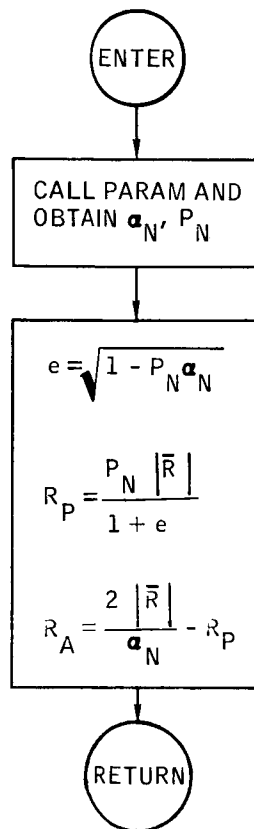


Figure B-11.- Flow chart of subroutine APSIDE.

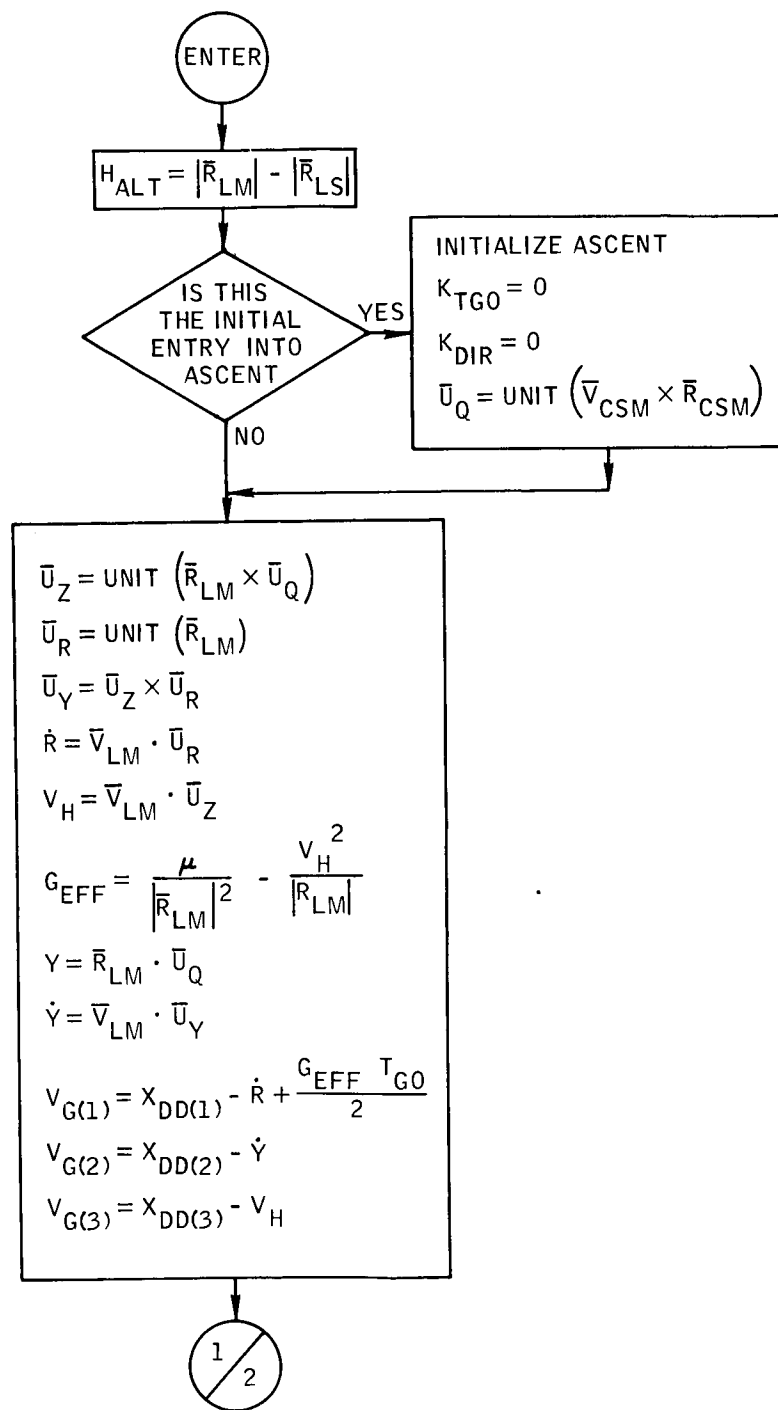
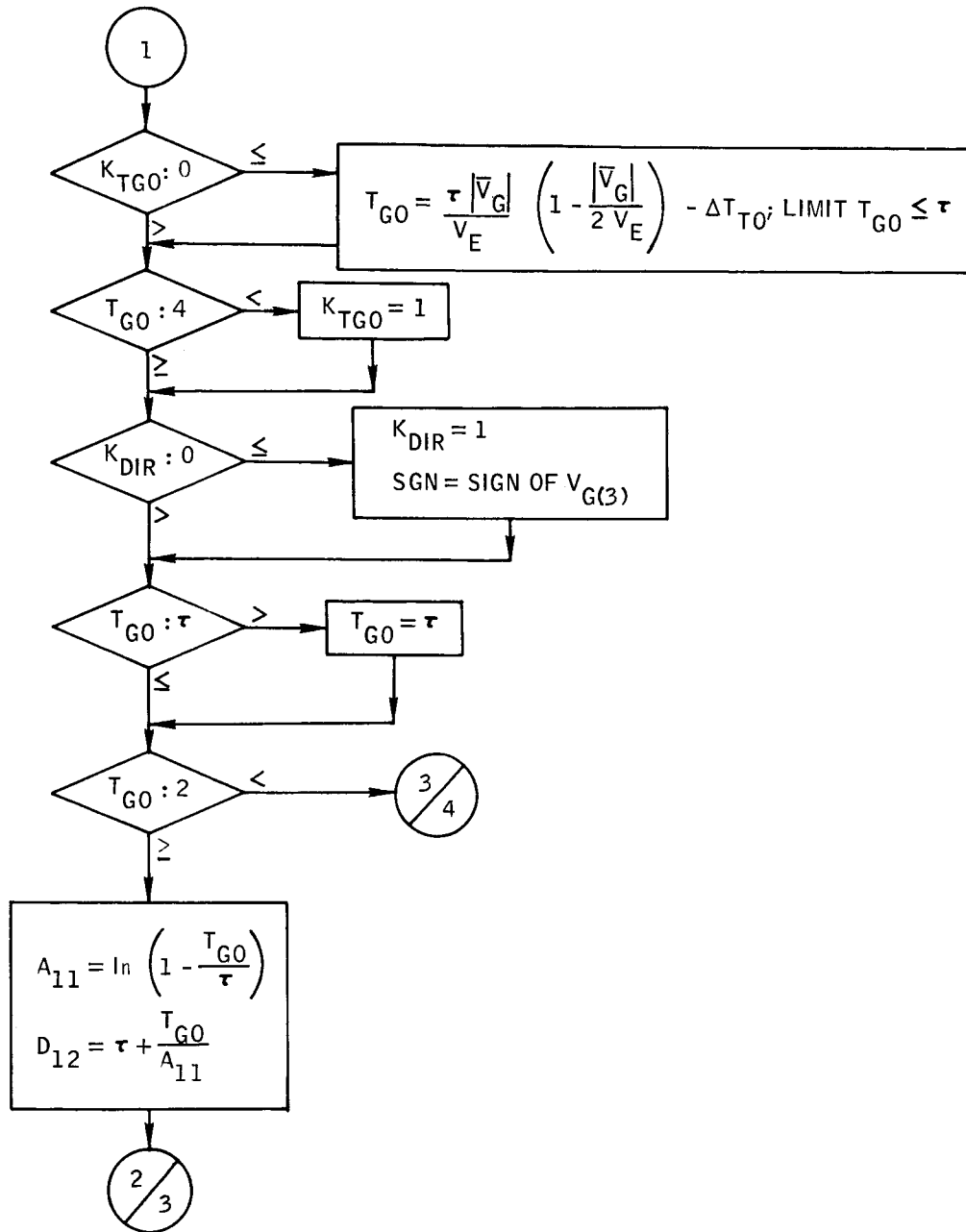


Figure B-12.- Flow chart of subroutine ASCENT.



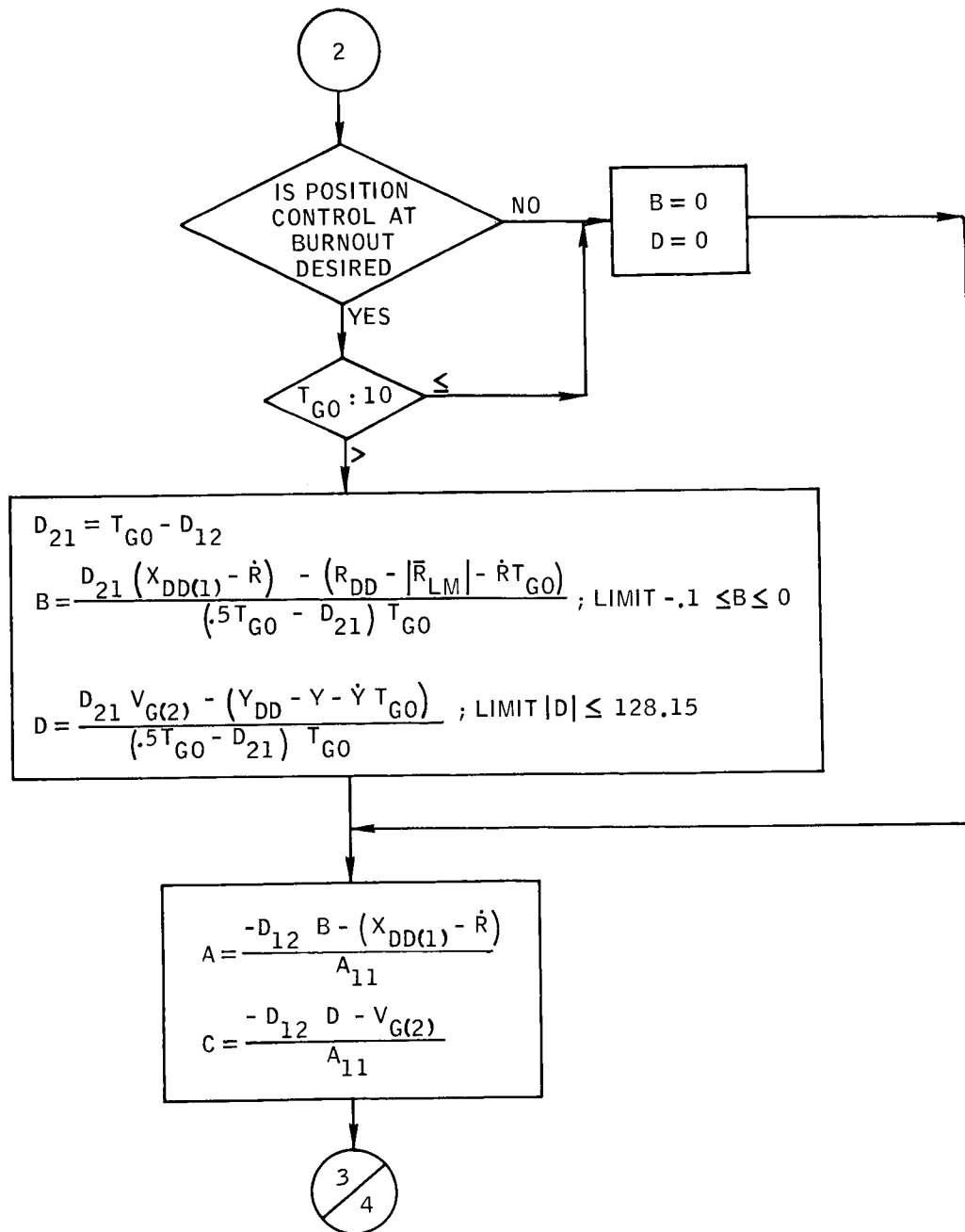
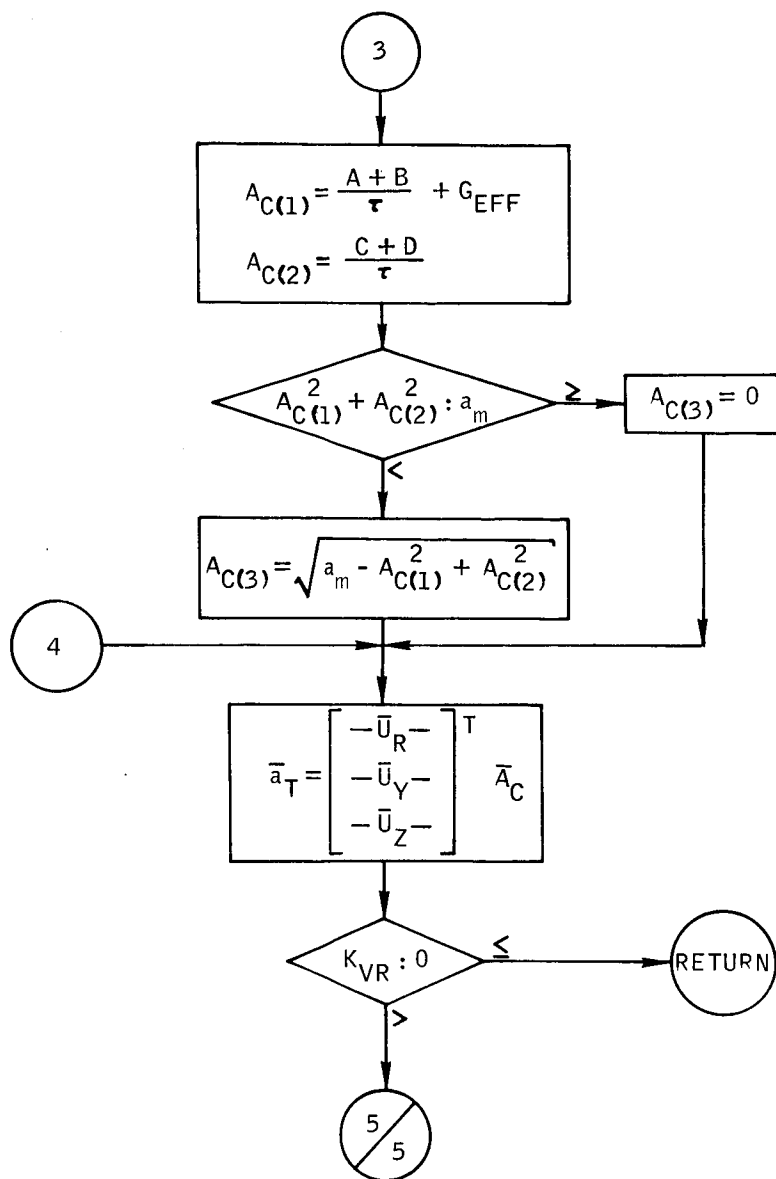


Figure B-12.- Continued.





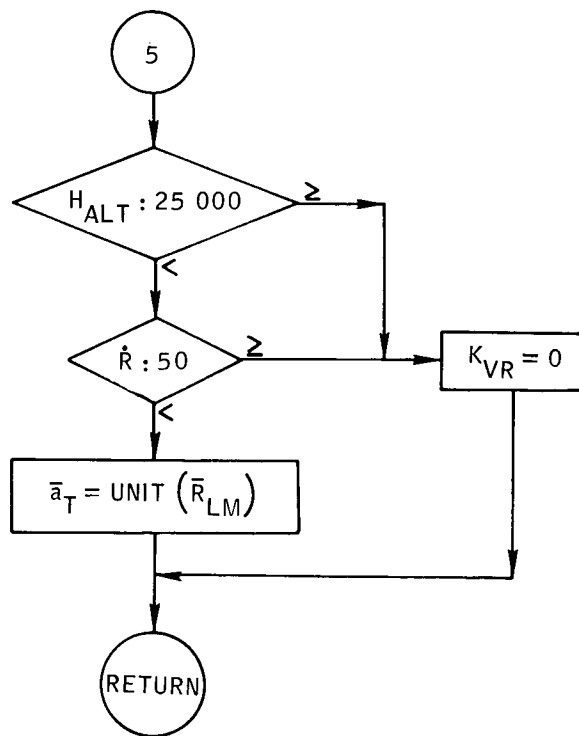


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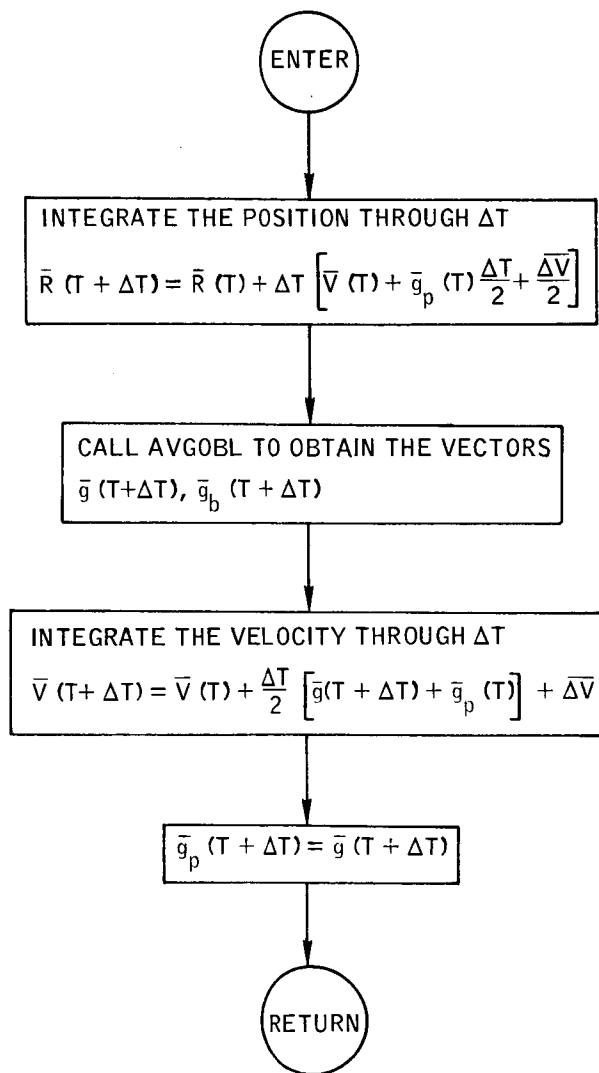


Figure B-13. - Flow chart of subroutine AVEG.

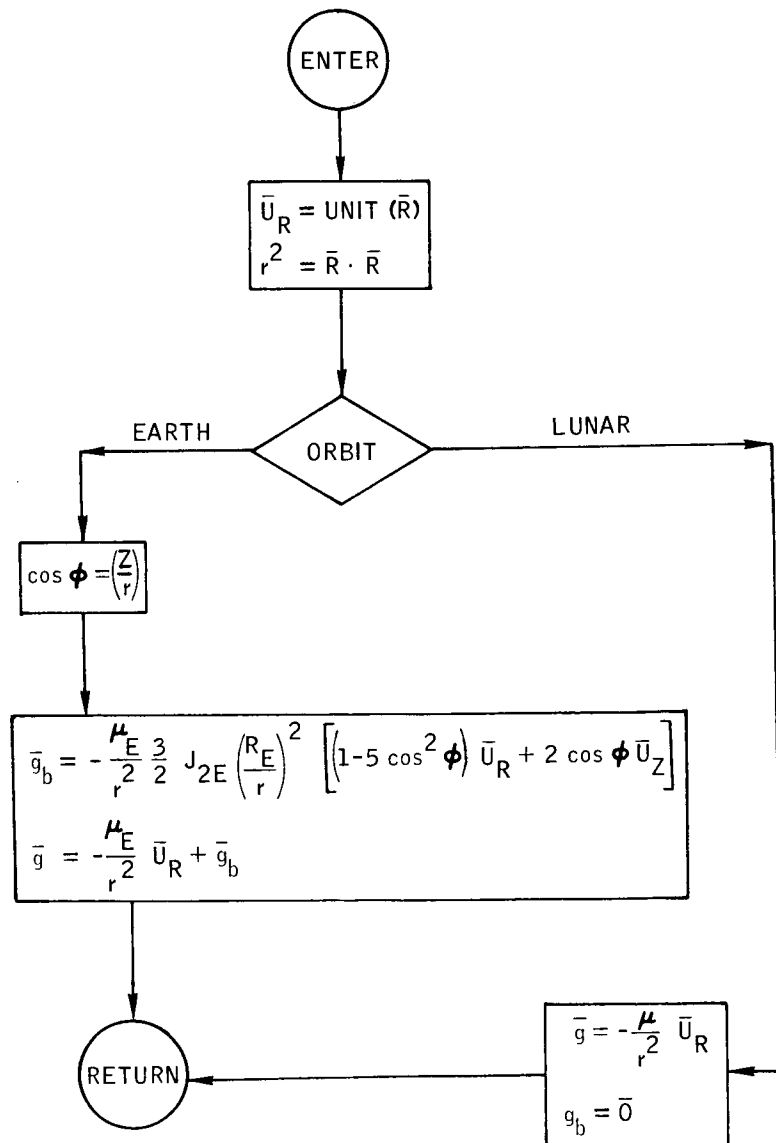


Figure B-14.- Flow chart of subroutine AVG0BL.

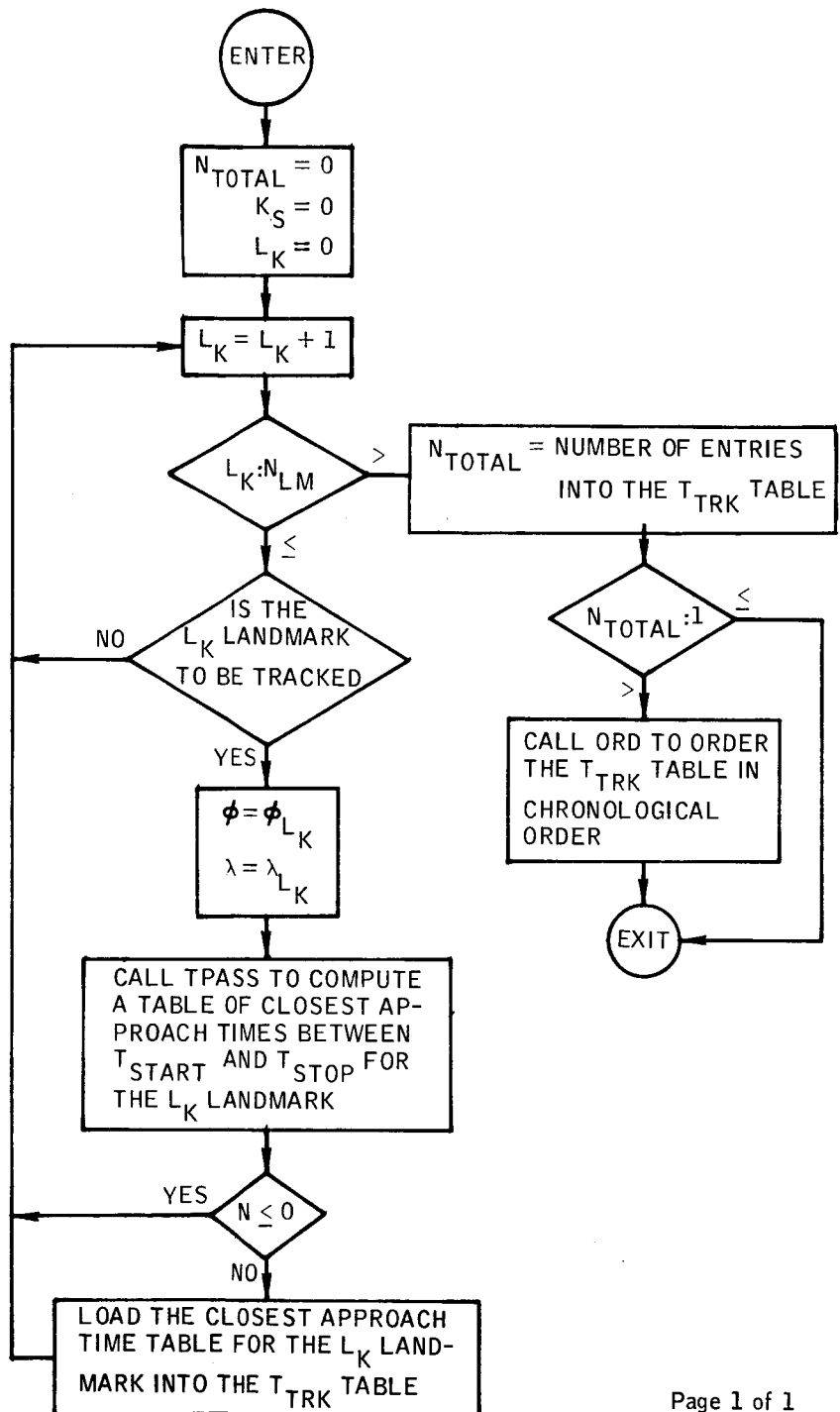


Figure B-15.- Flow chart of subroutine CATIME.

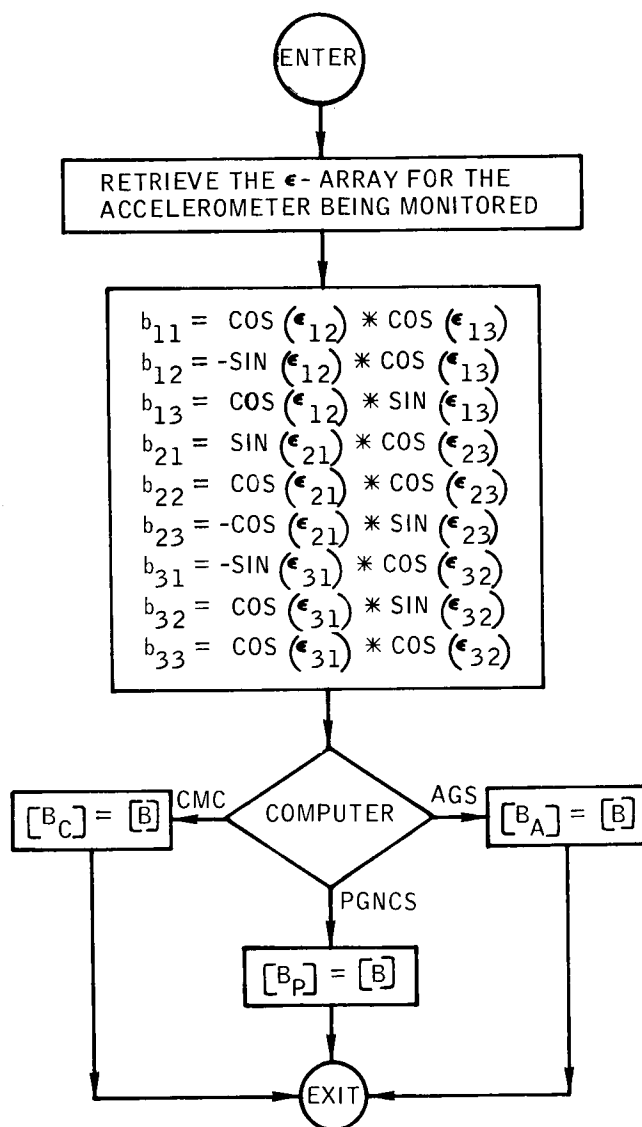


Figure B-16.- Flow chart of subroutine CBA.

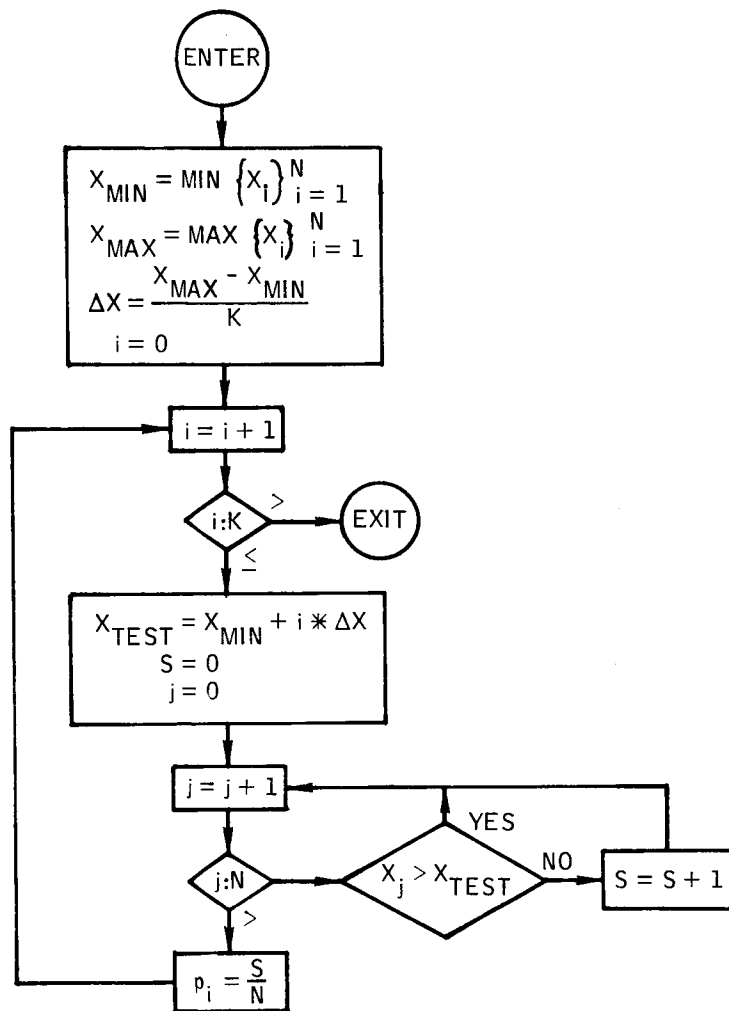


Figure B-17. - Flow chart of subroutine CDFUNC.

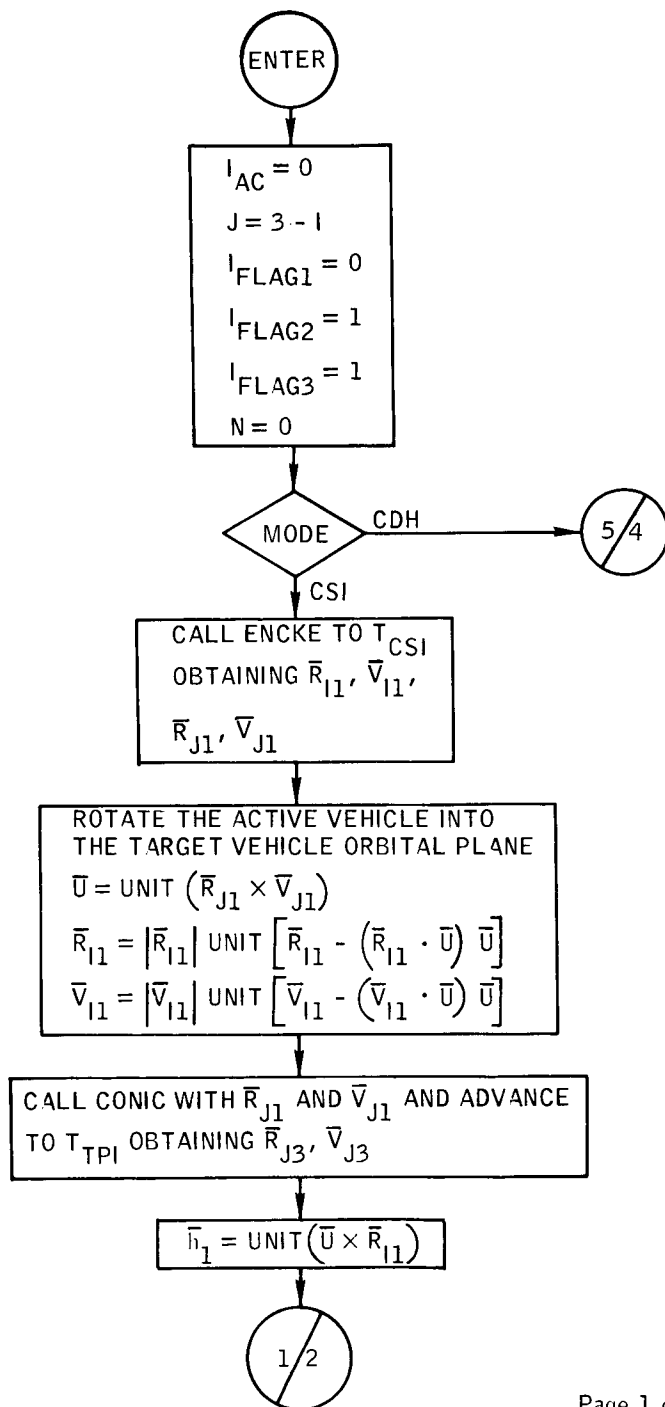


Figure B-18.- Flow chart of subroutine CFP.

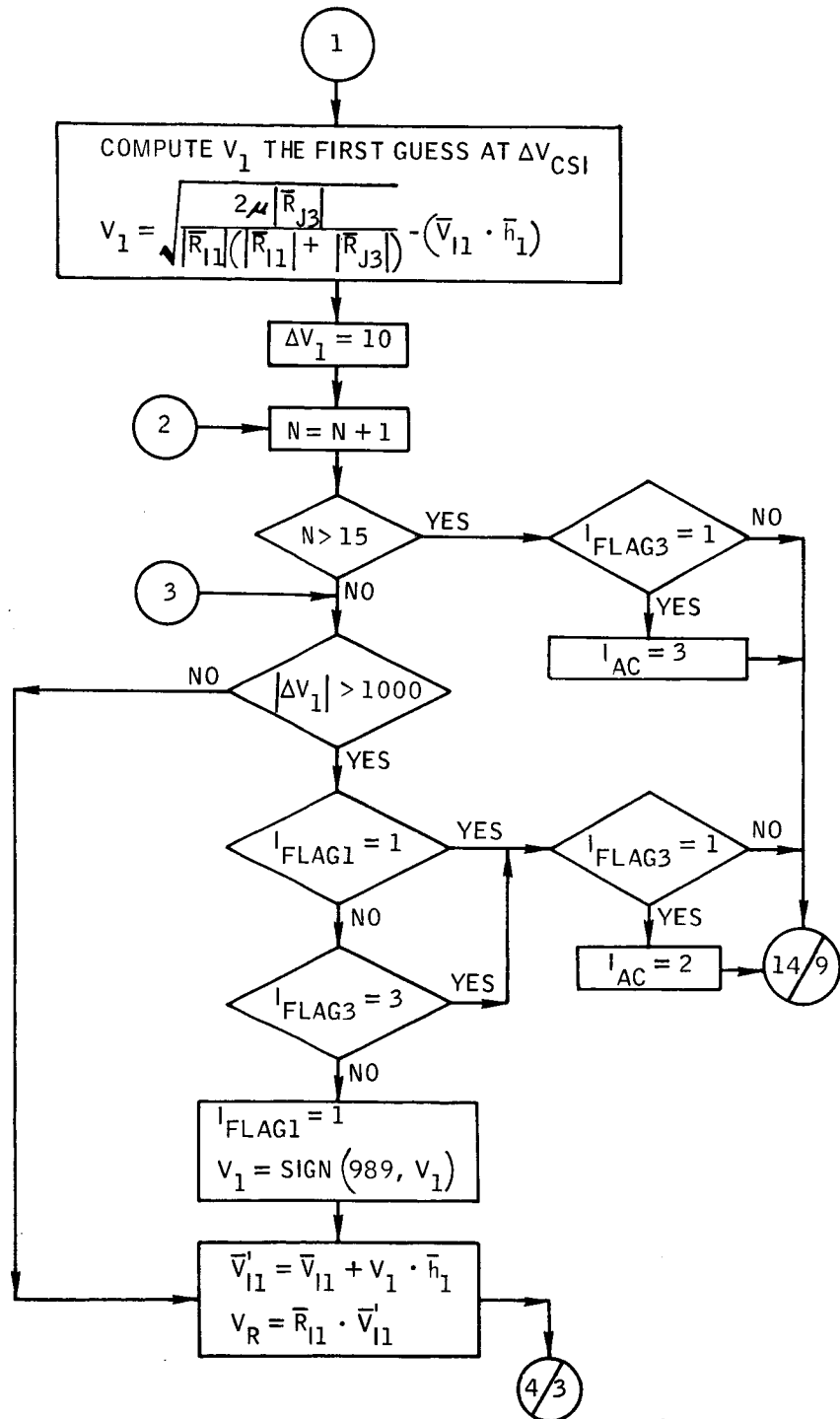


Figure B-18.- Continued.



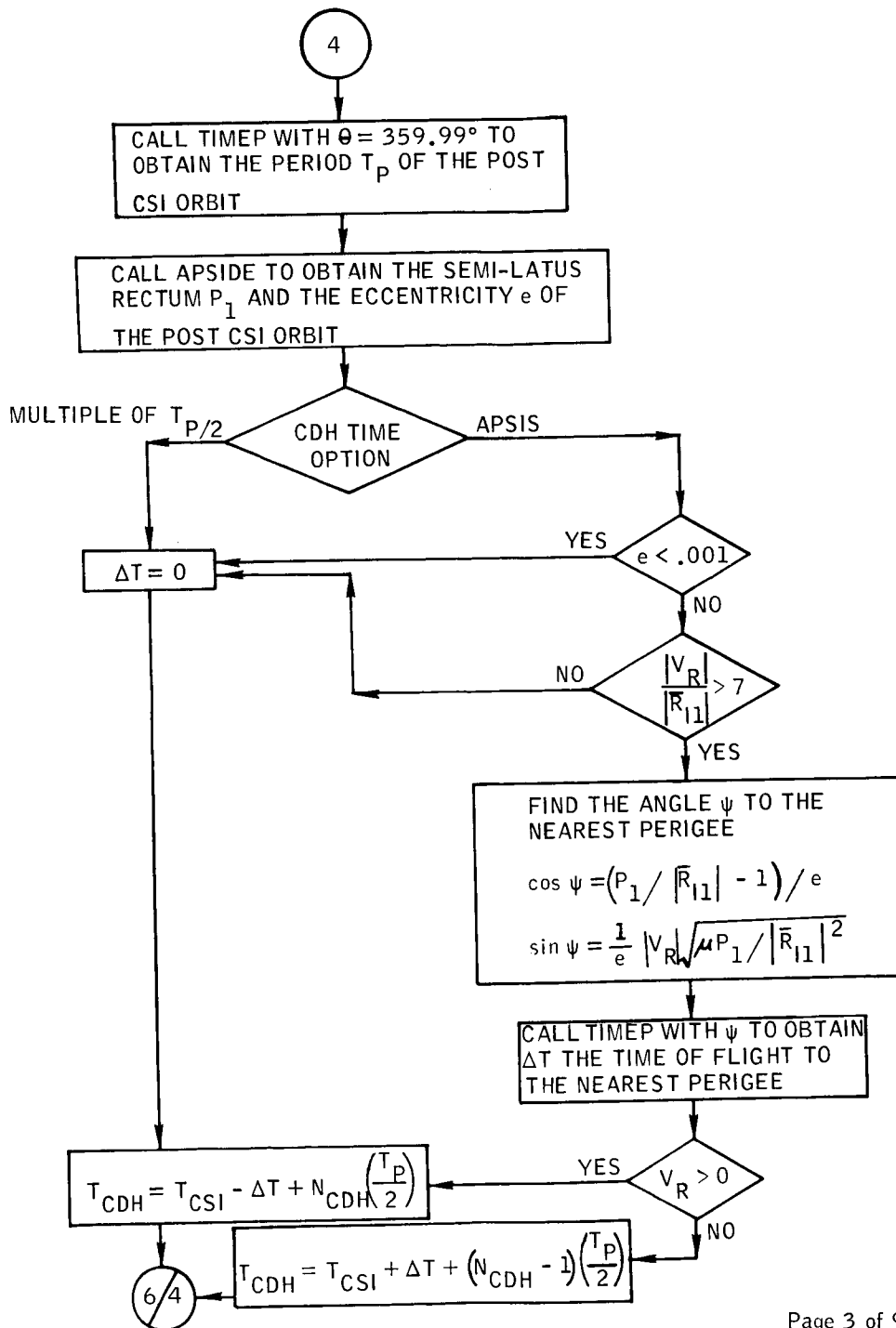


Figure B-18.- Continued.

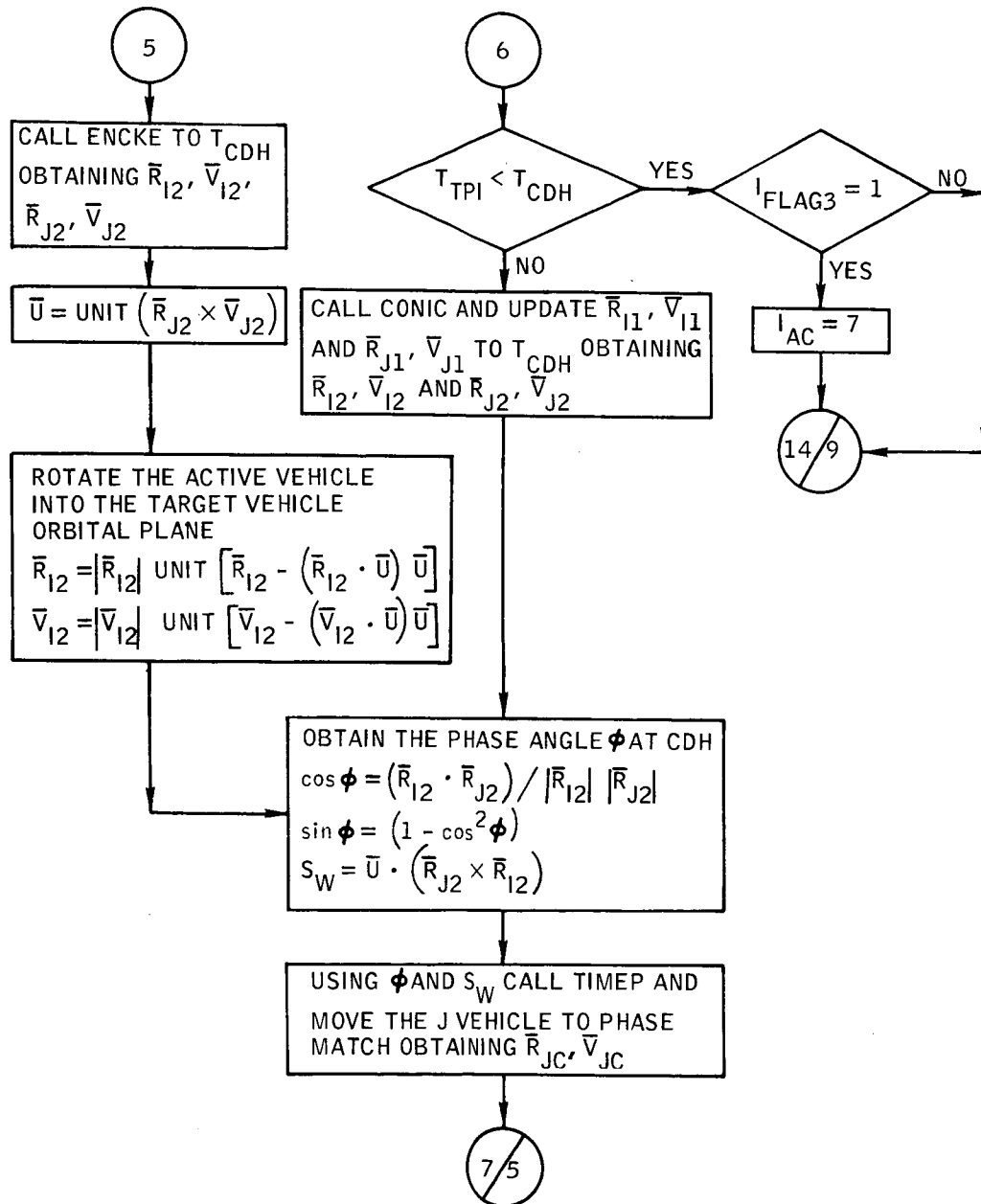


Figure B-18.- Continued.

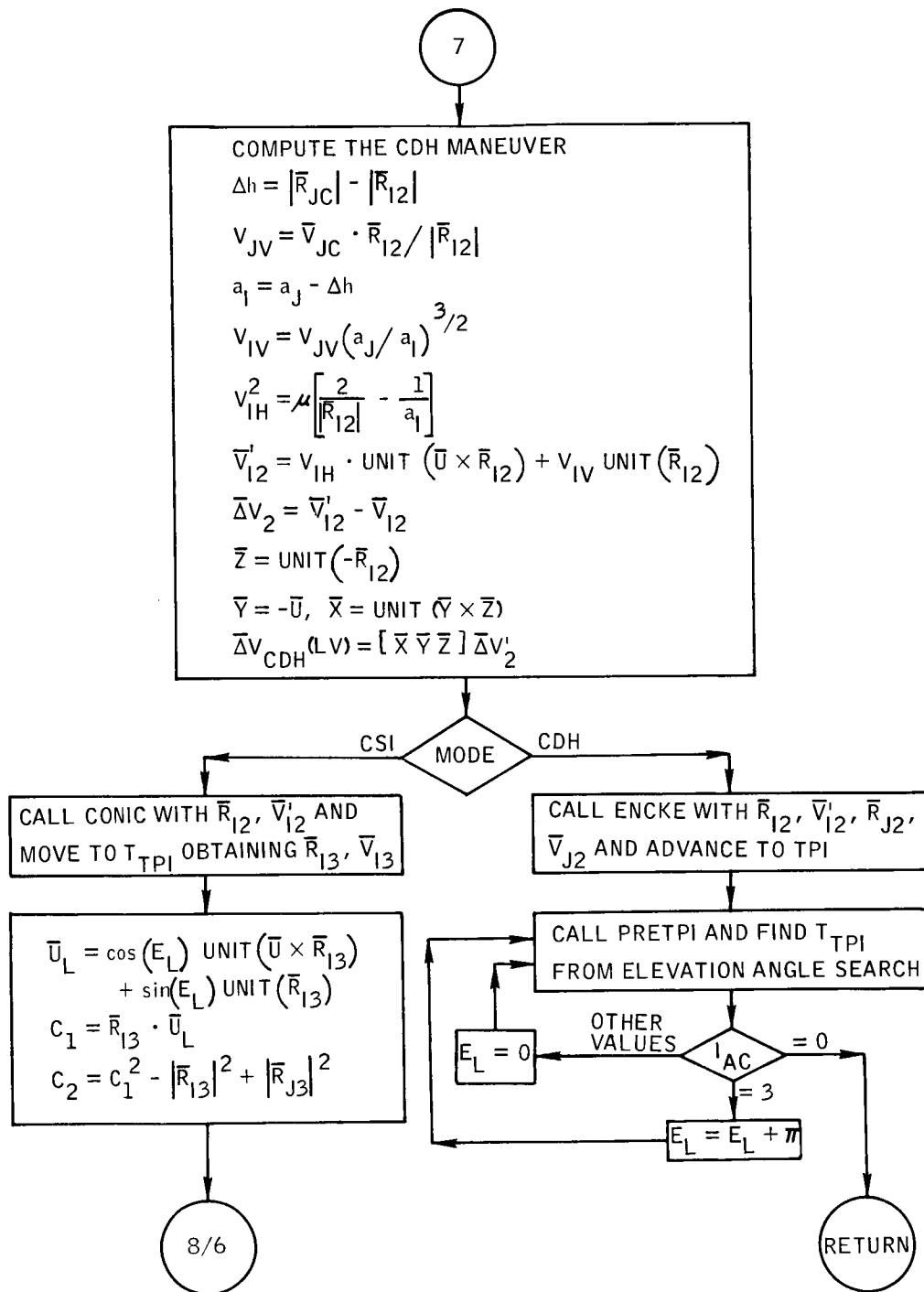


Figure B-18.- Continued.

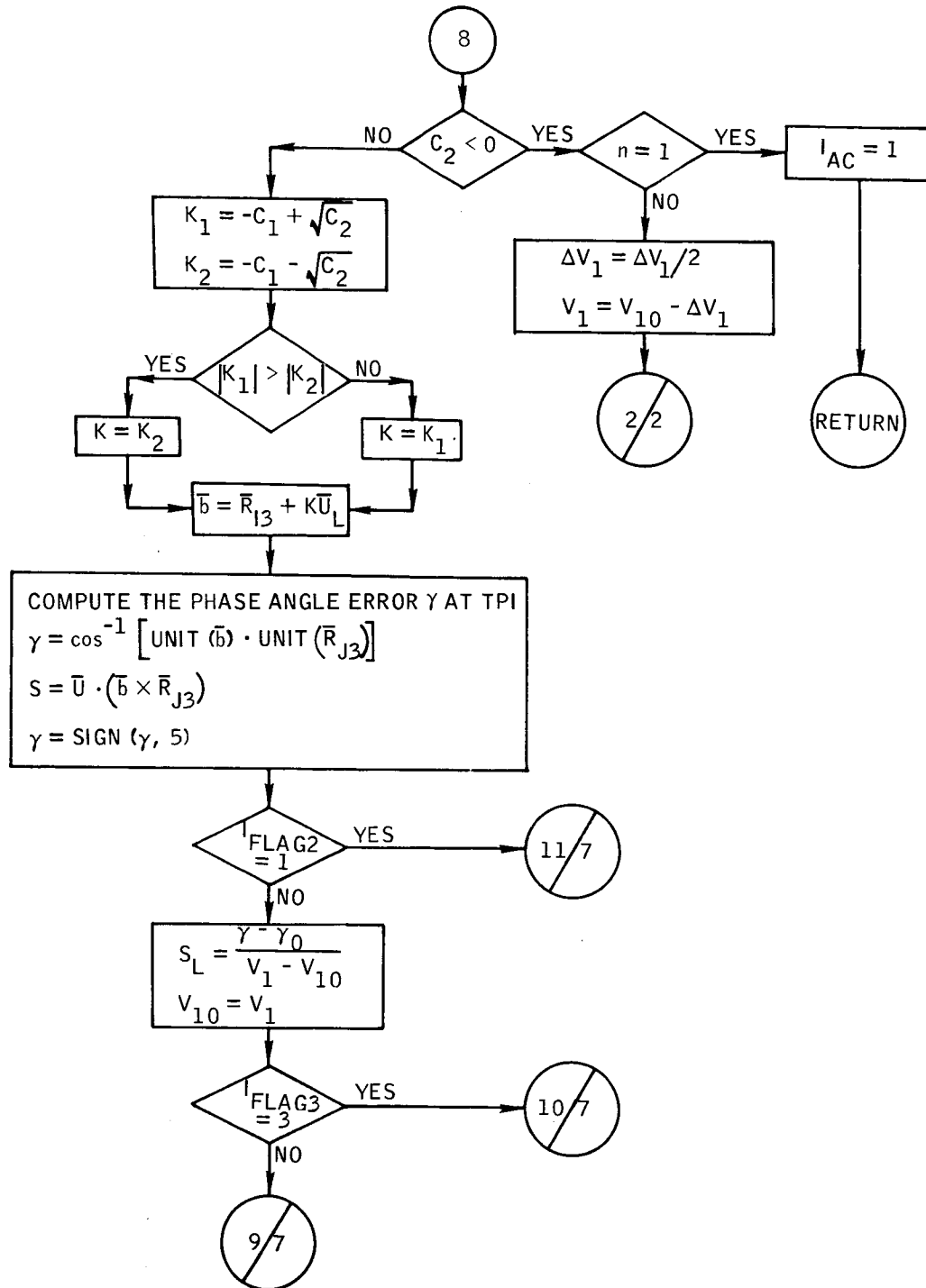


Figure B-18.- Continued.

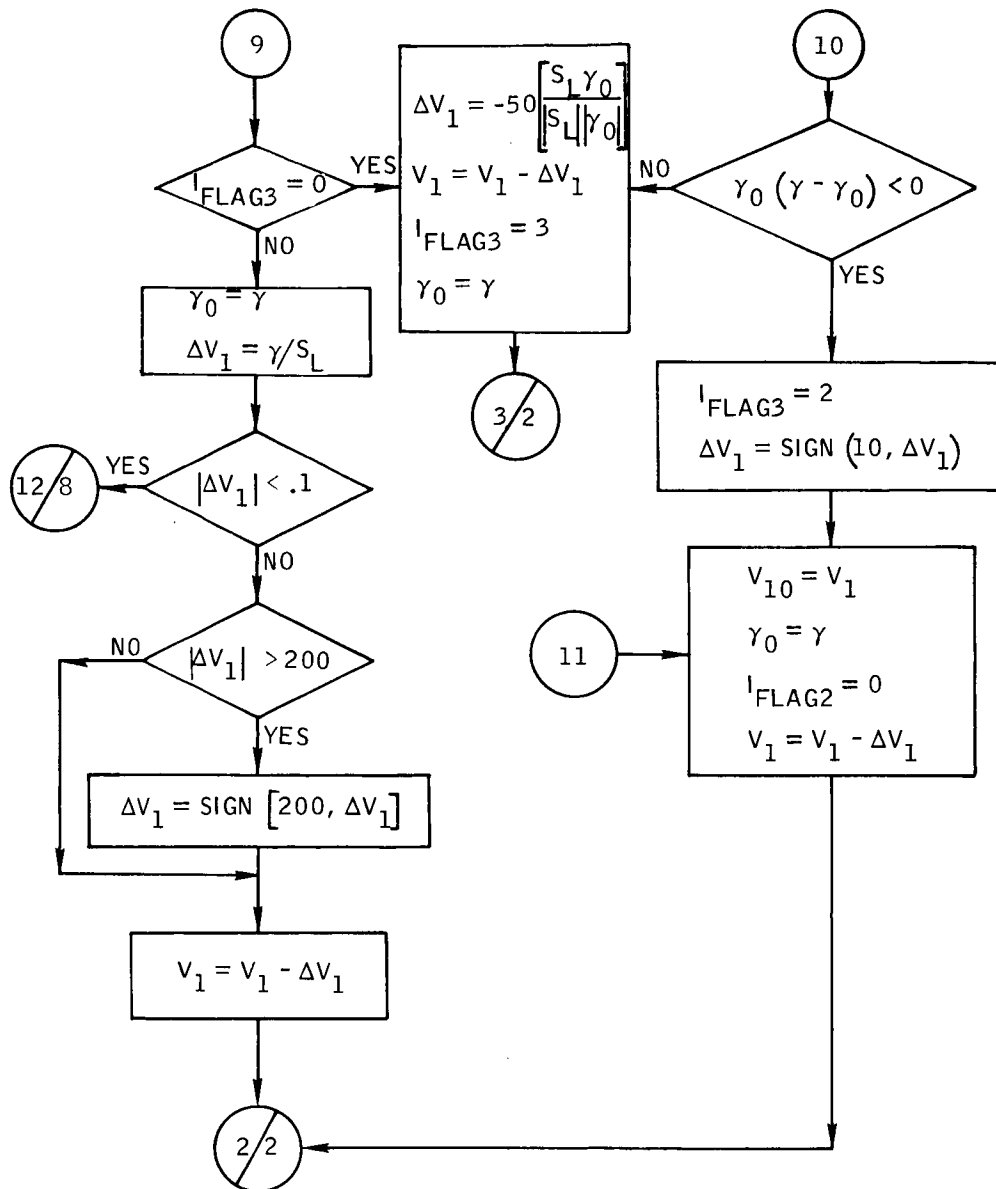


Figure B-18.- Continued.

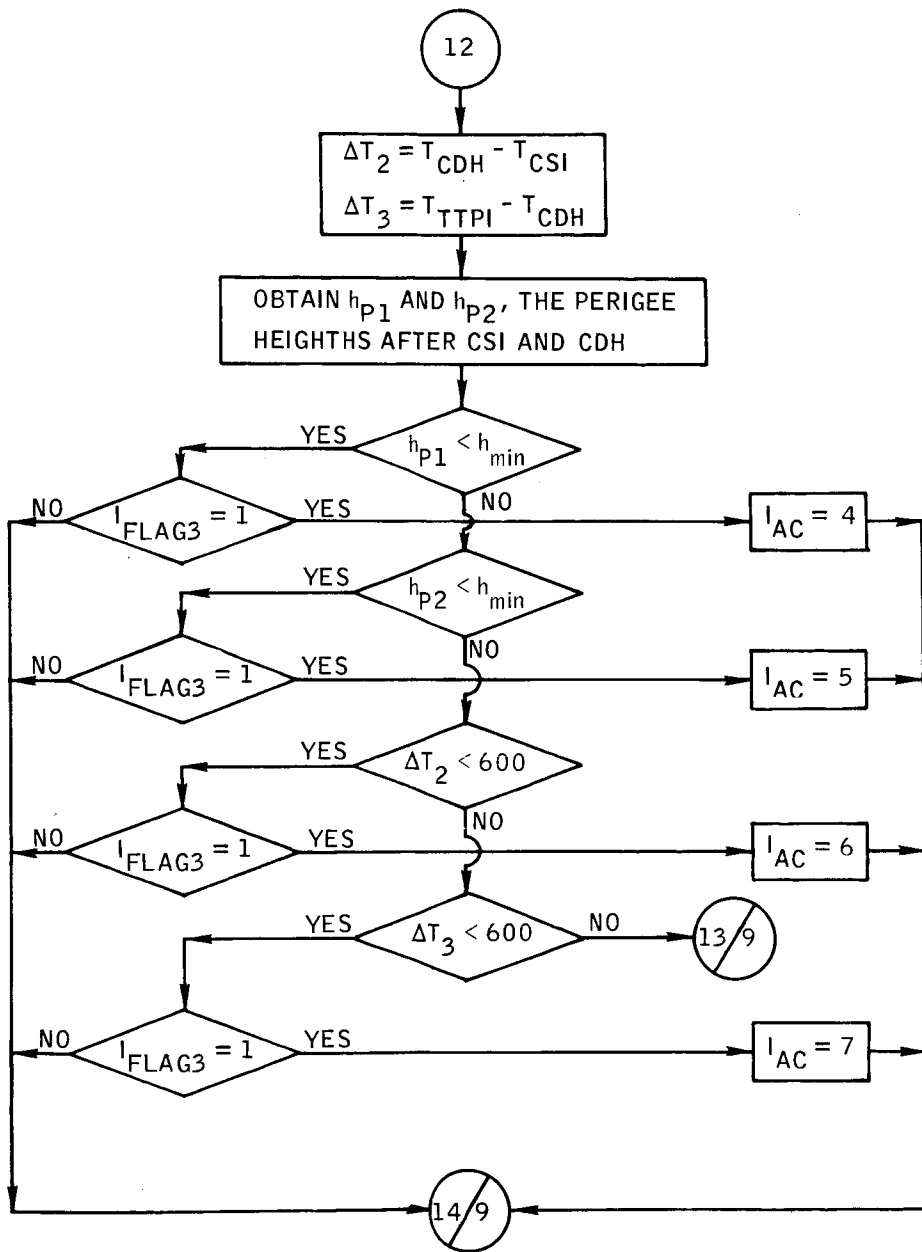


Figure B-18.- Continued.

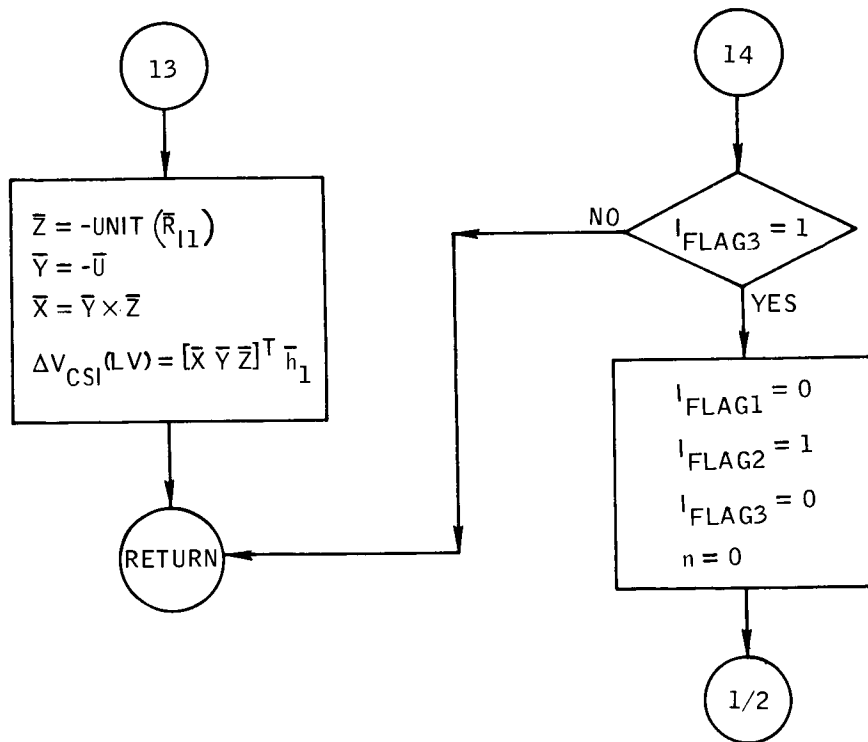


Figure B-18.- Concluded.

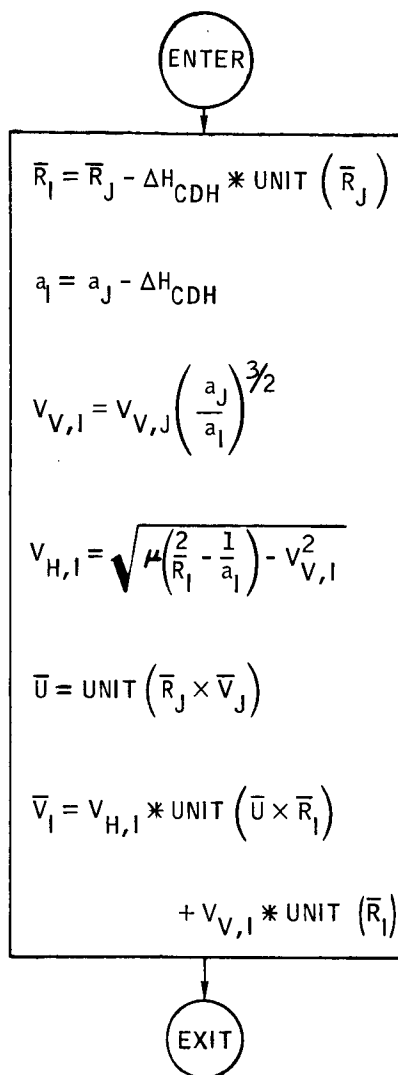


Figure B-19.- Flow chart of subroutine COE.



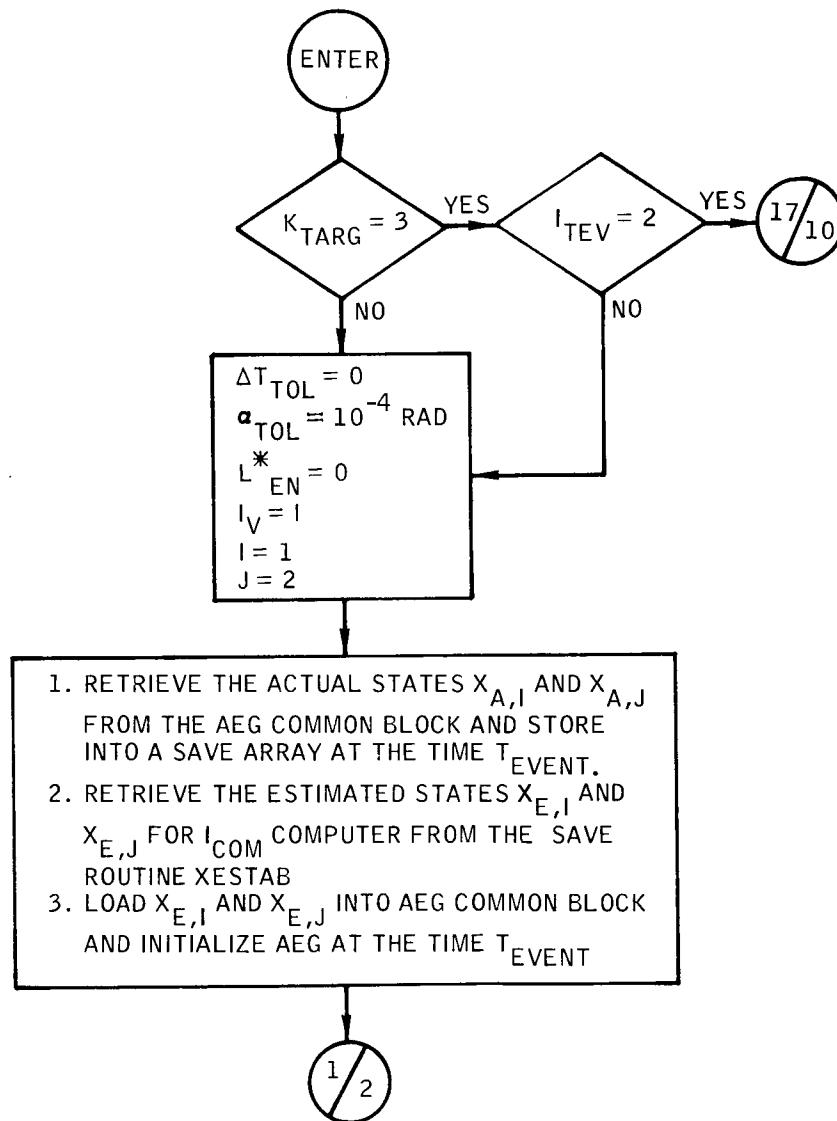


Figure B-20.- Flow chart of subroutine COMDK1.

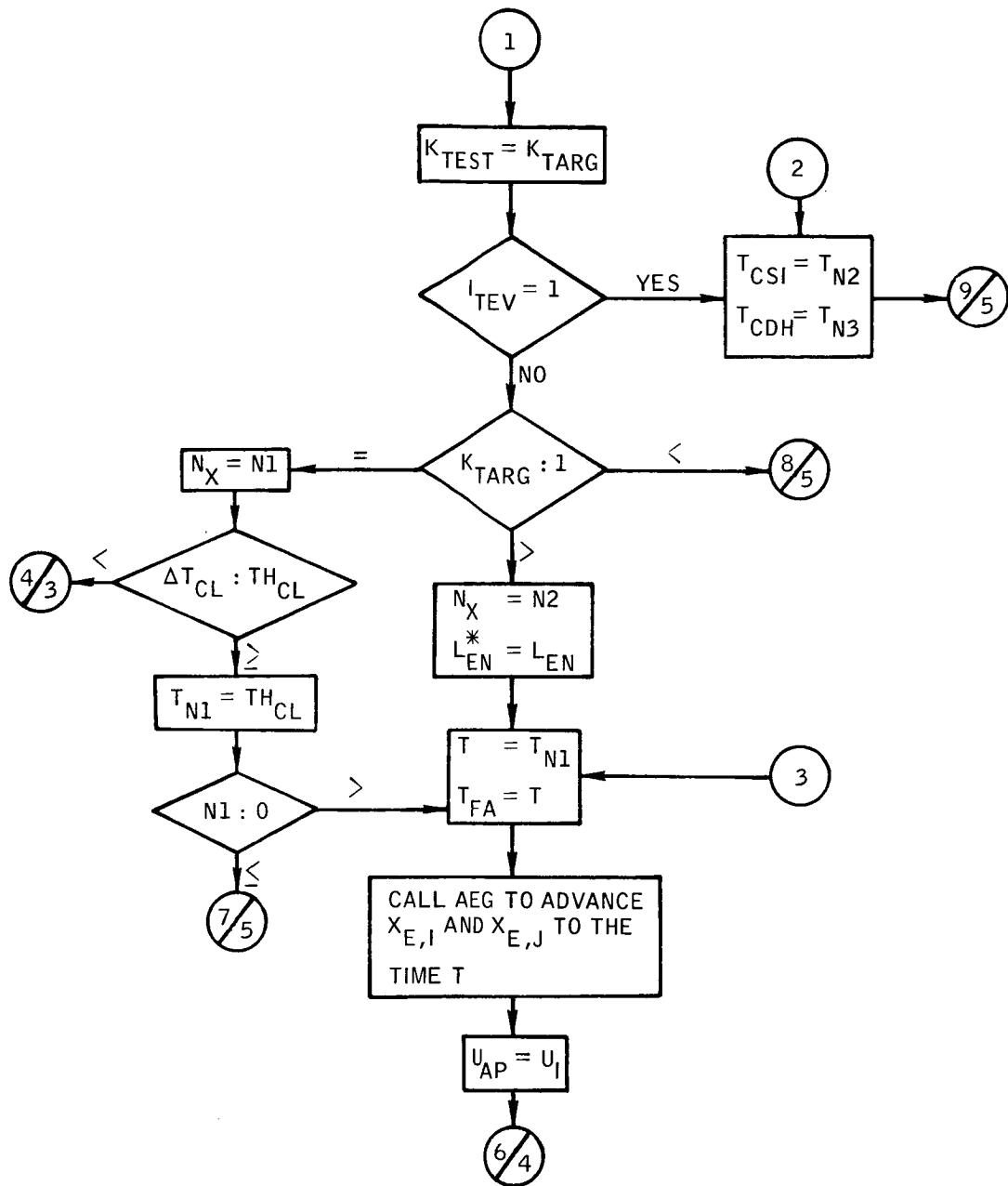


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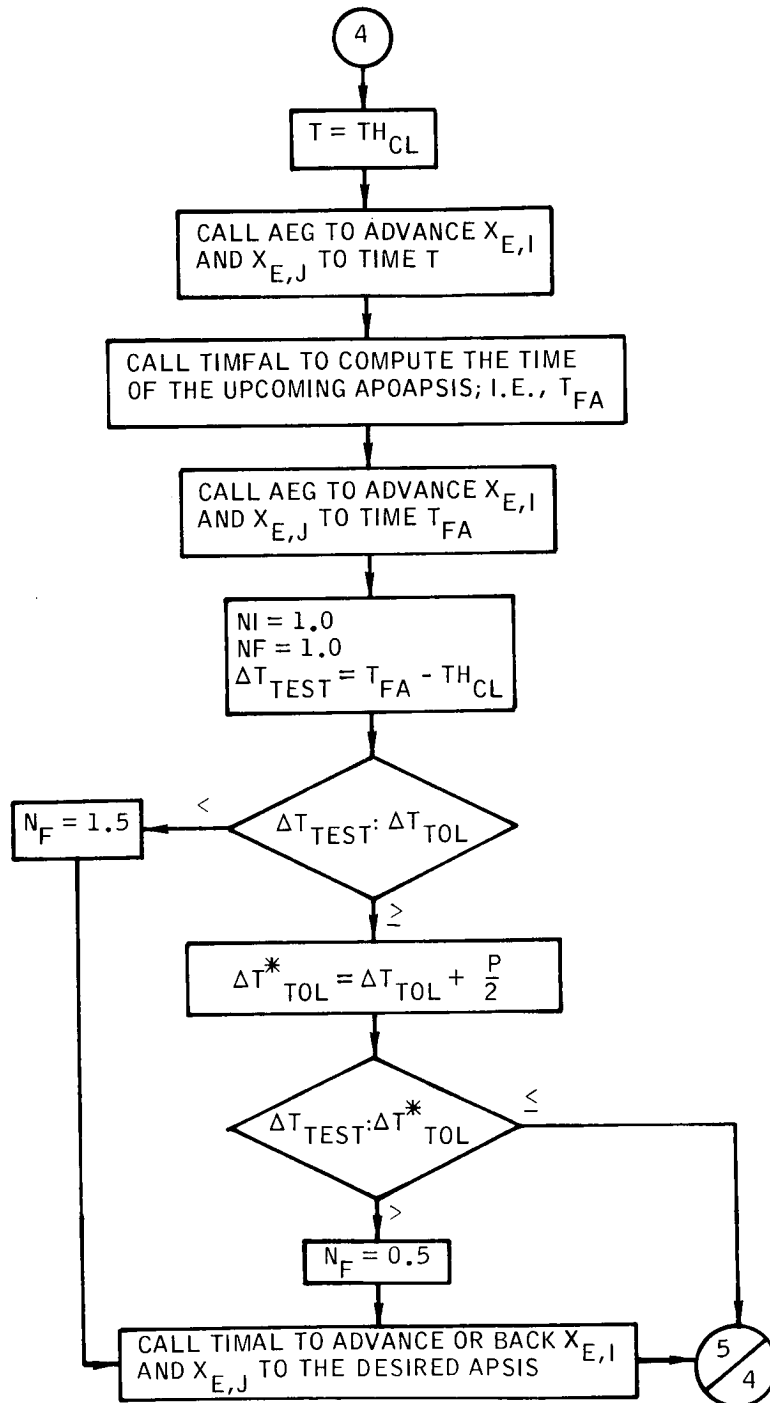


Figure B-20. - Continued.

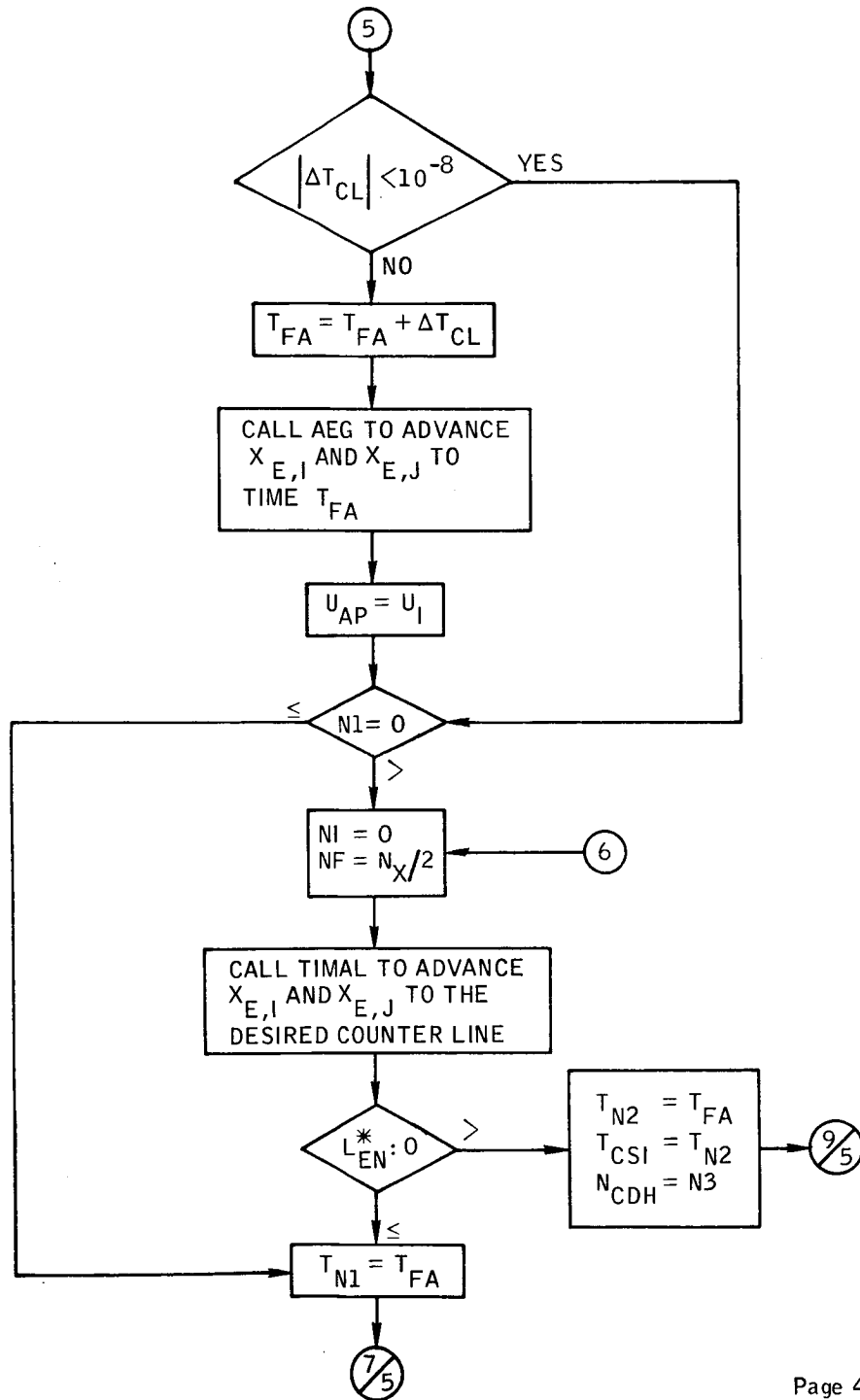


Figure B-20.- Continued.

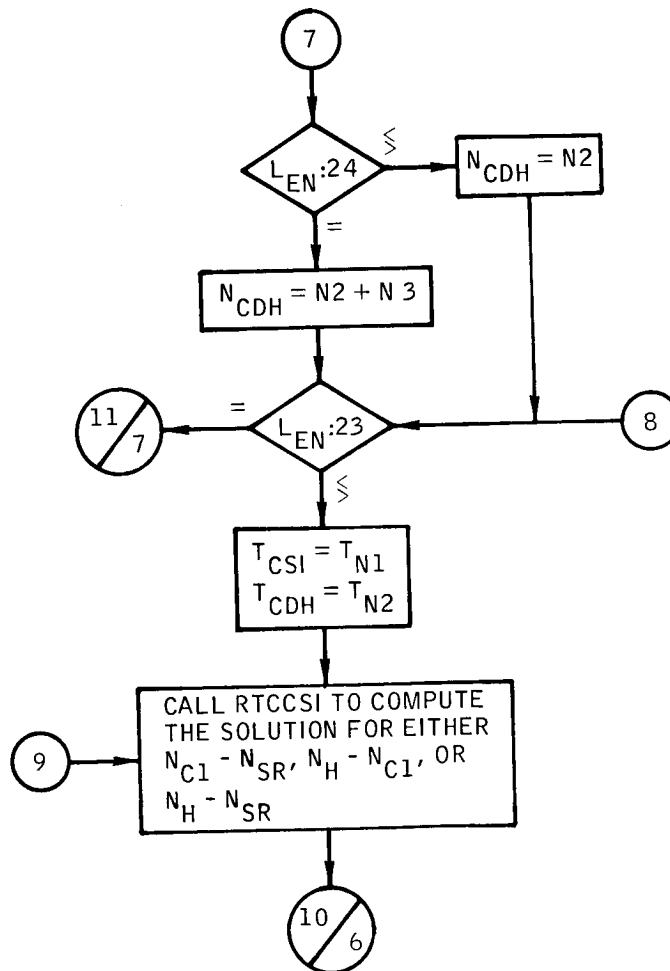


Figure B-20. - Continued.

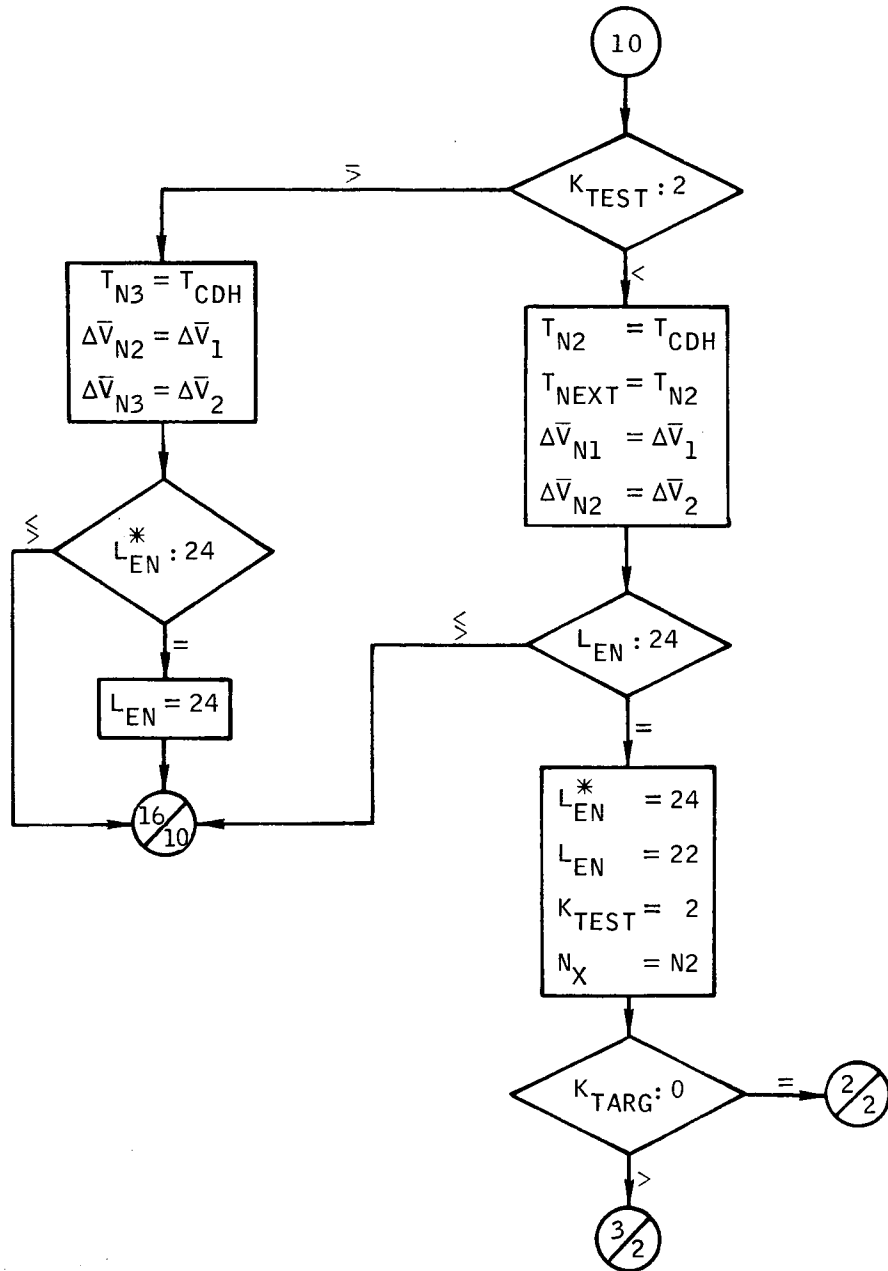


Figure B-20.- Continued.

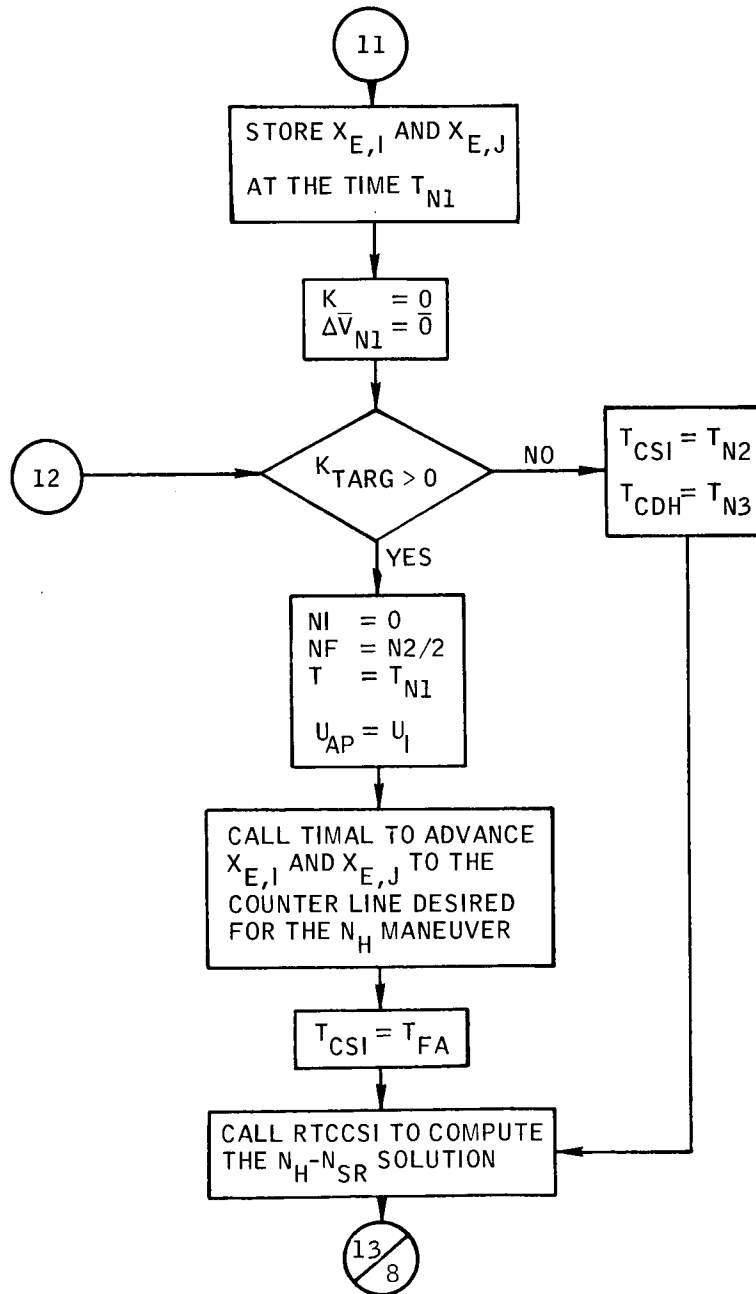


Figure B-20. - Continued.

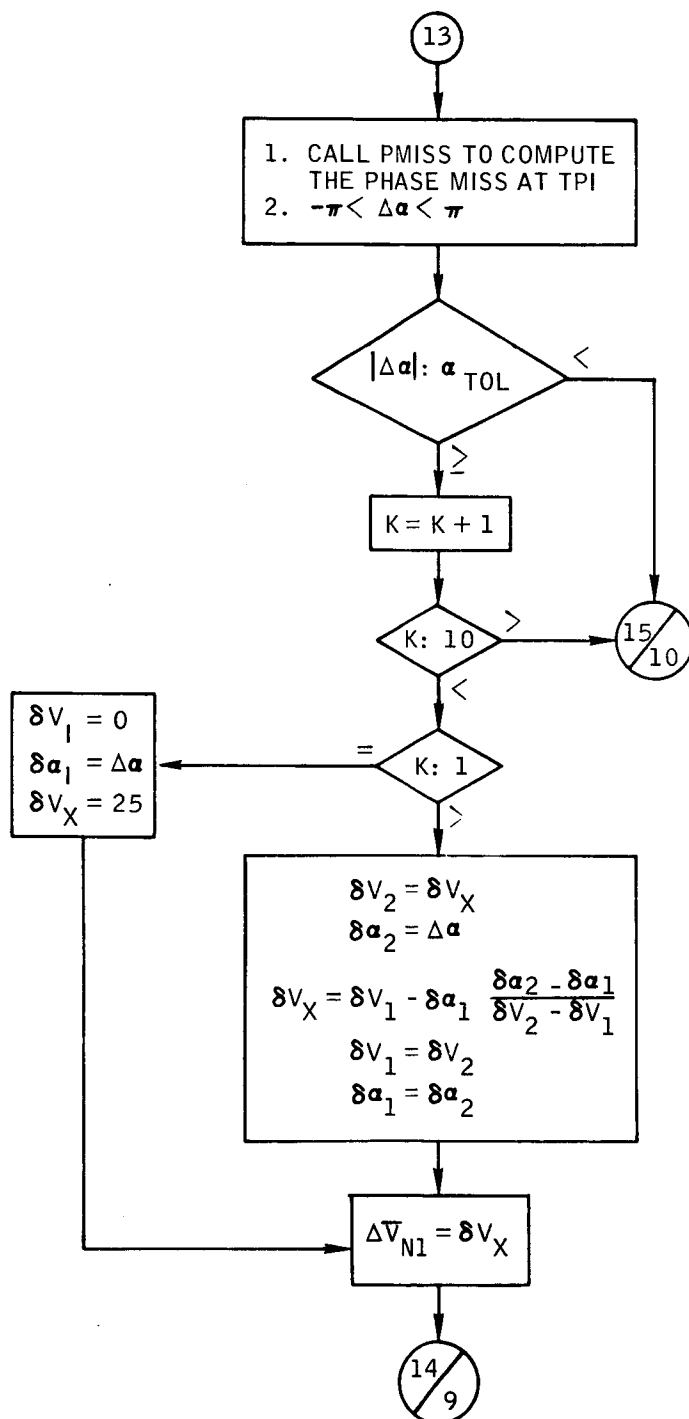
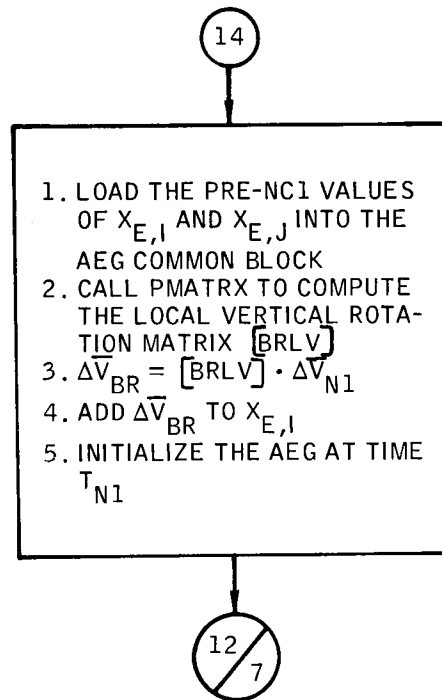


Figure B-20.- Continued.





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Figure B-20.- Continued.

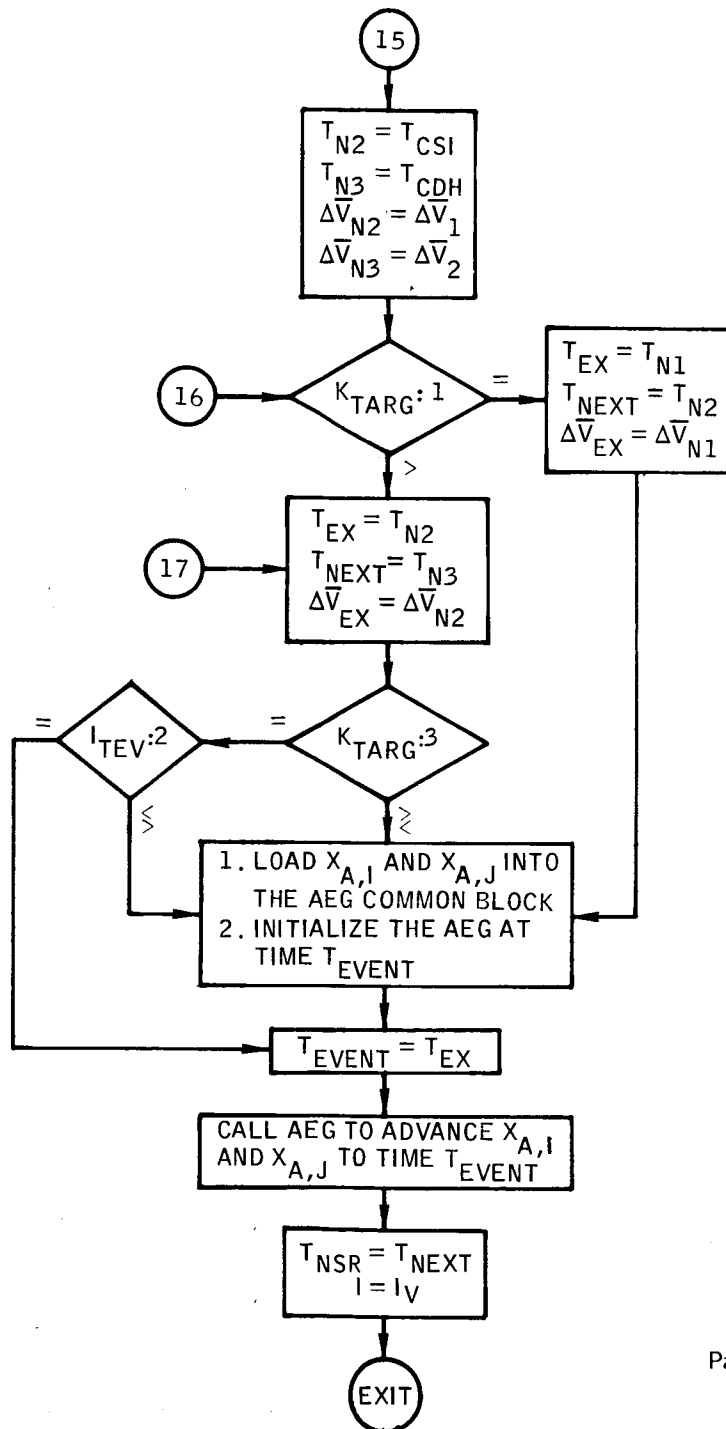


Figure B-20.- Concluded.

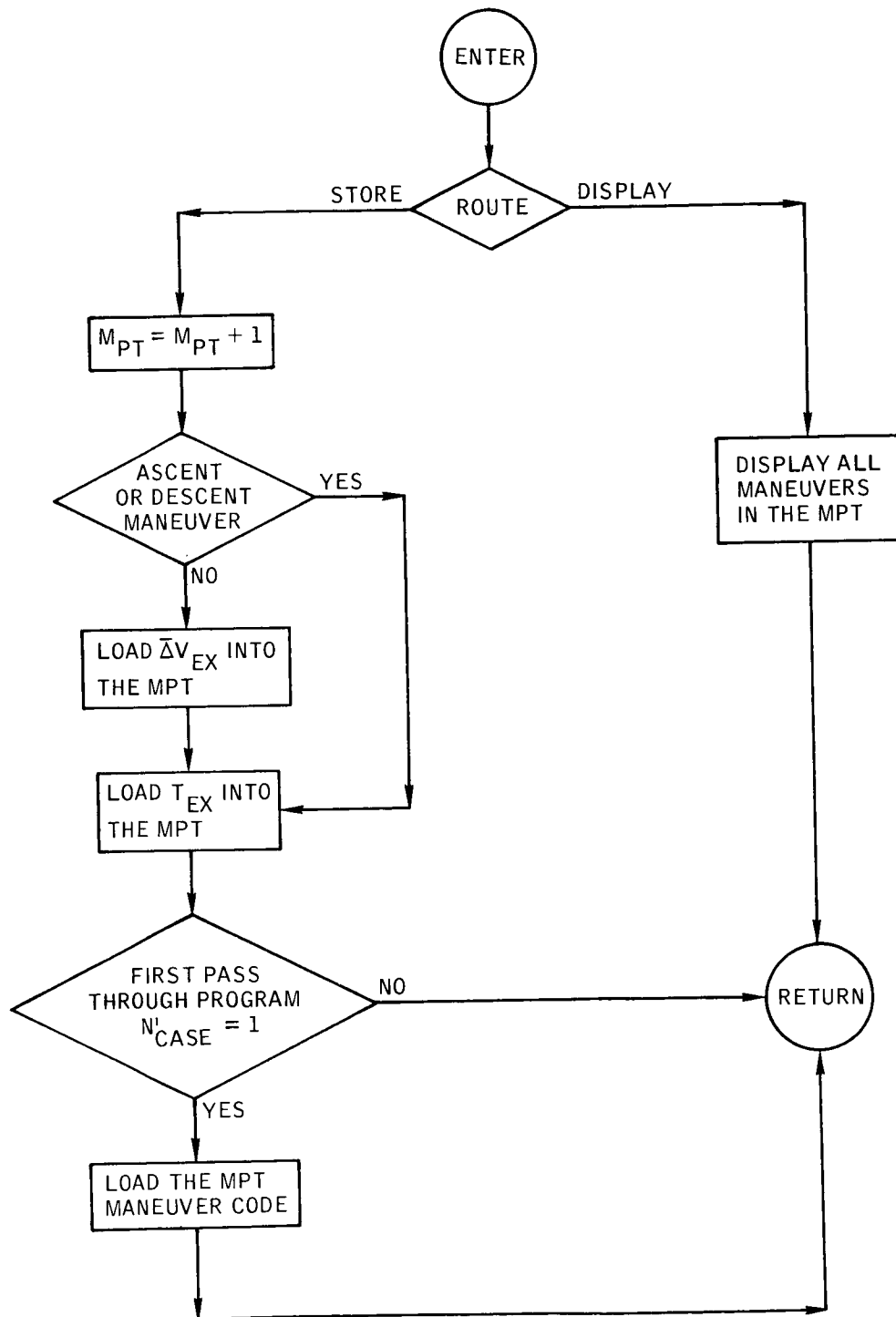


Figure B-21. - Flow chart of subroutine COMMPT.

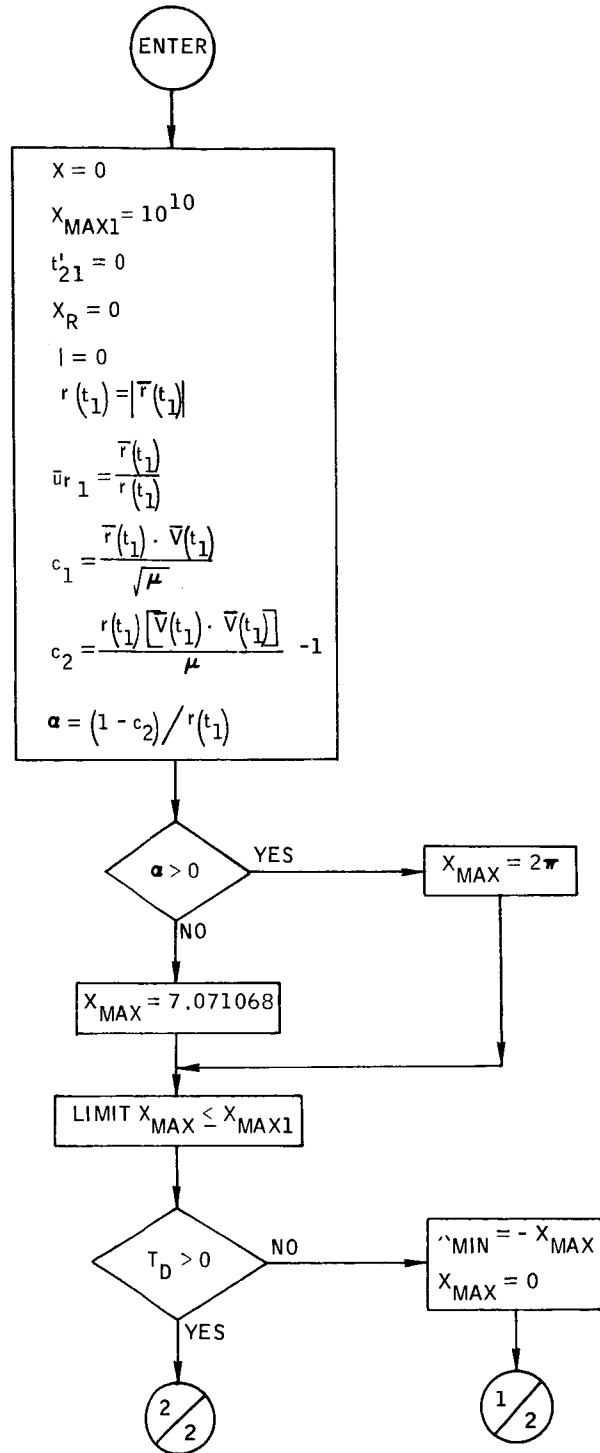
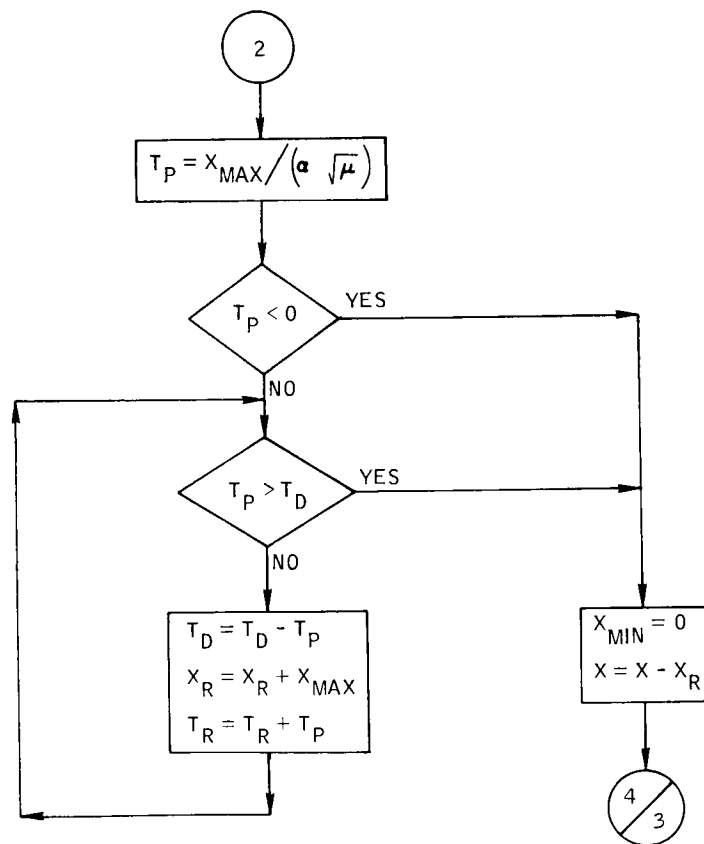
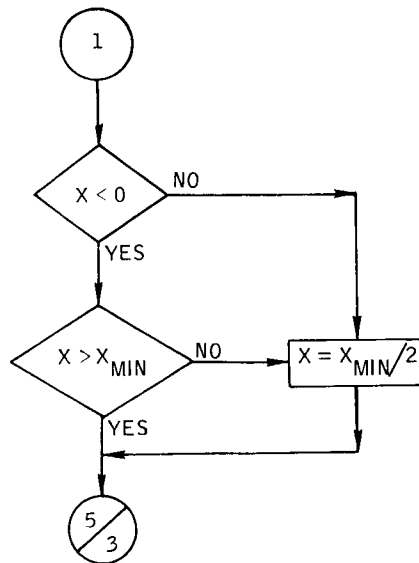


Figure B-22.- Flow chart of subroutine CONIC.



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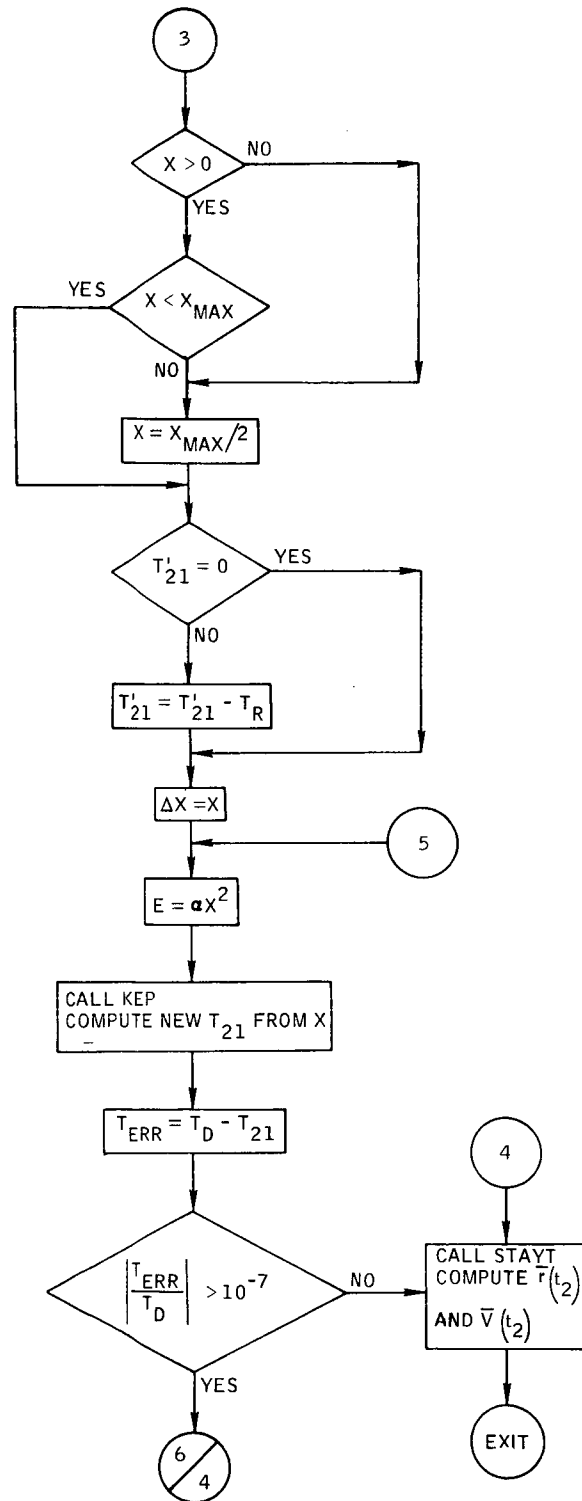


Figure B-22.- Continued.

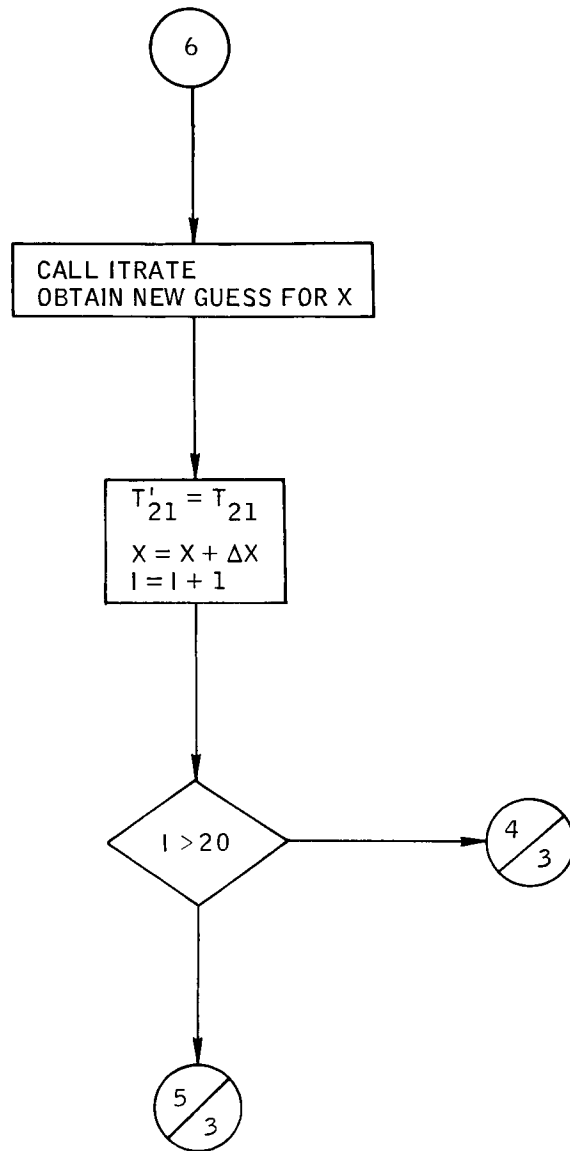


Figure B-22.- Concluded.

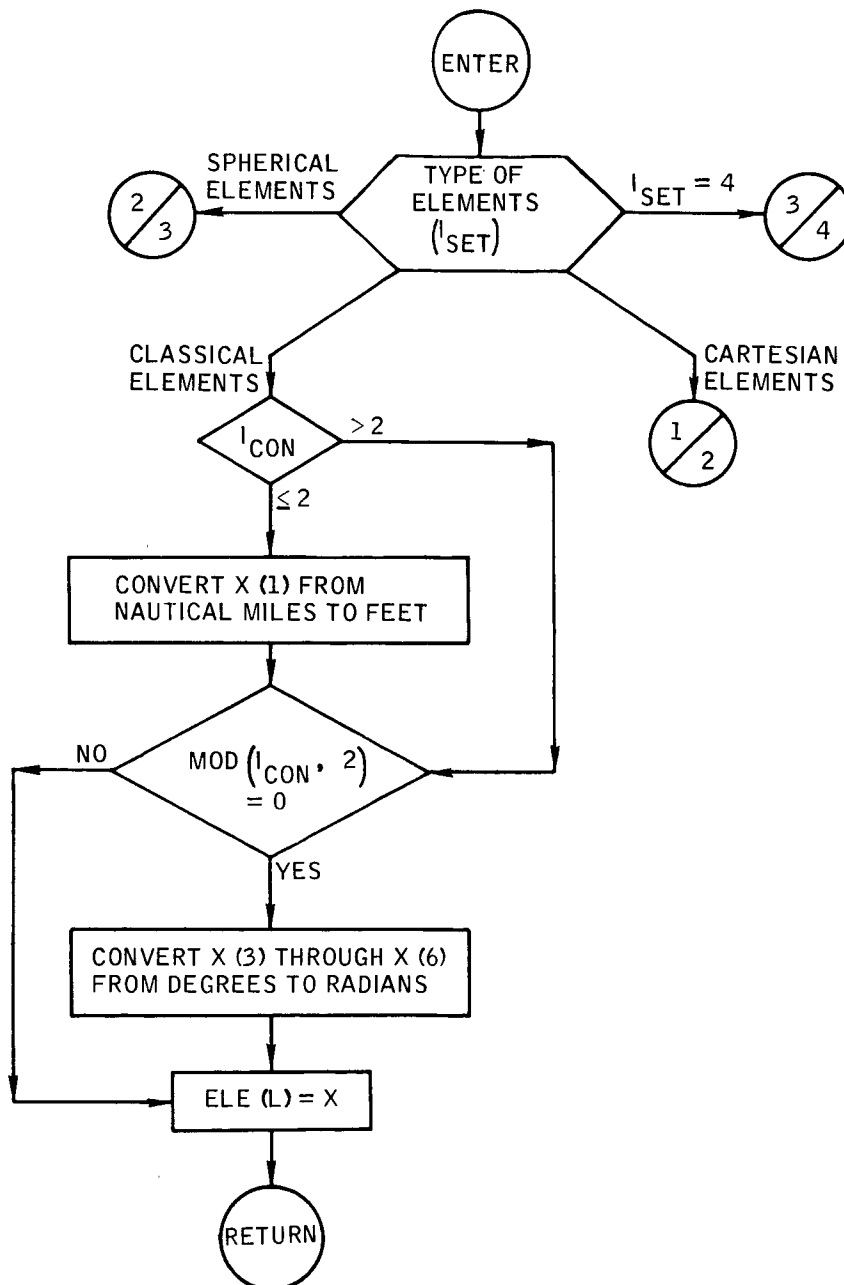


Figure B-23.- Flow chart of subroutine CONVRT.



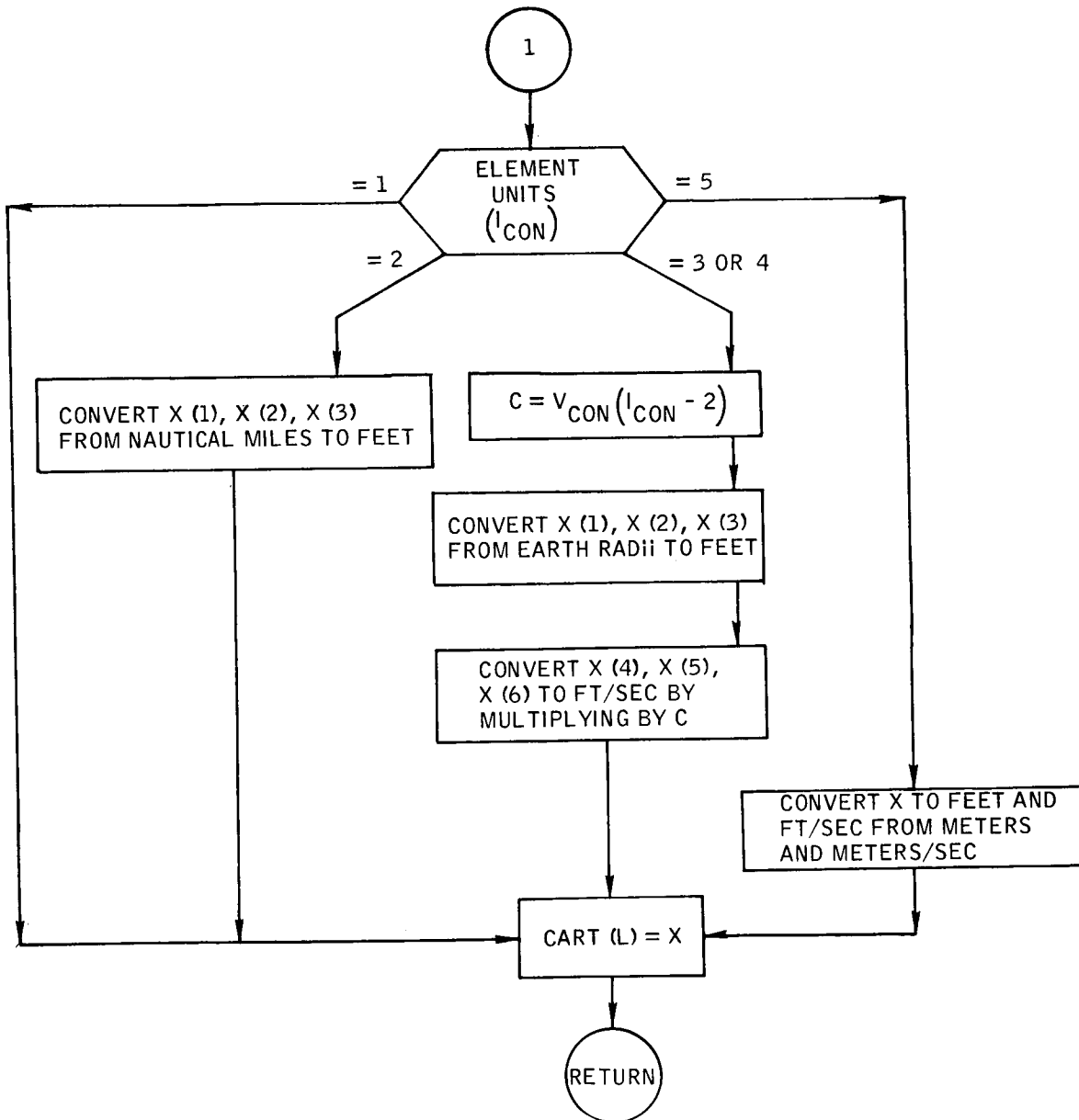


Figure B-23. - Continued.

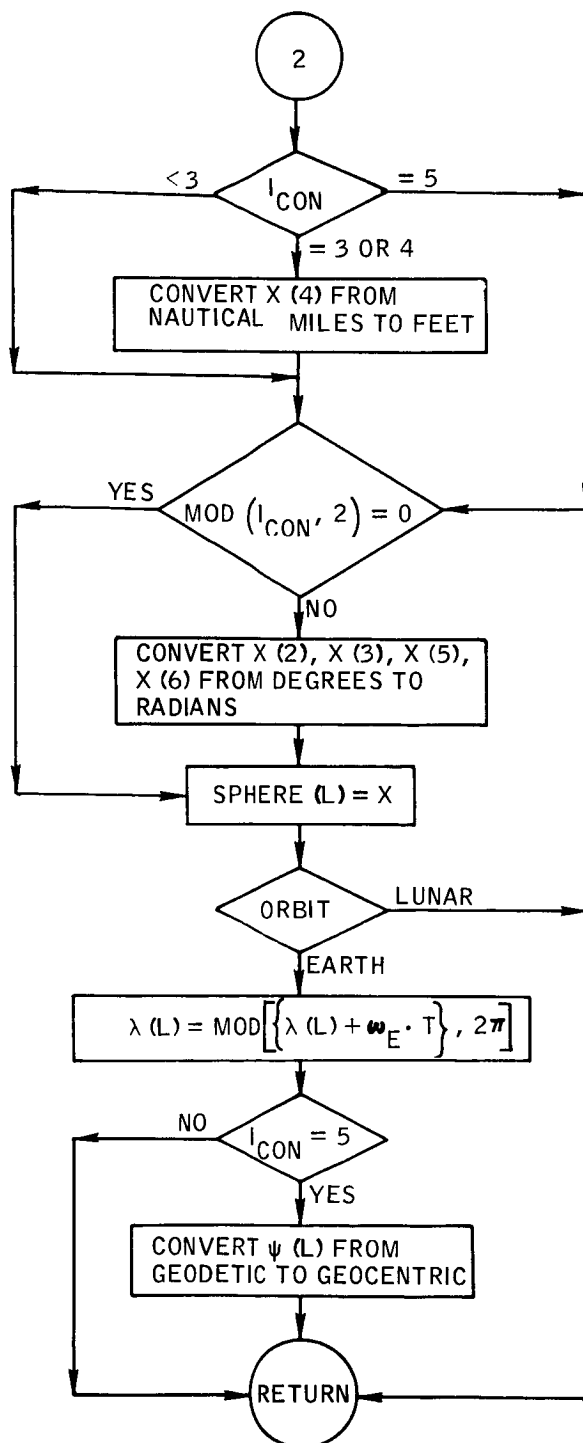


Figure B-23. - Continued.

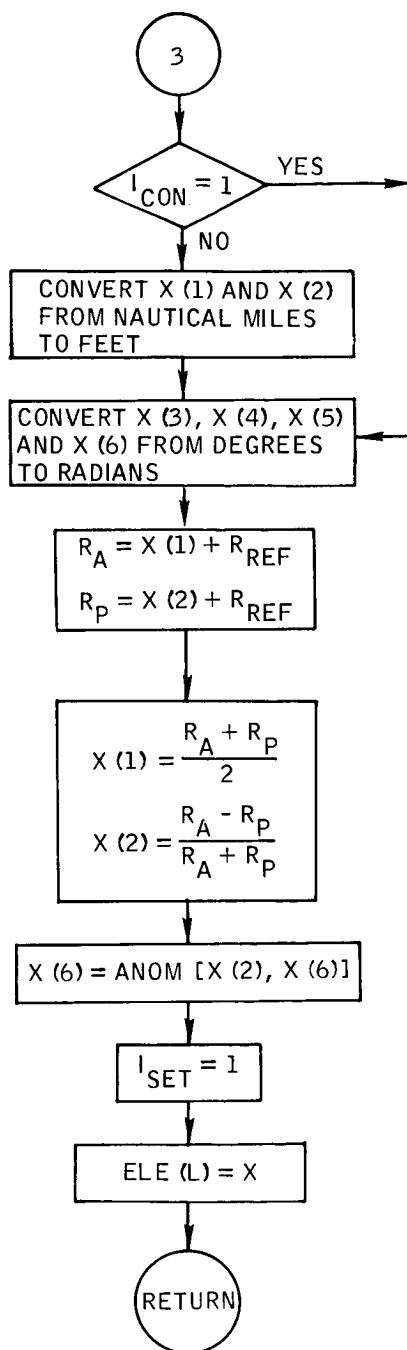


Figure B-23. - Concluded.

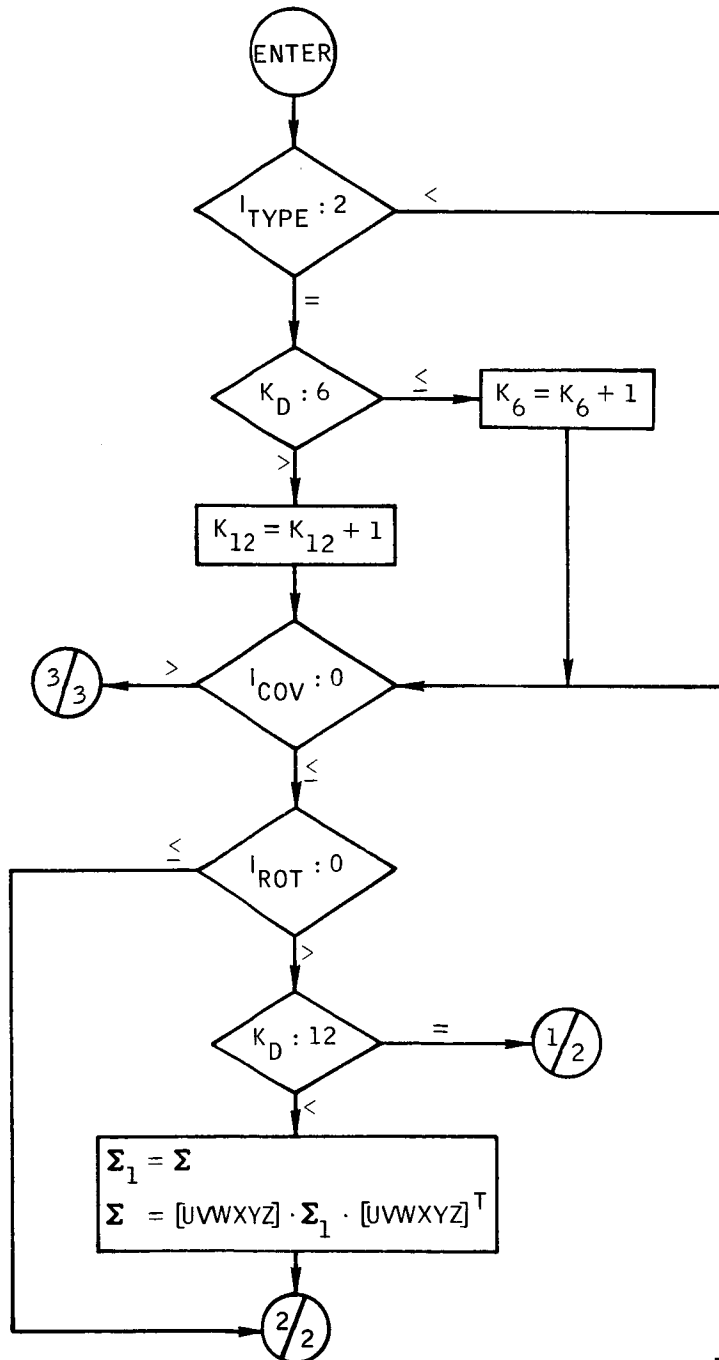


Figure B-24.- Flow chart of subroutine COVTAB.

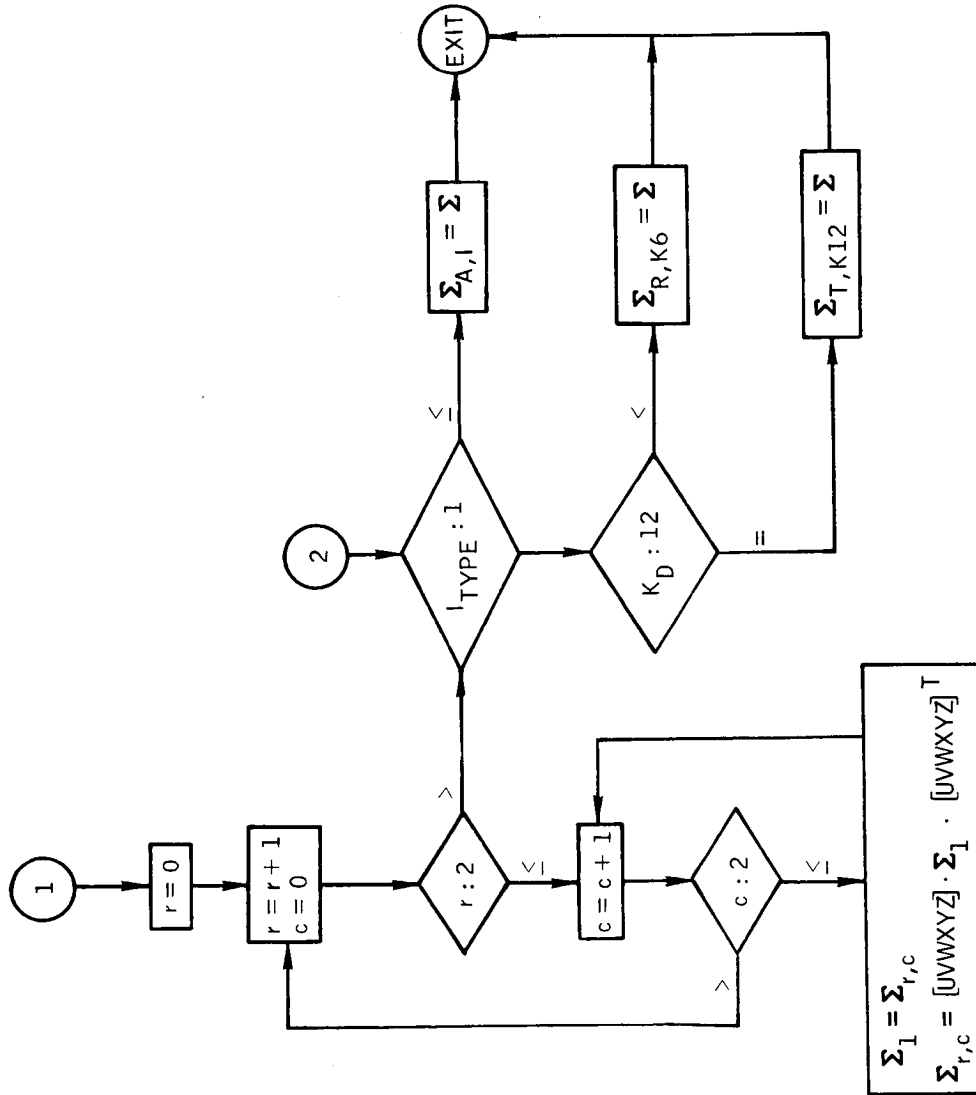


Figure B-24. - Continued.

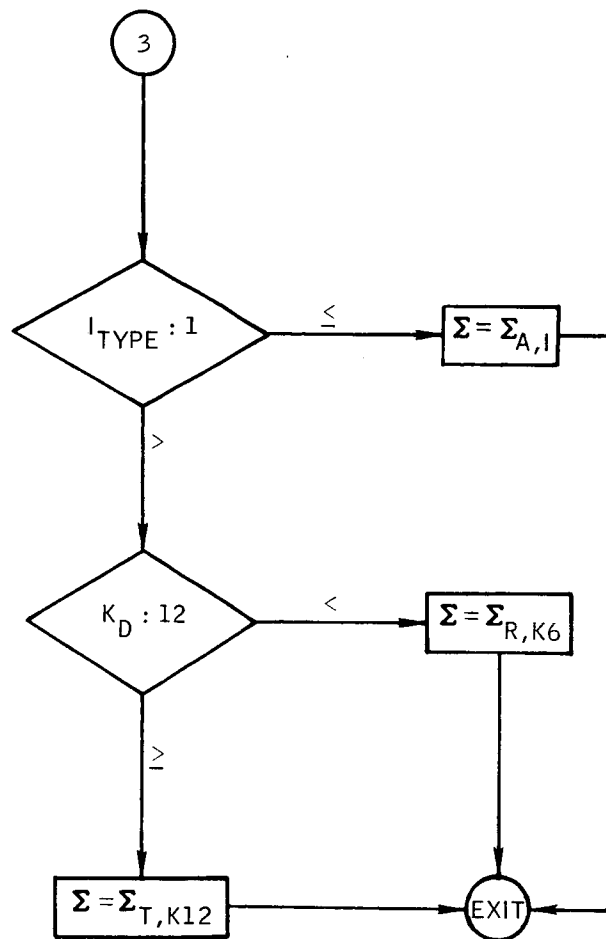


Figure B-24.- Concluded.

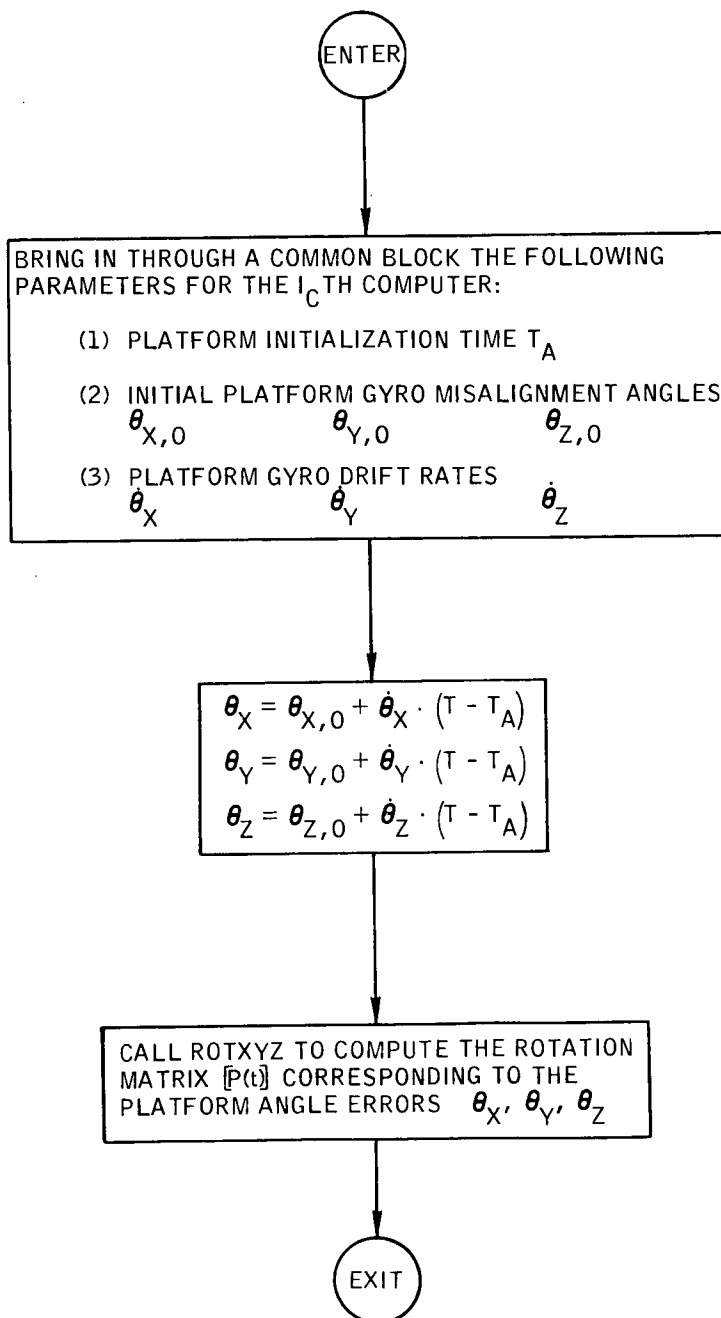


Figure B-25.- Flow chart of subroutine CPEM.

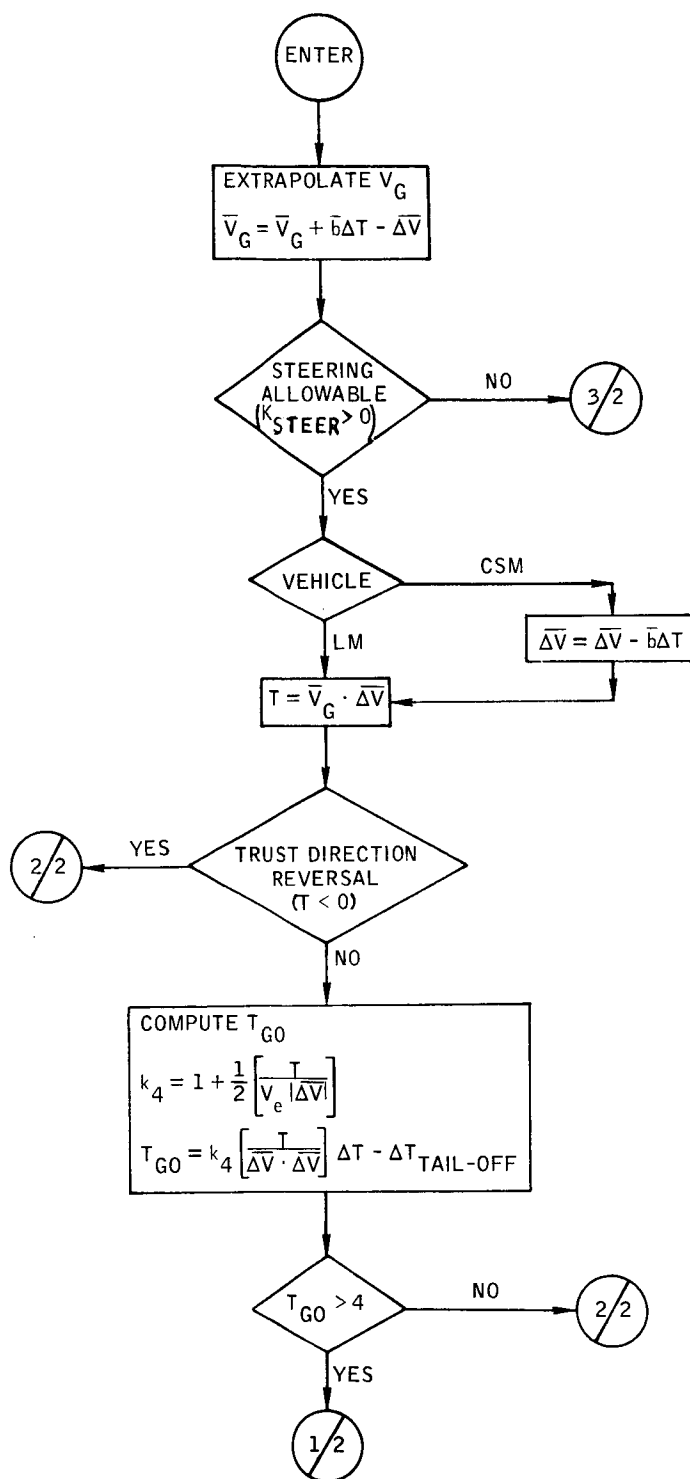


Figure B-26.- Flow chart of subroutine CR0SP.



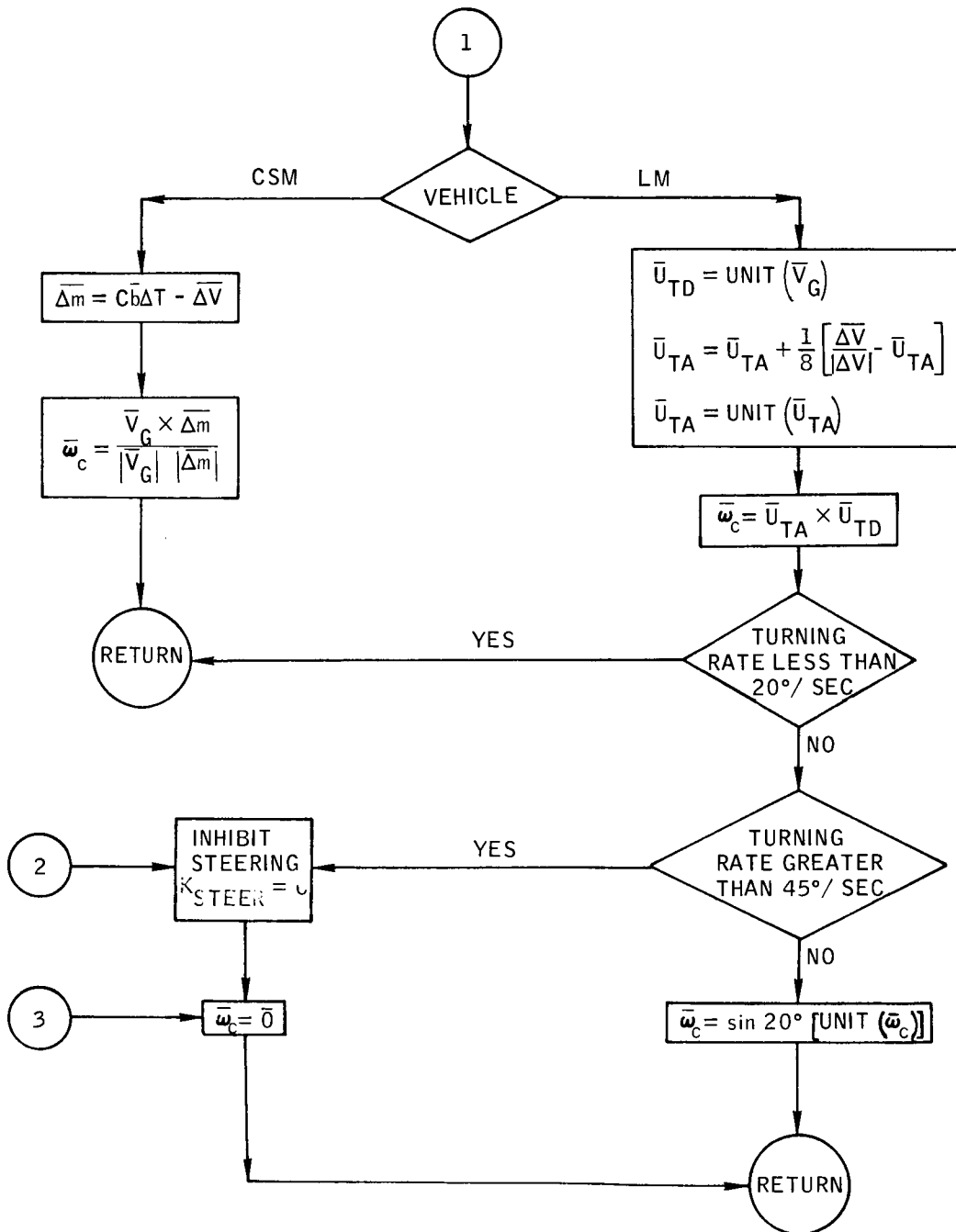


Figure B-26.- Concluded.

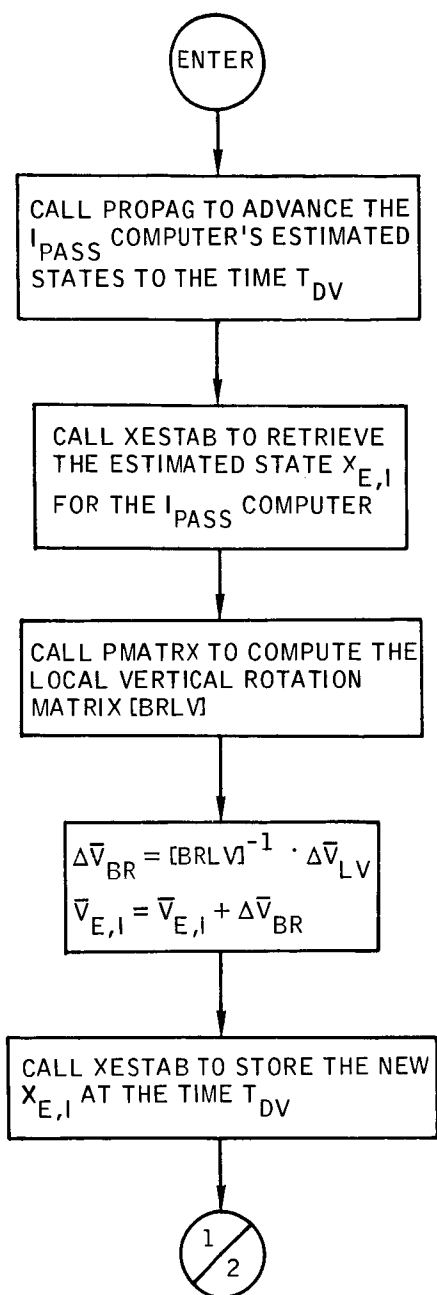


Figure B-27.- Flow chart of subroutine DELTAV.

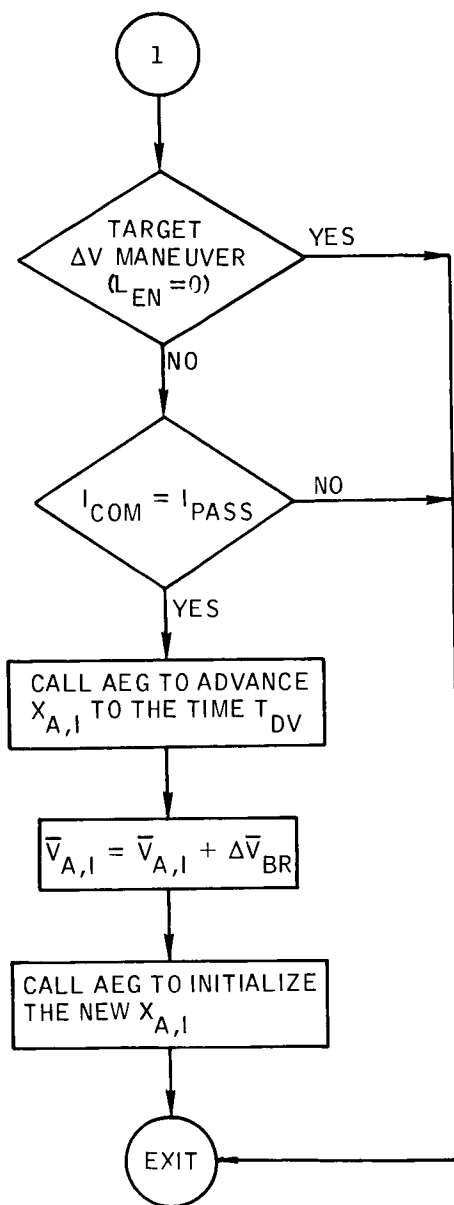


Figure B-27. - Concluded.

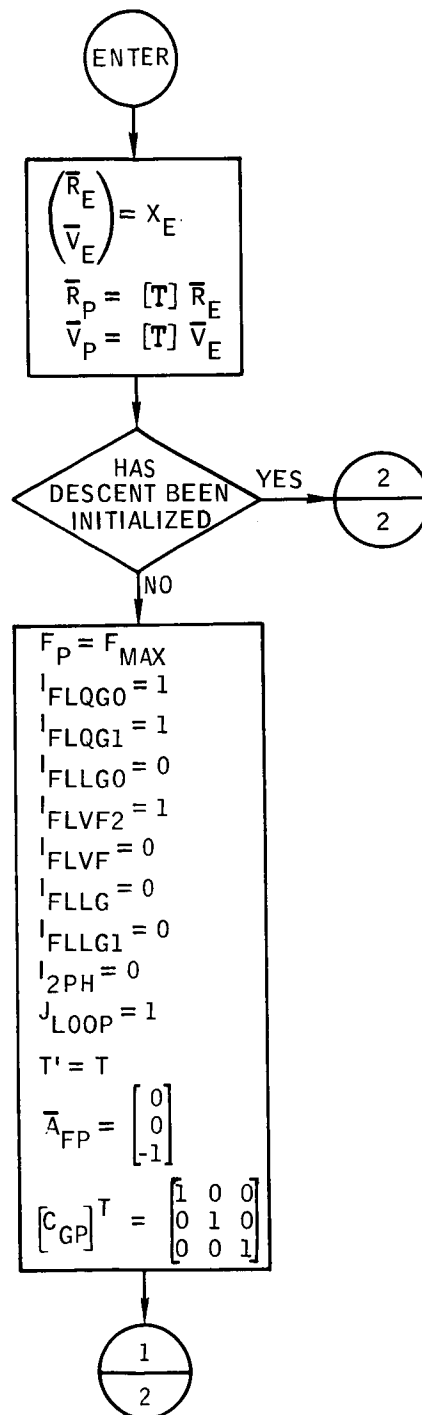


Figure B-28.- Flow chart of subroutine DESCENT.

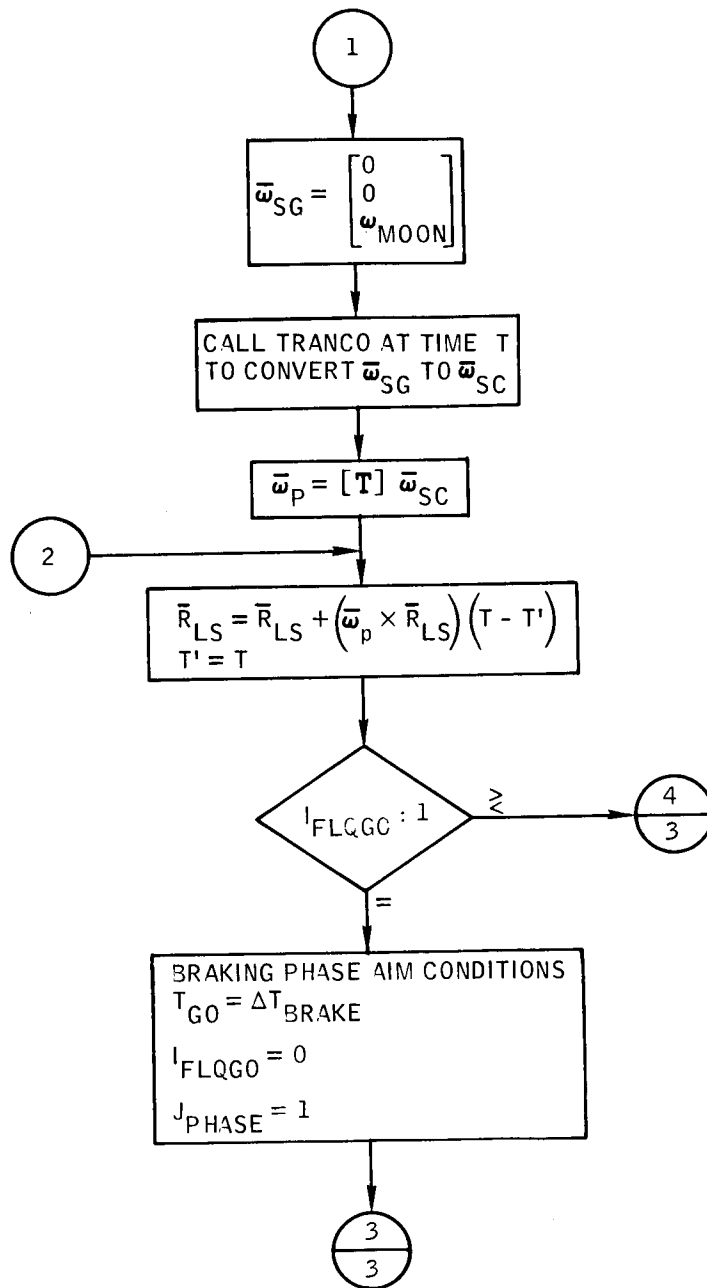
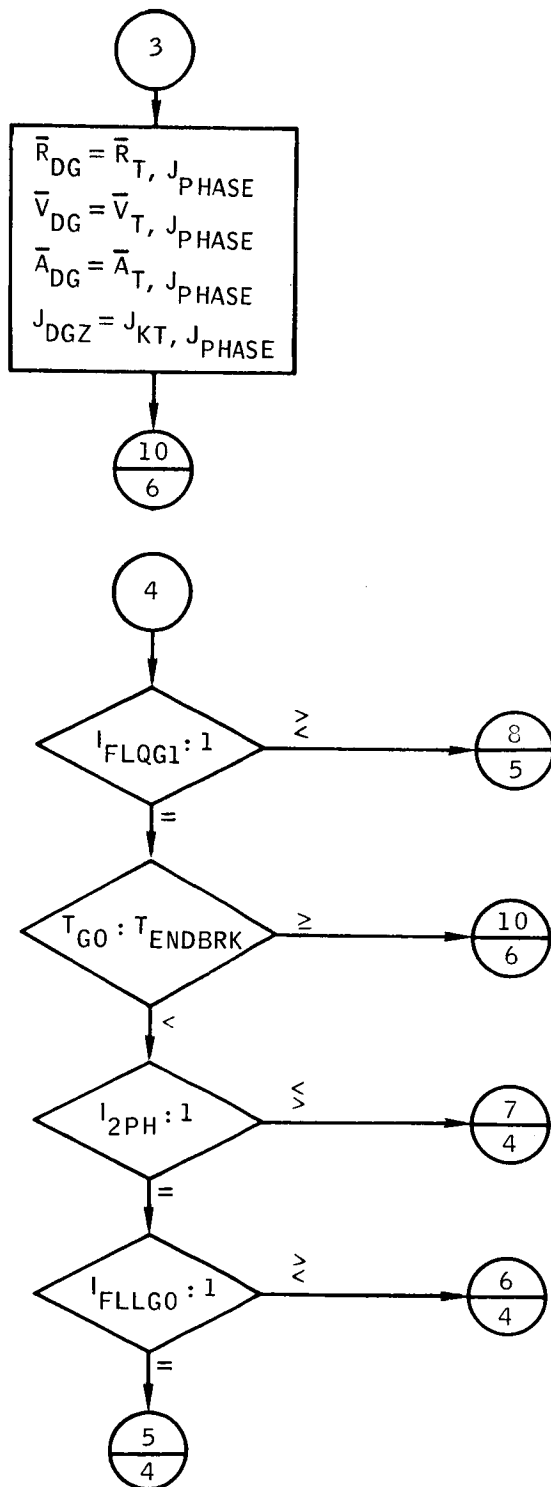


Figure B-28.- Continued.



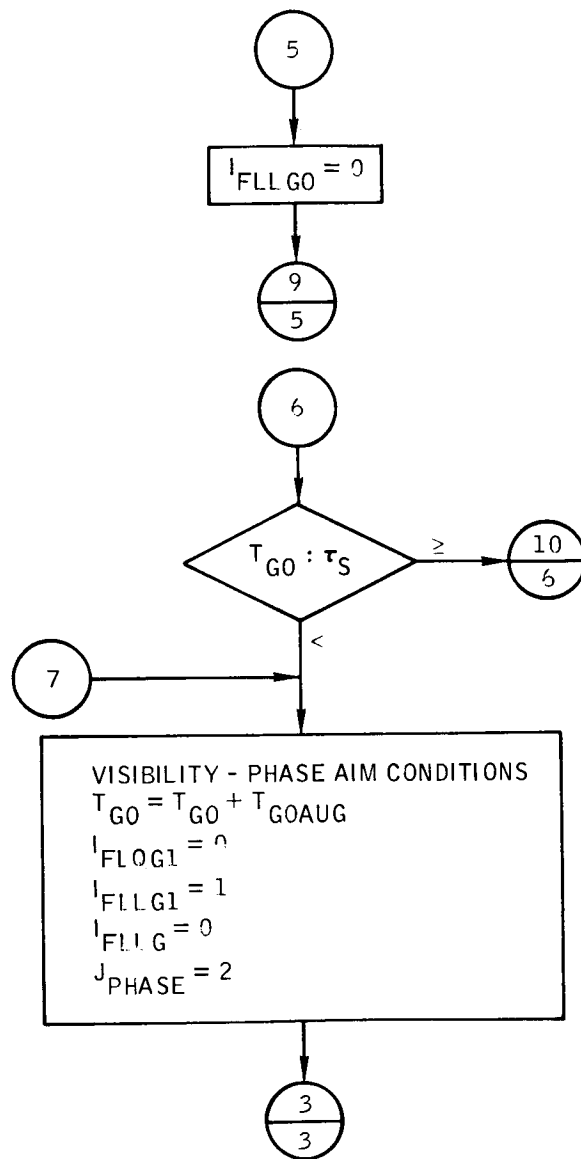


Figure B-28.- Continued.

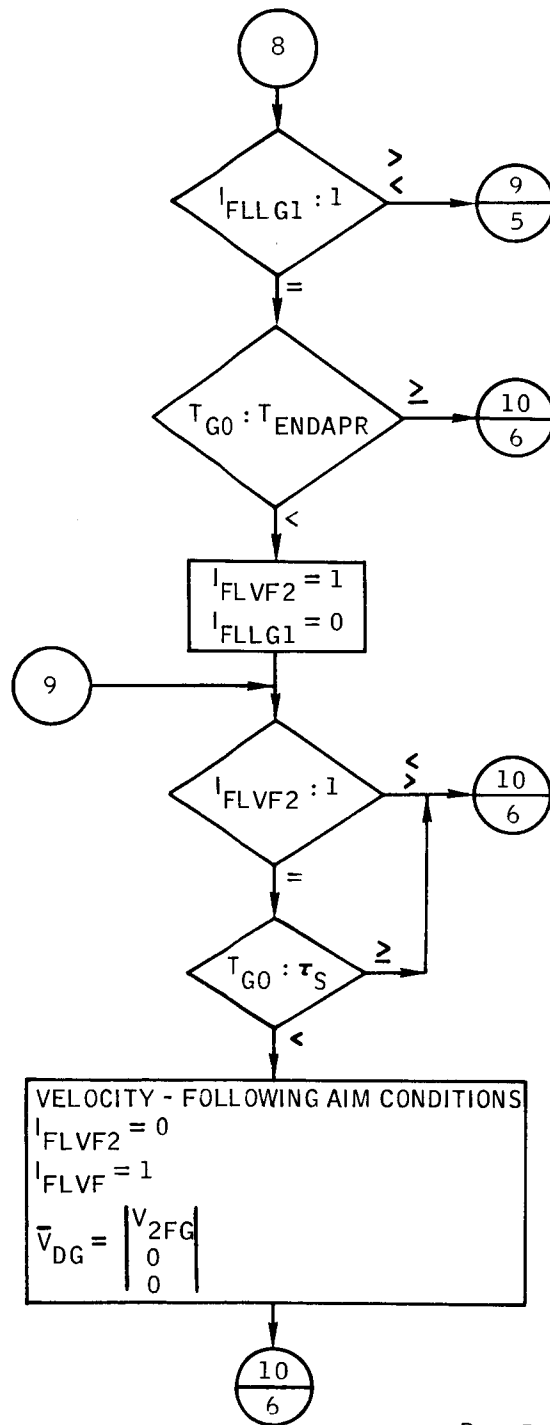


Figure B-28.- Continued.



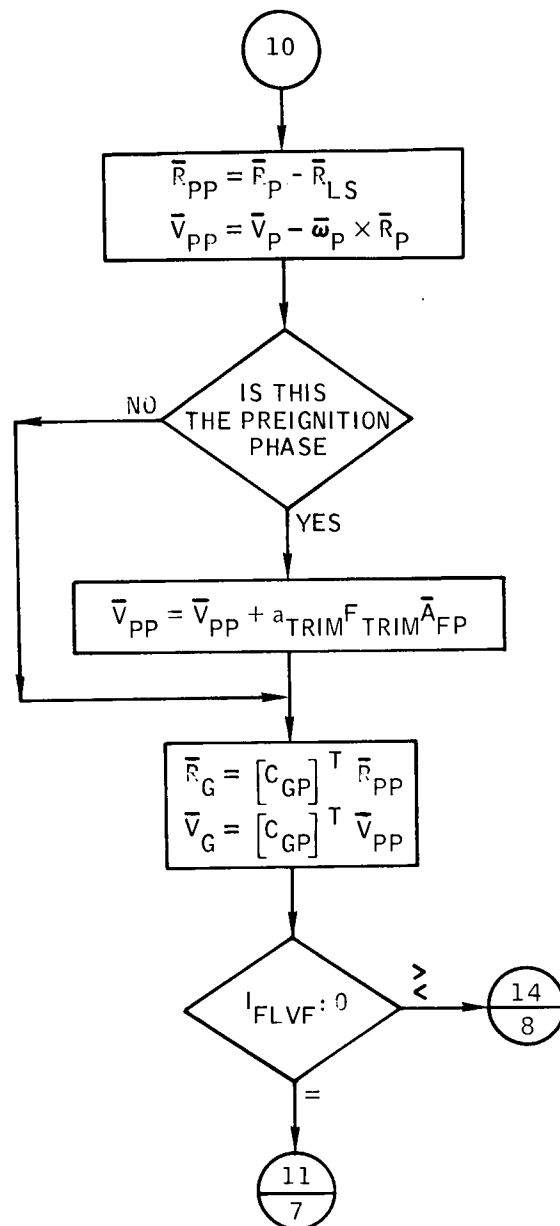
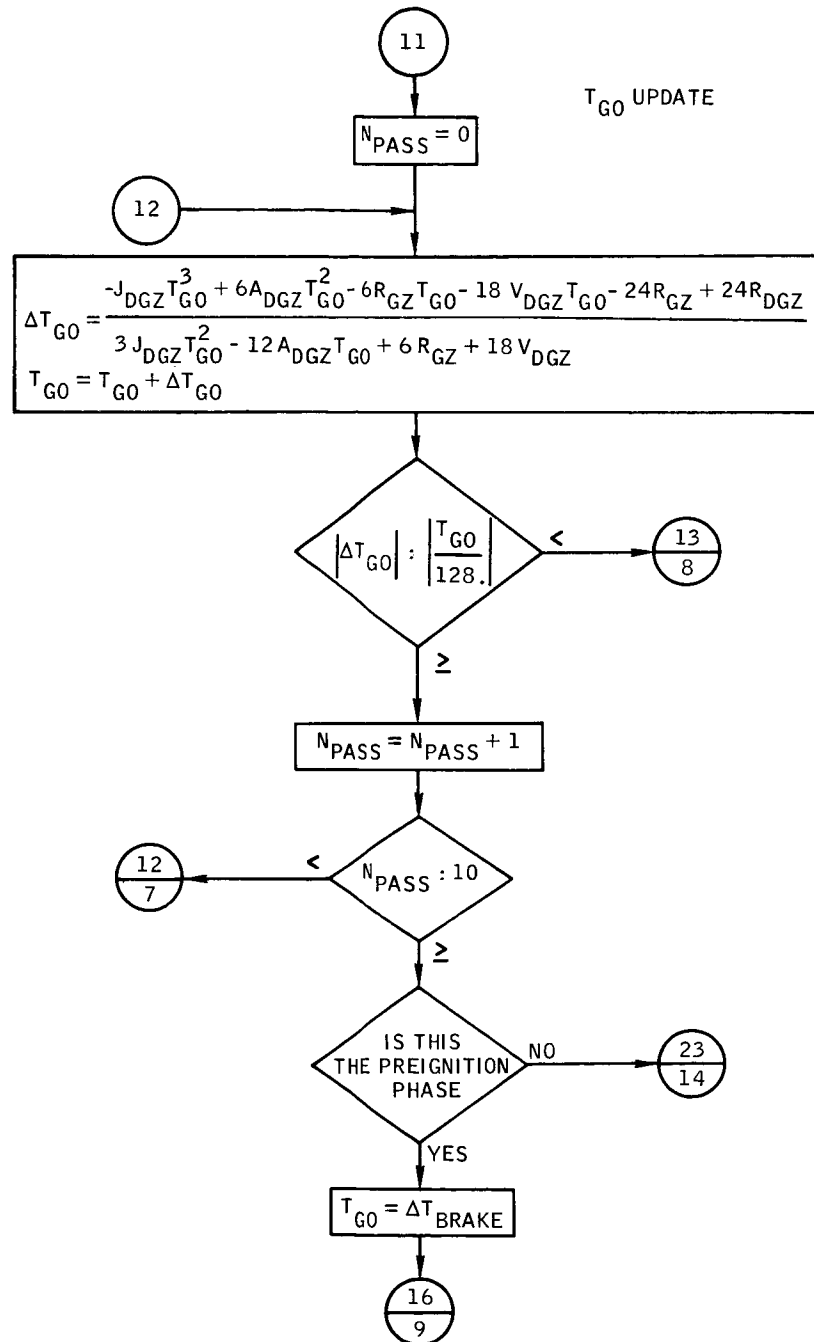
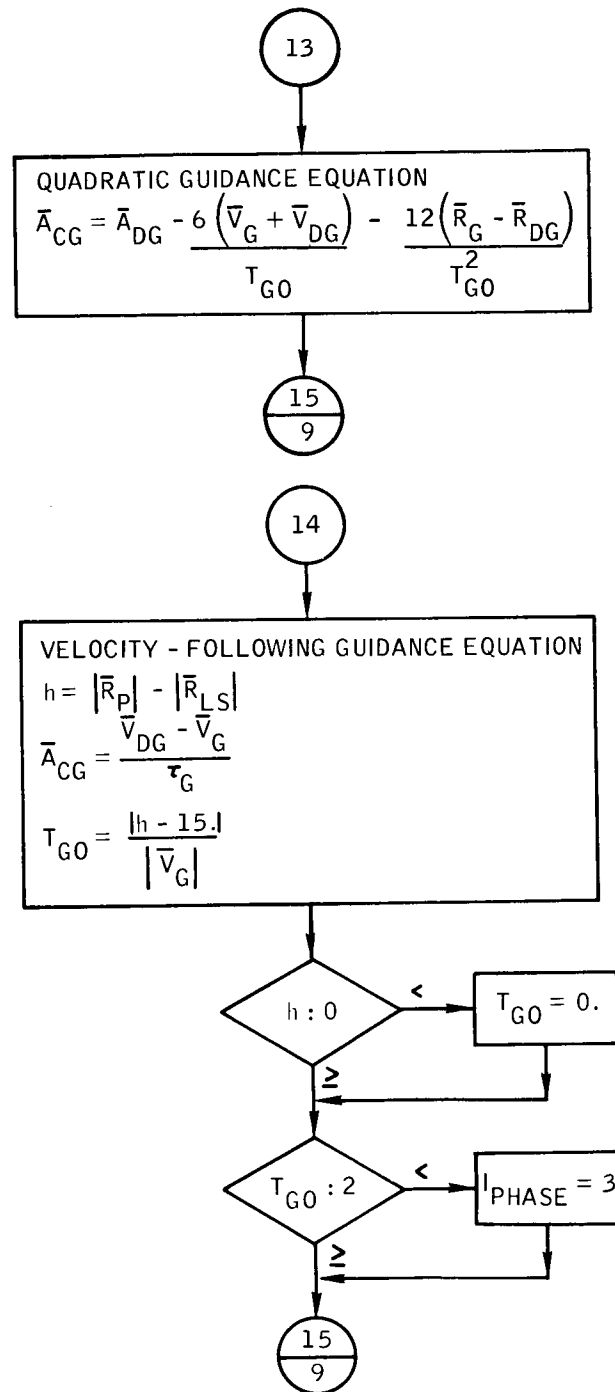


Figure B-28.- Continued.





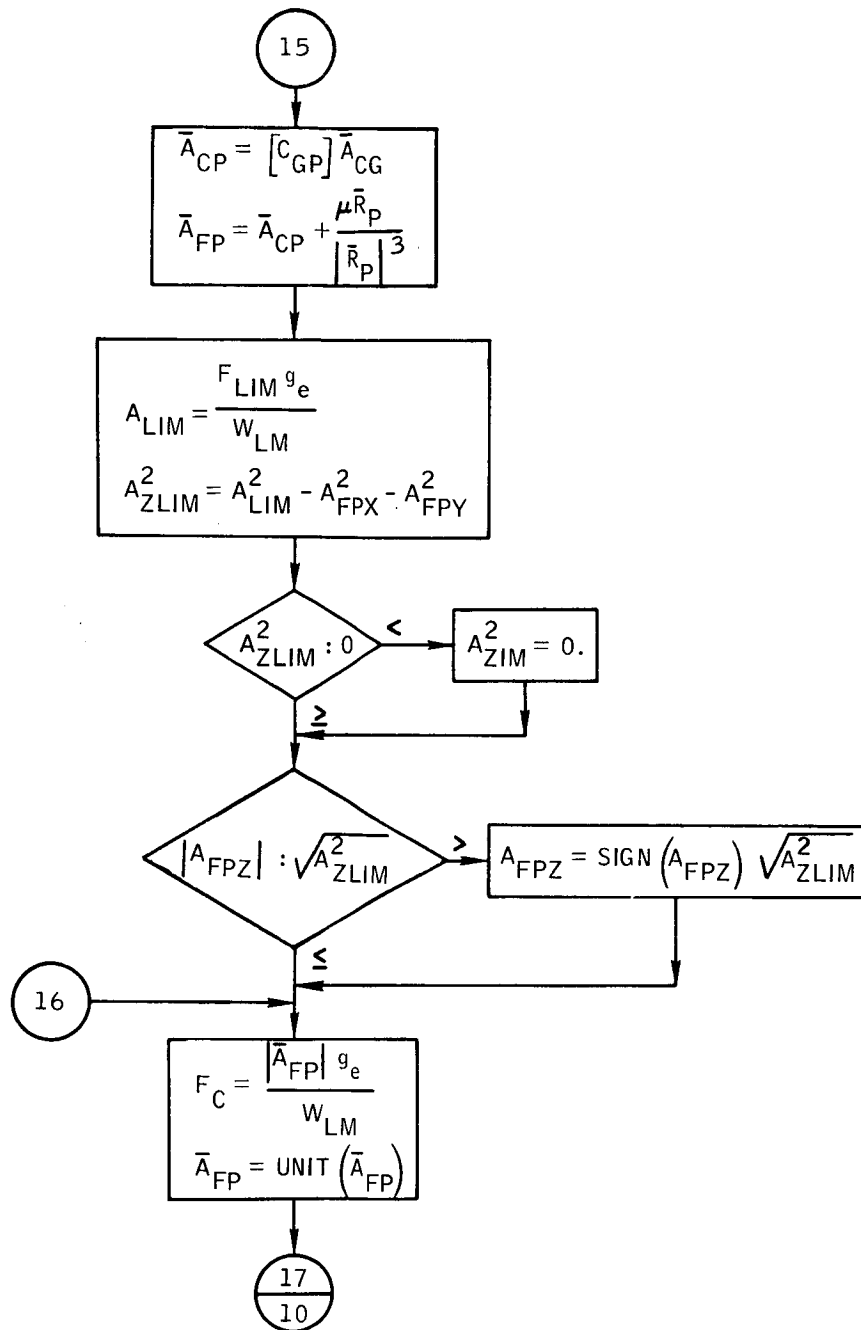


Figure B-28.- Continued.

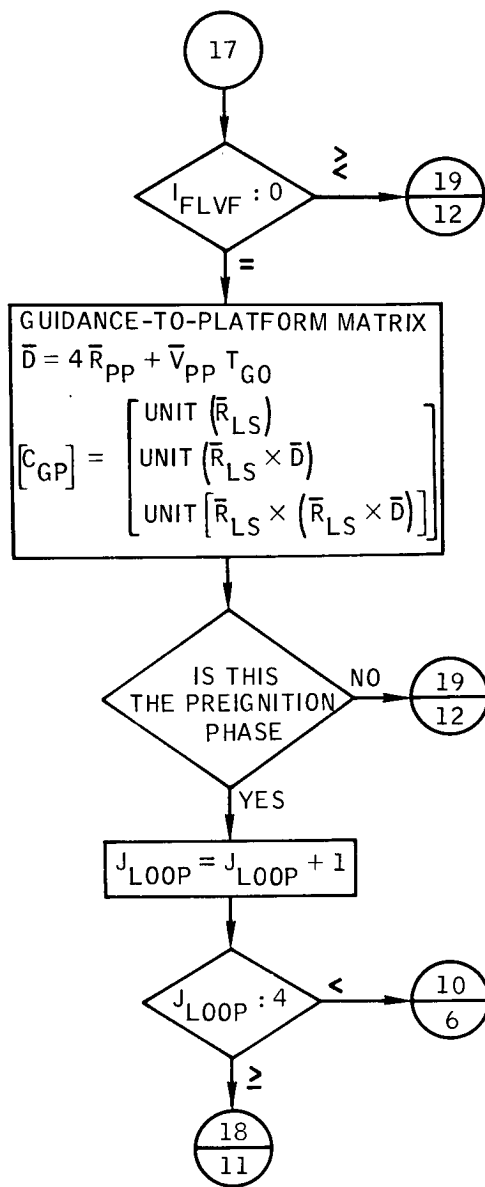
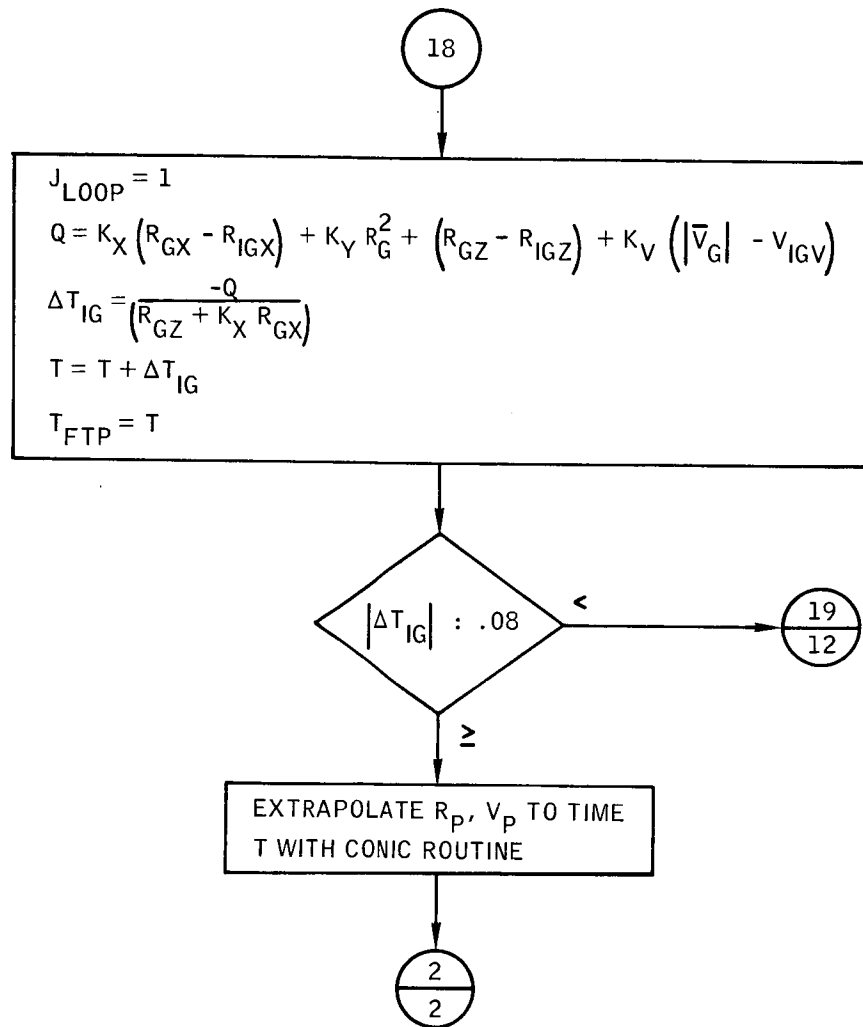
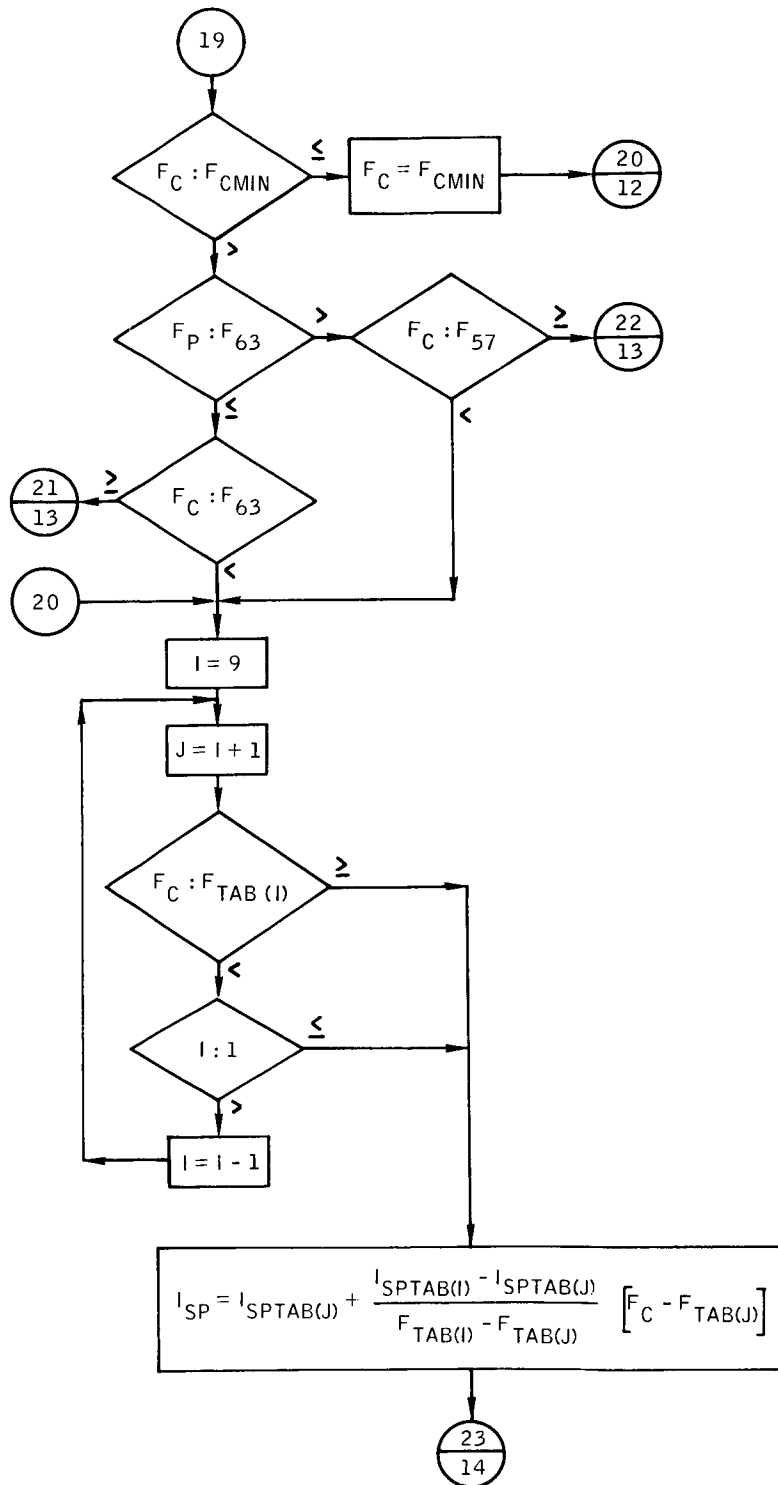
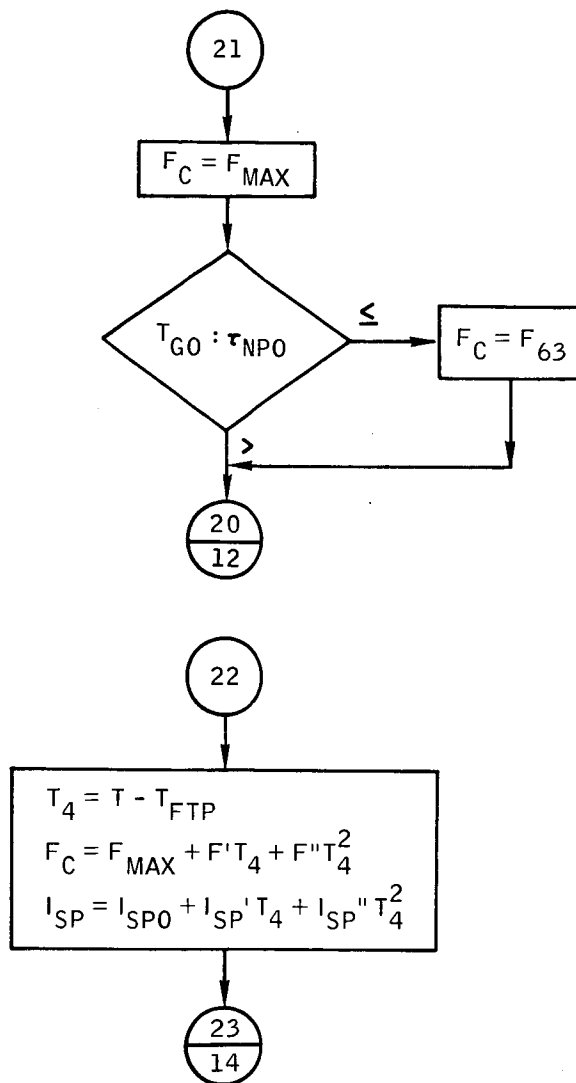


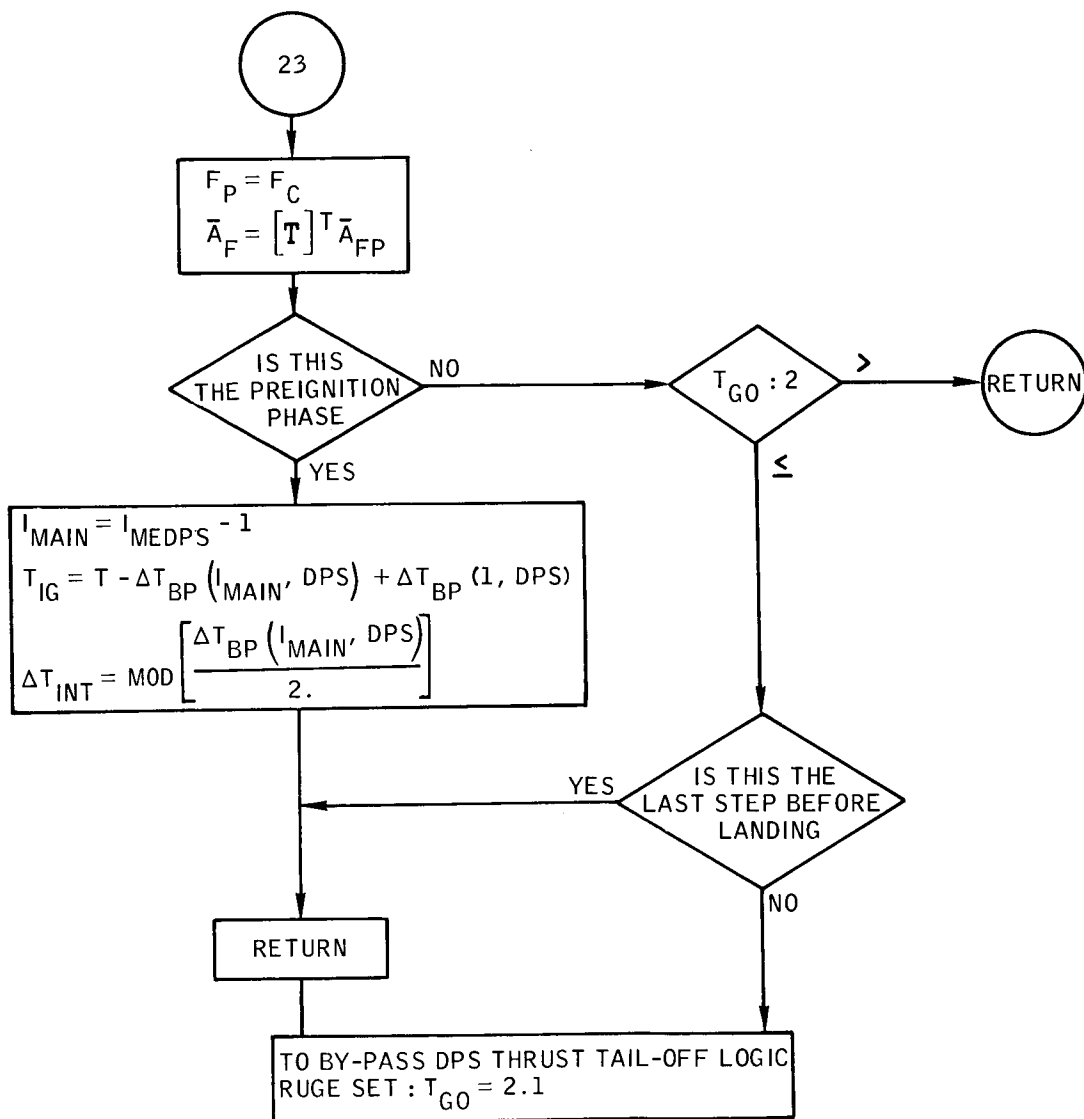
Figure B-28.- Continued.











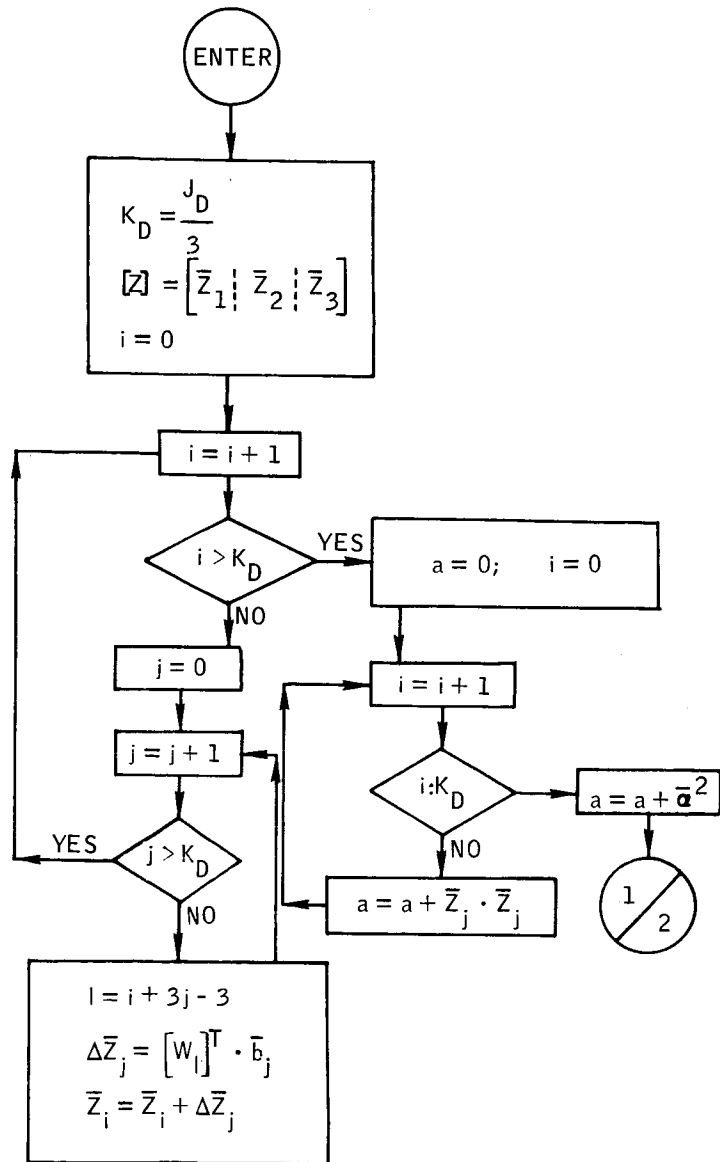
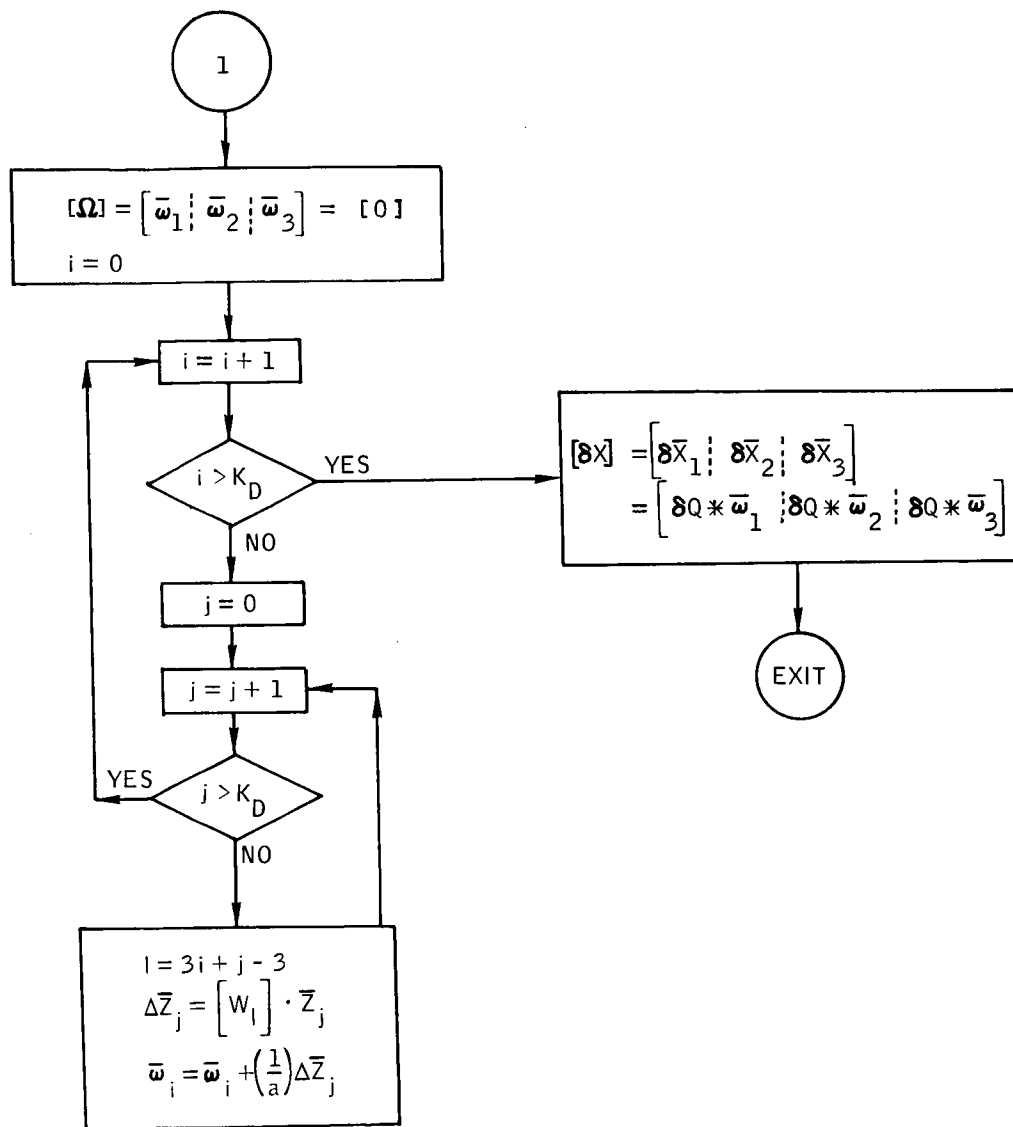


Figure B-29.- Flow chart of subroutine DINCP1.



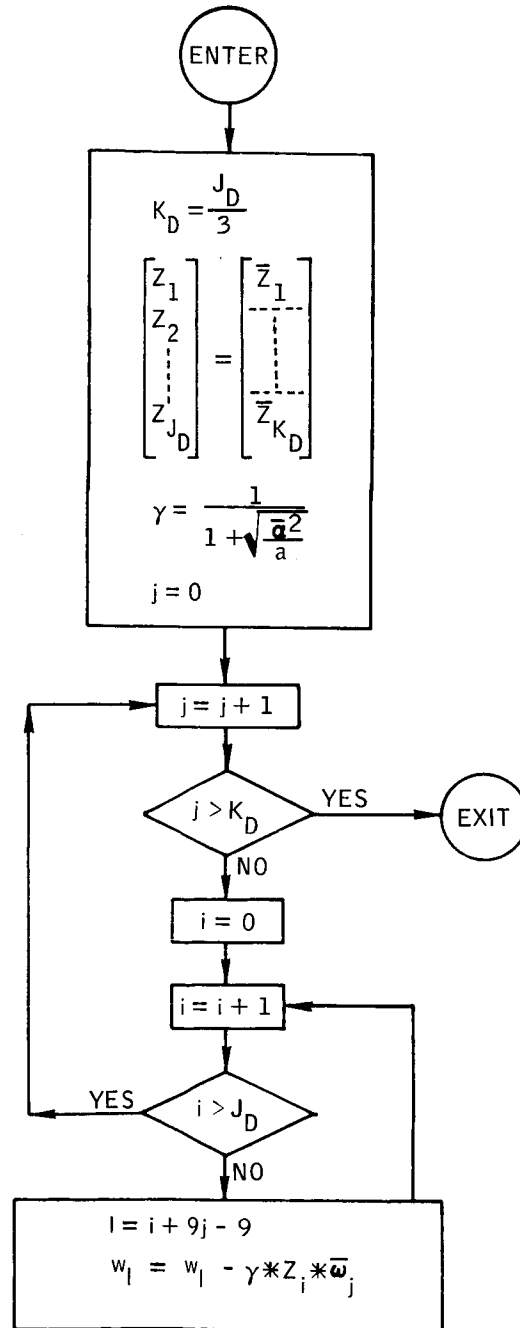


Figure B-30.- Flow chart of subroutine DINCP2.

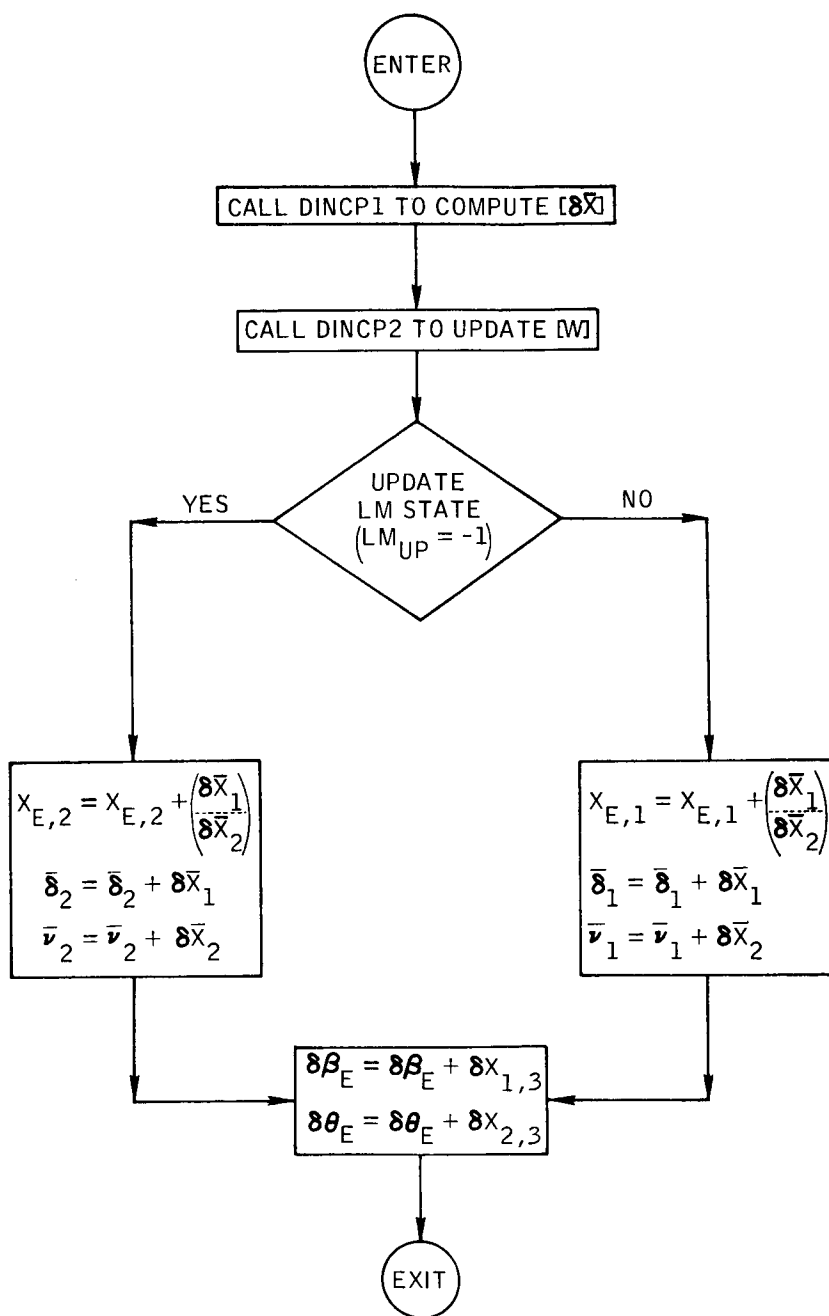


Figure B-31.- Flow chart of subroutine DMESIP.

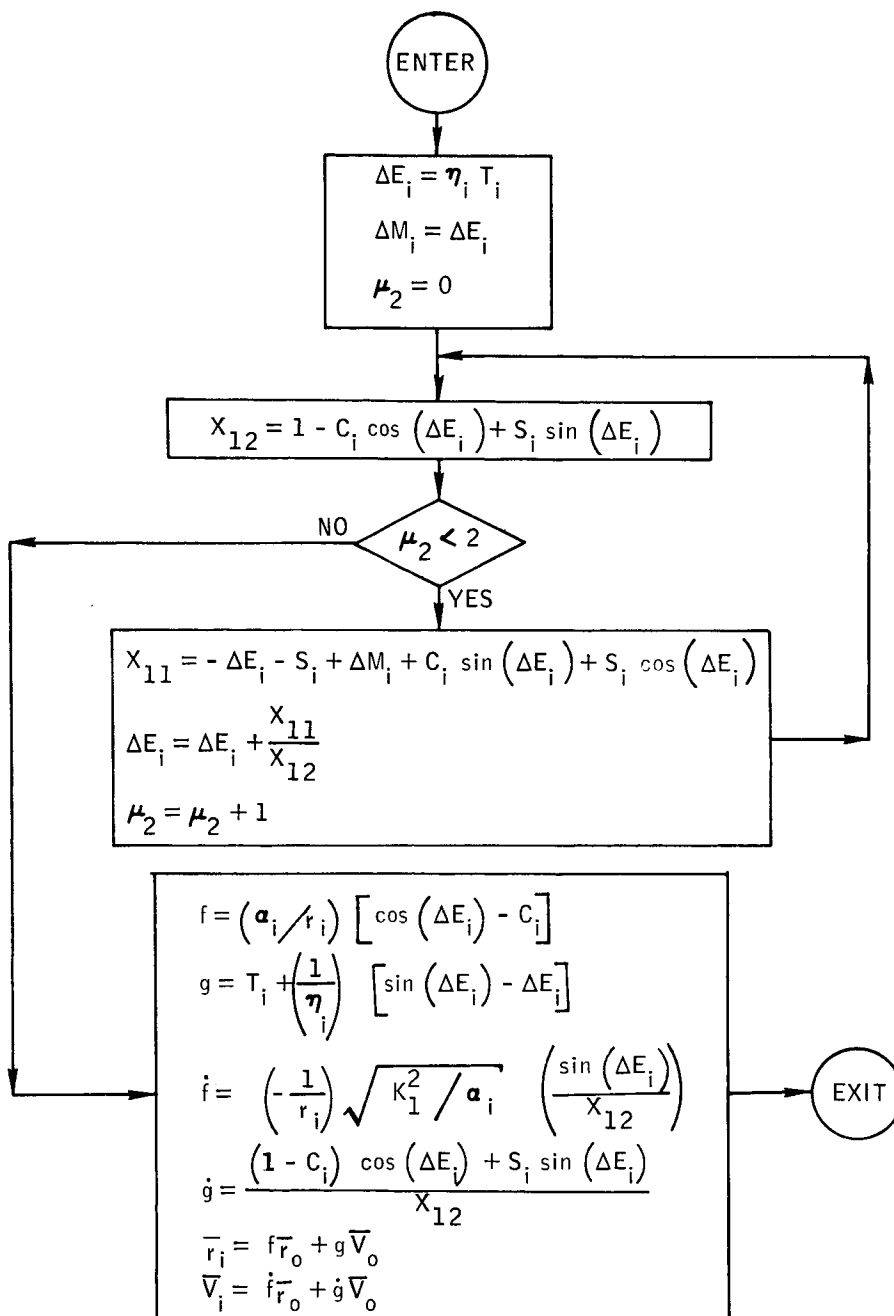


Figure B-32. - Flow chart of subroutine ELPRE.

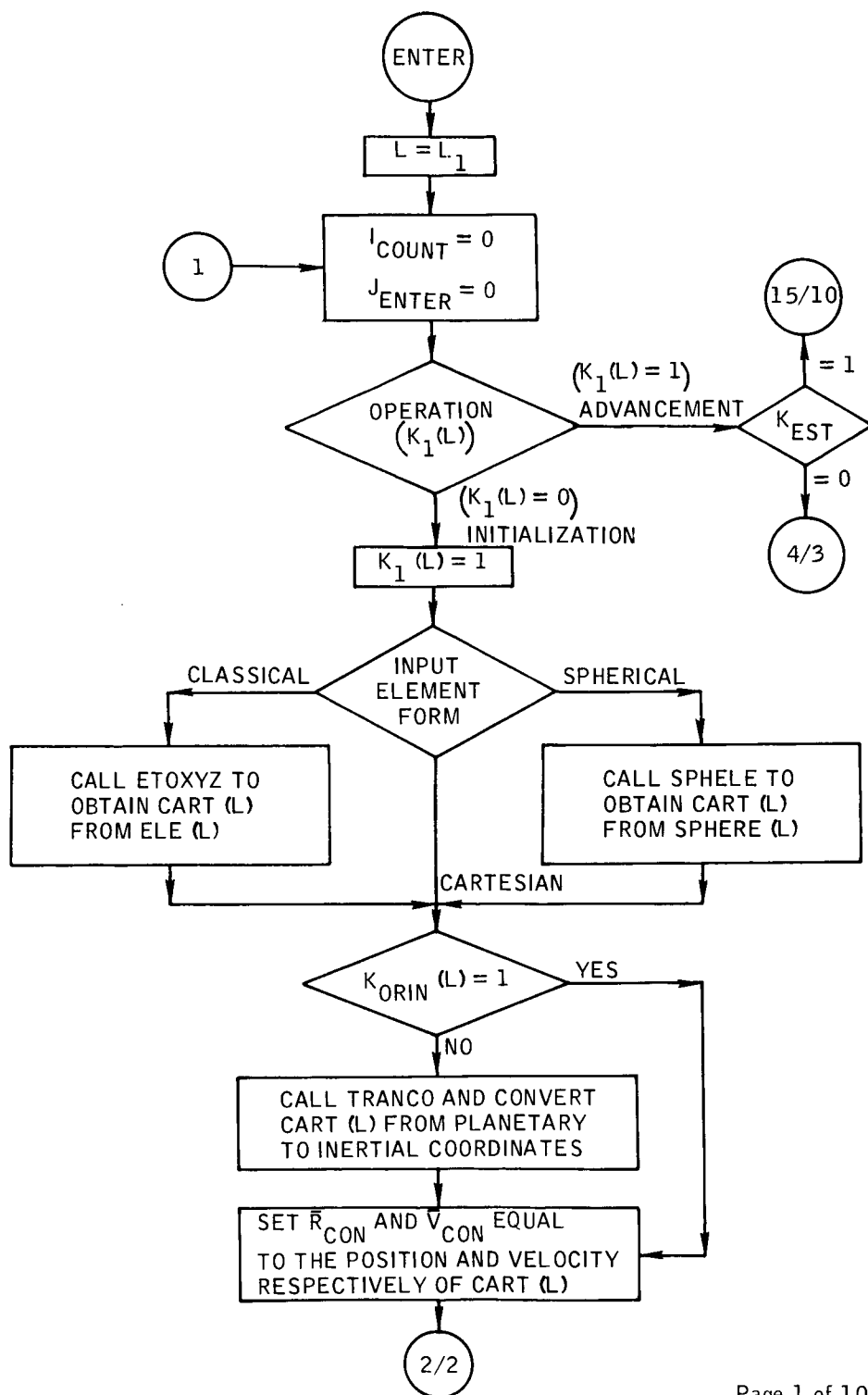
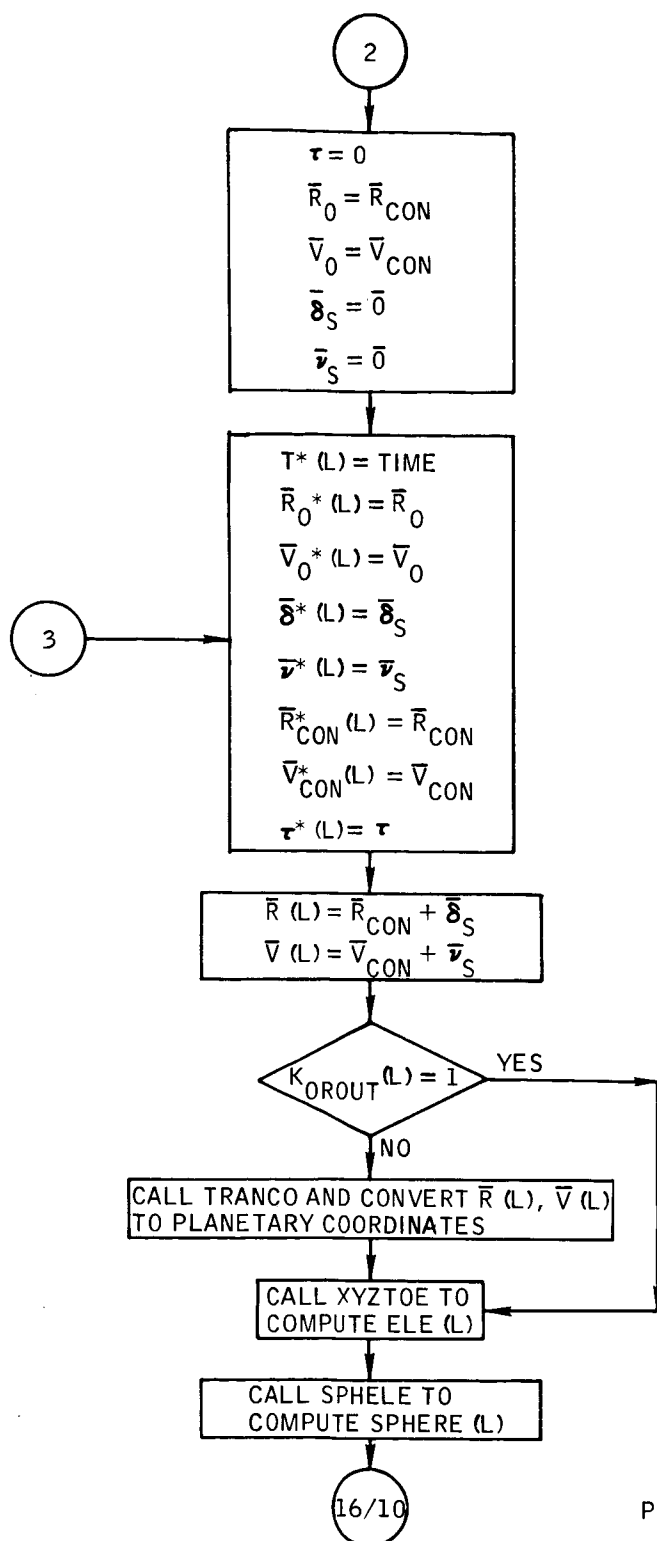


Figure B-33. - Flow chart of subroutine ENCKE.





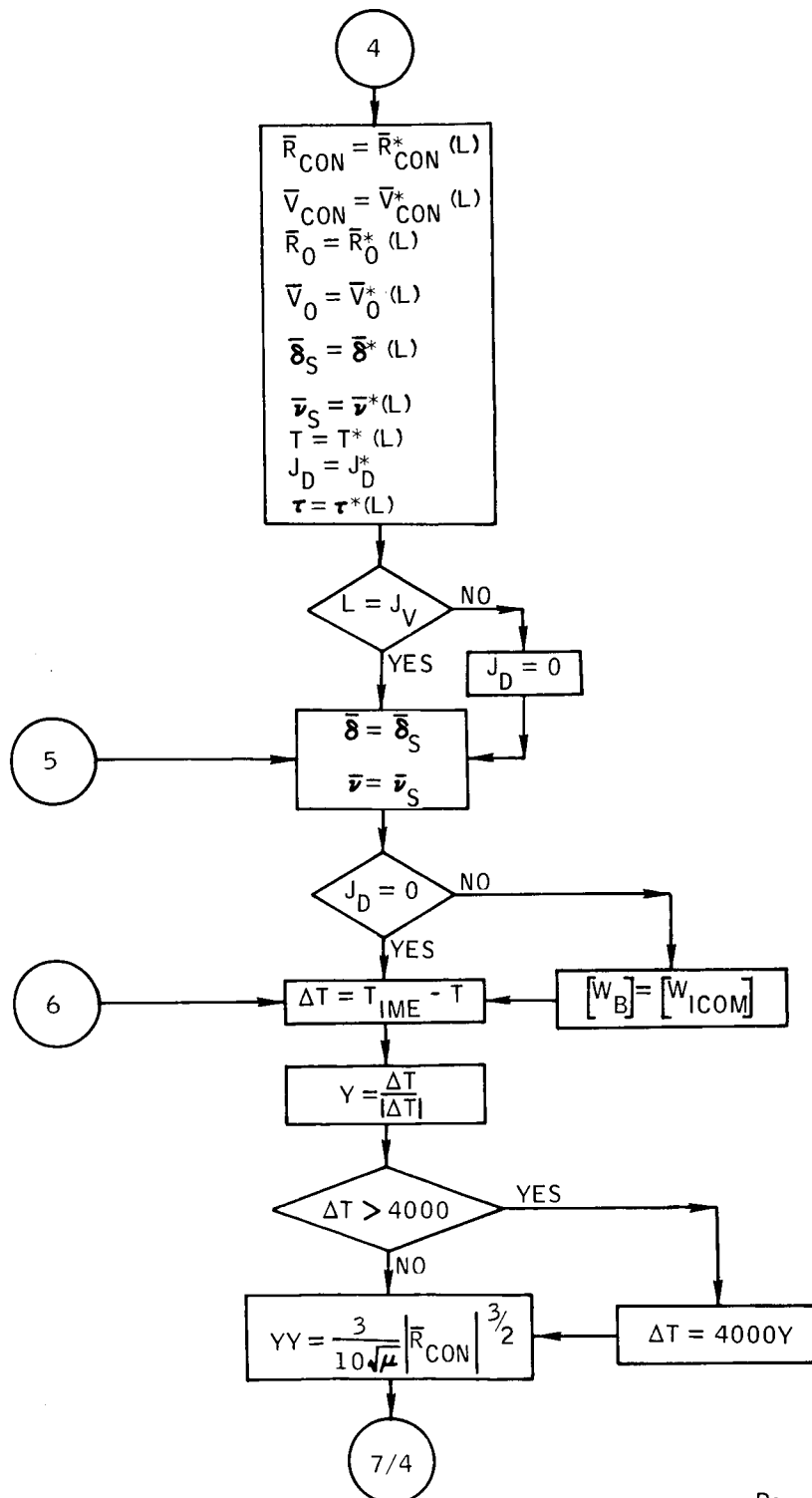


Figure B-33. - Continued.

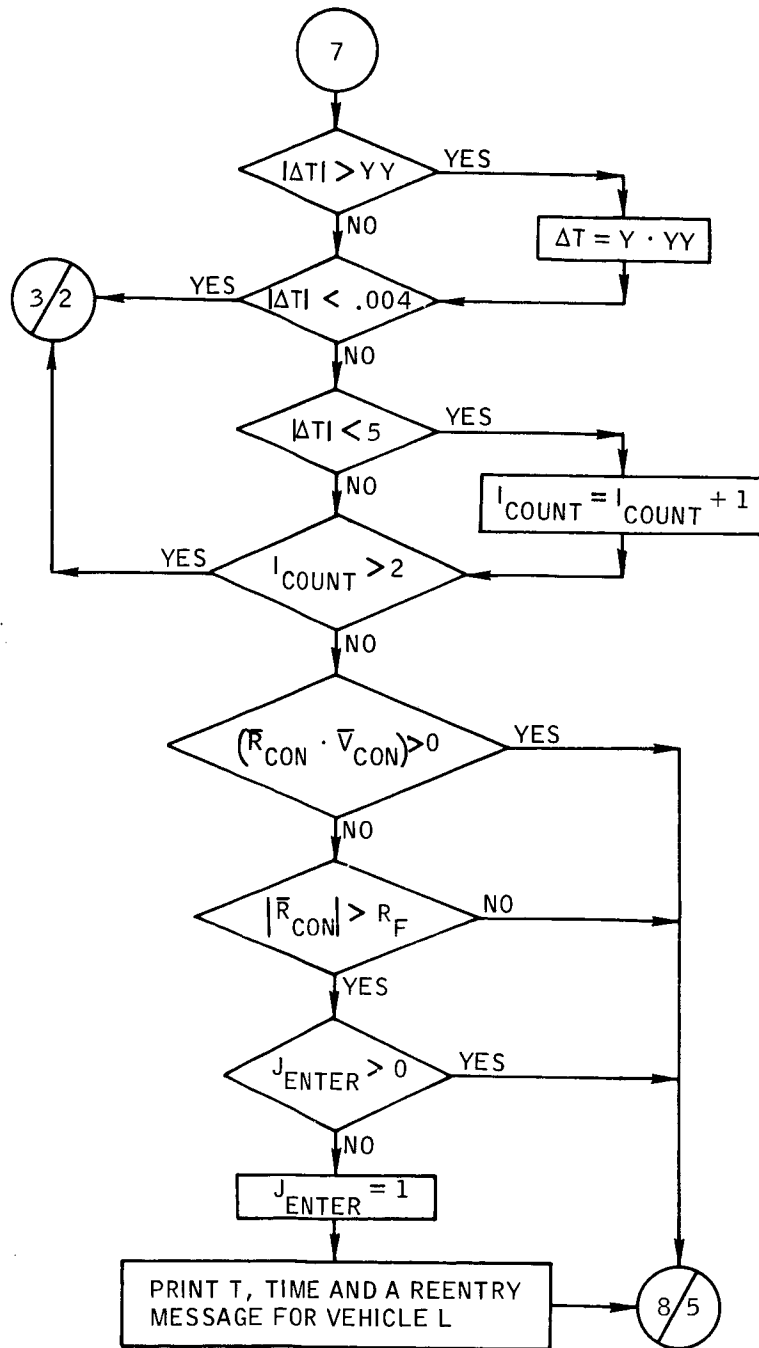


Figure B-33. - Continued.

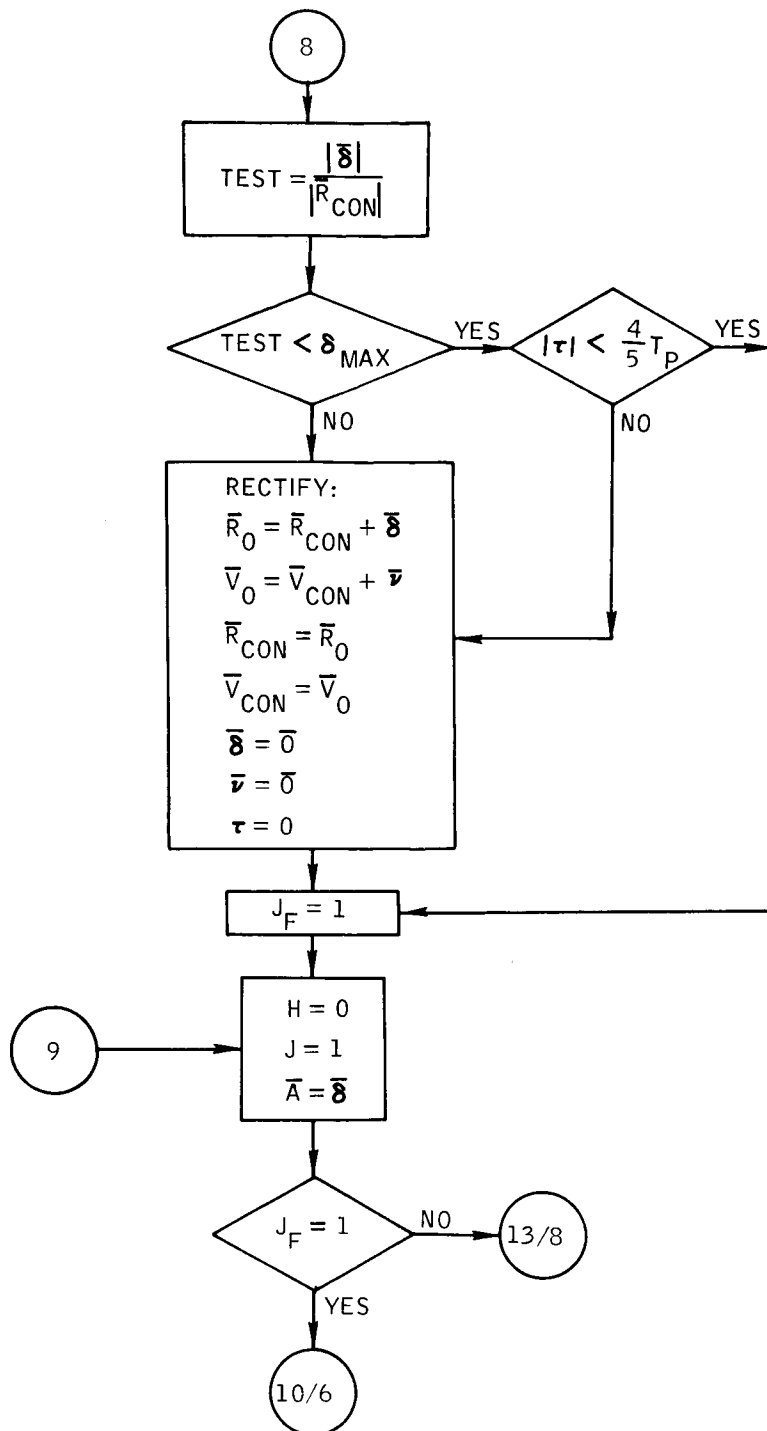


Figure B-33. - Continued.

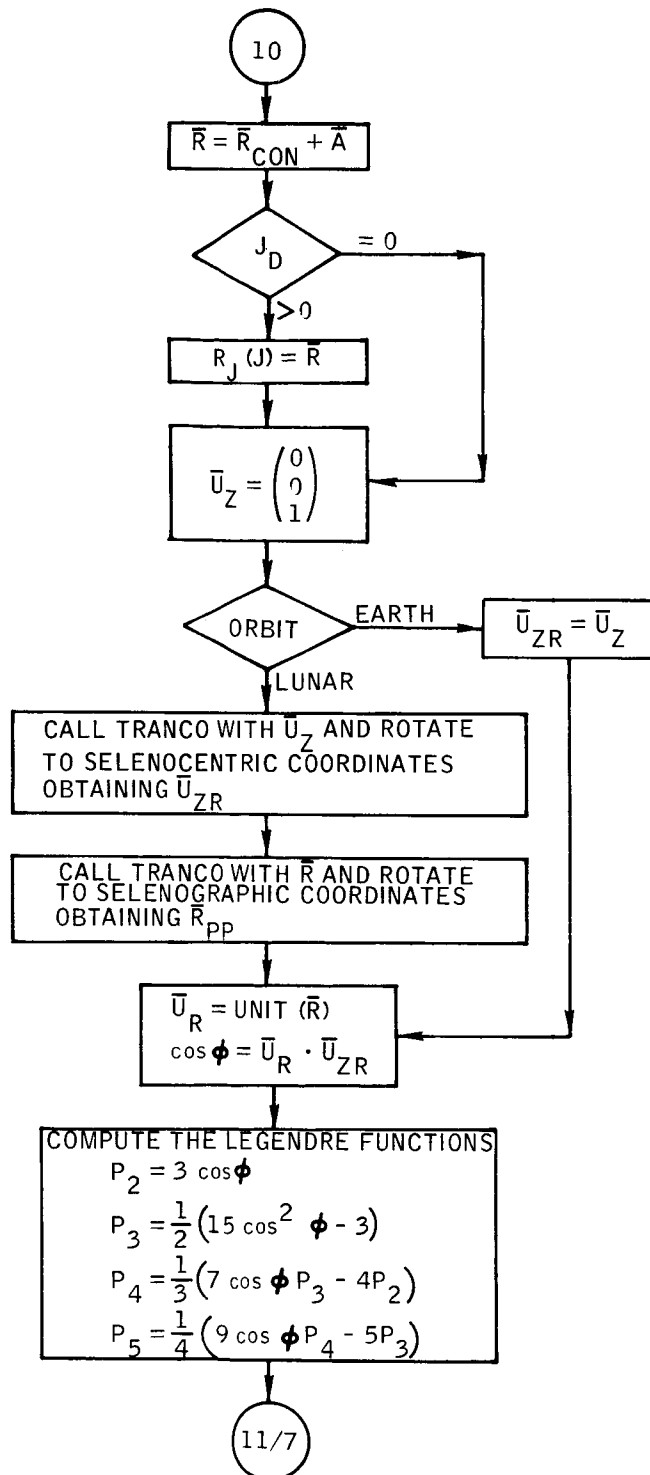


Figure B-33.- Continued.

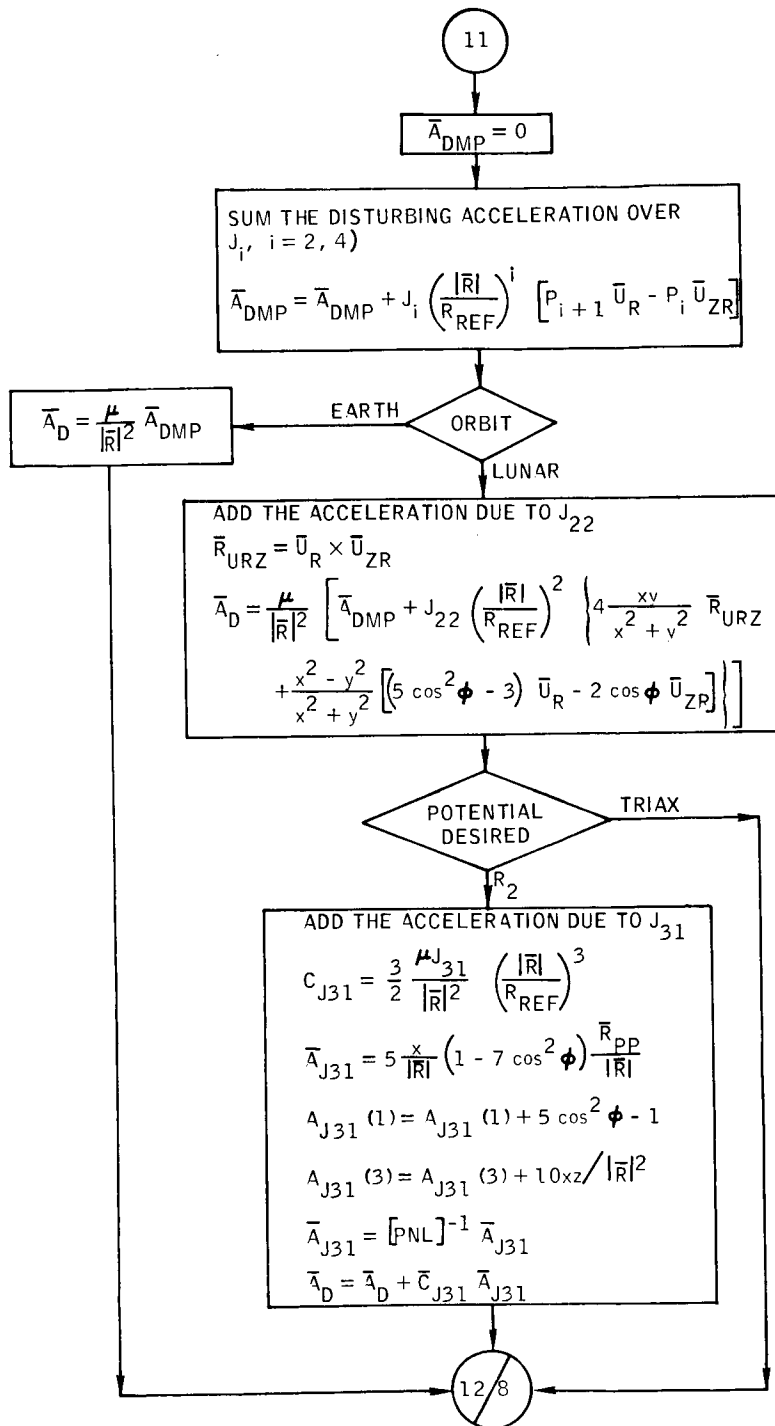


Figure B-33. - Continued.

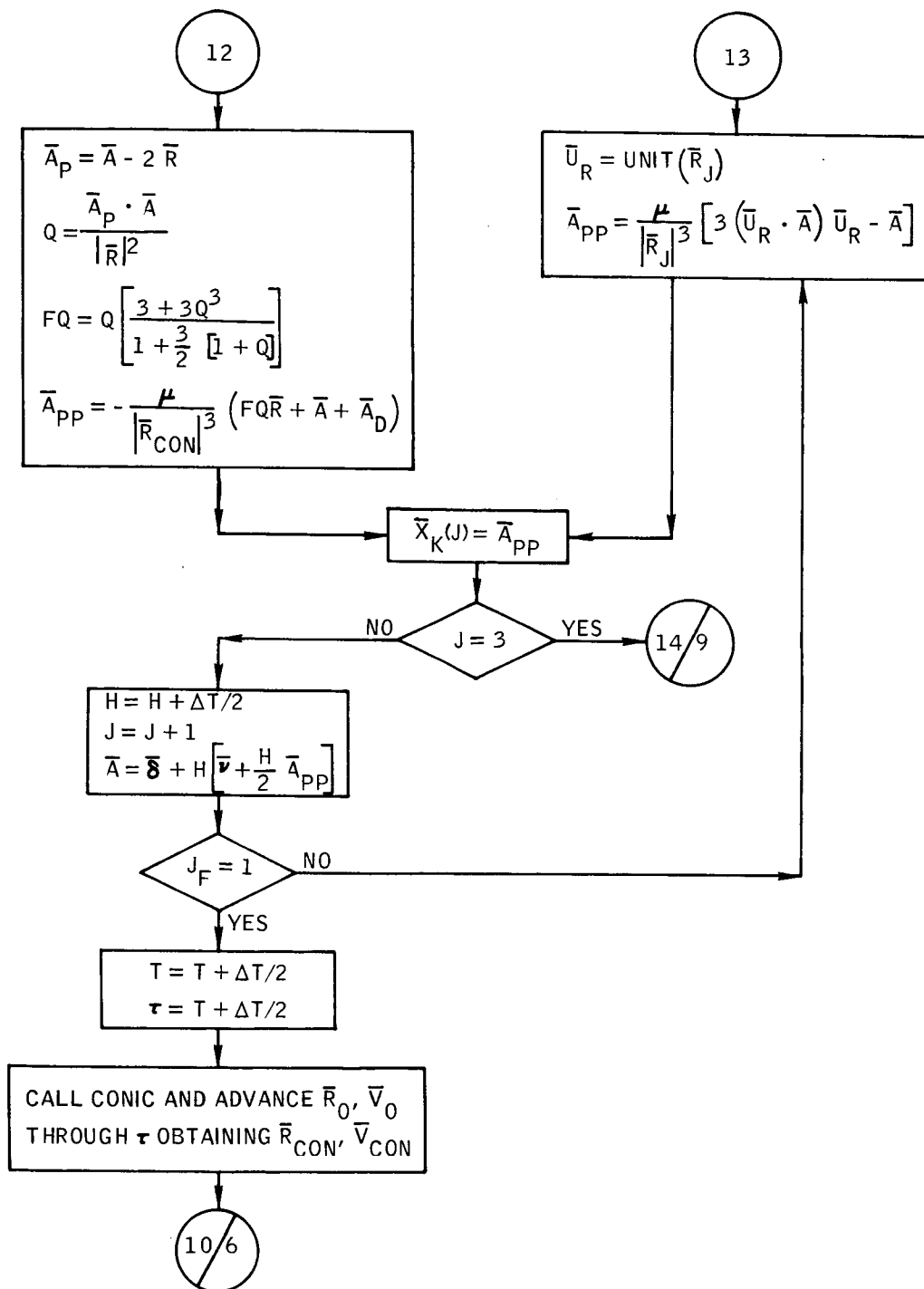


Figure B-33.- Continued.

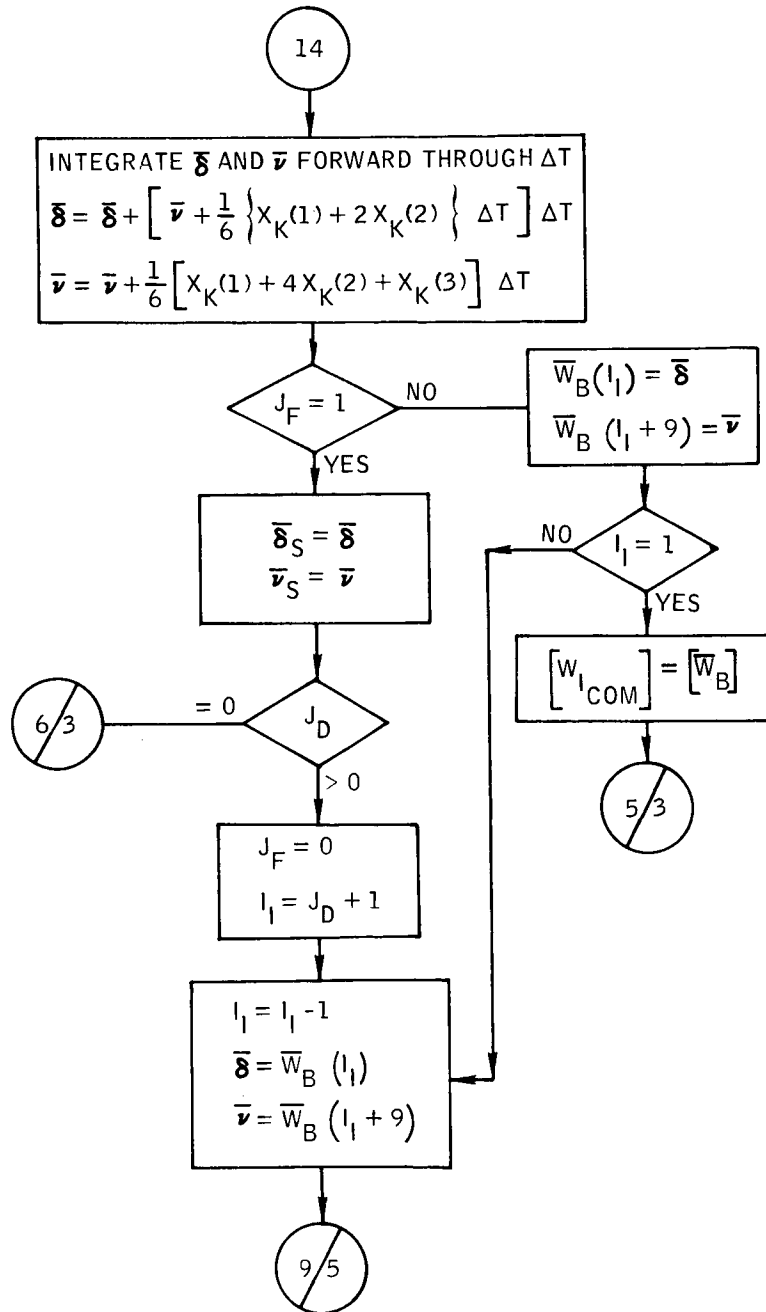


Figure B-33. - Continued.

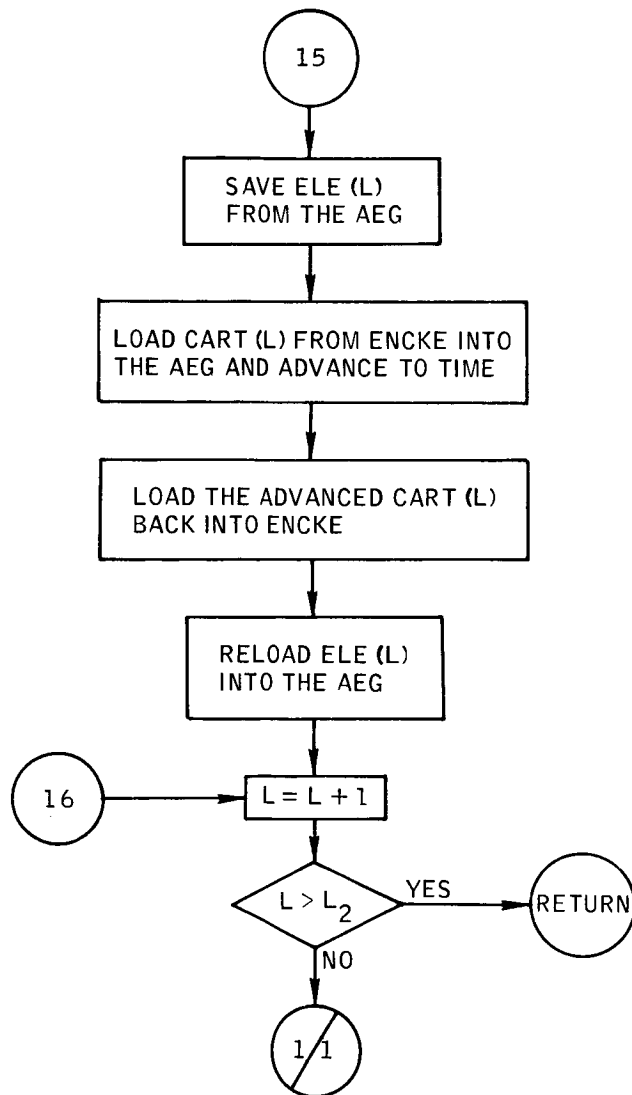


Figure B-33.- Concluded. Page 10 of 10



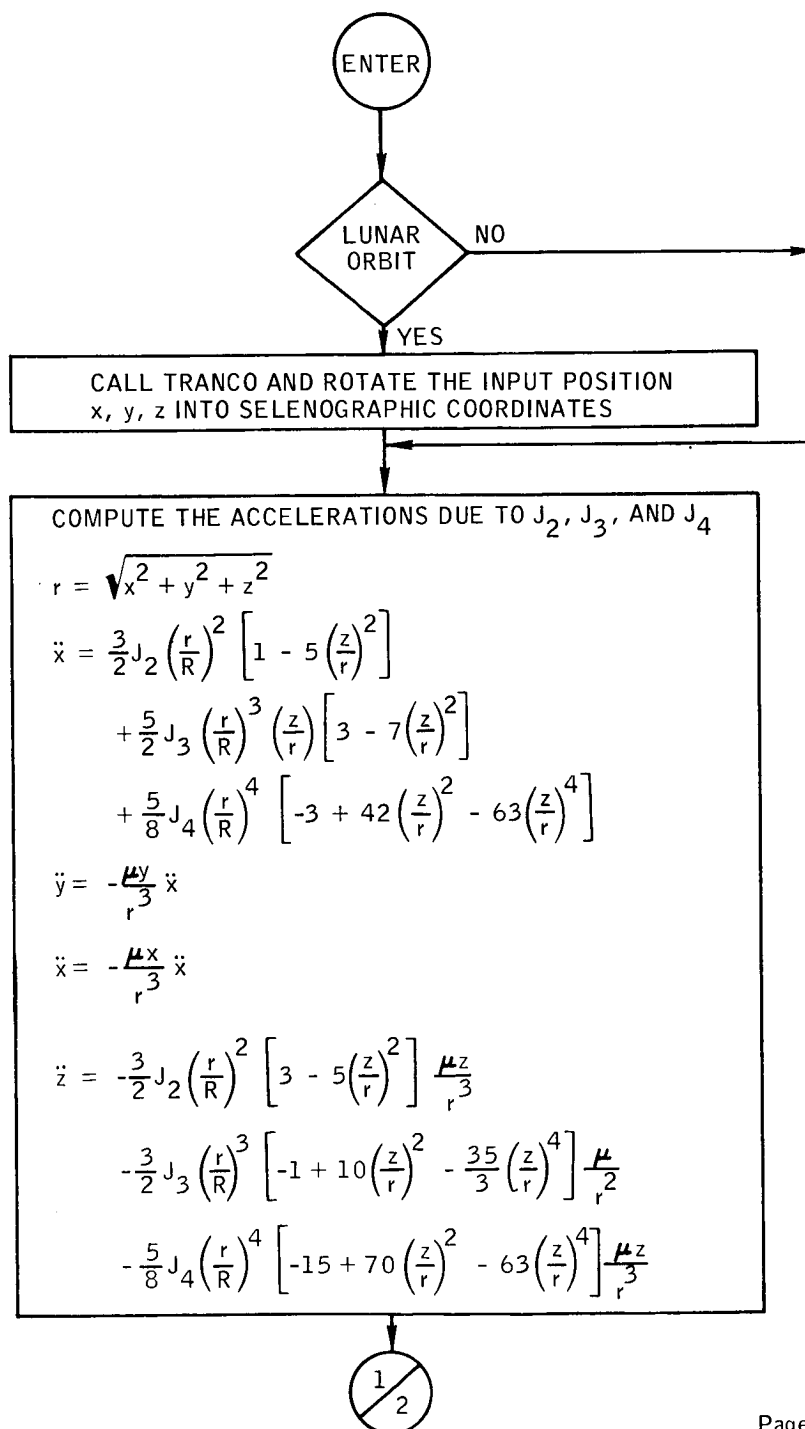


Figure B-34. - Flow chart of subroutine EPERT.

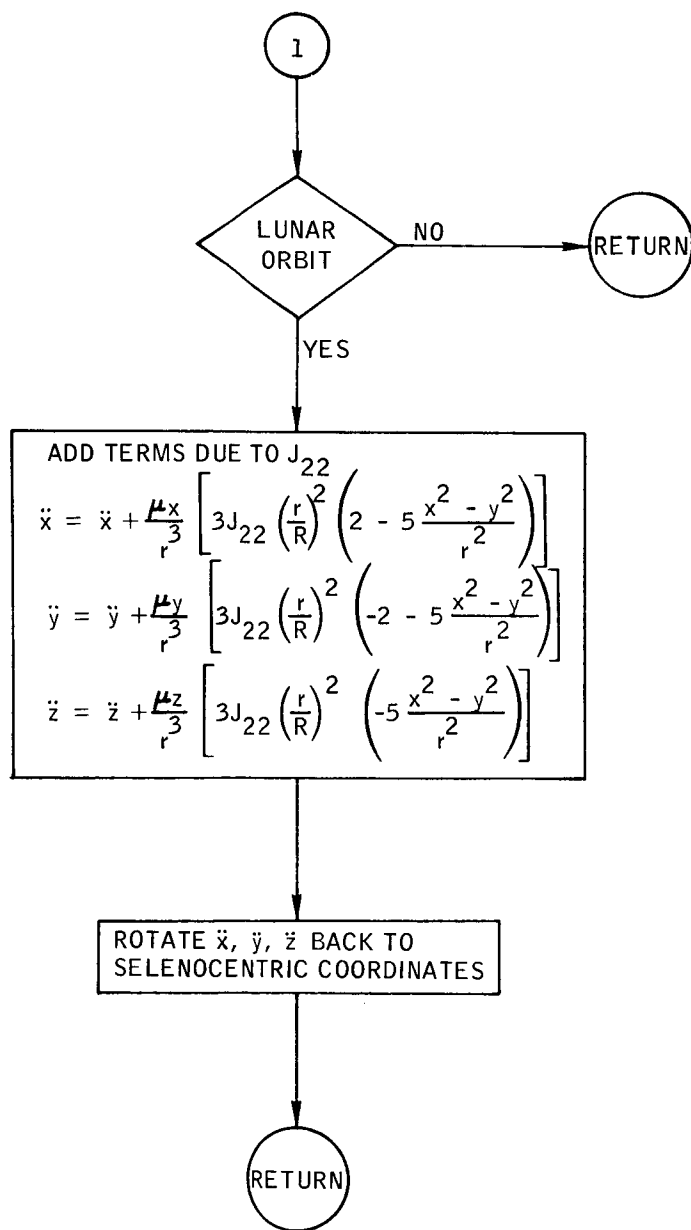


Figure B-34.- Concluded.

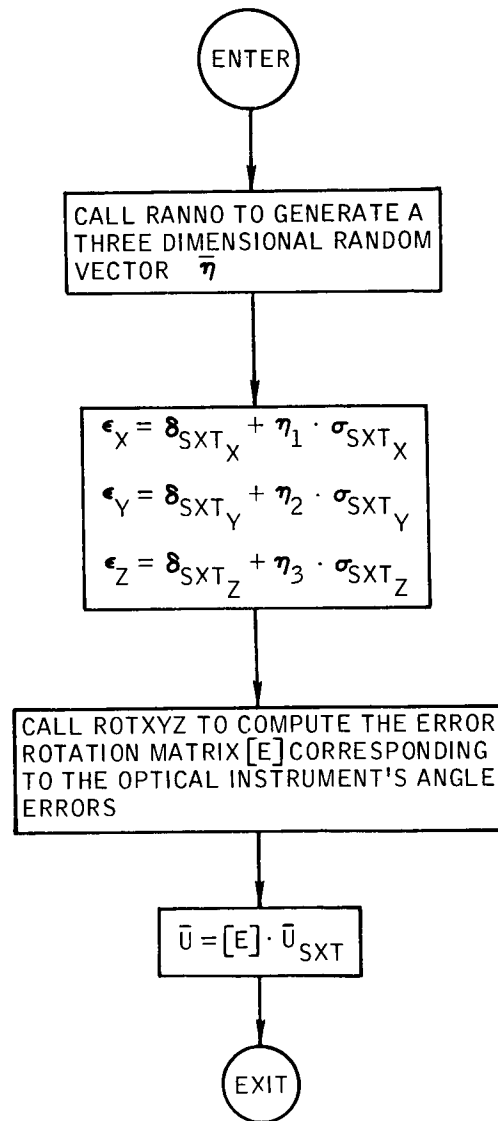


Figure B-35.- Flow chart of subroutine ERRSXT.

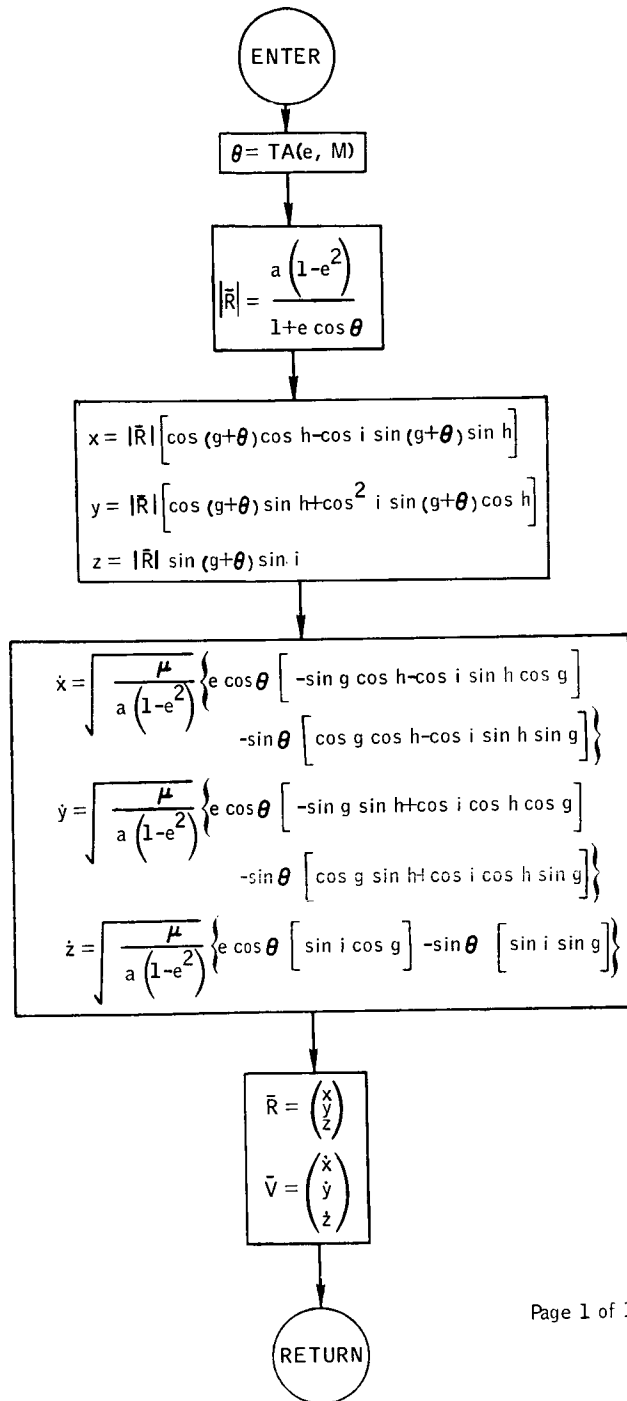


Figure B-36.- Flow chart of subroutine ETOXYZ.

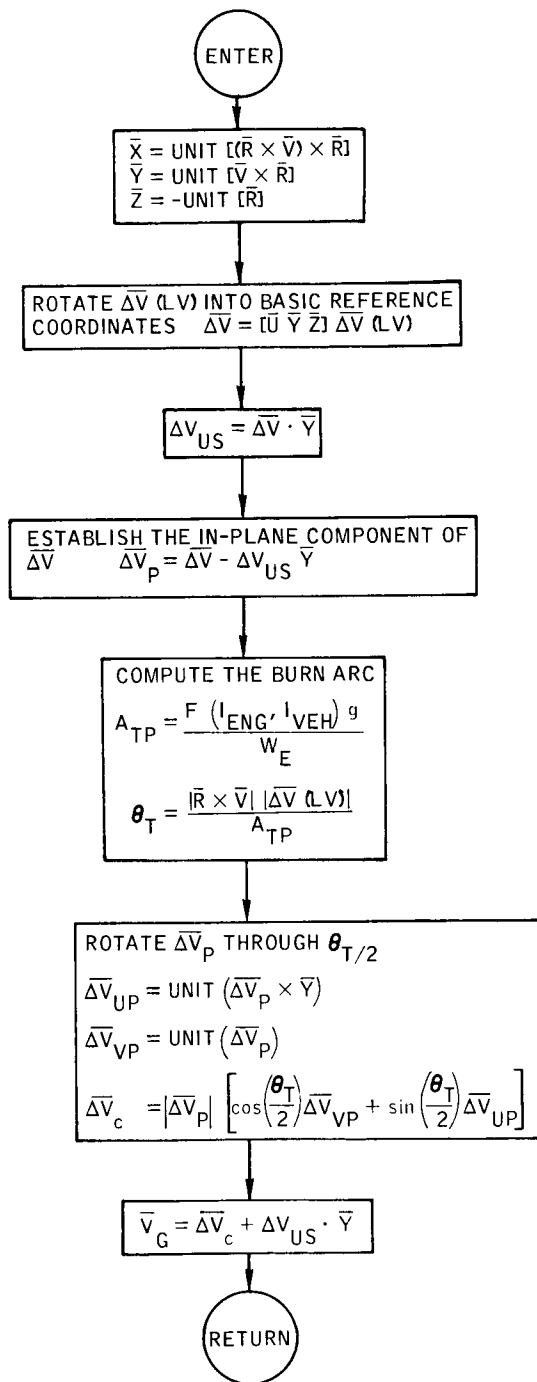


Figure B-37.- Flow chart of subroutine EXDV.

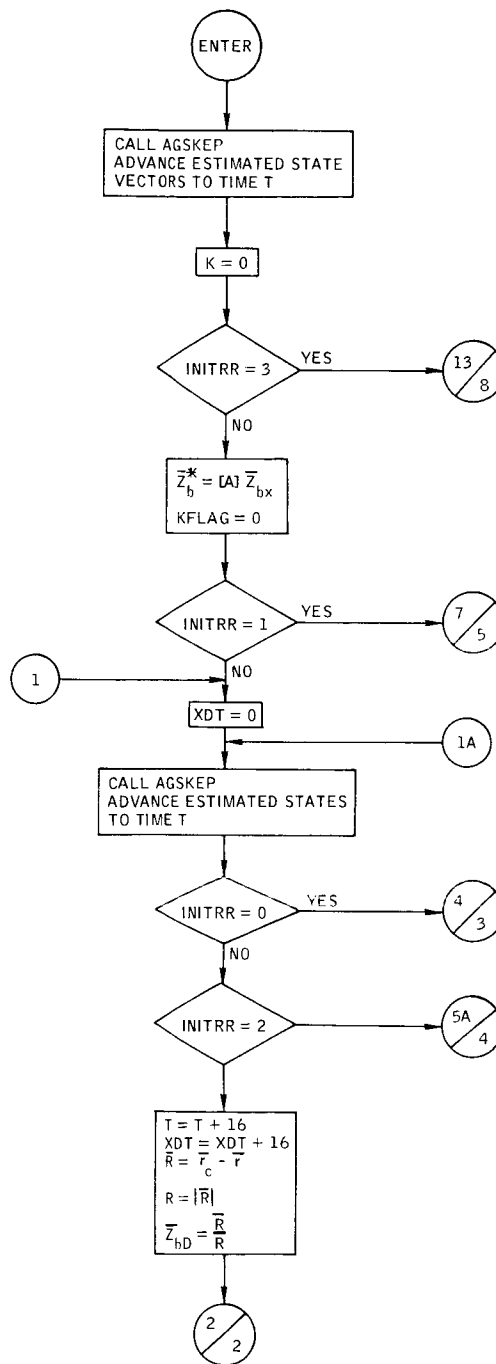


Figure B-38.- Flow chart of subroutine FILTER.

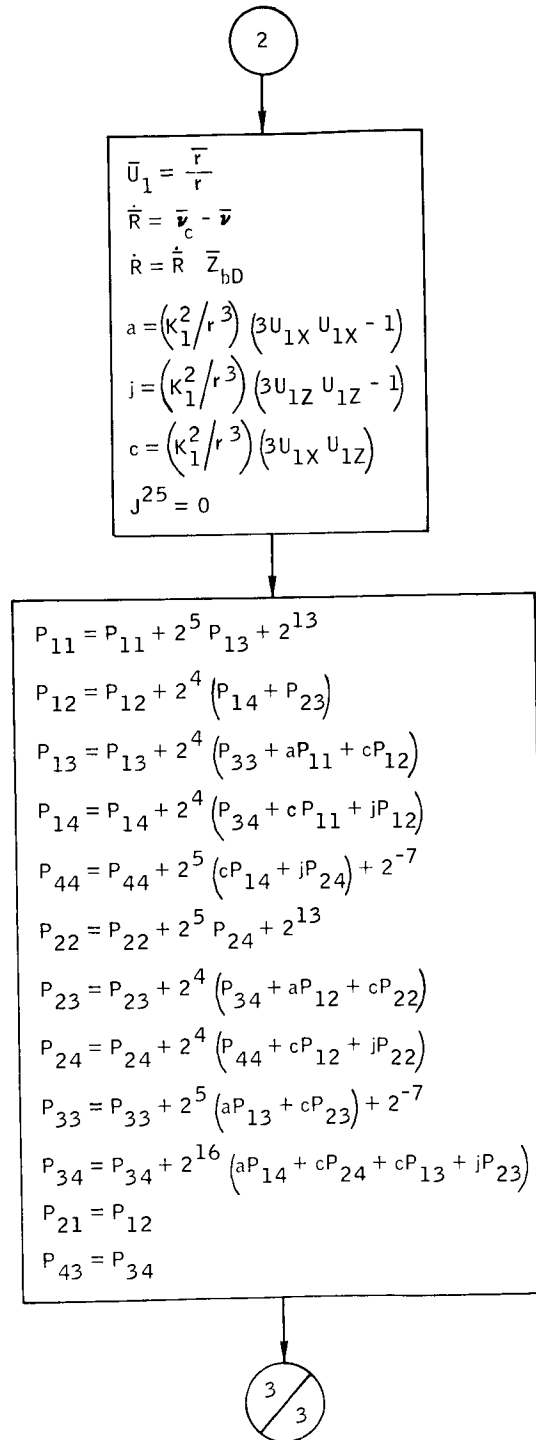


Figure B-38.- Continued.

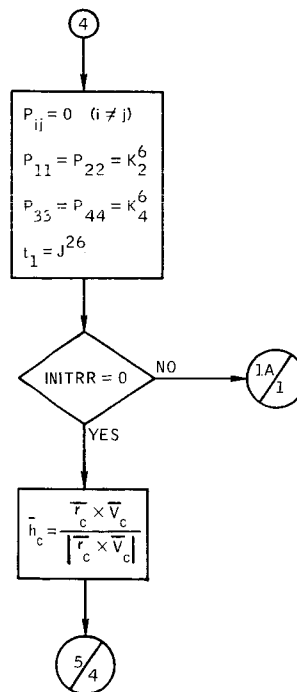
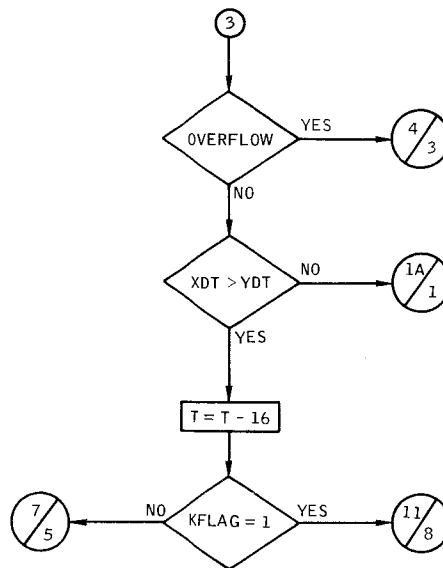
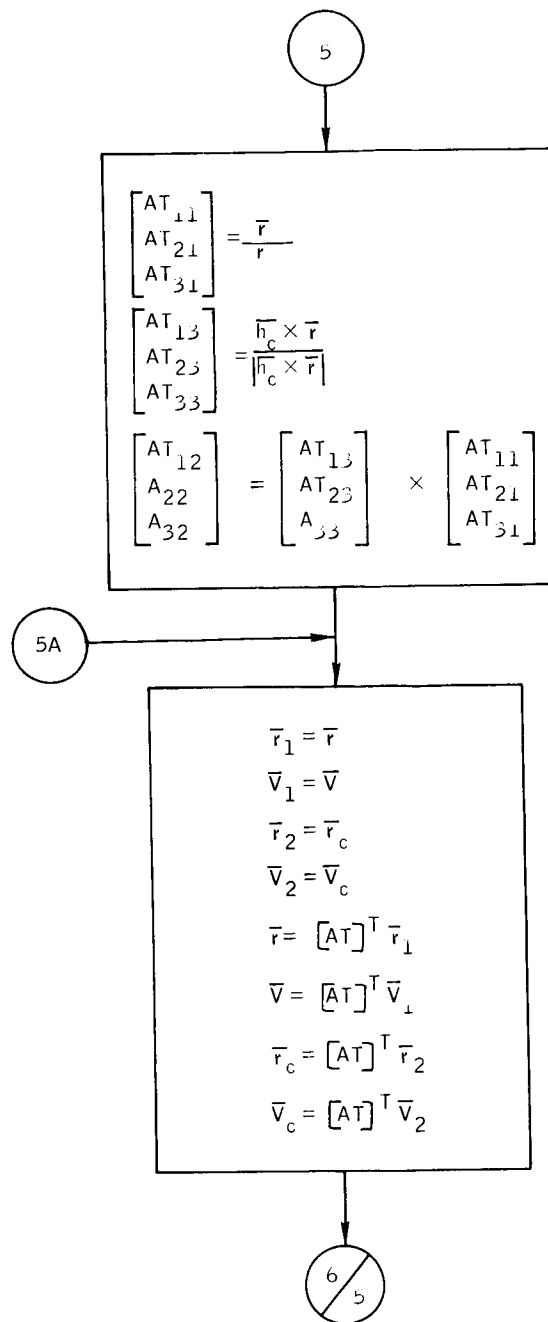


Figure B-38.- Continued.





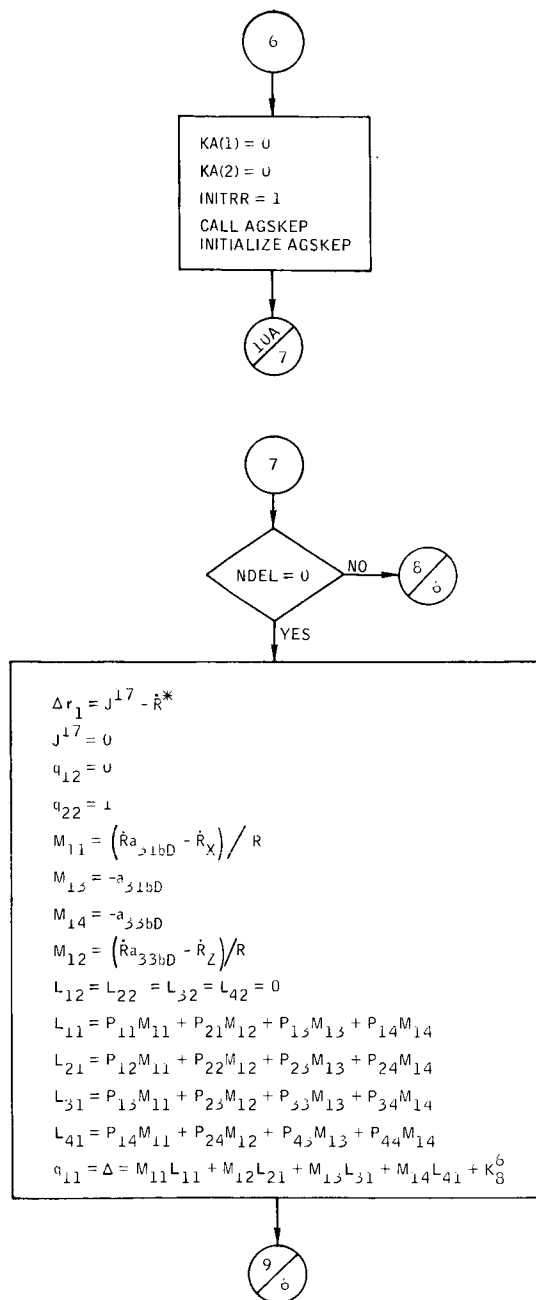


Figure B-38, - Continued.

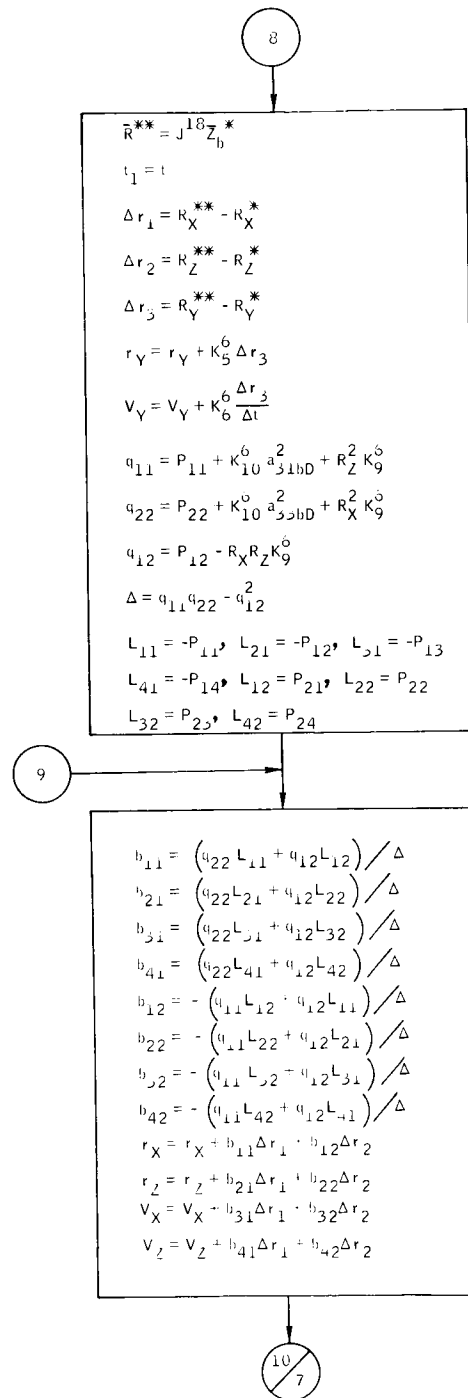
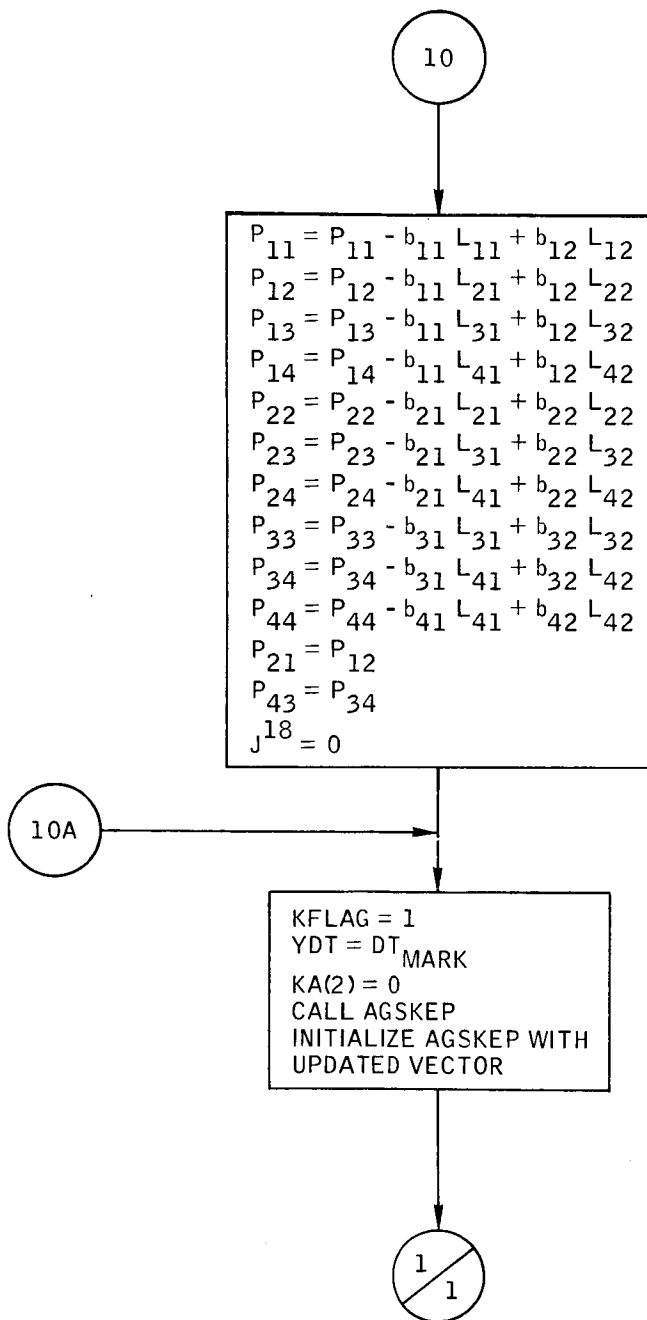
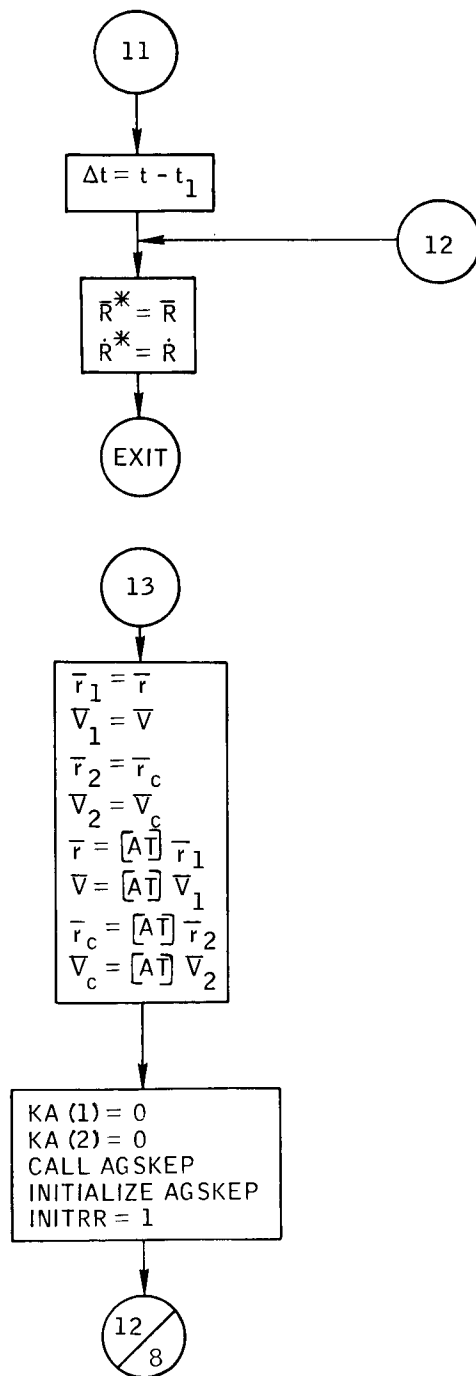


Figure B-38, - Continued.





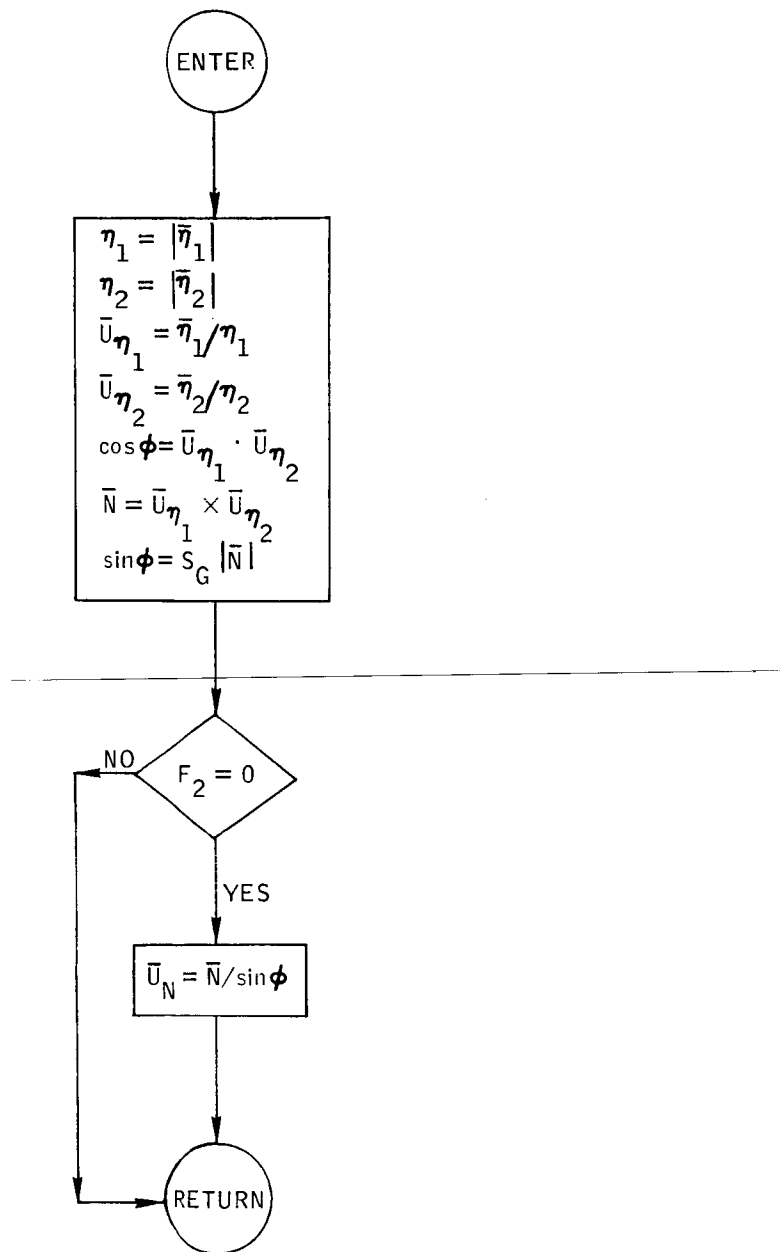


Figure B-39.- Flow chart of subroutine GEOMET.

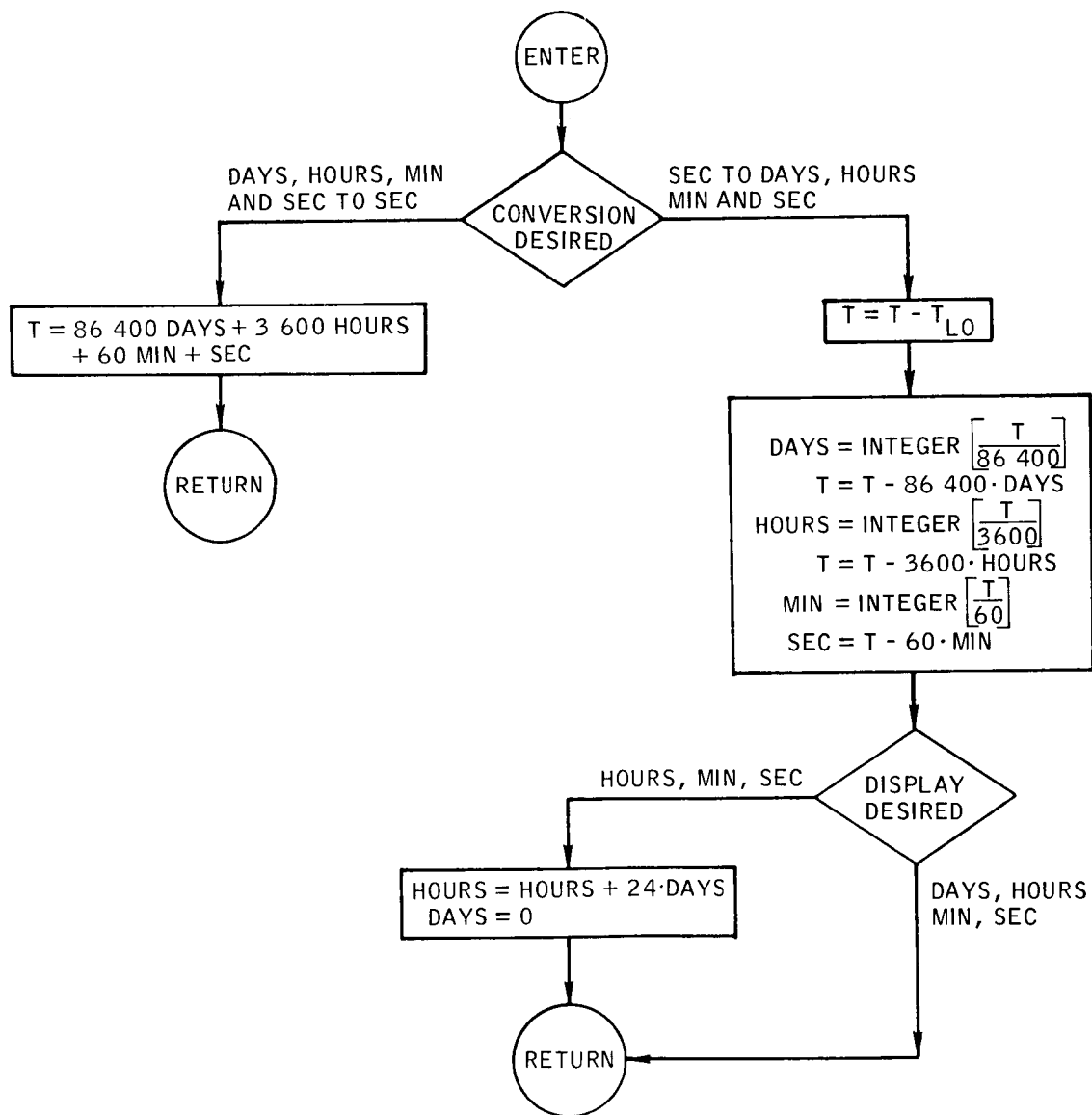


Figure B-40.- Flow chart of subroutine GMTIME.

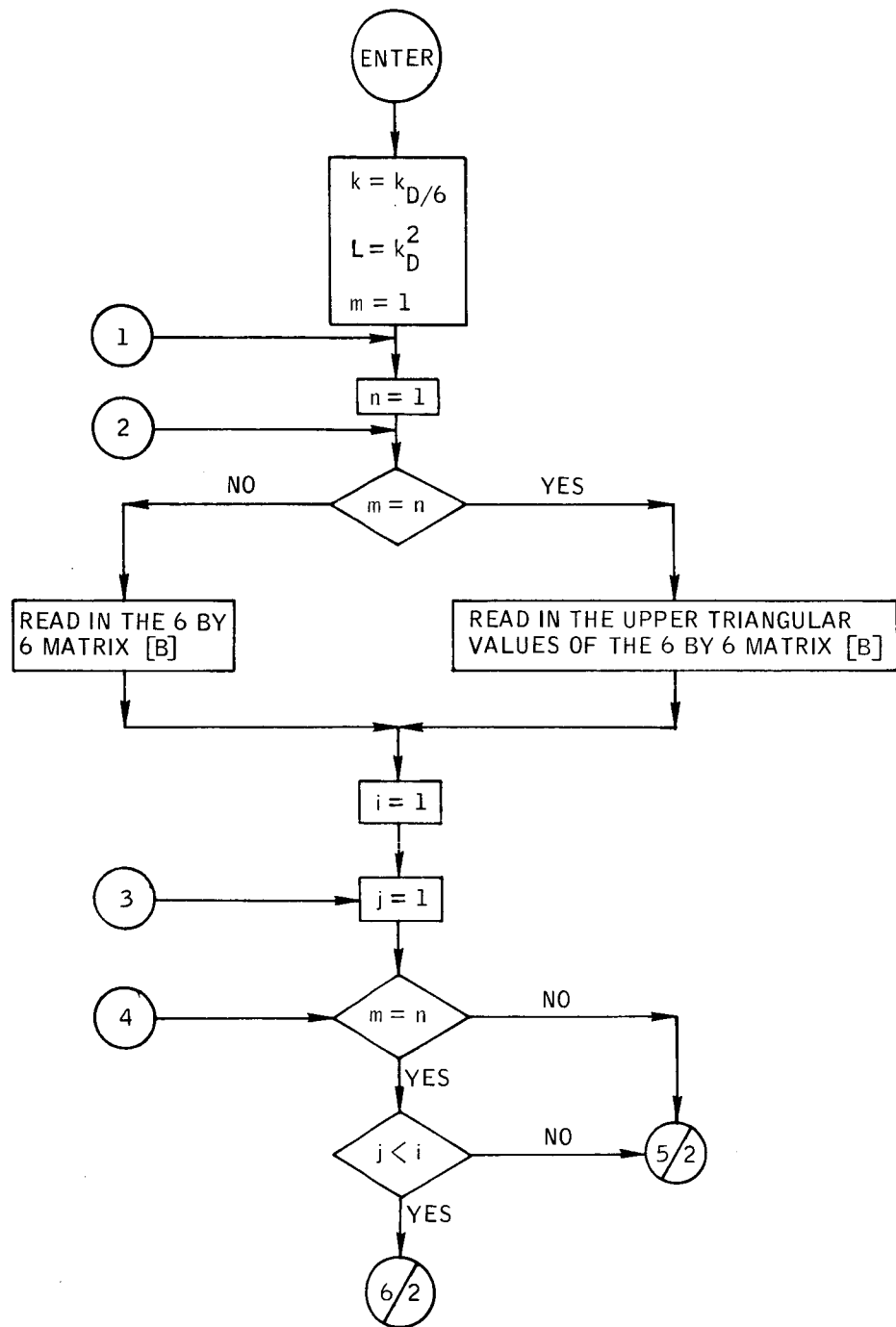


Figure B-41.- Flow chart of subroutine INCOV.



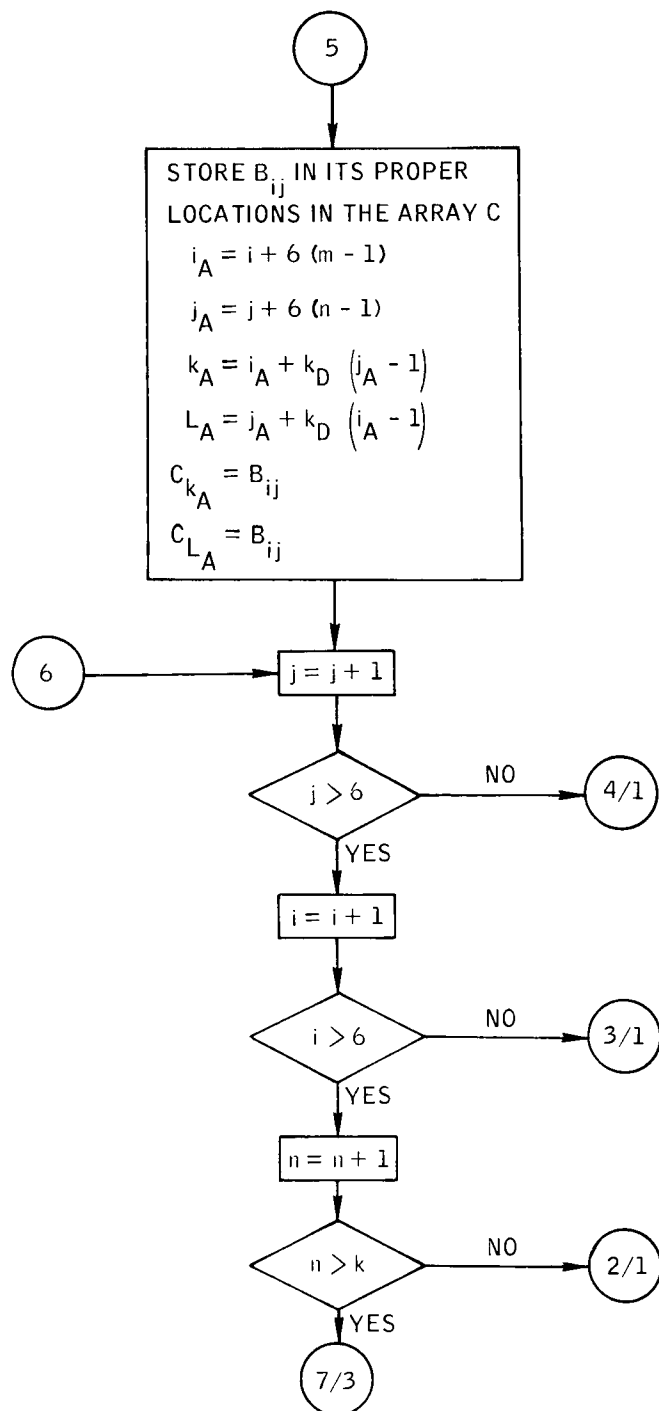


Figure B-41.- Continued.

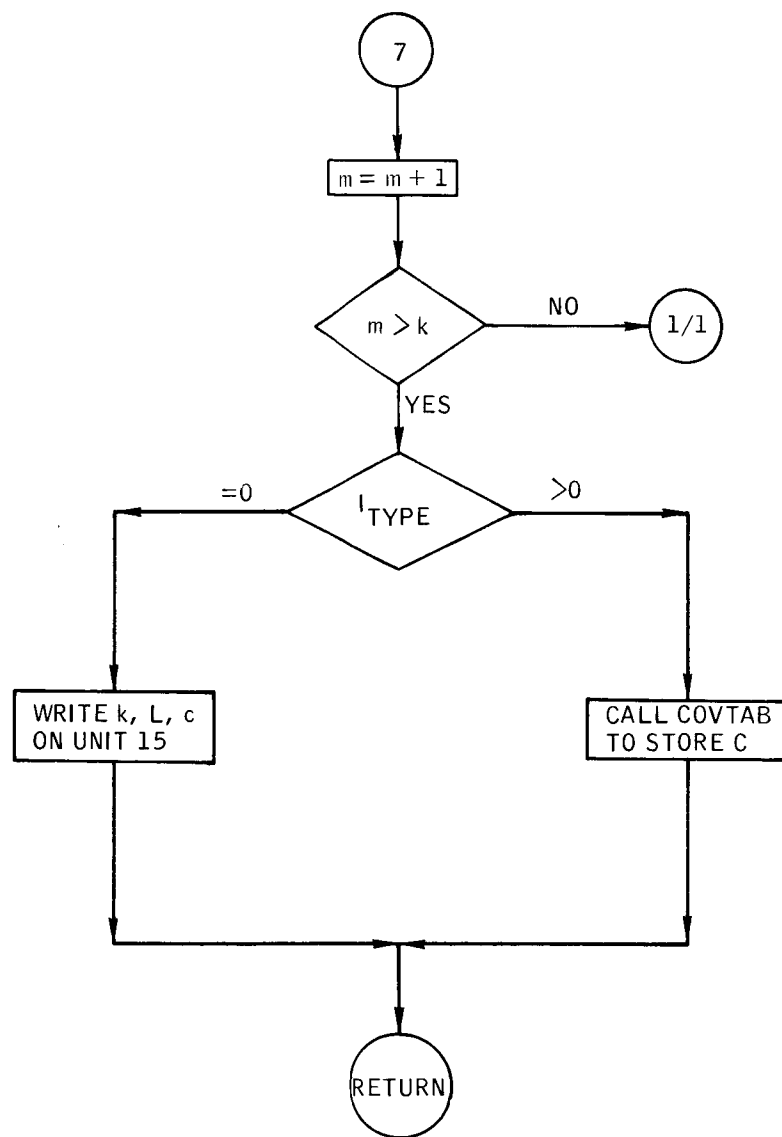


Figure B-41.- Concluded.

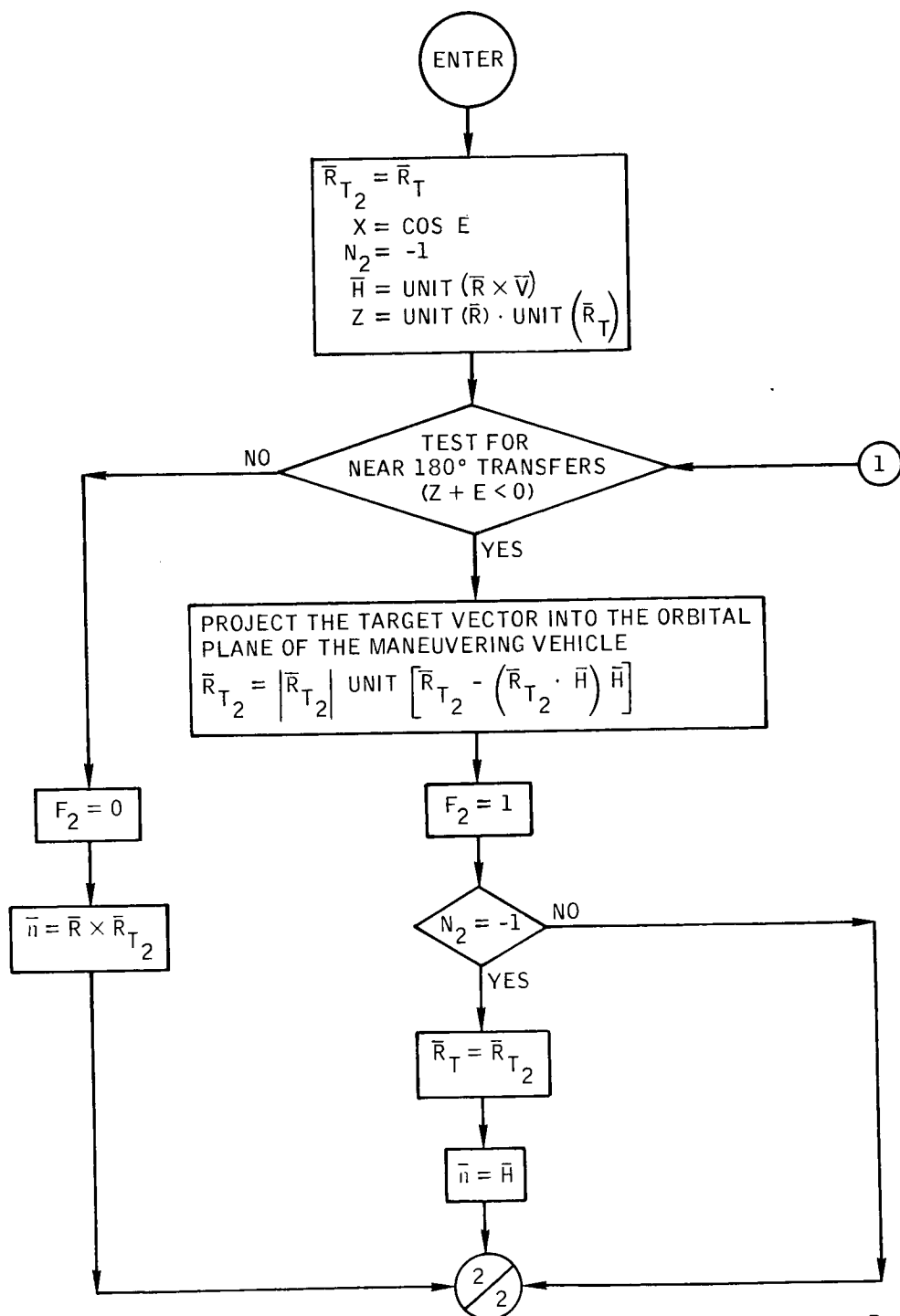


Figure B-42.- Flow chart of subroutine INITV.

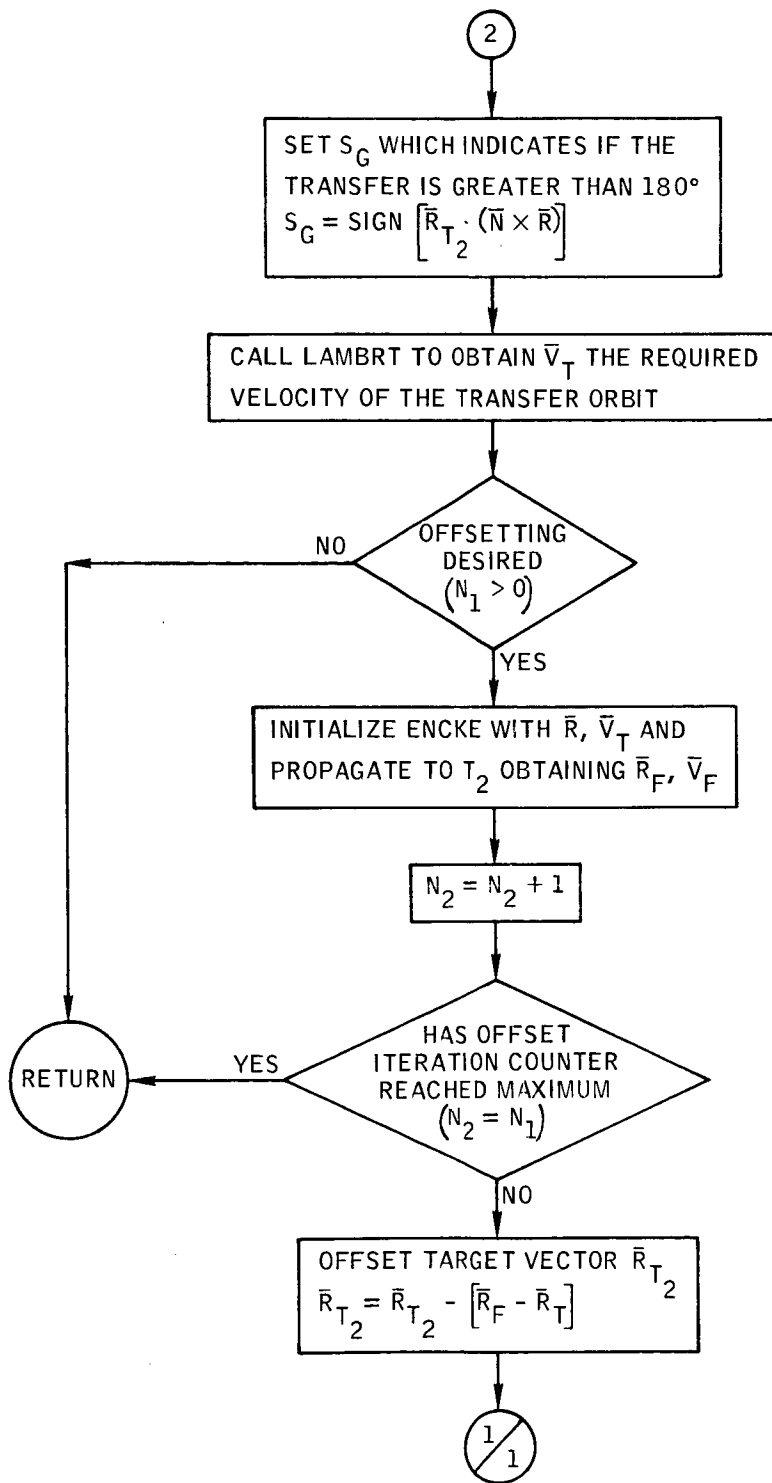


Figure B-42.- Concluded.

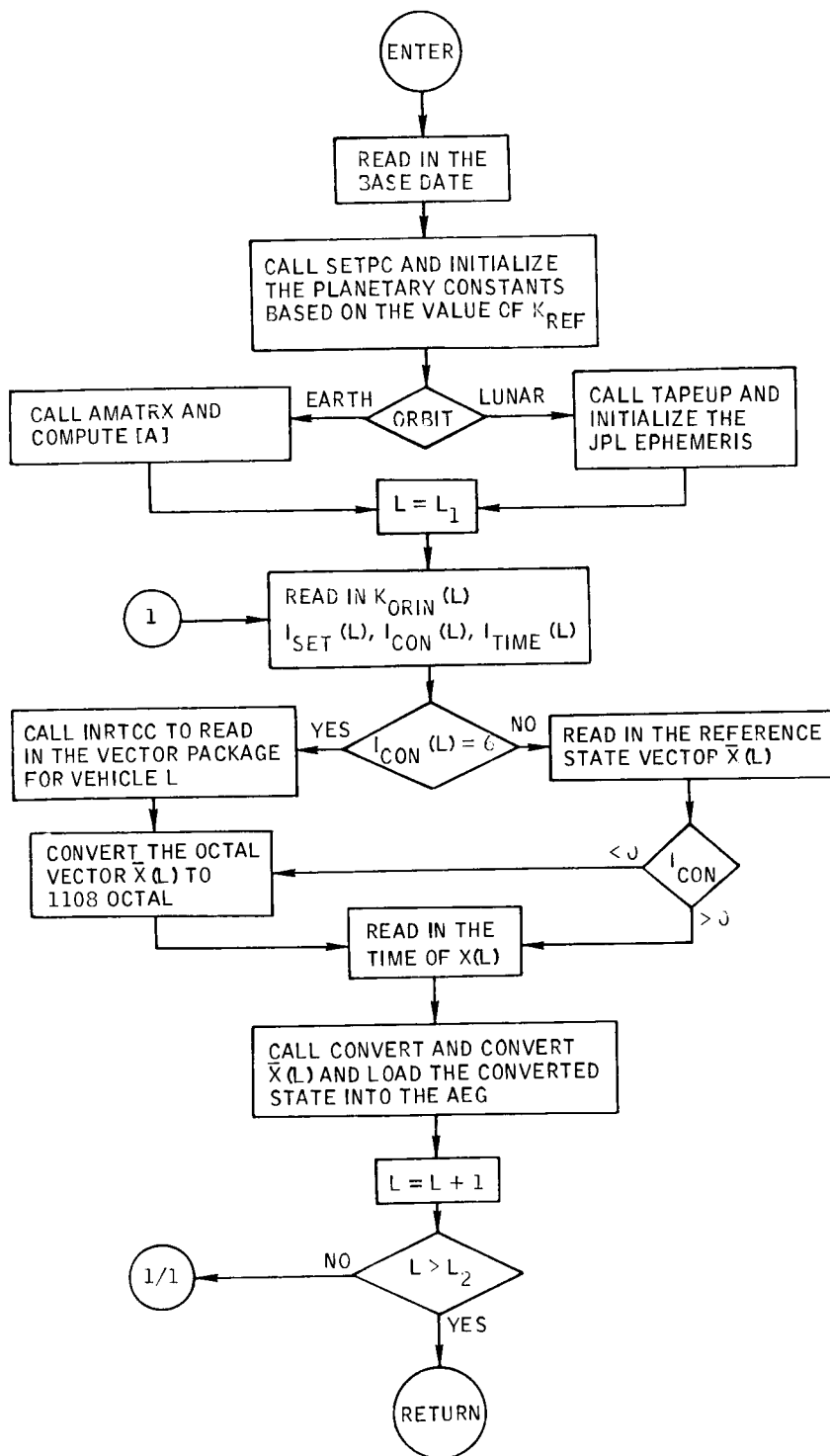


Figure B-43.- Flow chart of subroutine INPUT.

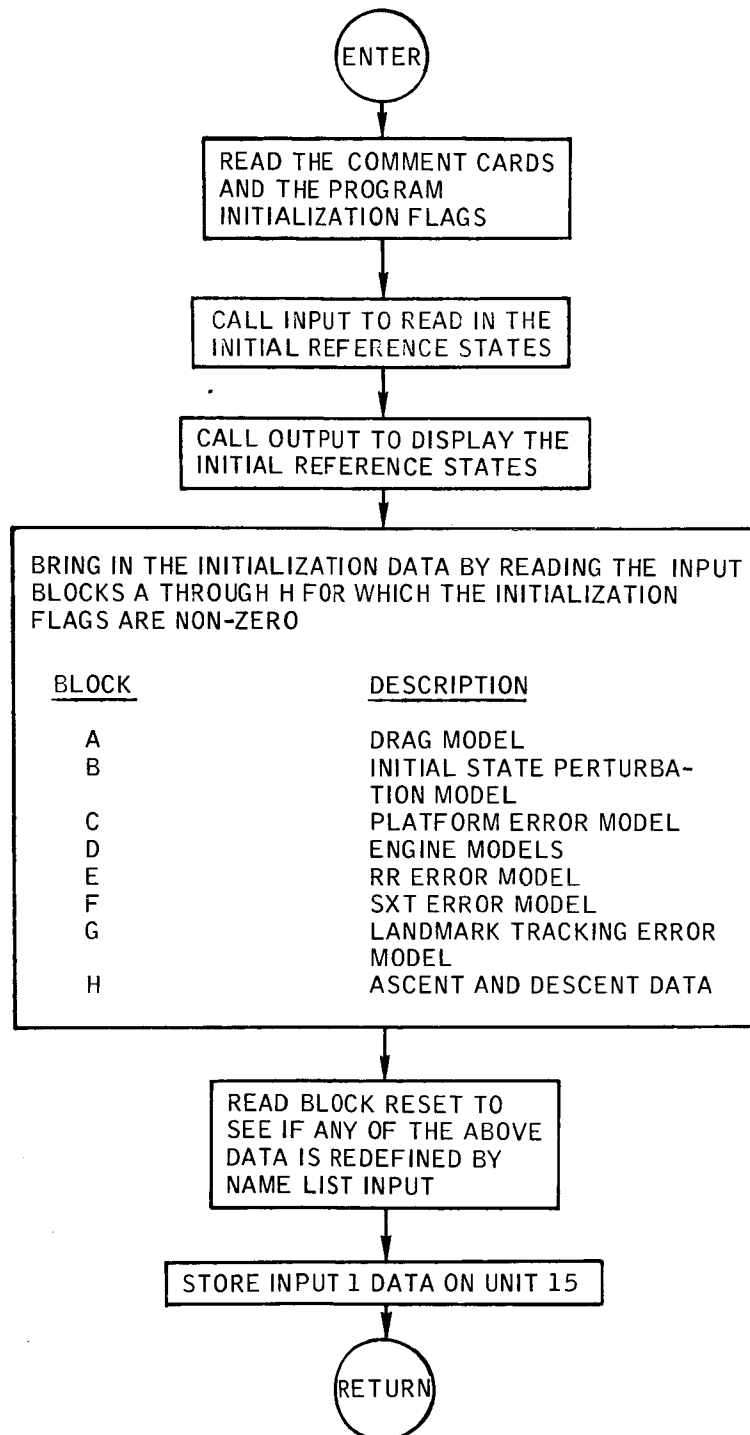


Figure B-44.- Flow chart of subroutine INPUT 1.

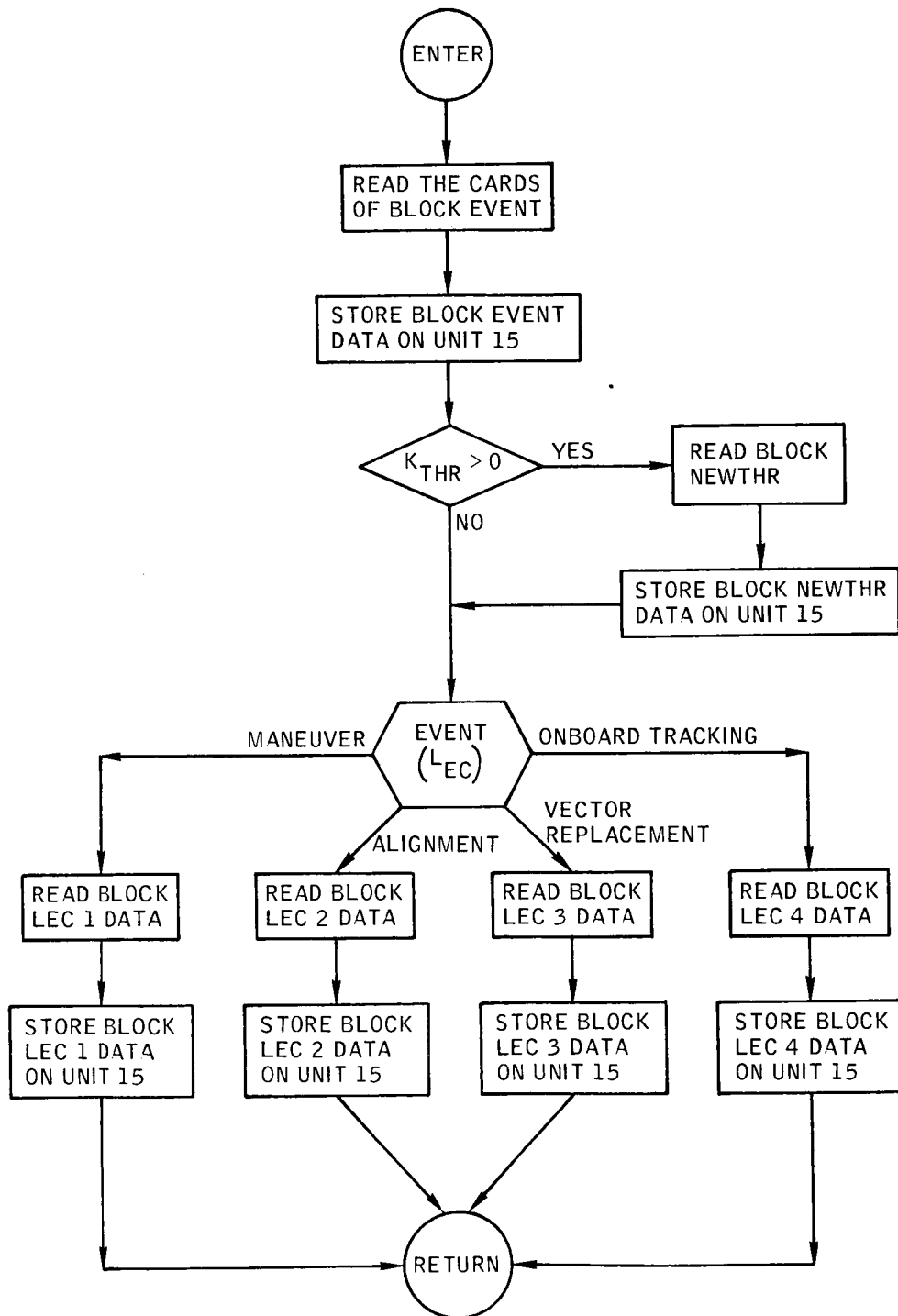


Figure B-45.- Flow chart of subroutine INPUT 2.

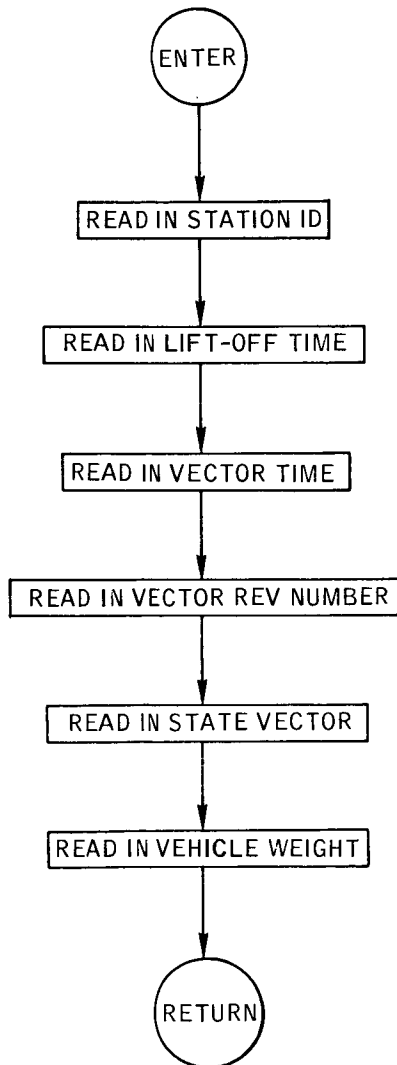


Figure B-46.- Flow chart of subroutine INRTCC.



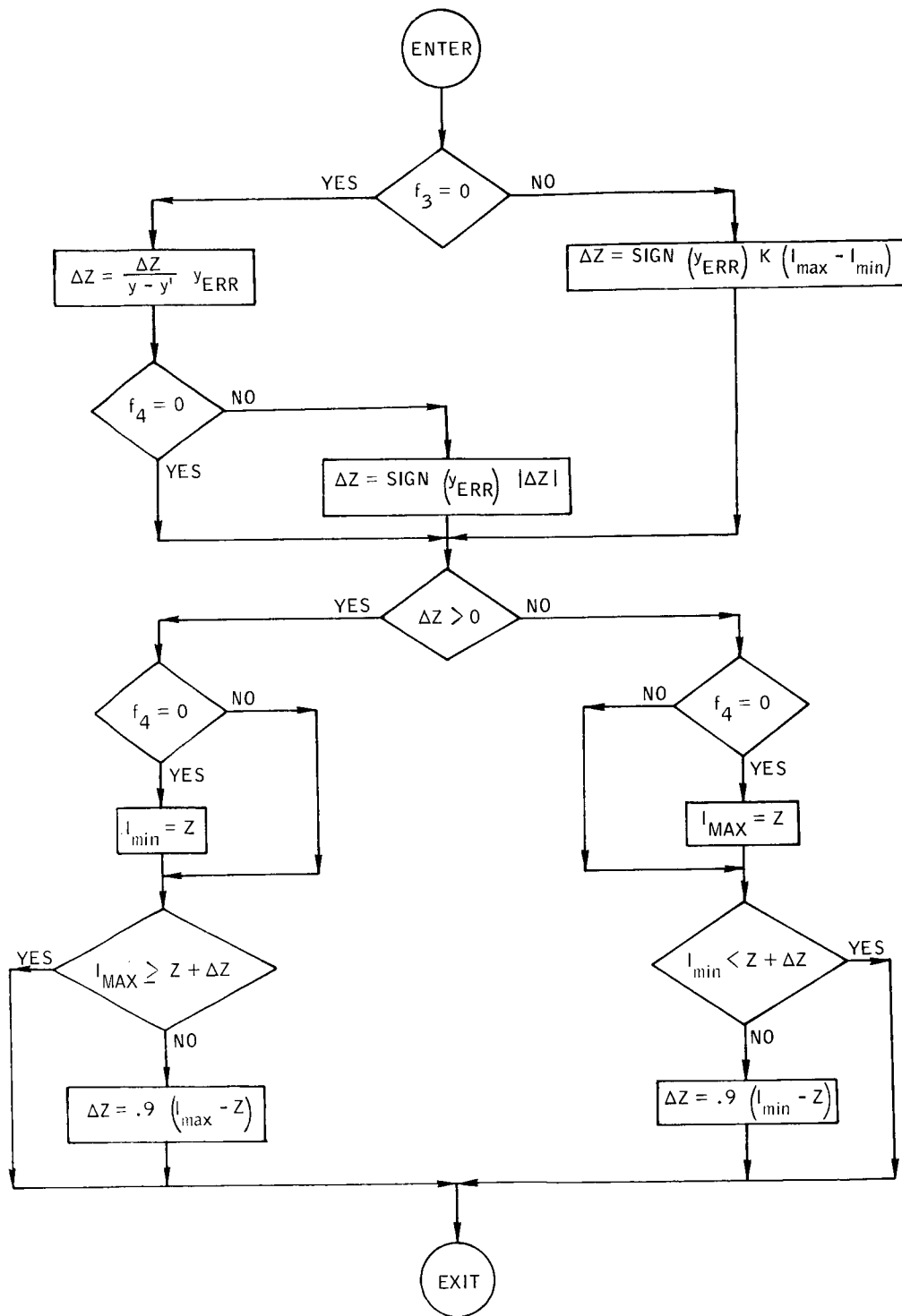


Figure B-47.- Flow chart of subroutine ITRATE.

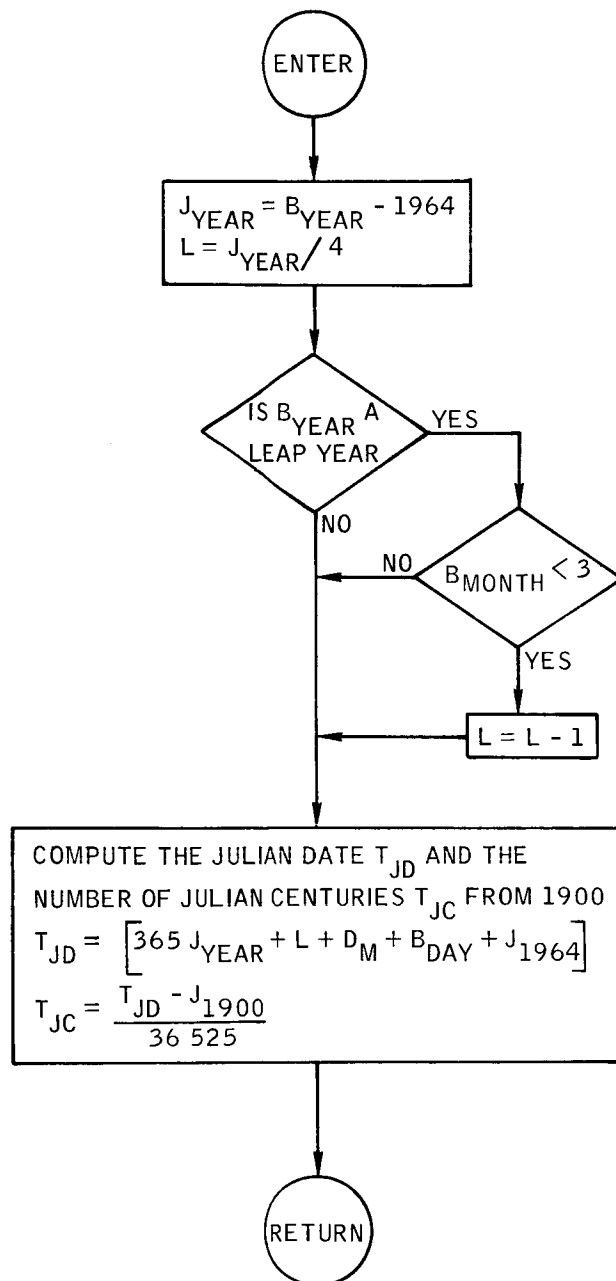


Figure B-48.- Flow chart of subroutine JDATE.

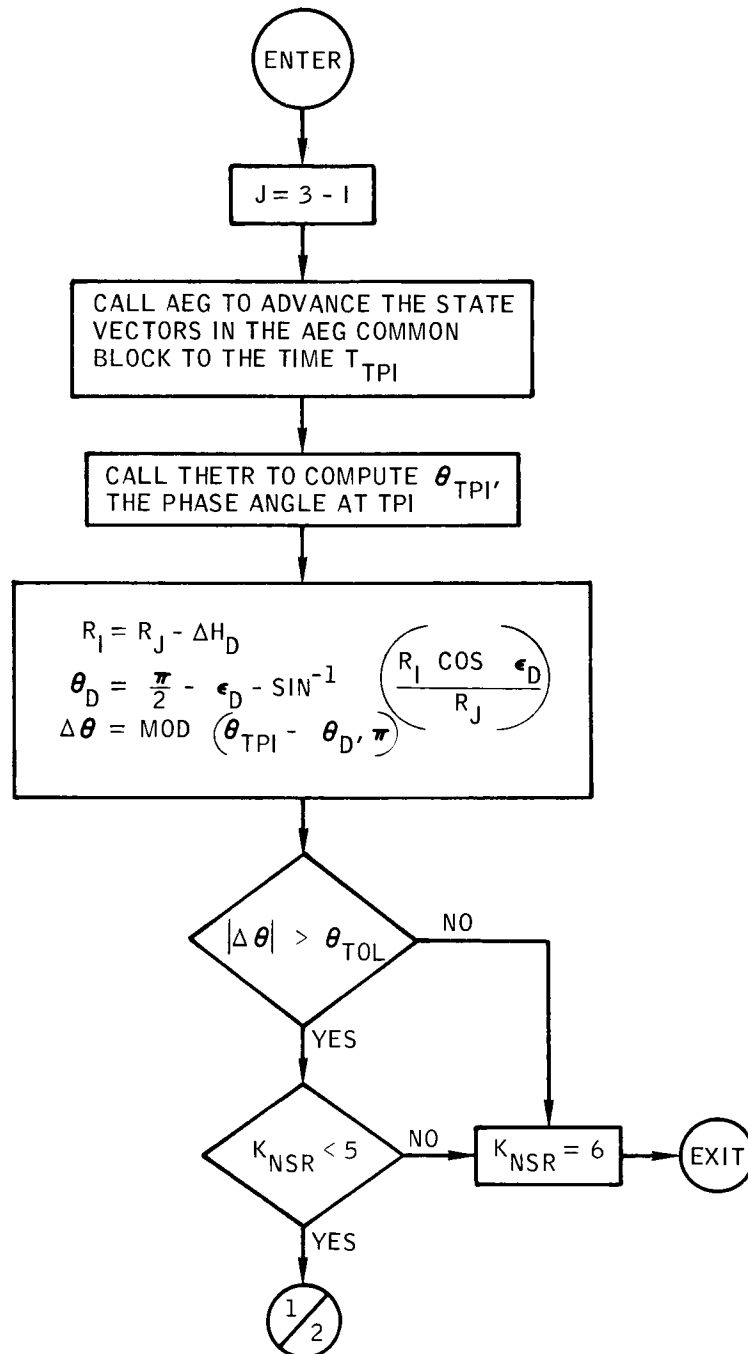


Figure B-49.- Flow chart of subroutine JOCDH.

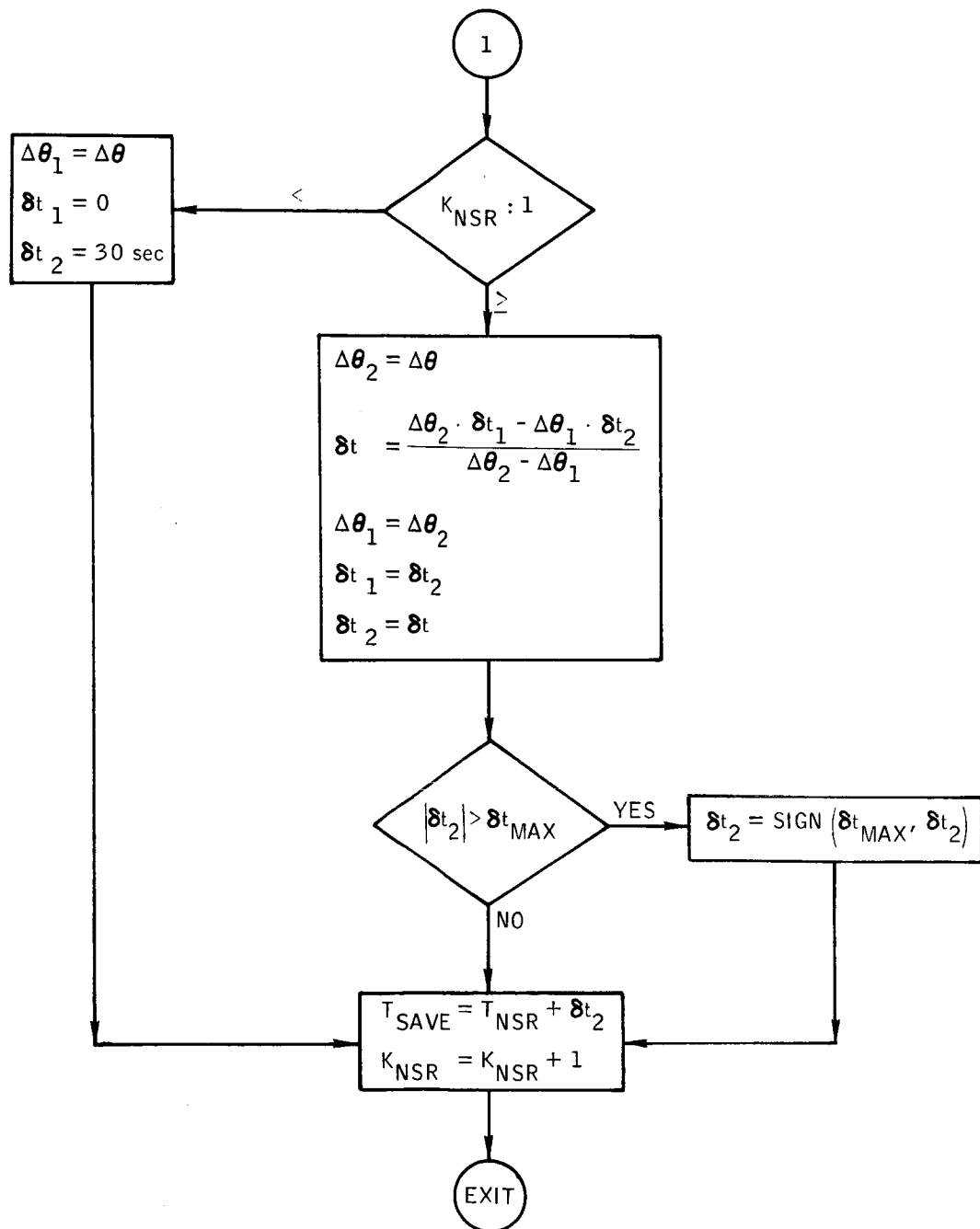


Figure B-49.- Concluded.

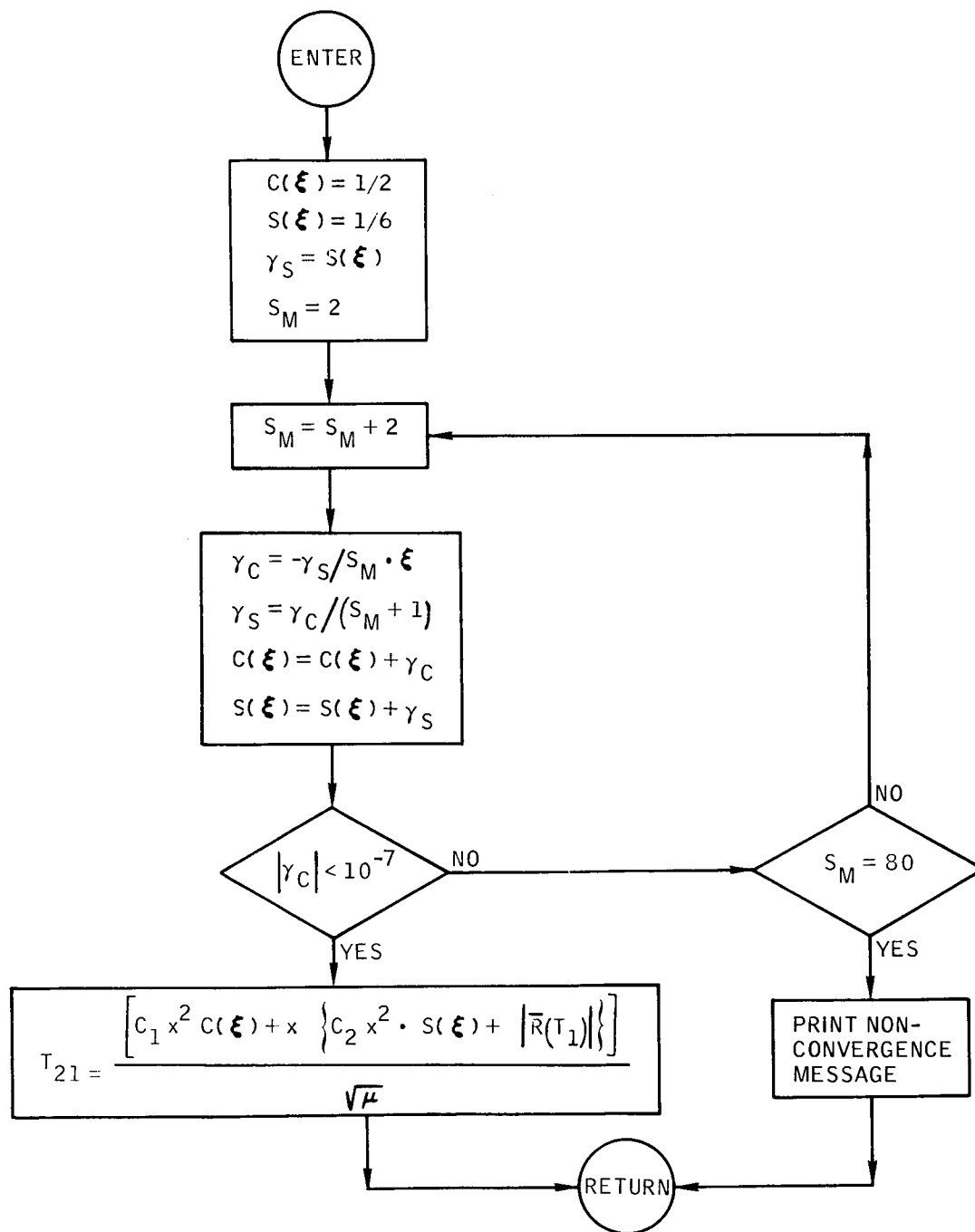


Figure B-50.- Flow chart of subroutine KEP.

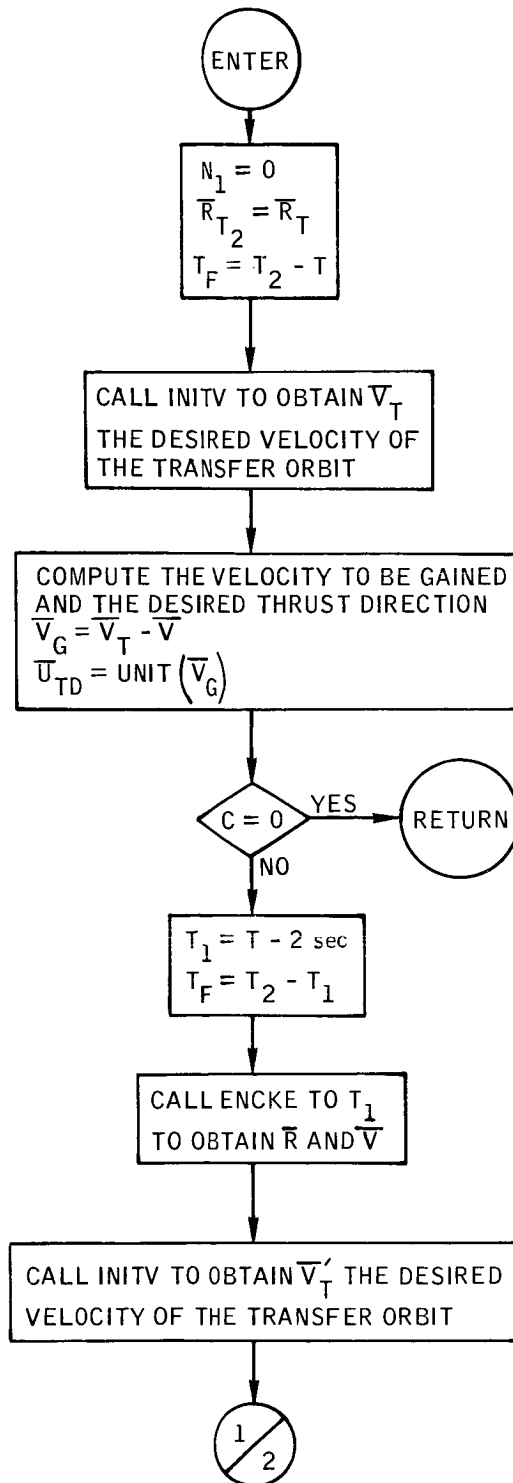


Figure B-51.- Flow chart of subroutine LAMAIM.

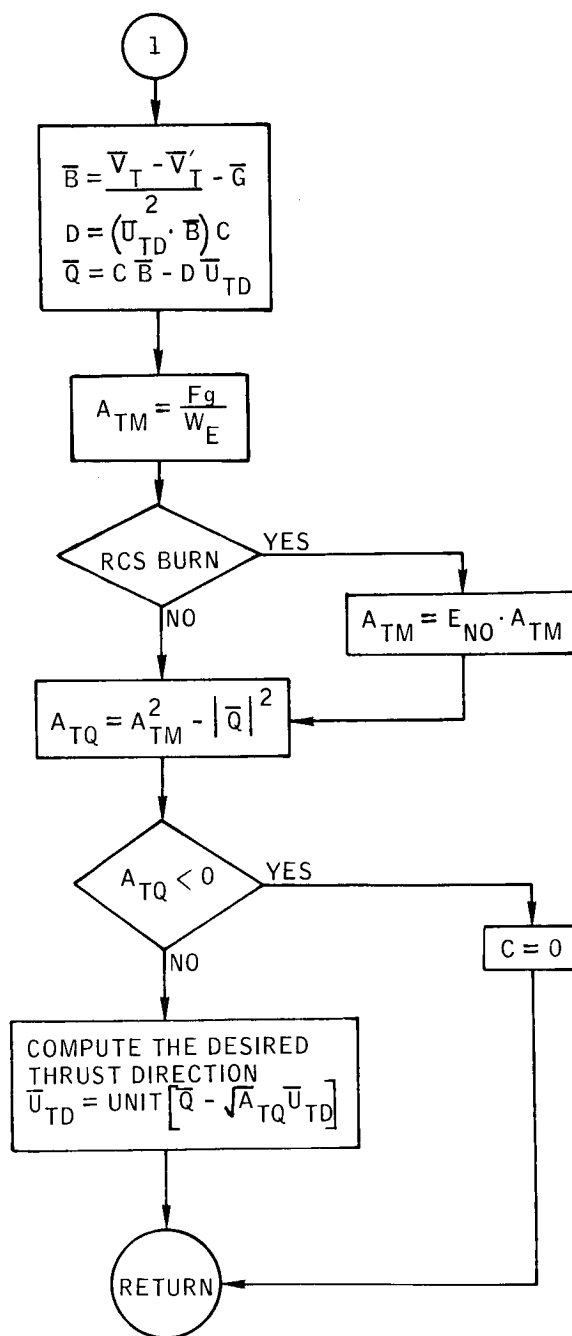


Figure B-51.- Concluded.

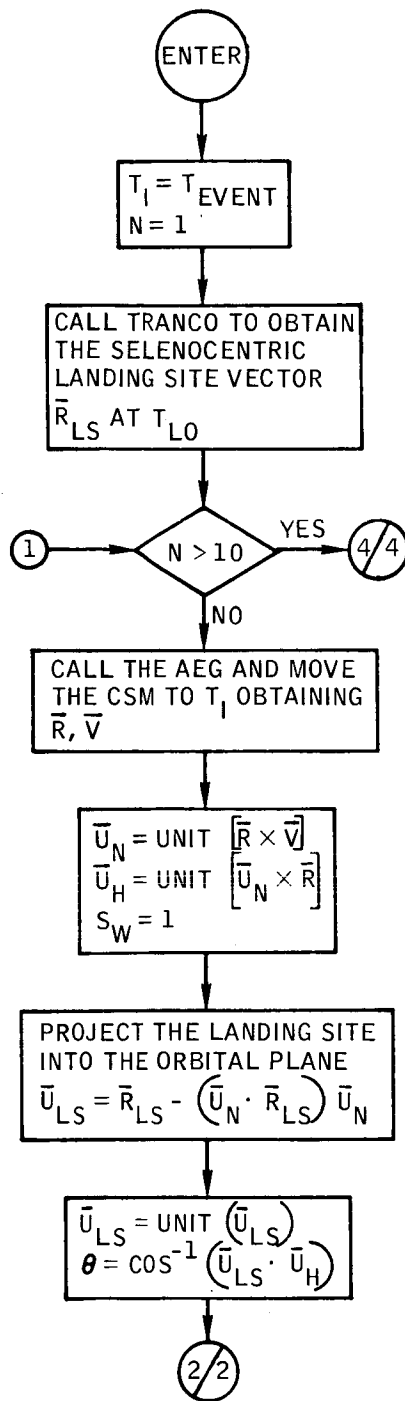


Figure B-52.- Flow chart of subroutine LOPC.



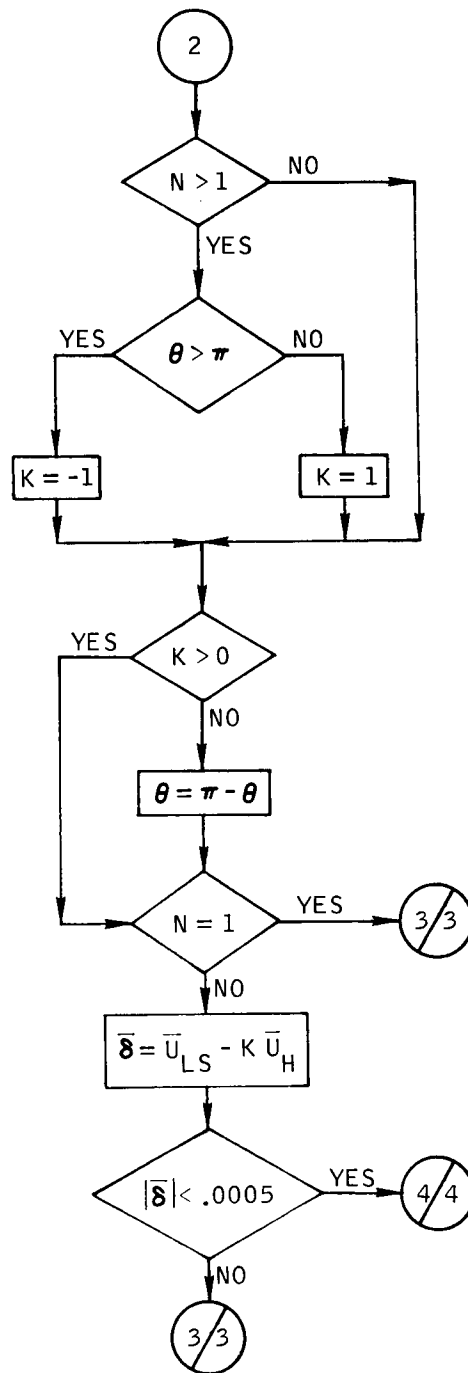


Figure B-52.- Continued.

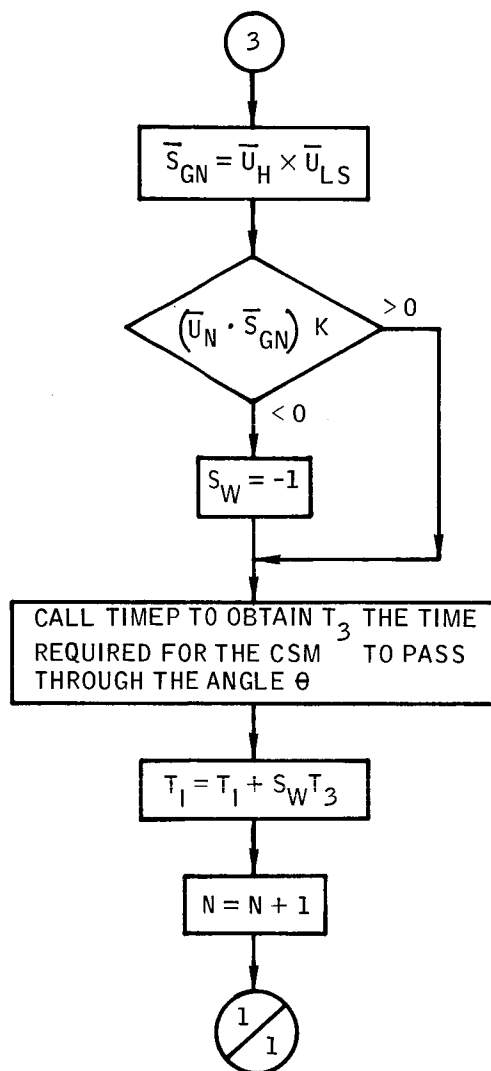


Figure B-52.- Continued.

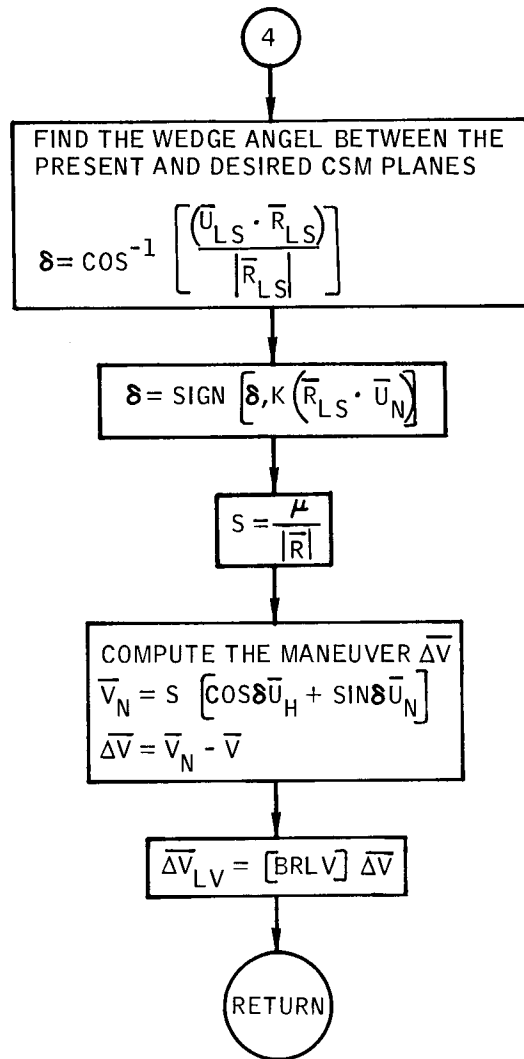


Figure B-52.- Concluded.

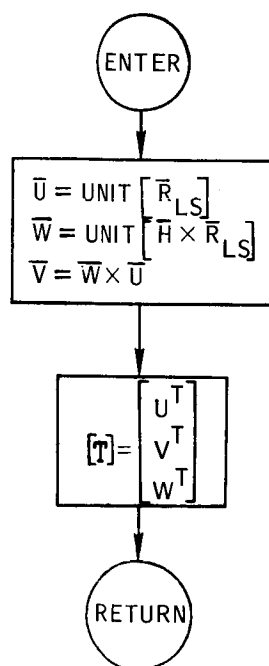


Figure B-53.- Flow chart of subroutine LSALGN.

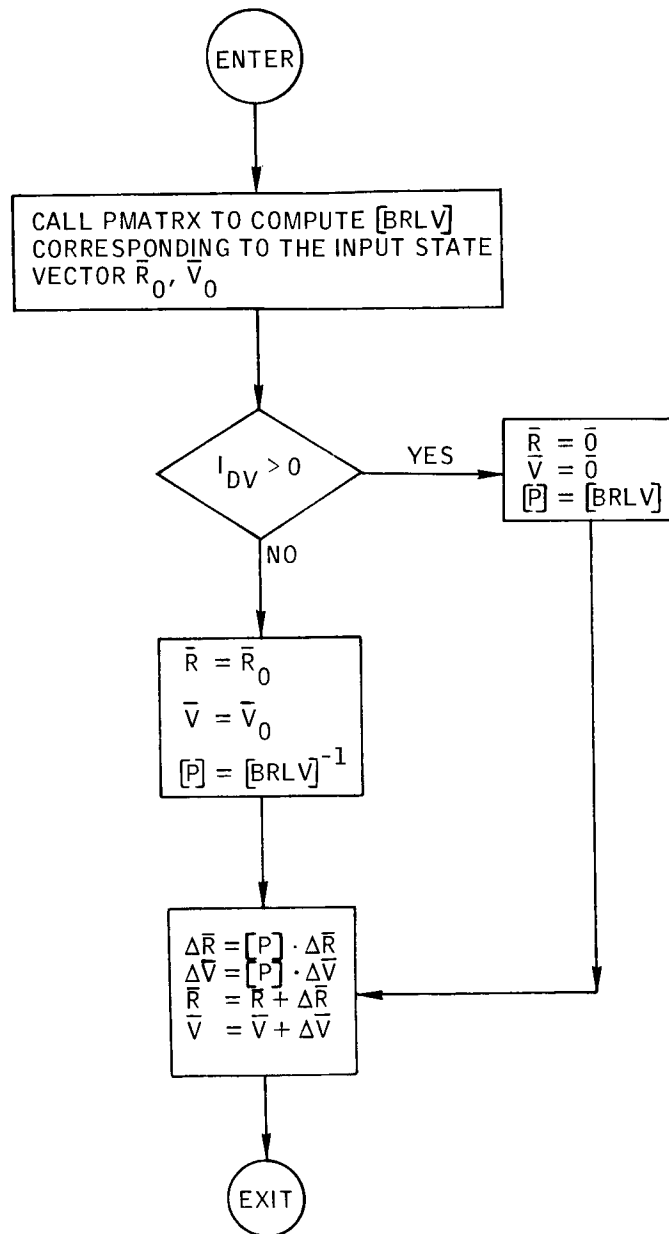


Figure B-54.- Flow chart of subroutine LVLHDX.

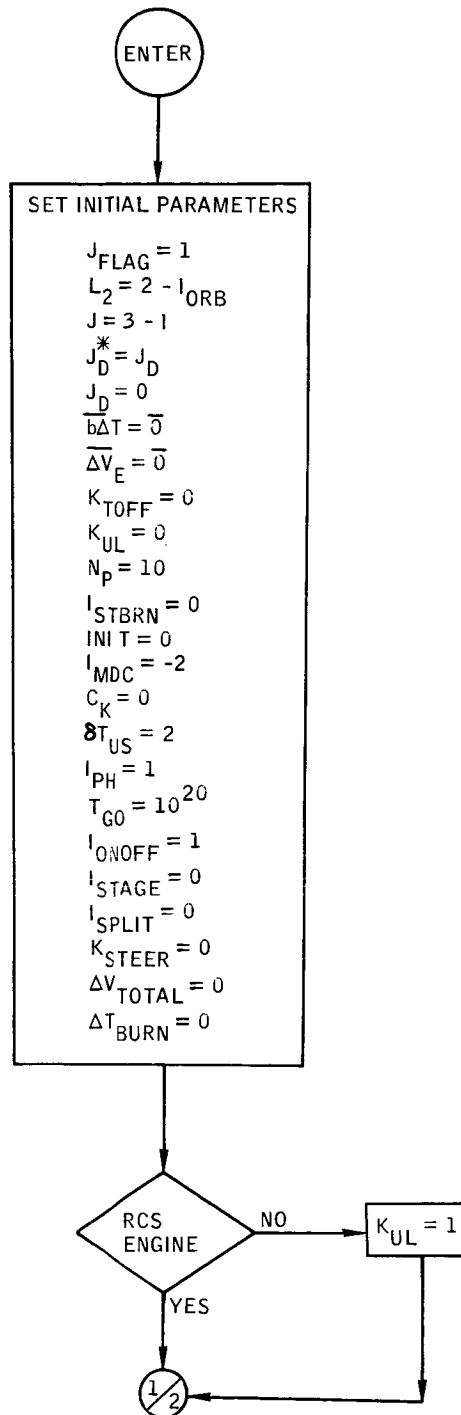


Figure B-55.- Flow chart of subroutine MANEUV.

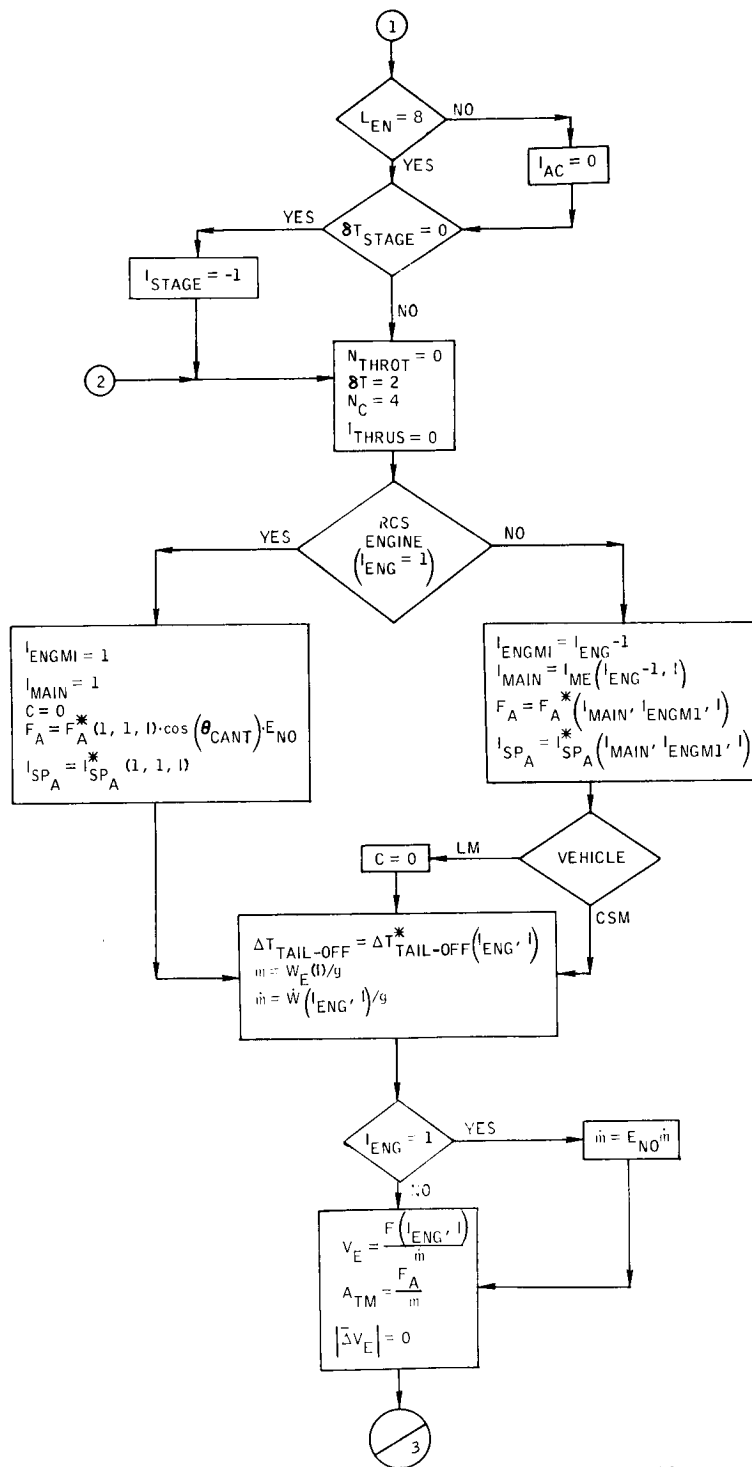


Figure B-55. - Continued.

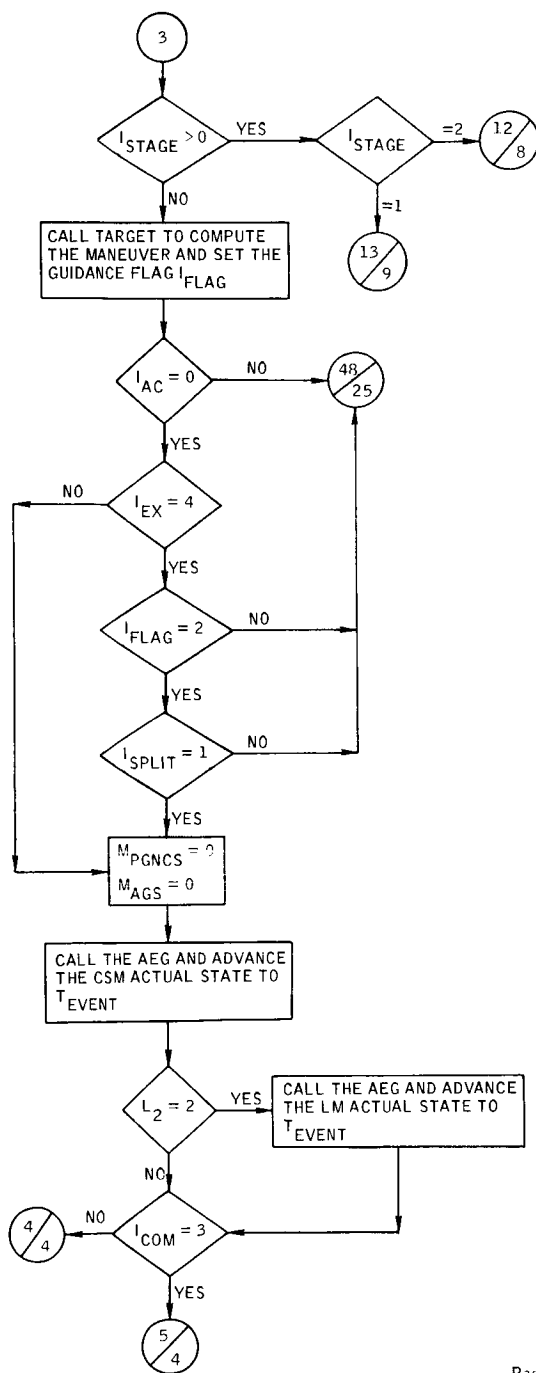


Figure B-55. - Continued.



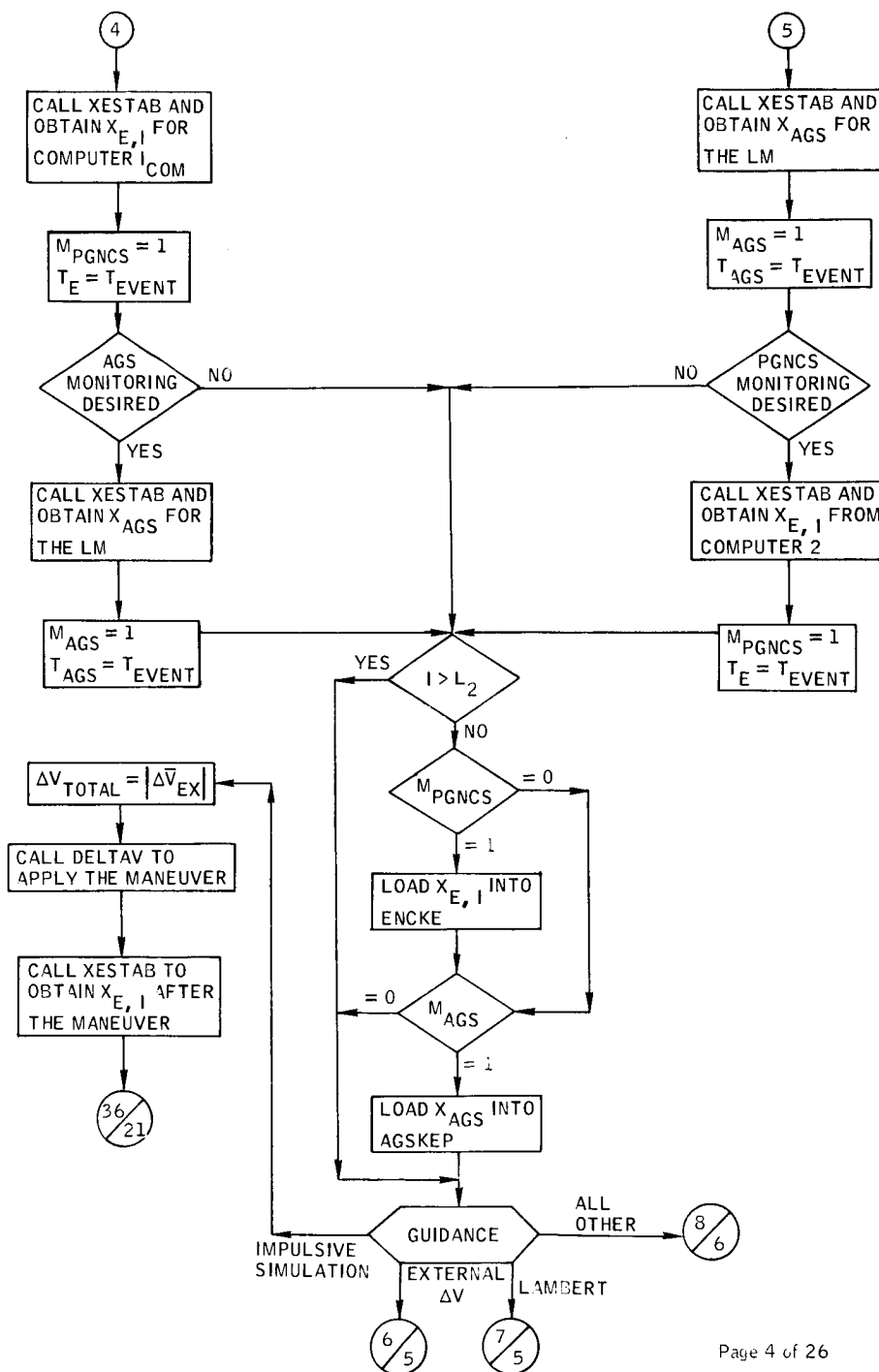


Figure B-55. - Continued.

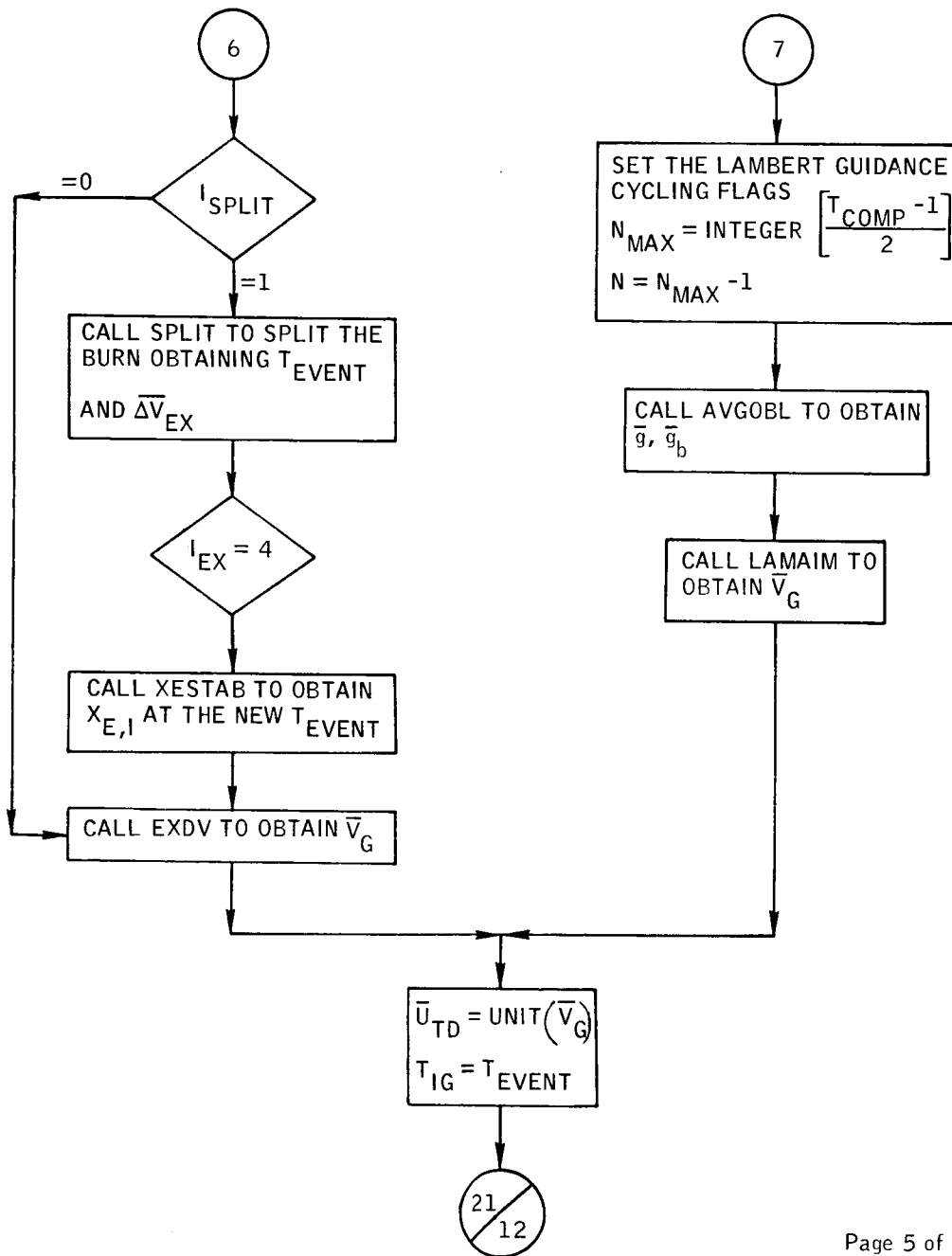


Figure B-55. - Continued.

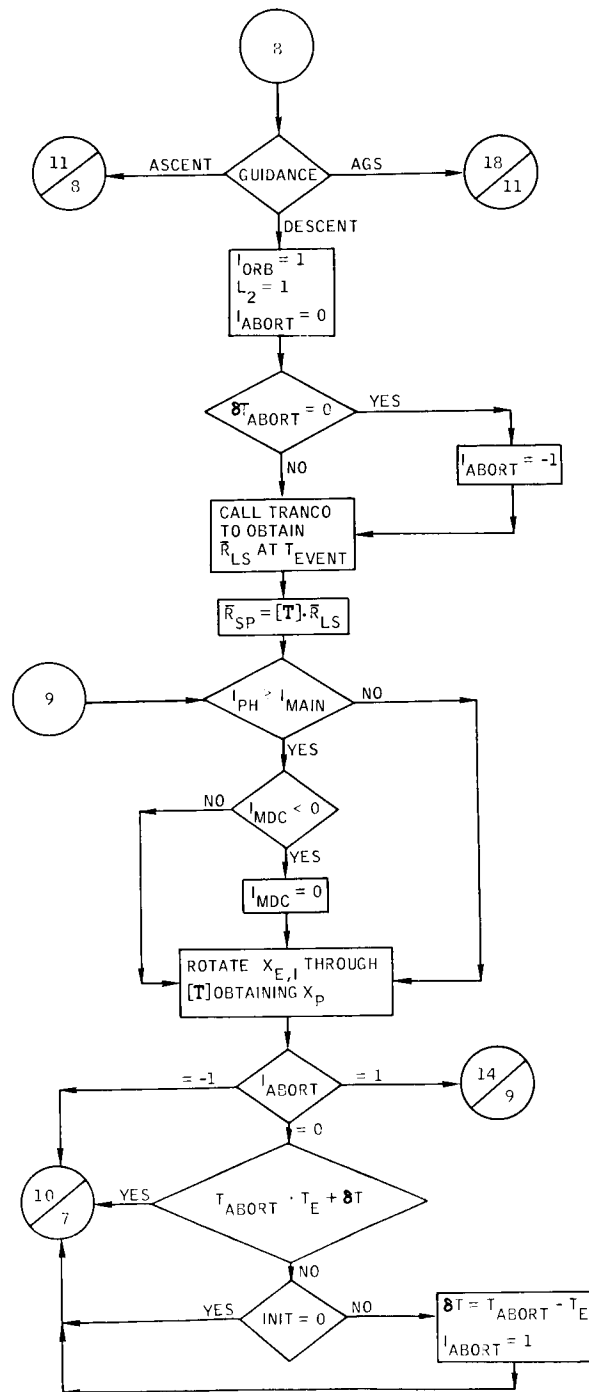


Figure B 55. - Continued.

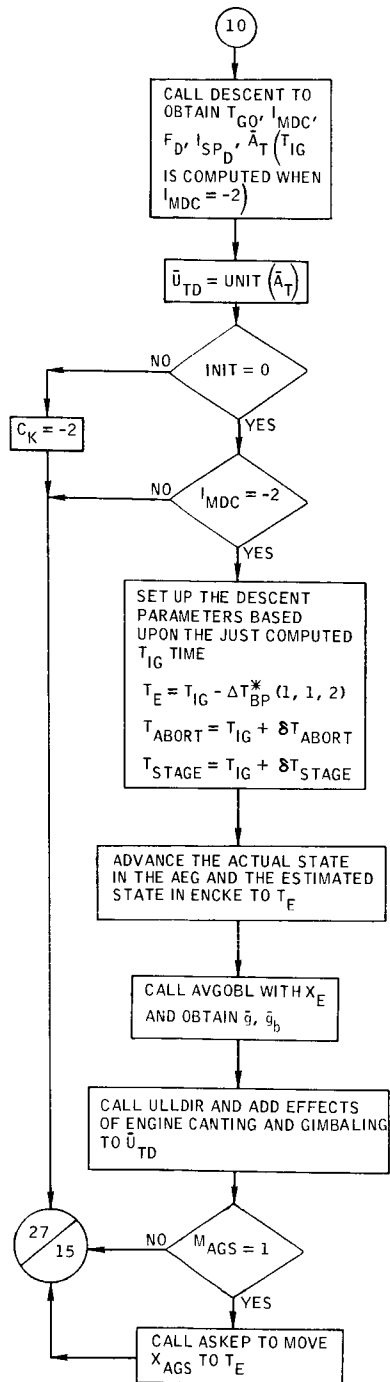


Figure B-55. - Continued.

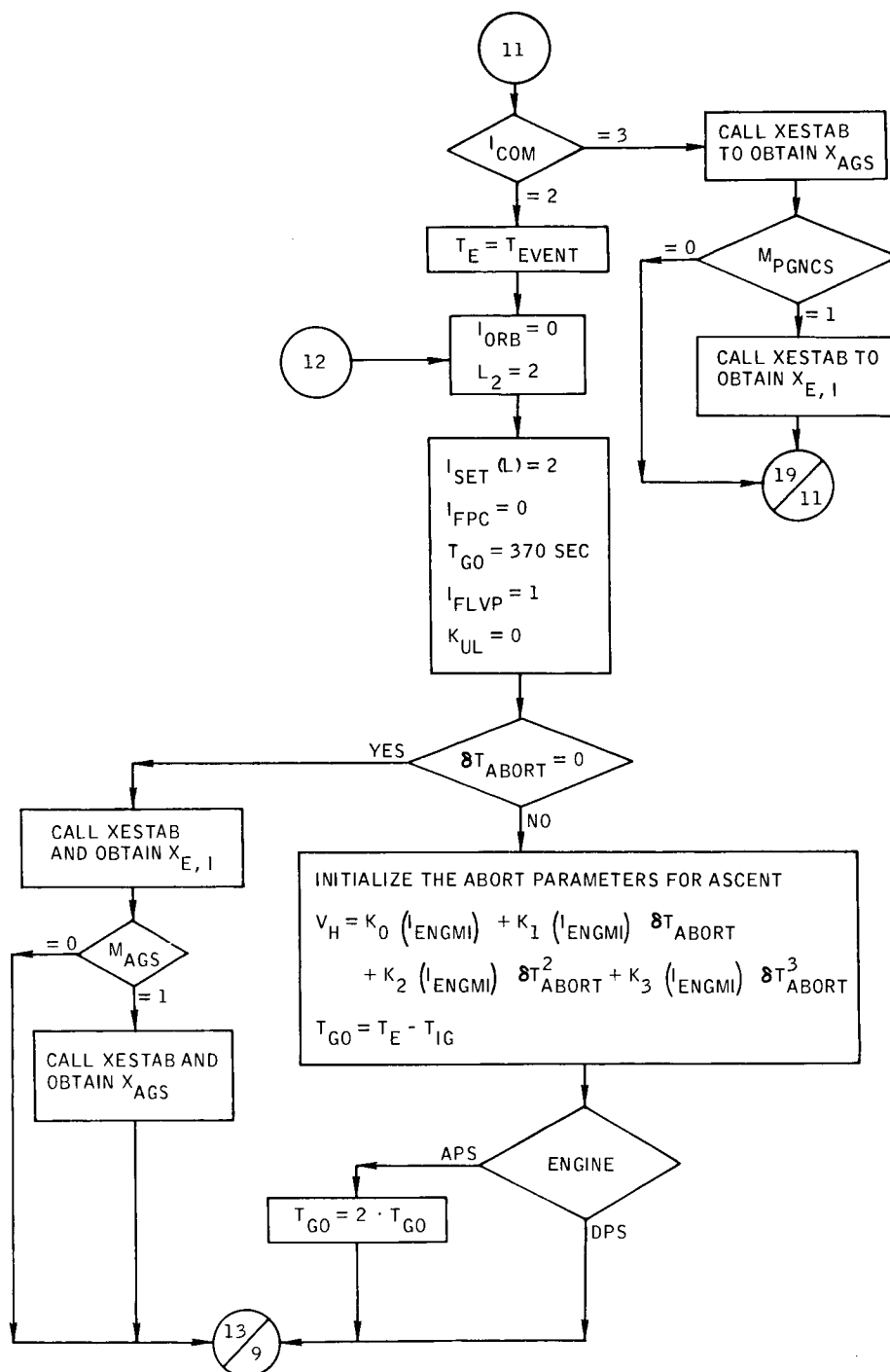


Figure B-55. - Continued.

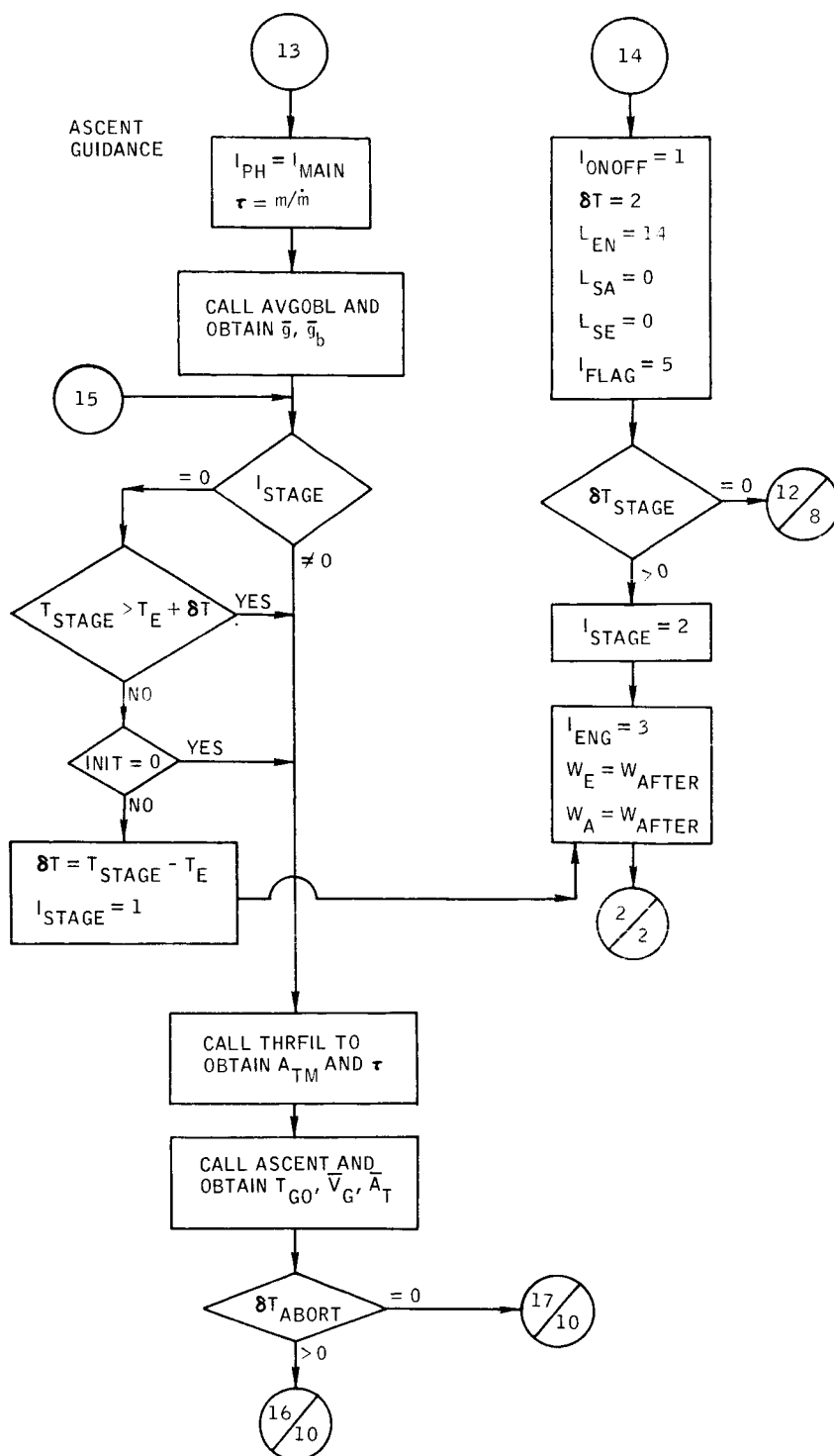


Figure B-55. - Continued.

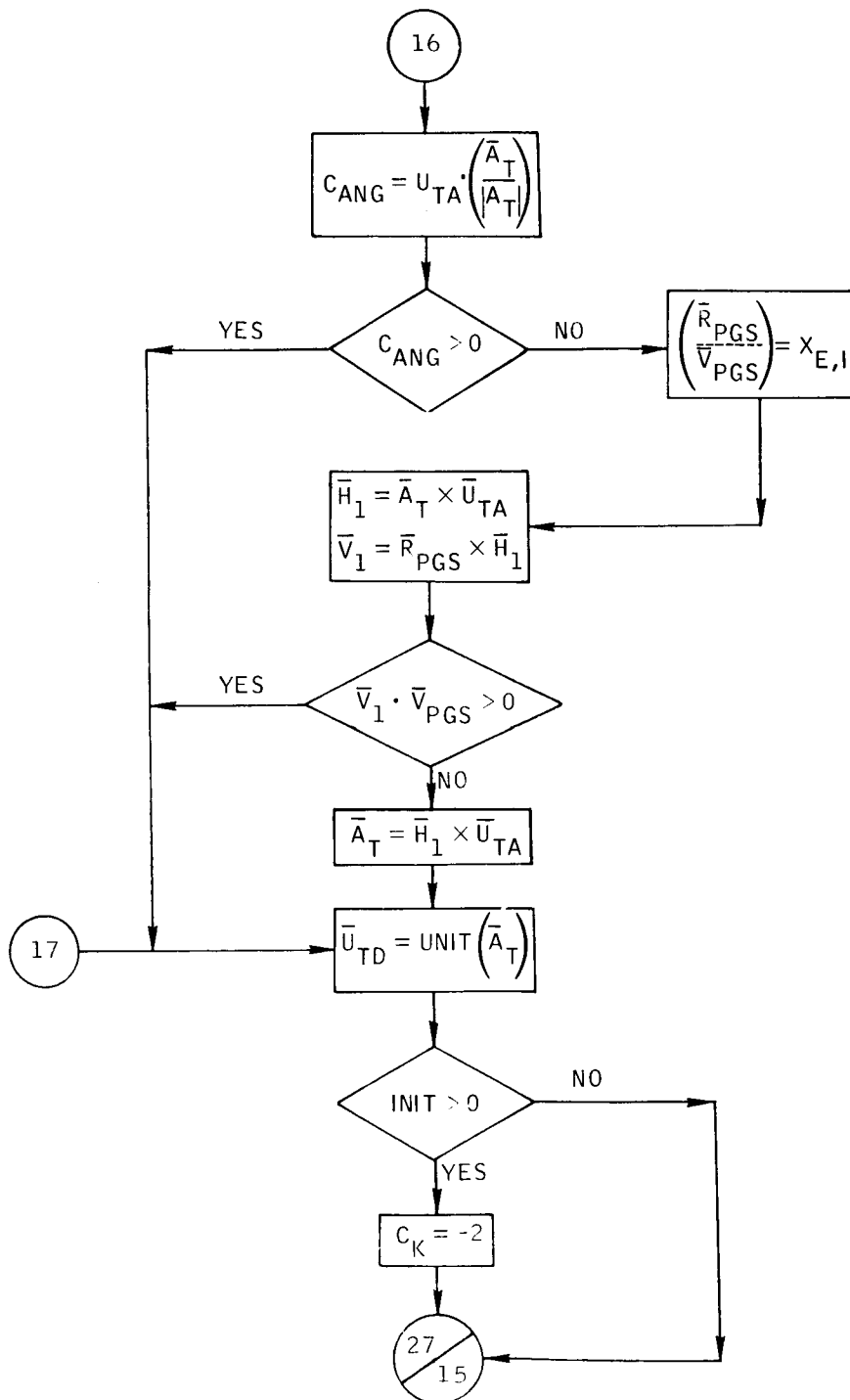


Figure B-55. - Continued.

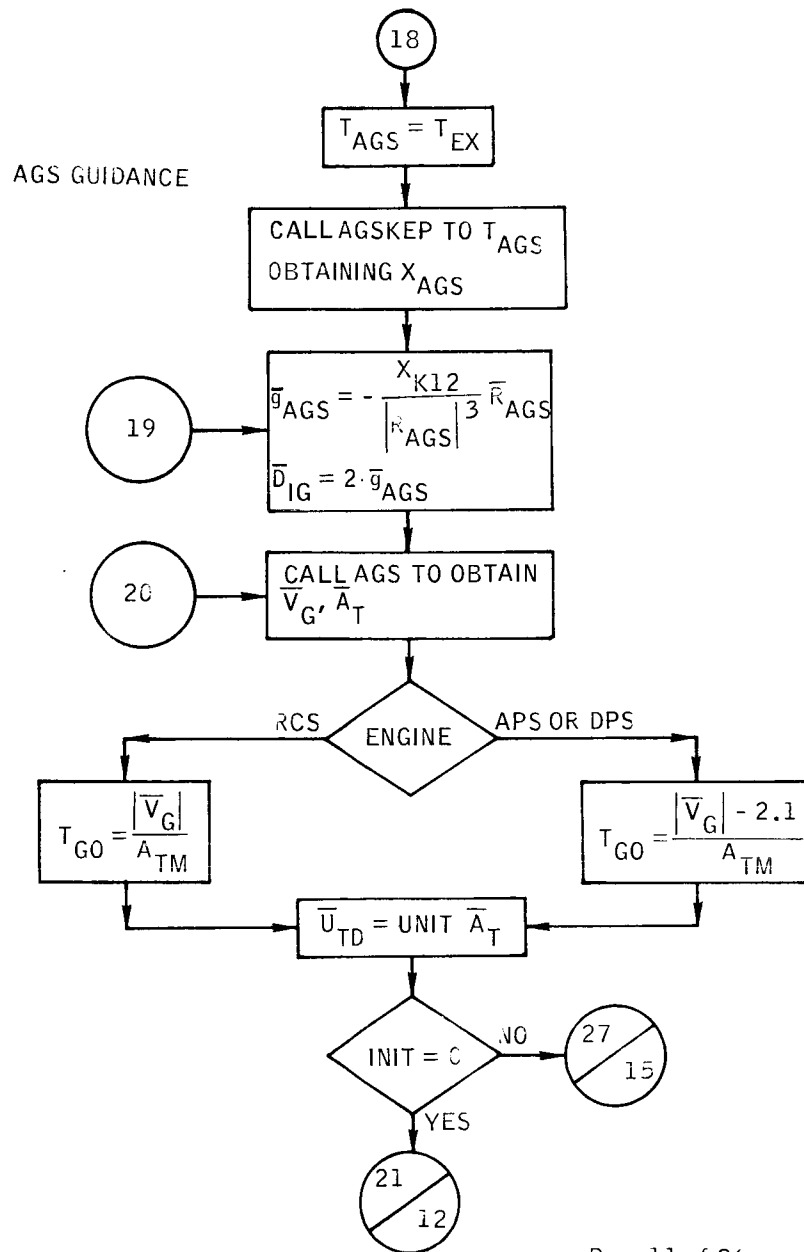


Figure B-55. - Continued.



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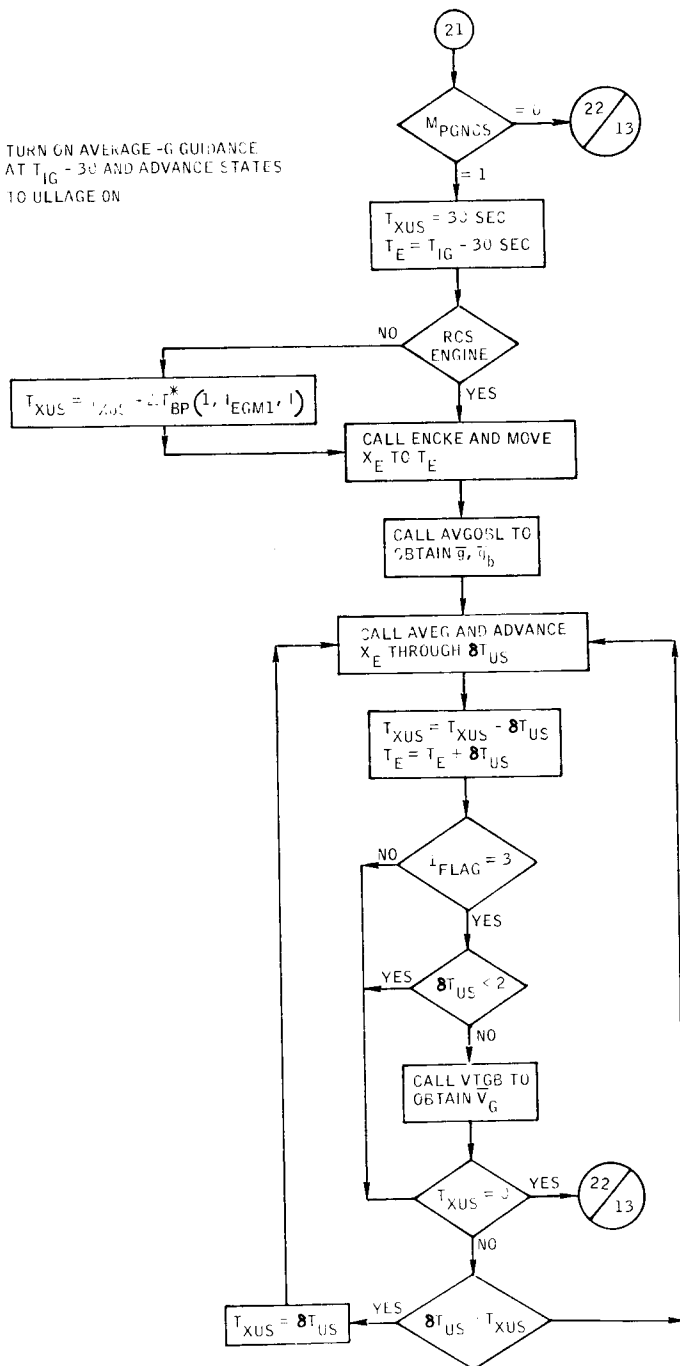


Figure B 55. - Continued.

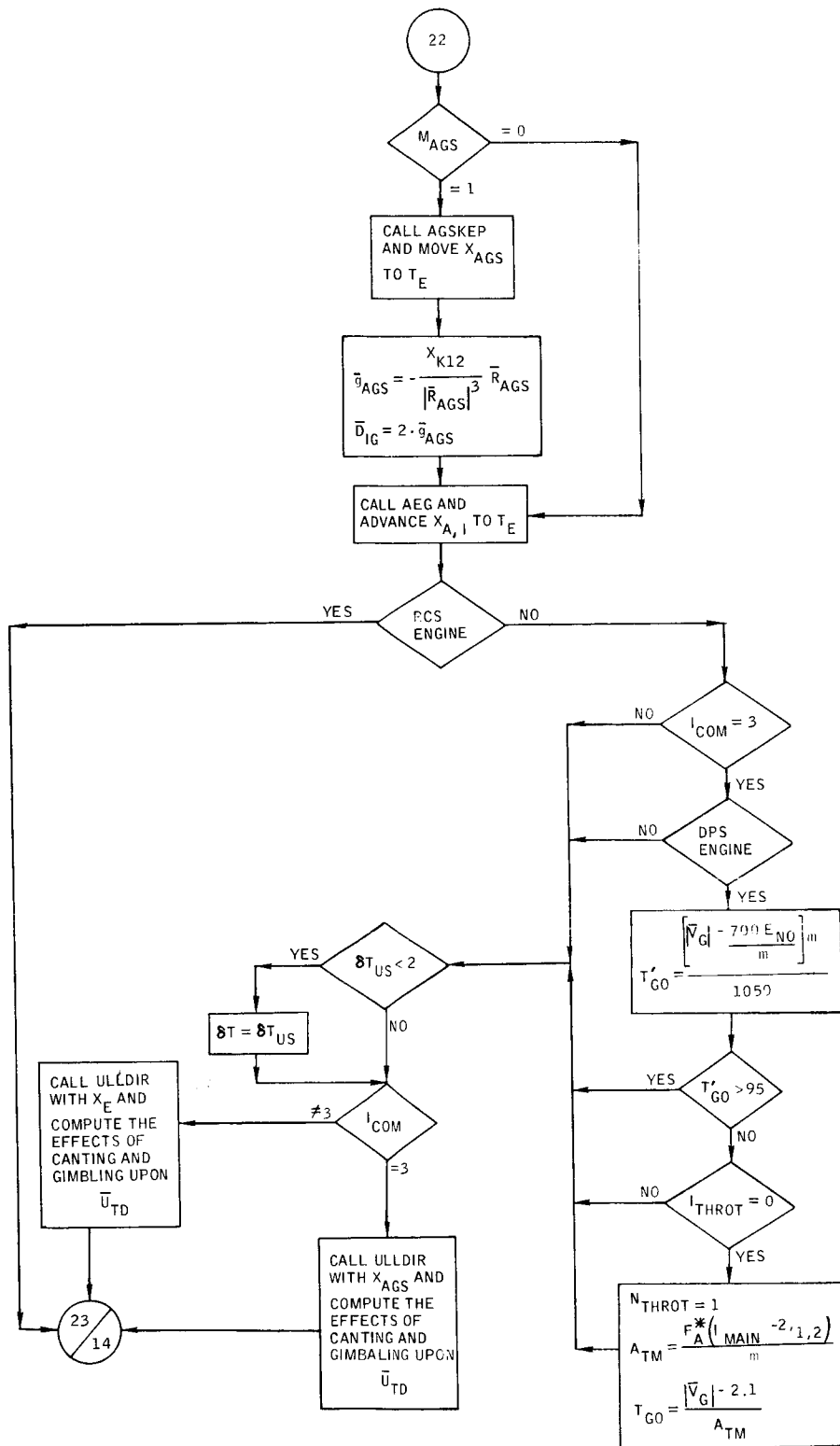


Figure B-55. - Continued.

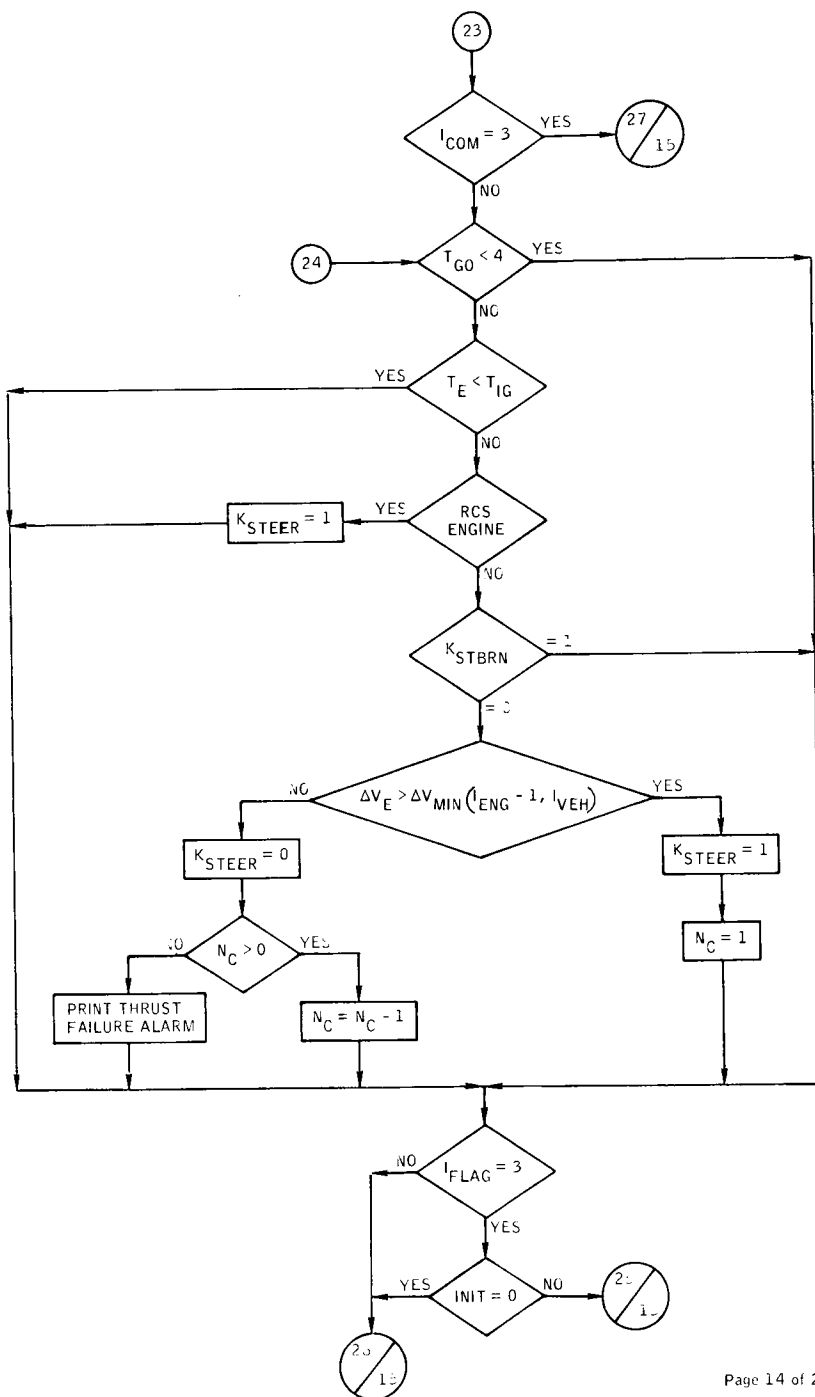


Figure B-55.- Continued.

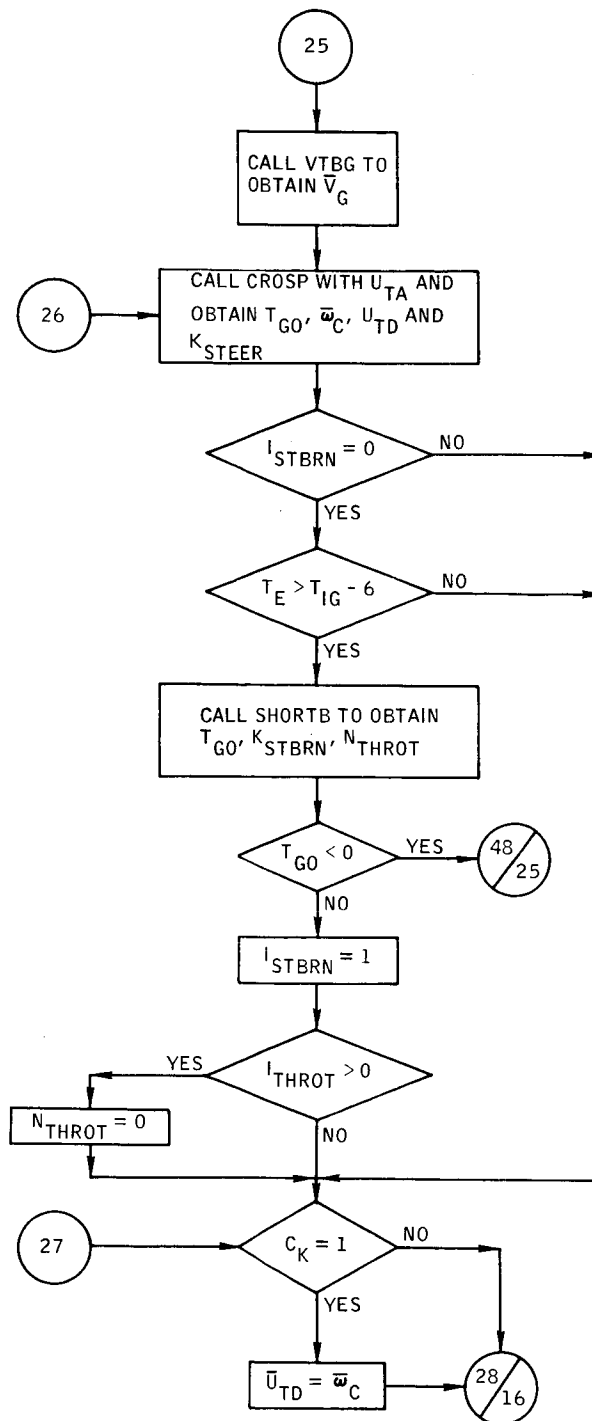


Figure B-55. - Continued.

SIMULATE EFFECTS OF PLATFORM  
MISALIGNMENT ERRORS ON THE  
COMMANDED THRUST DIRECTION

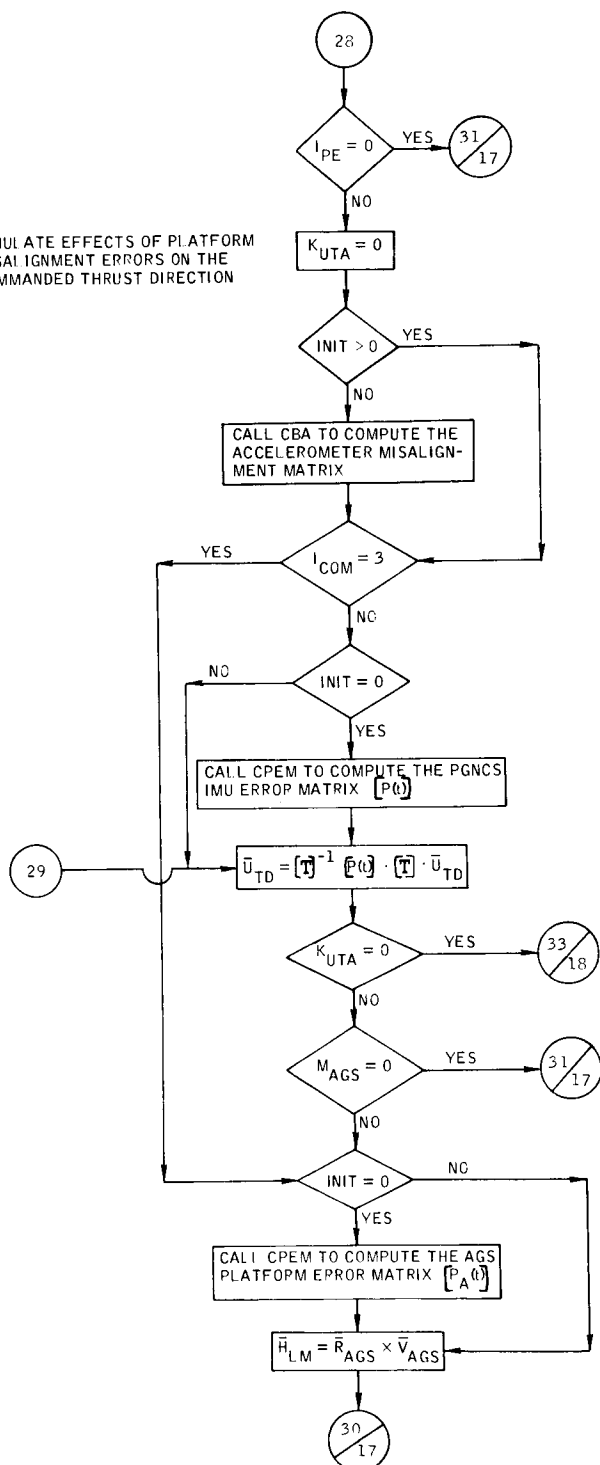


Figure B-55.- Continued.

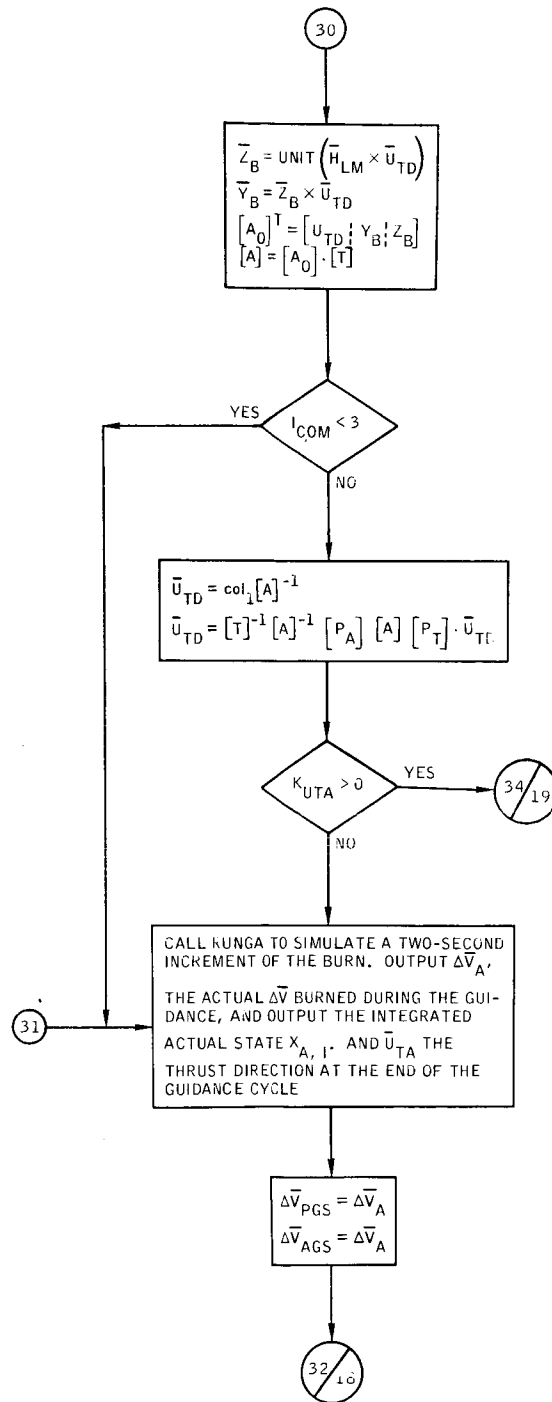


Figure B-55. - Continued.

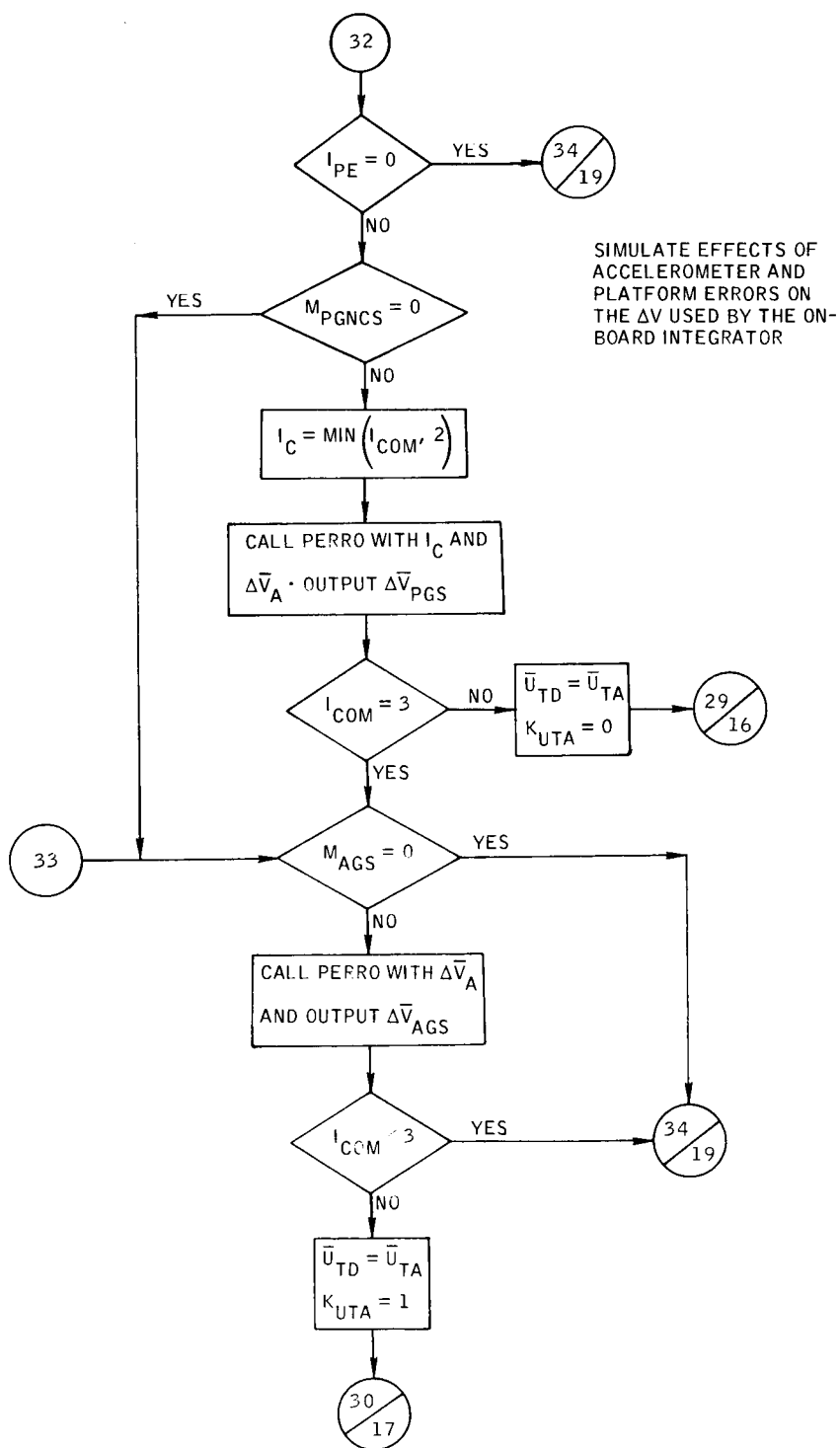


Figure B-55. - Continued.

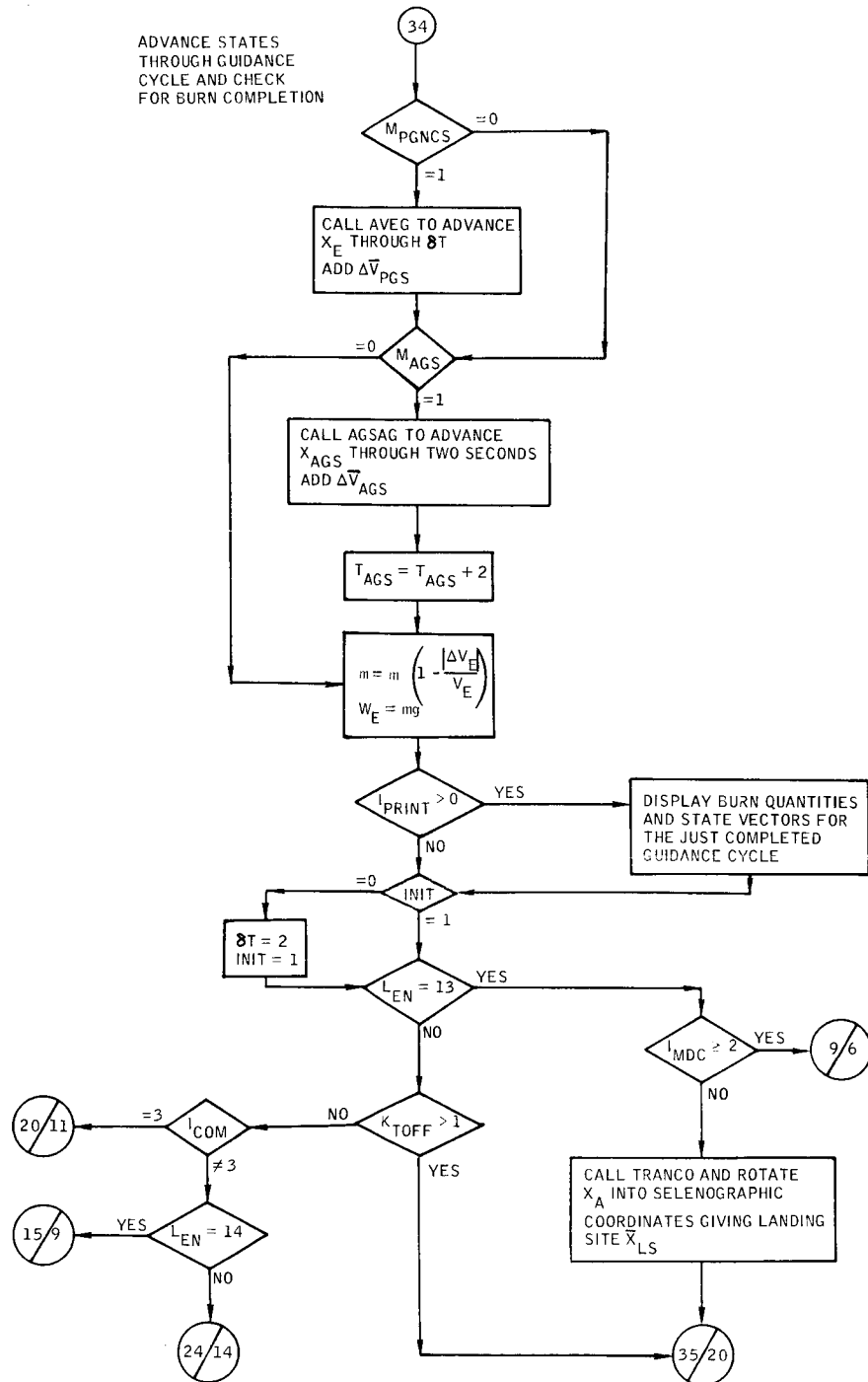


Figure B-55. - Continued.



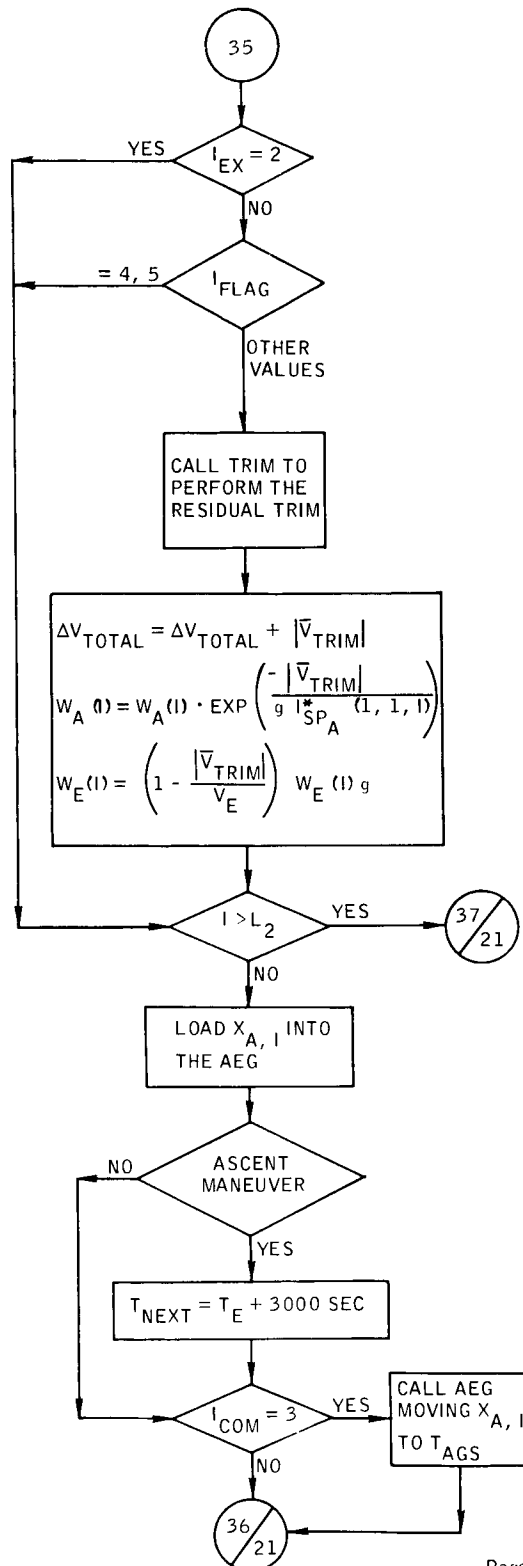


Figure B-55.- Continued.

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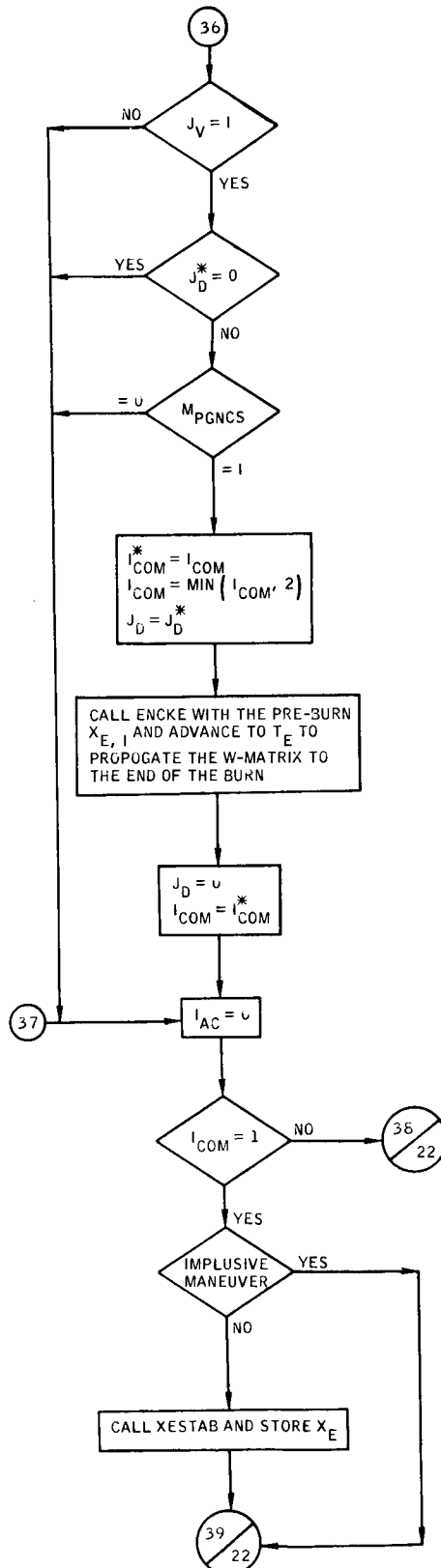


Figure B-55. - Continued.

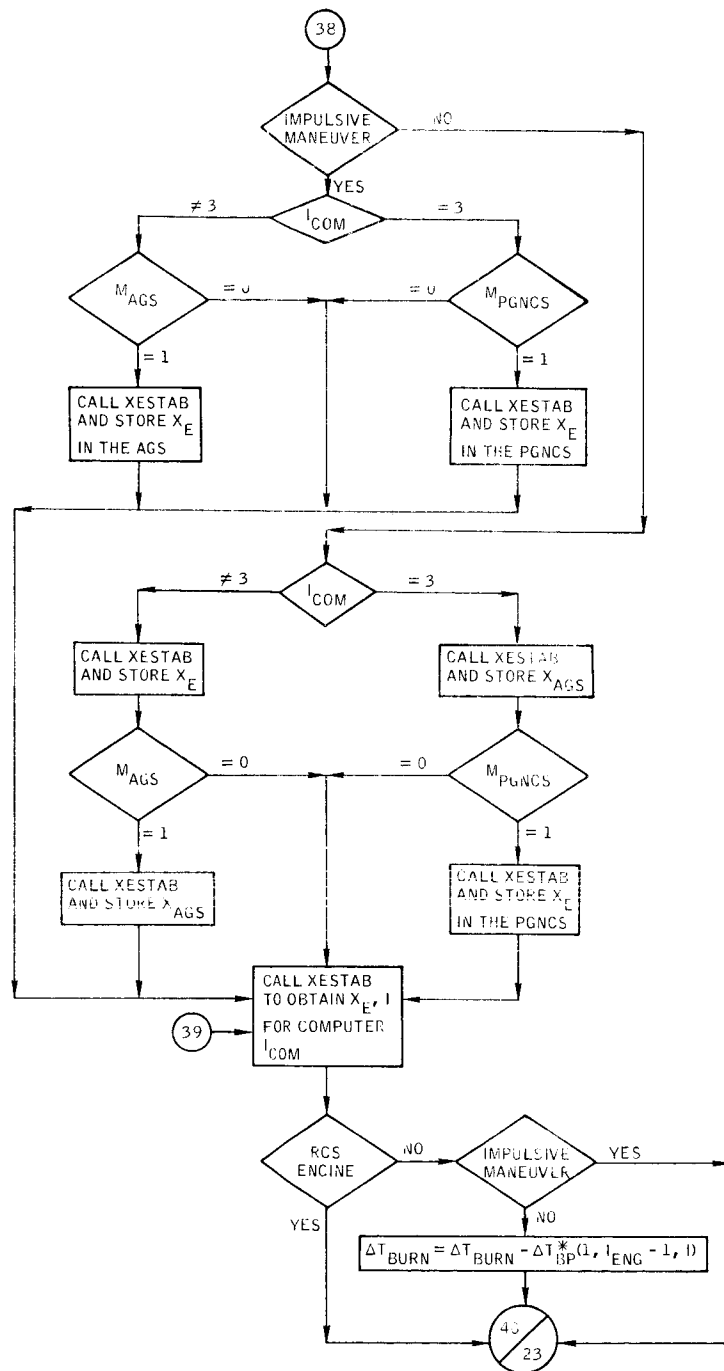


Figure B-55. - Continued.

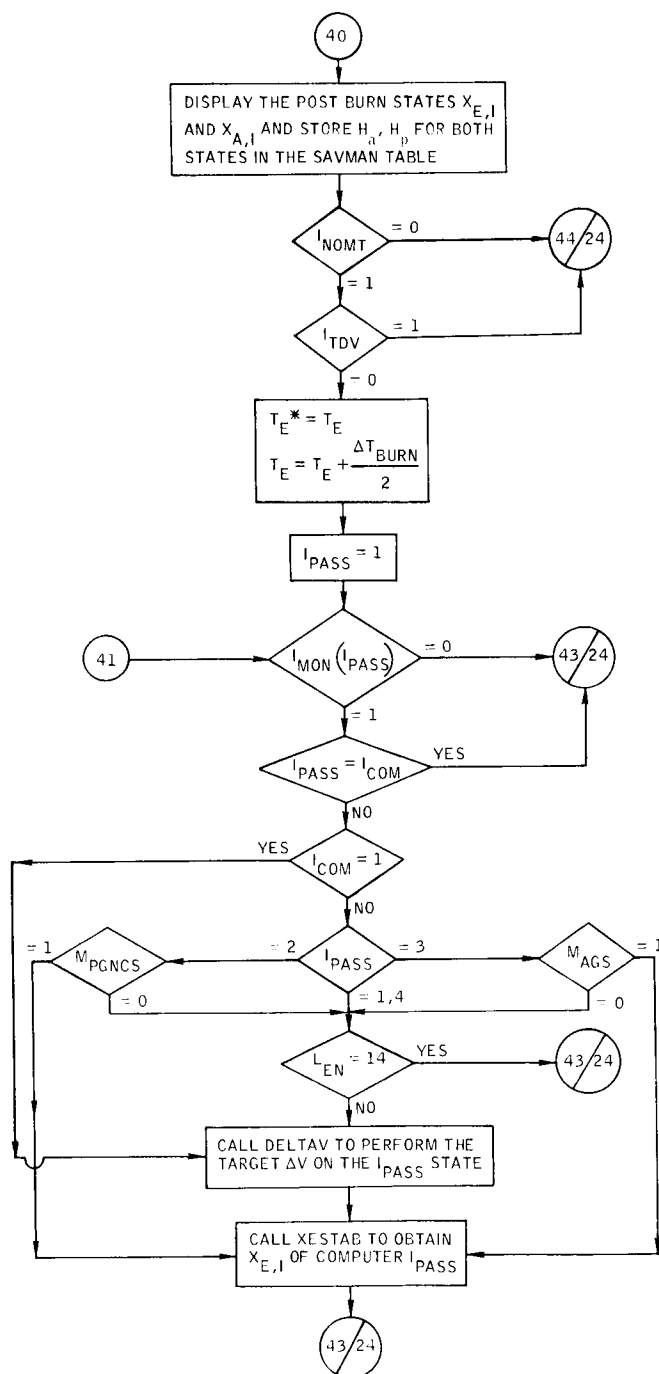


Figure B-55. - Continued.

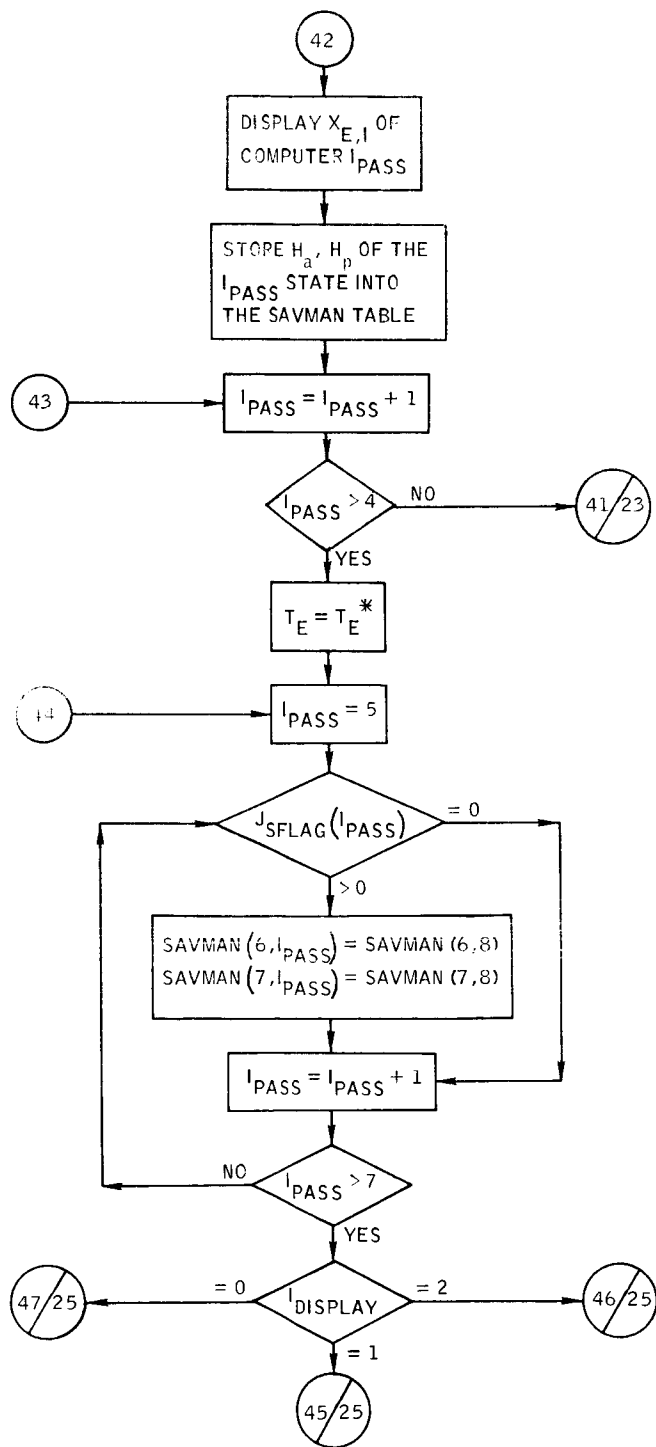


Figure B-55. - Continued.

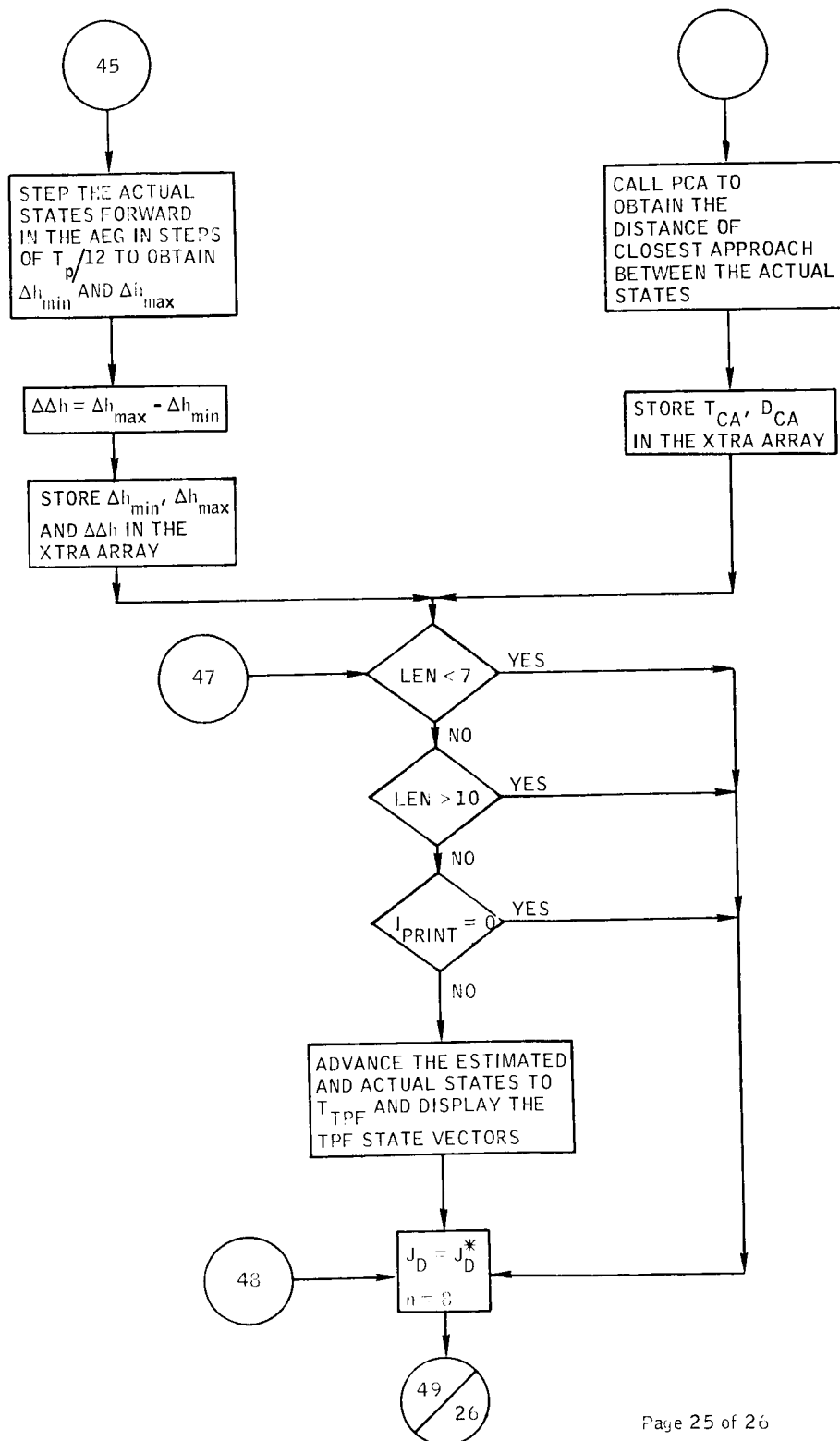
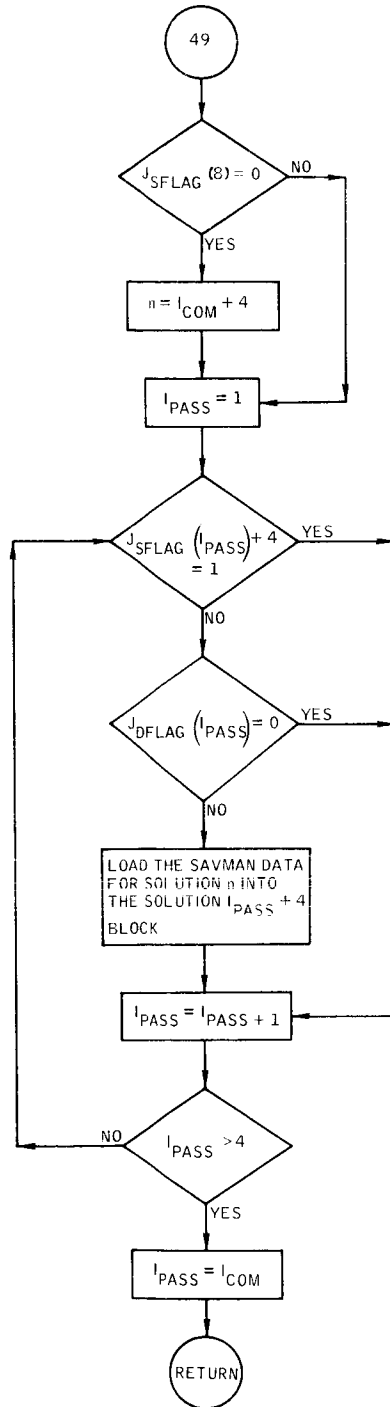


Figure B-55, - Continued.





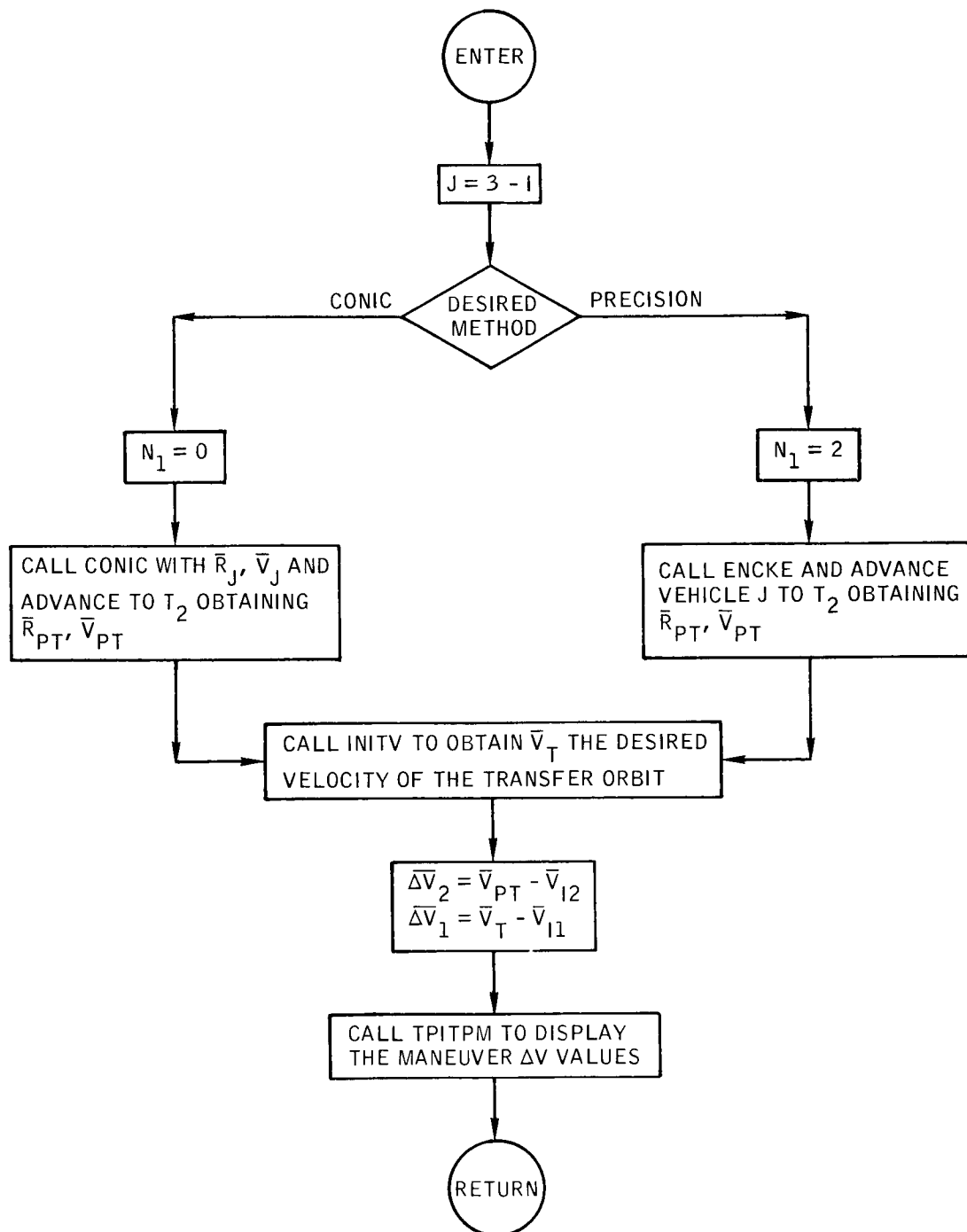


Figure B-56.- Flow chart of subroutine MIDCRS.

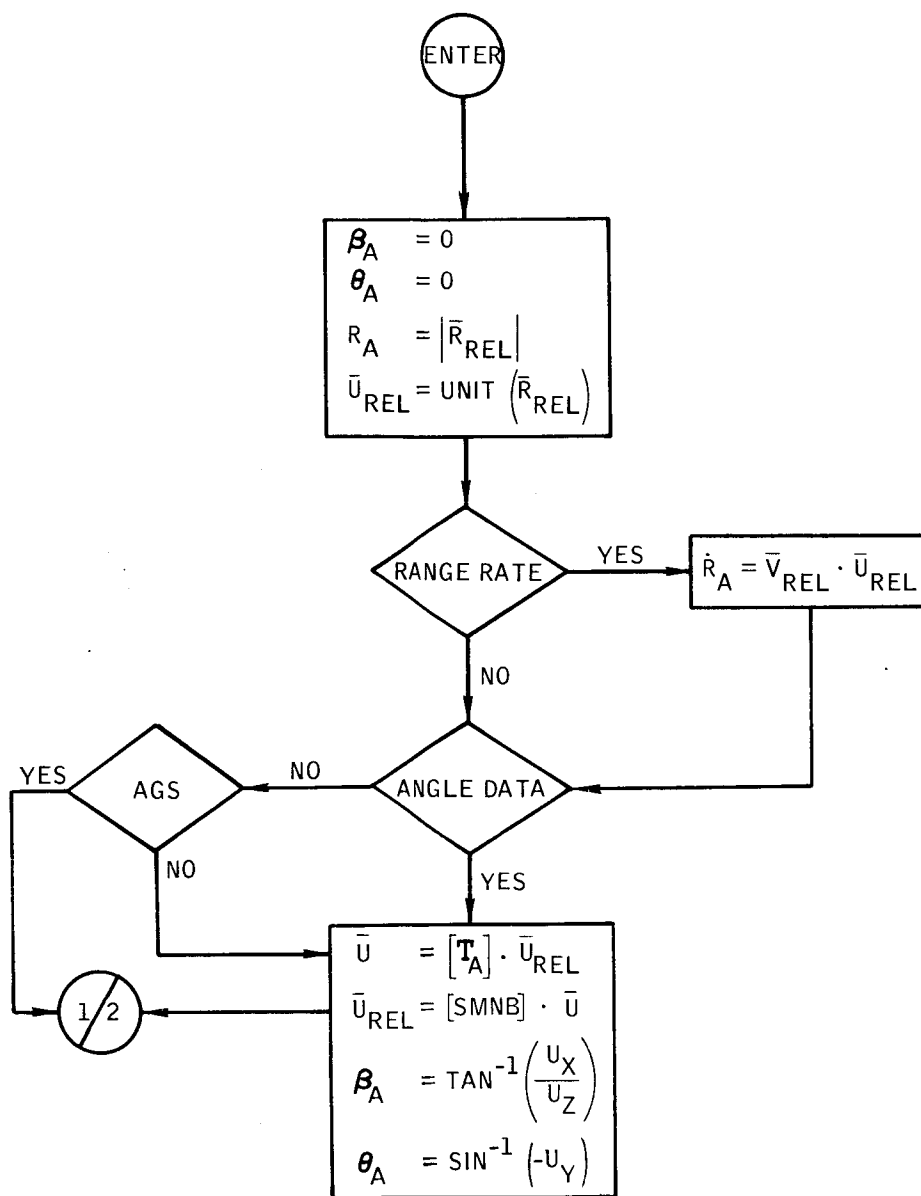


Figure B-57. - Flow chart of subroutine OBS.

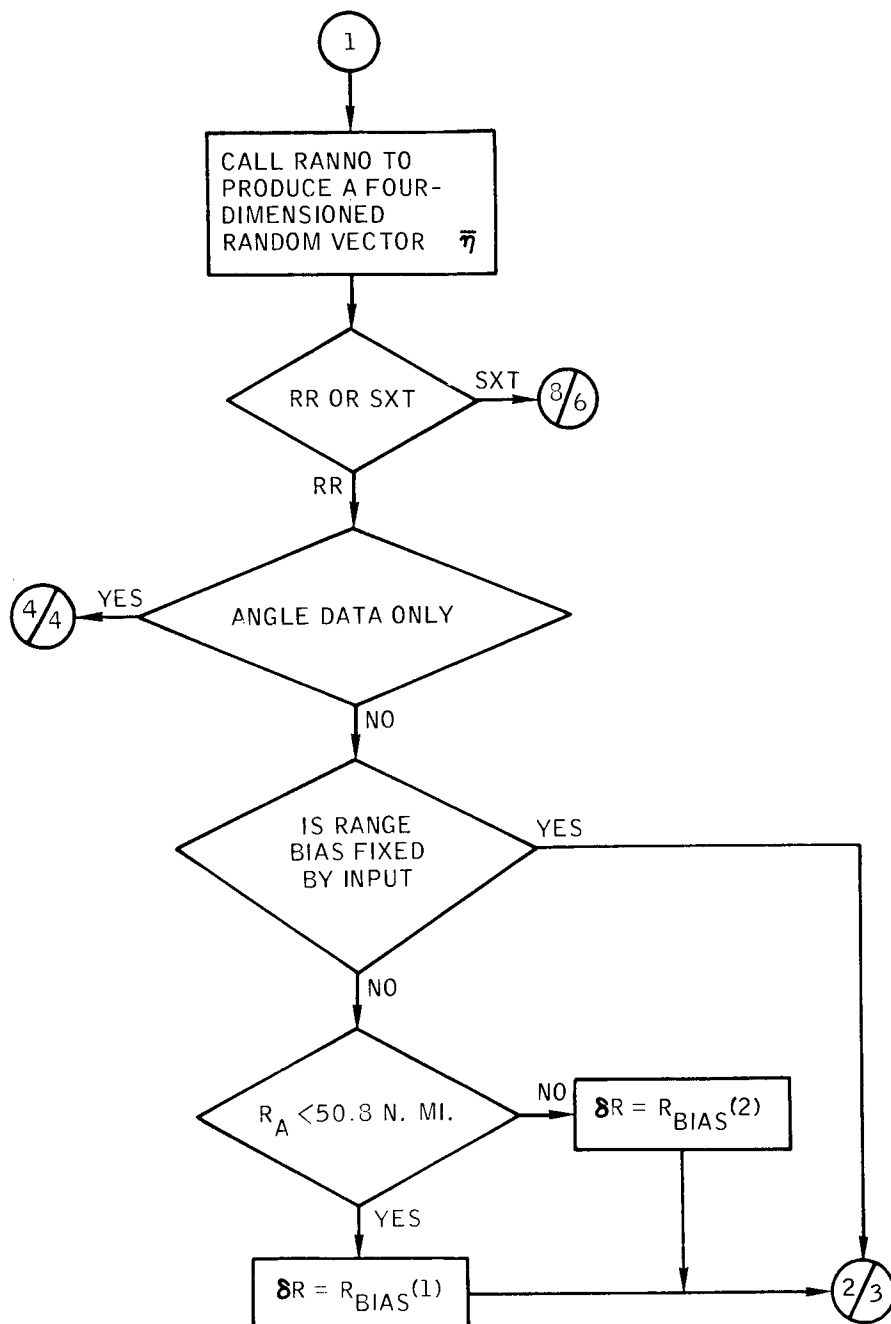


Figure B-57.- Continued.

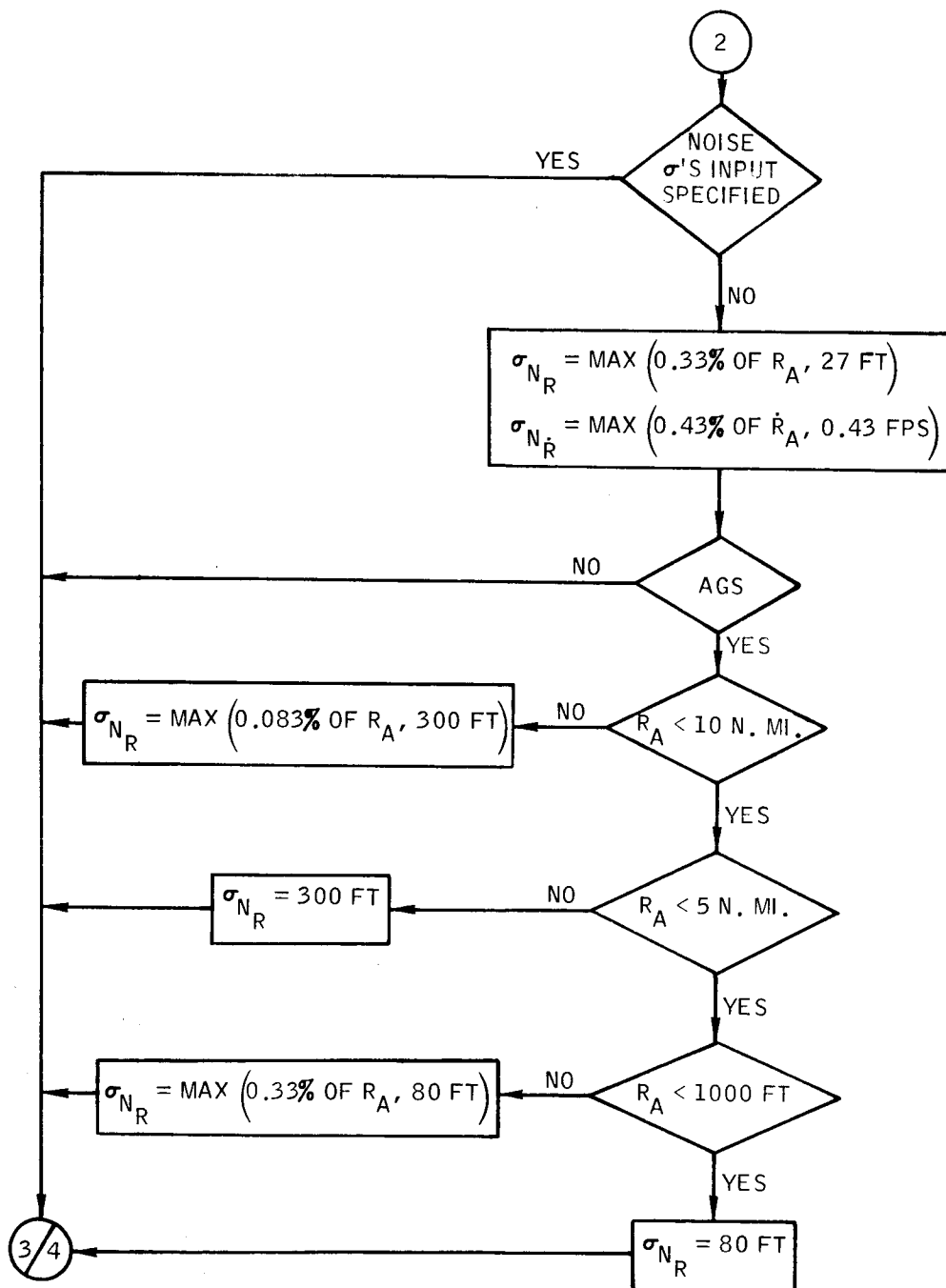


Figure B-57. - Continued.

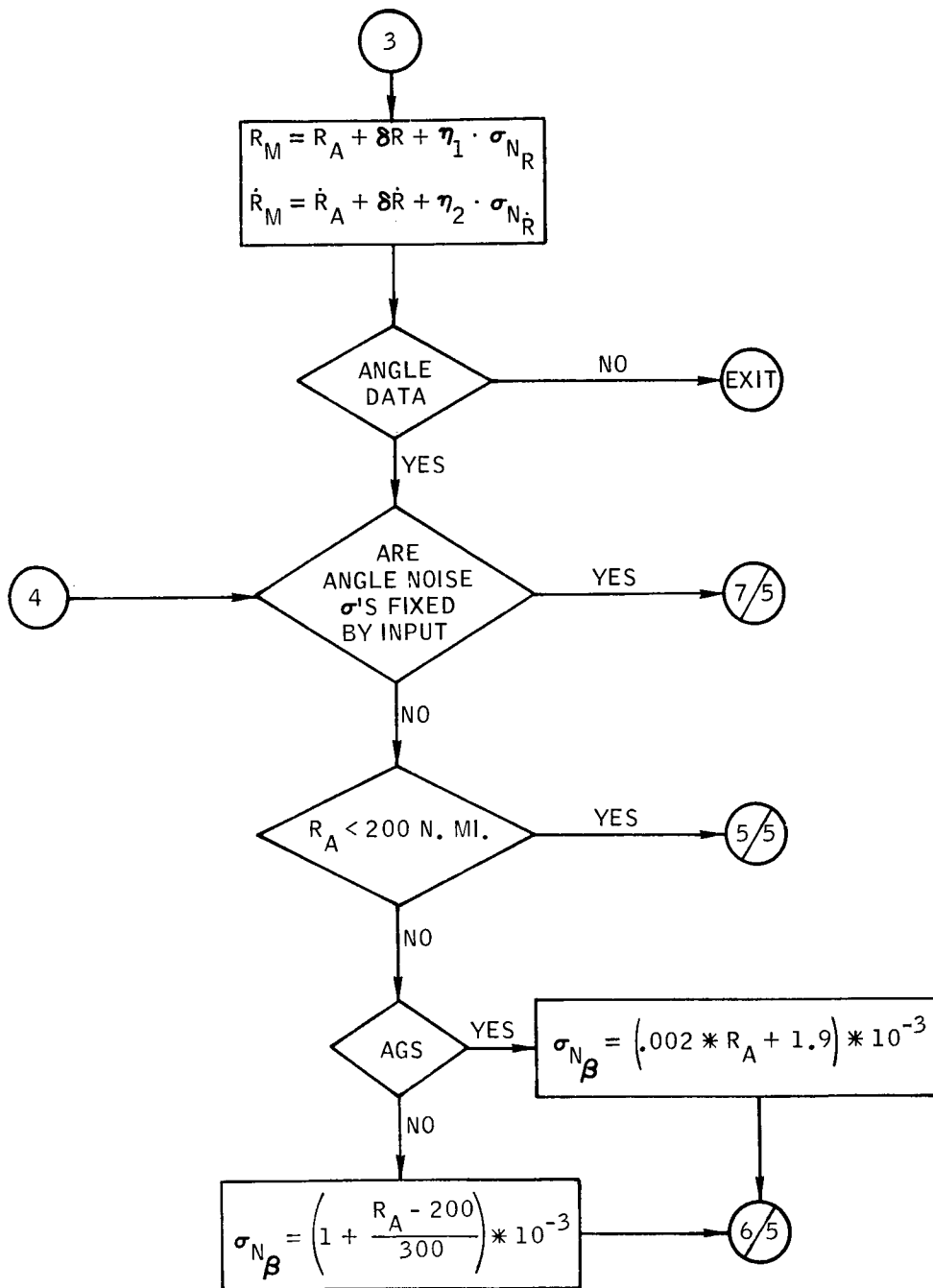


Figure B-57. - Continued.

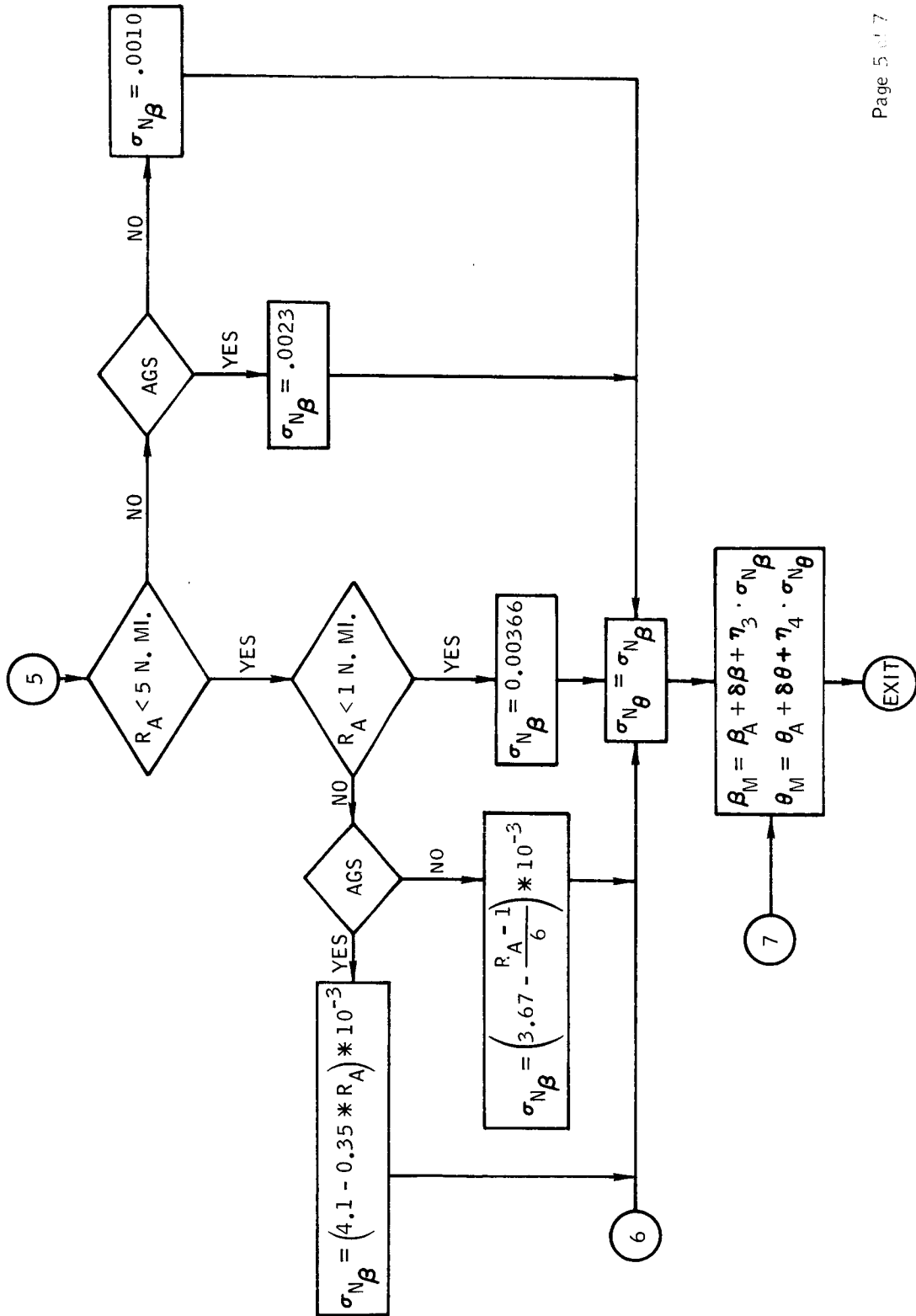


Figure B-57. - Continued.

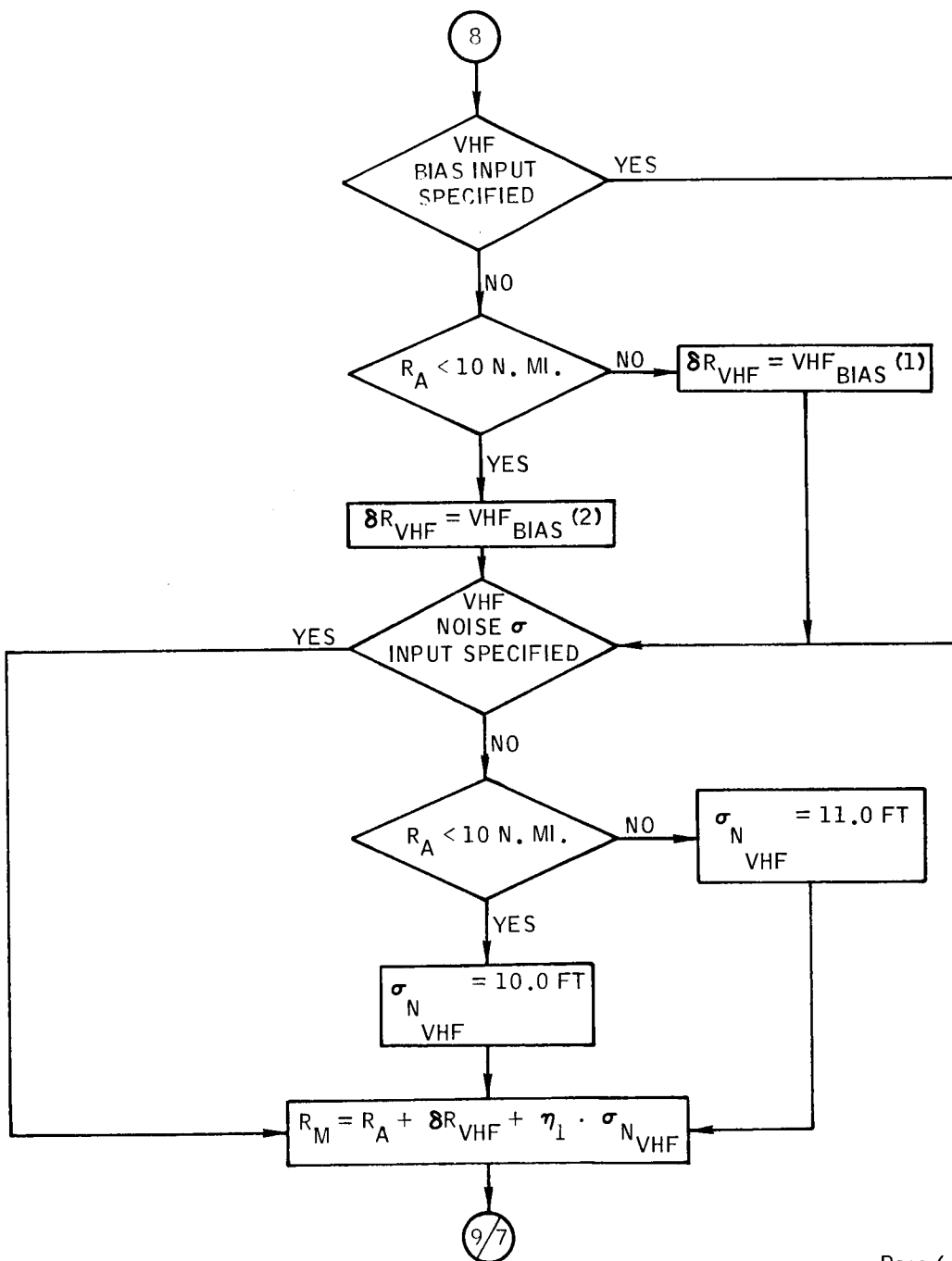


Figure B-57. - Continued.

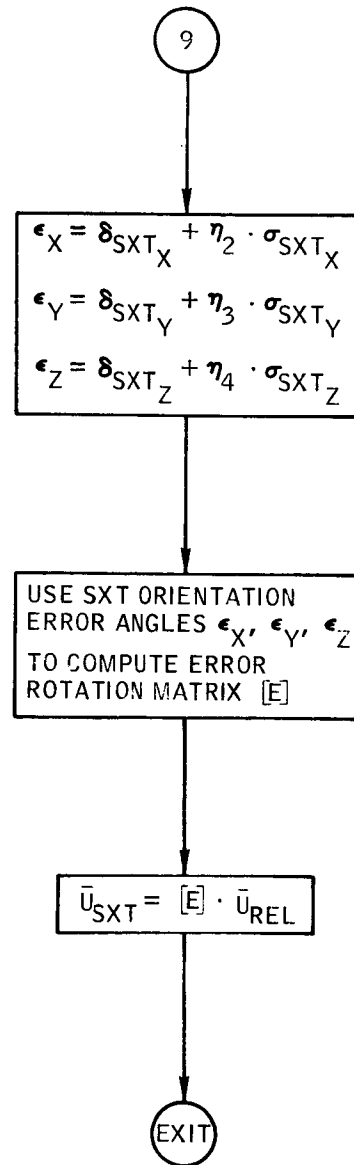


Figure B-57.- Concluded.



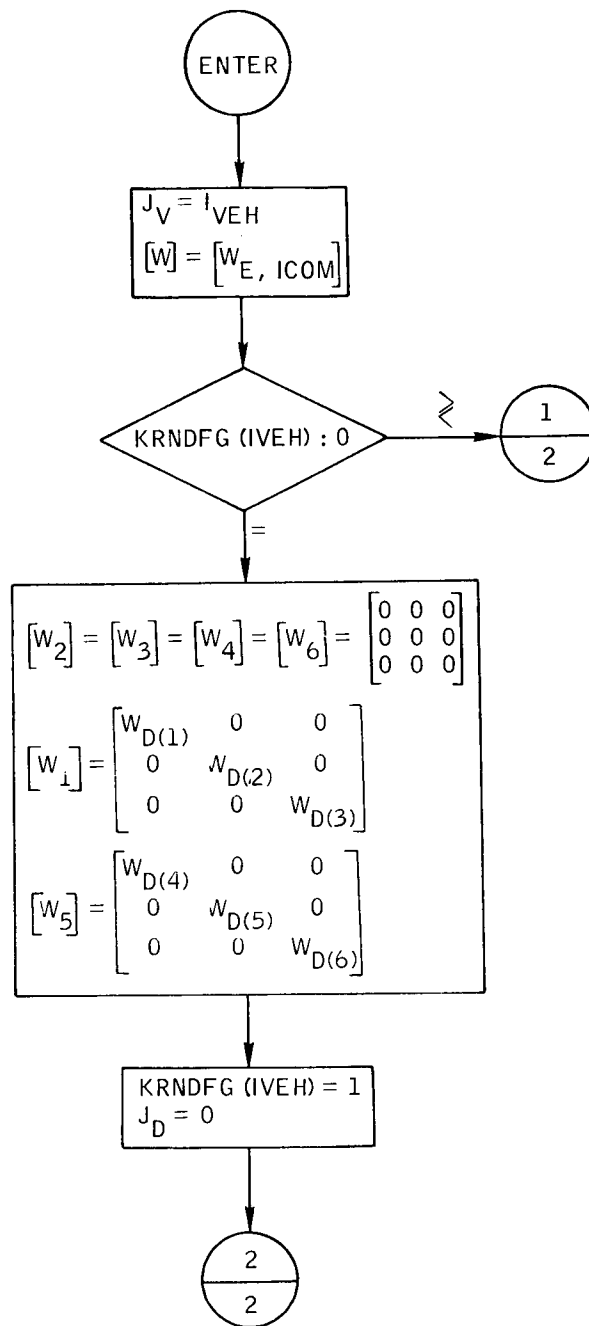


Figure B-58. - Flow chart of subroutine ONR.

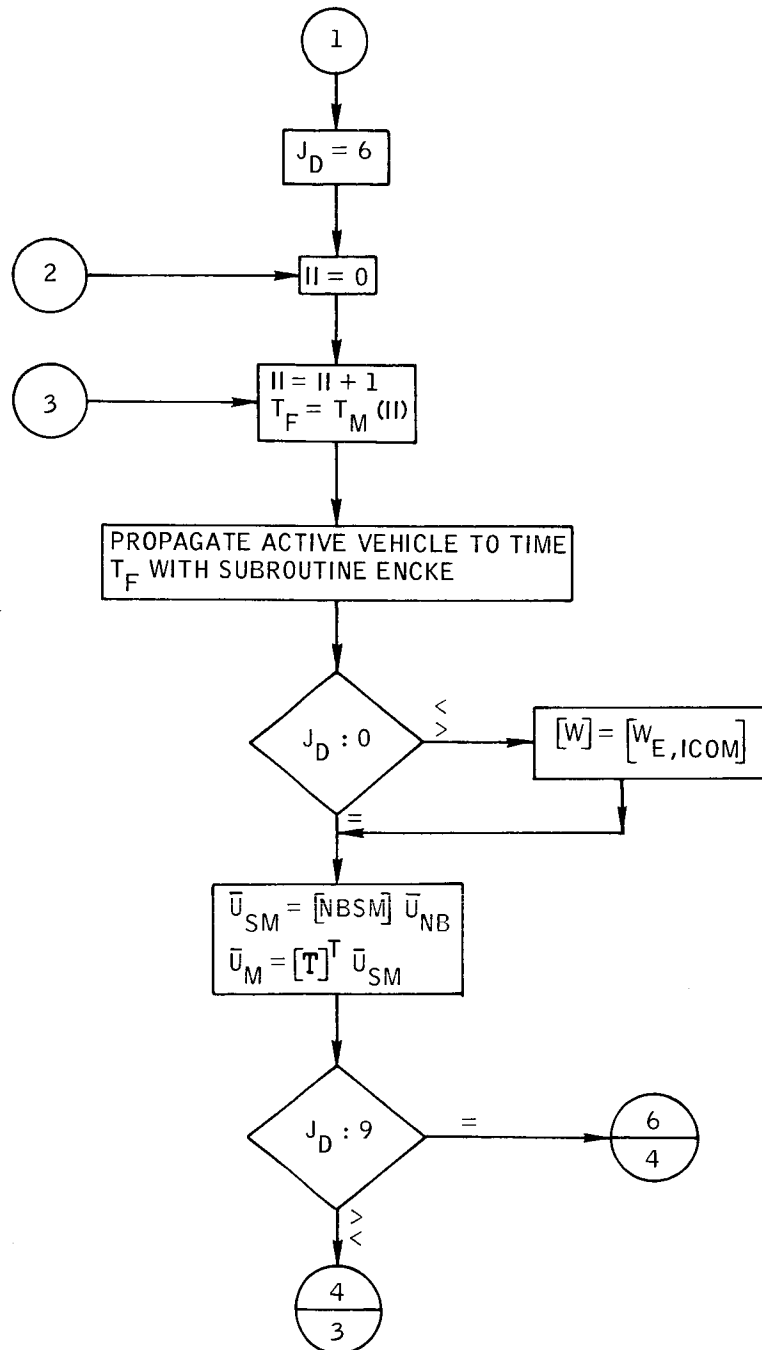


Figure B-58.- Continued.

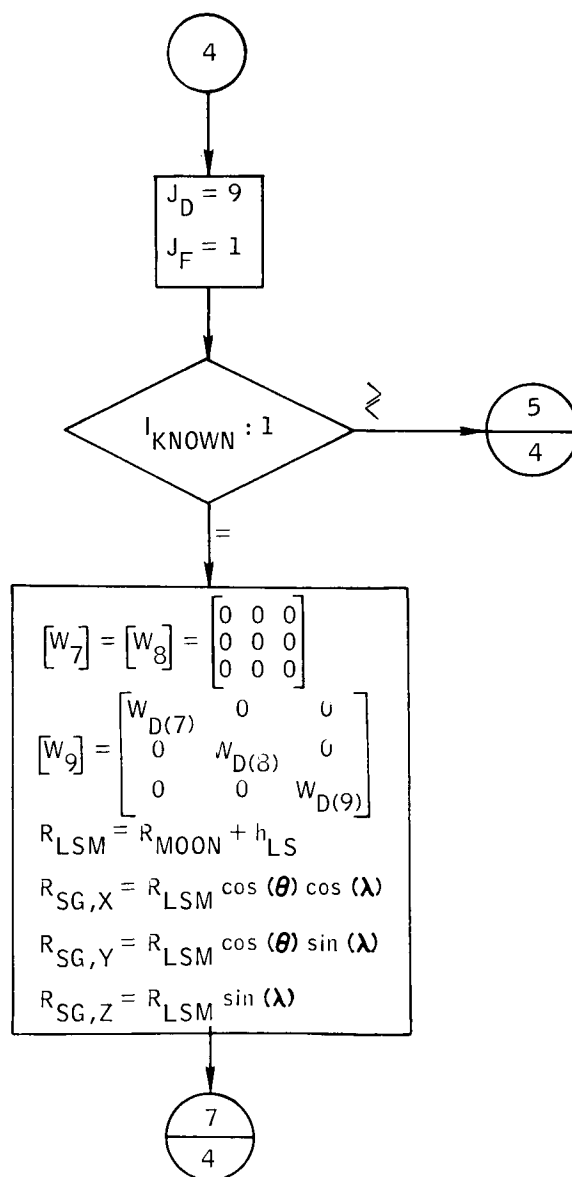


Figure B-58. - Continued.

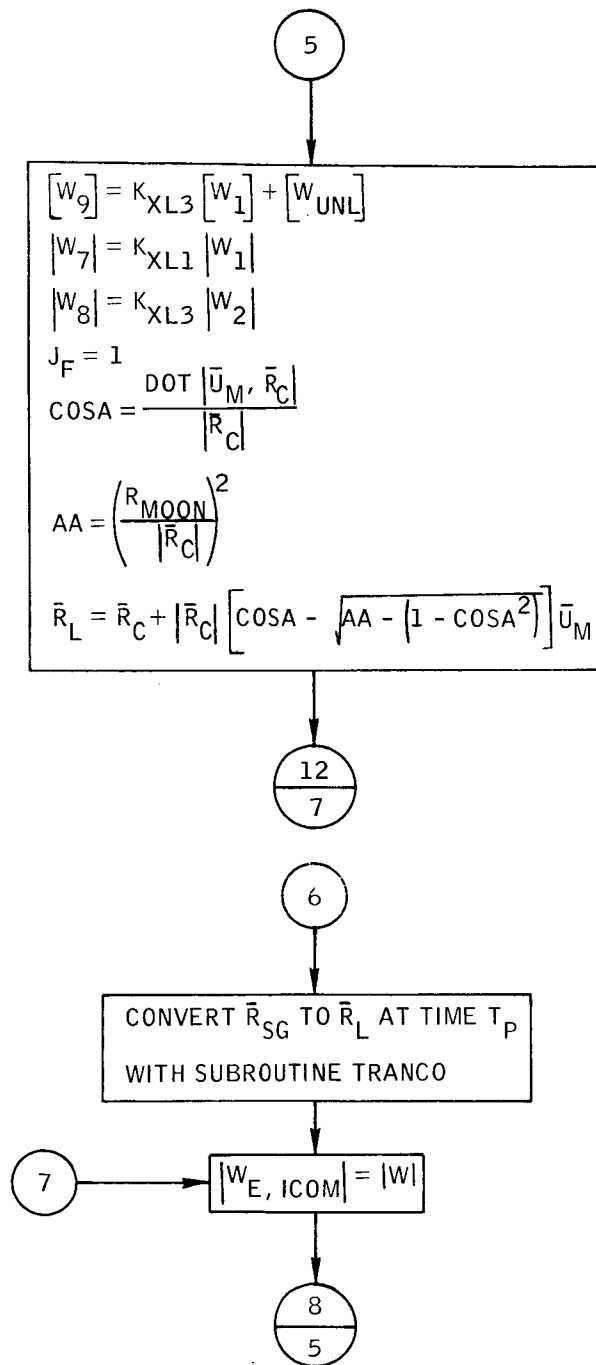


Figure B-58.- Continued.

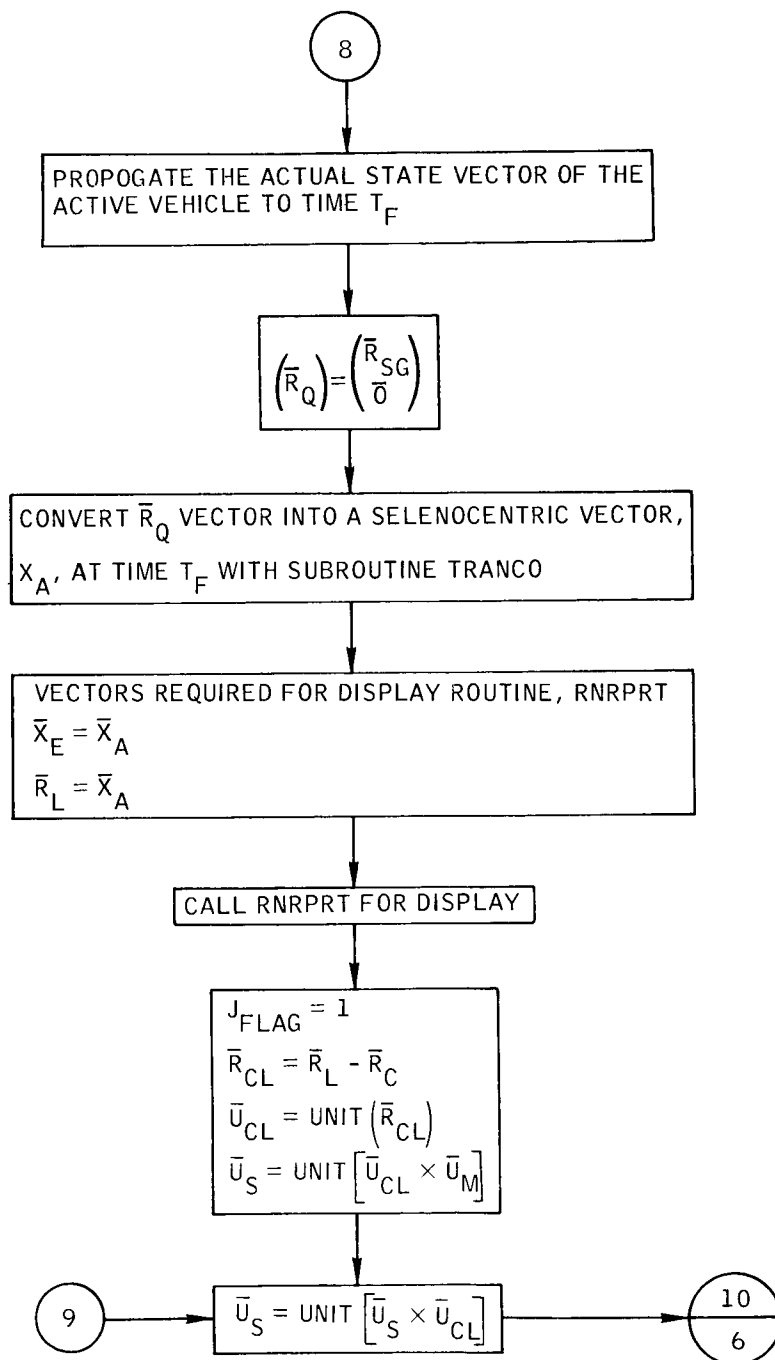


Figure B-58. - Continued.

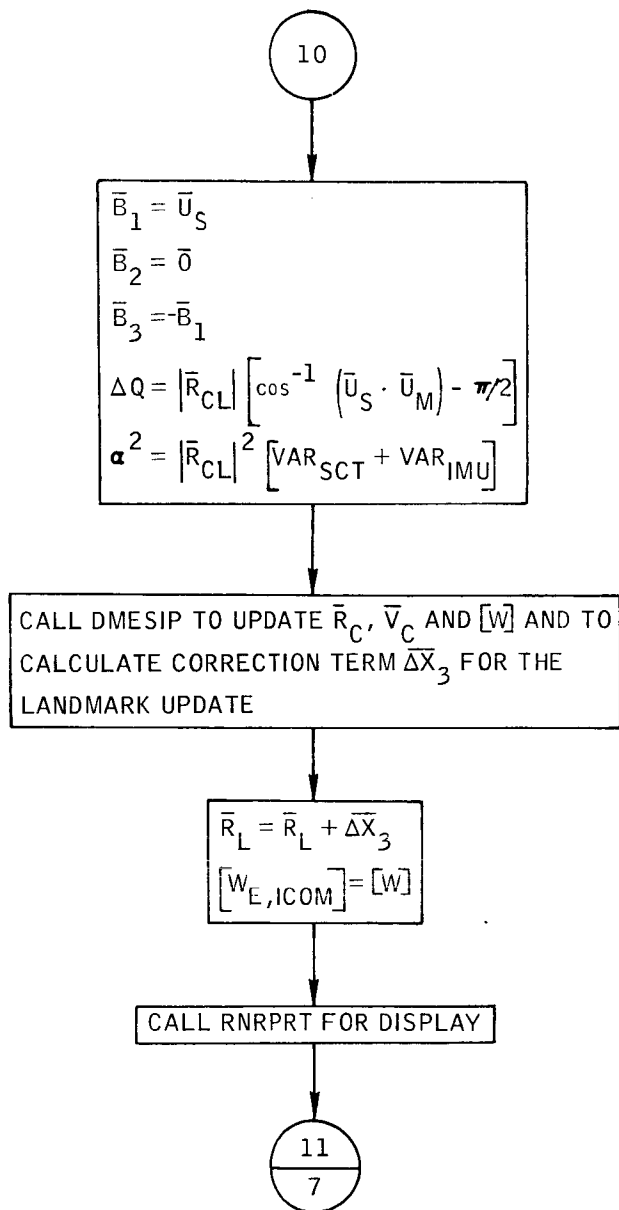


Figure B-58. - Continued.

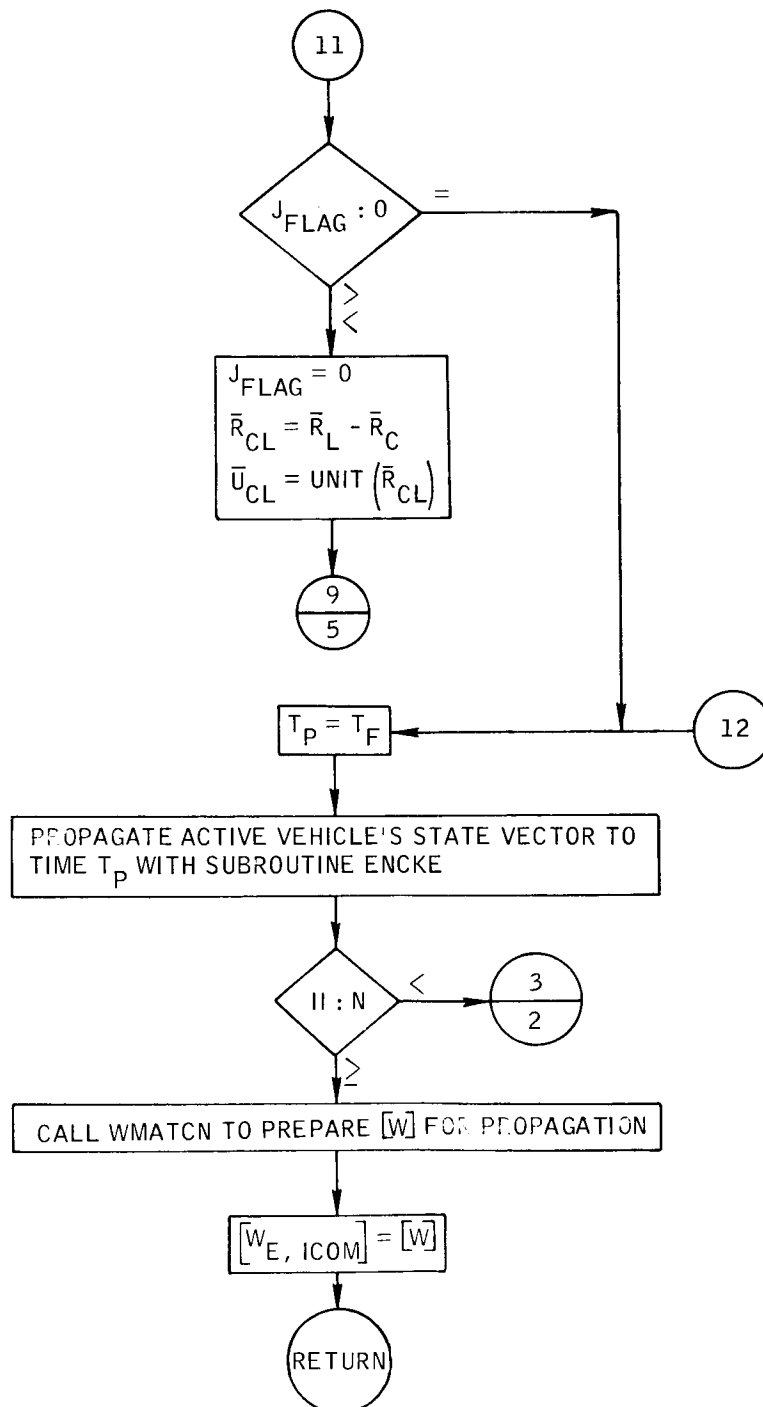


Figure B-58.- Concluded.

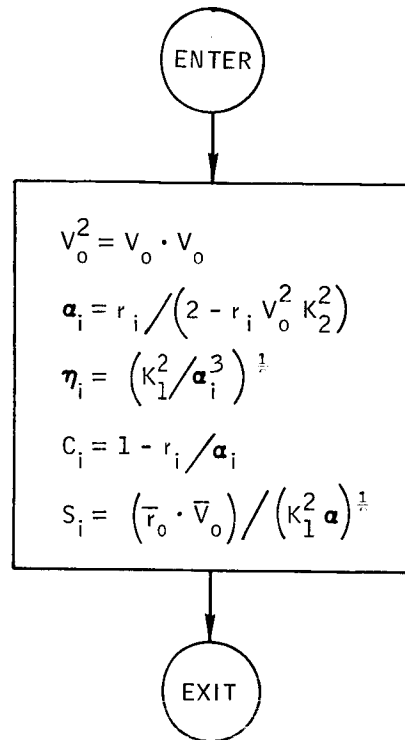


Figure B-59.- Flow chart of subroutine OPS.



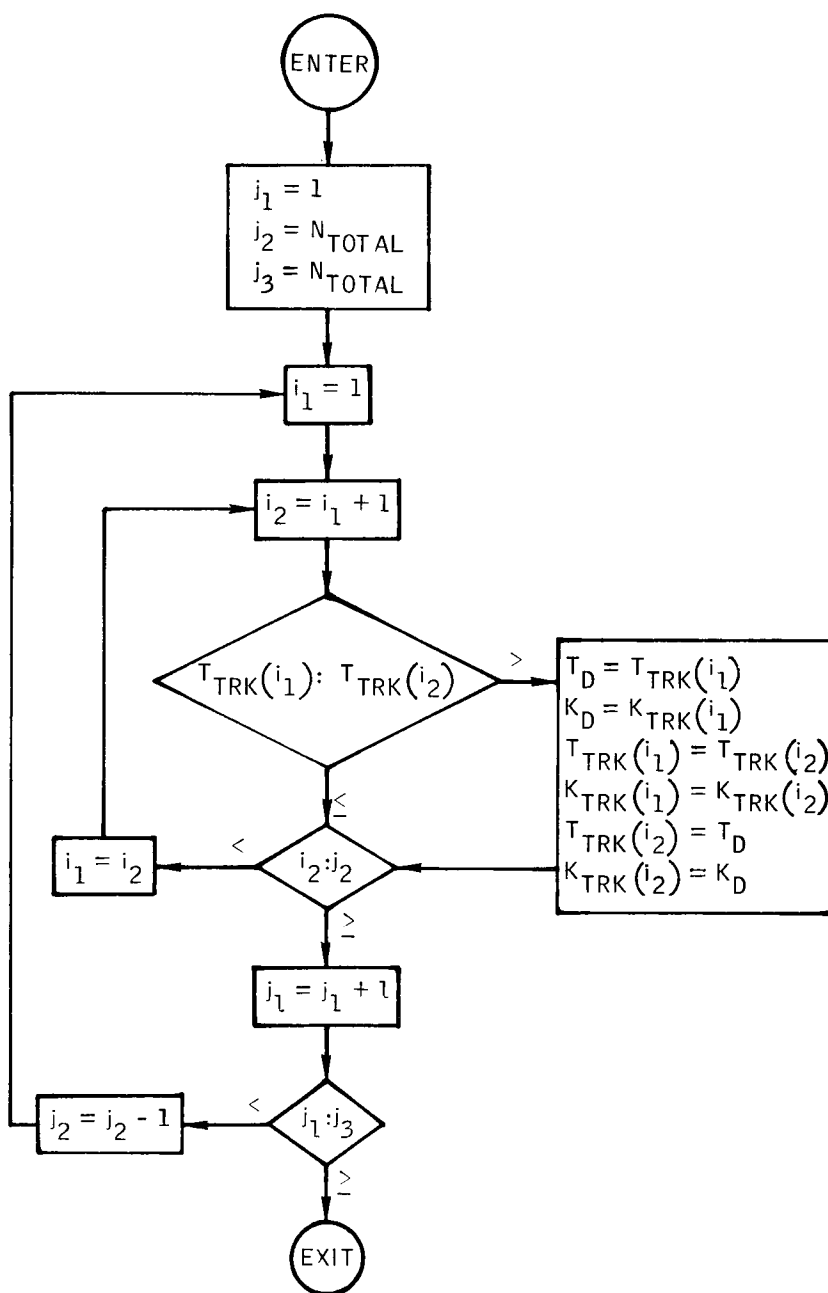


Figure B-60.- Flow chart of subroutine ORD.

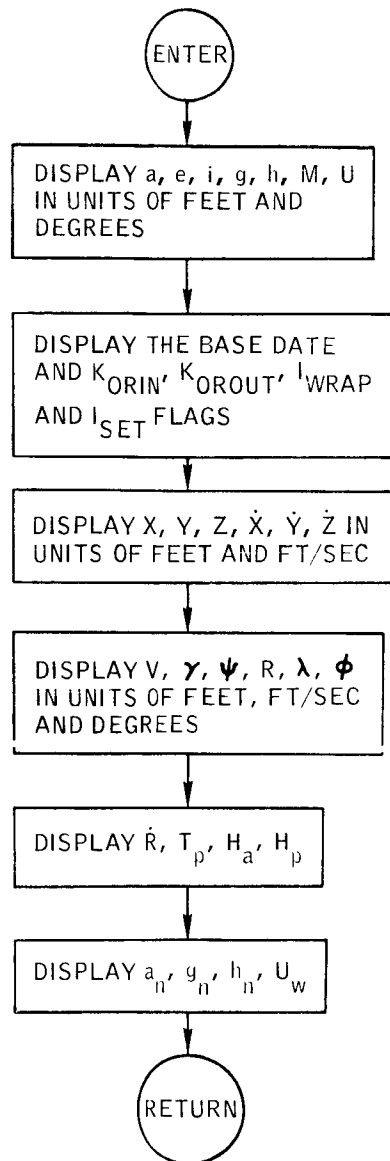


Figure B-61.- Flow chart of subroutine OUTPUT.

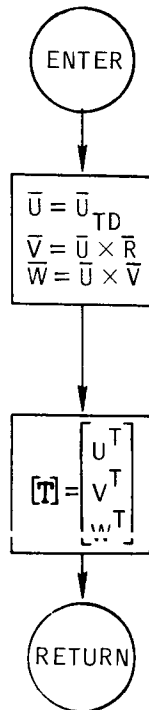


Figure B-62.- Flow chart of subroutine PALIGN.

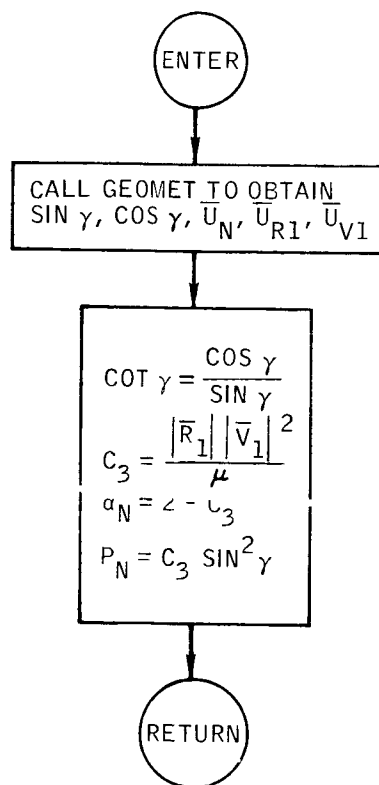


Figure B-63.- Flow chart of subroutine PARAM.

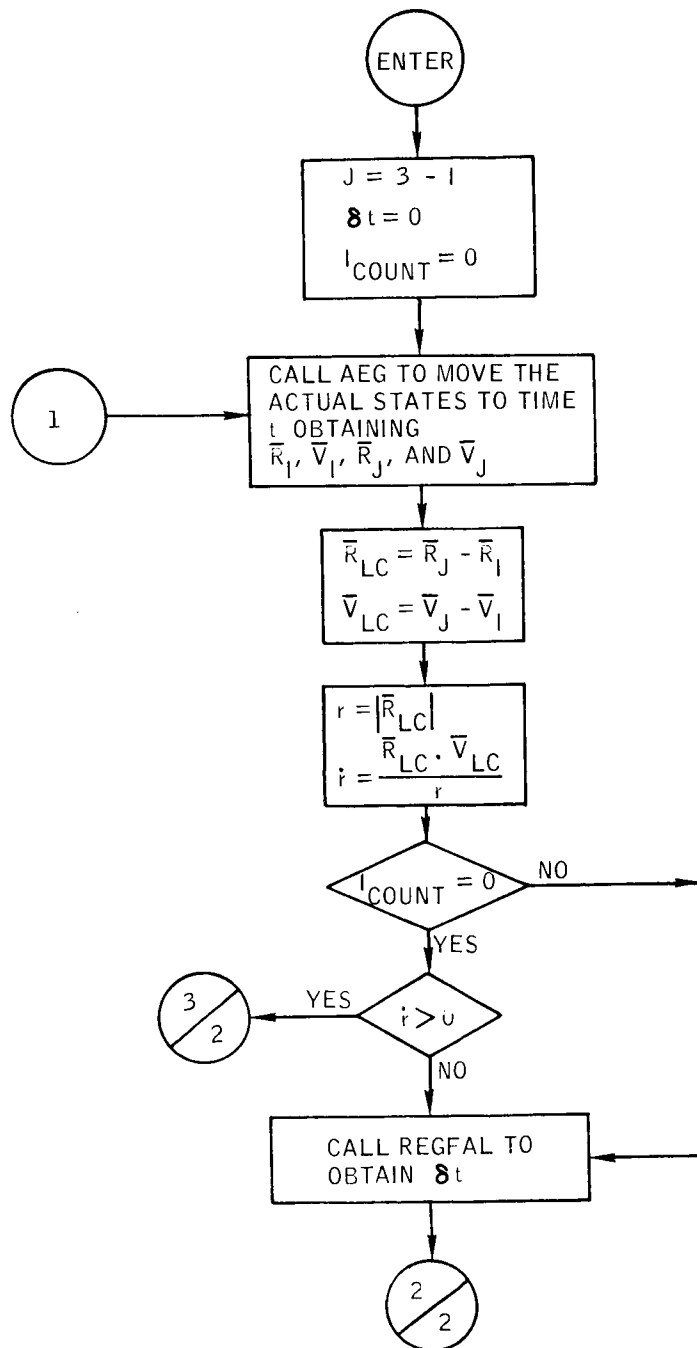


Figure B-64.- Flow chart of subroutine PCA.

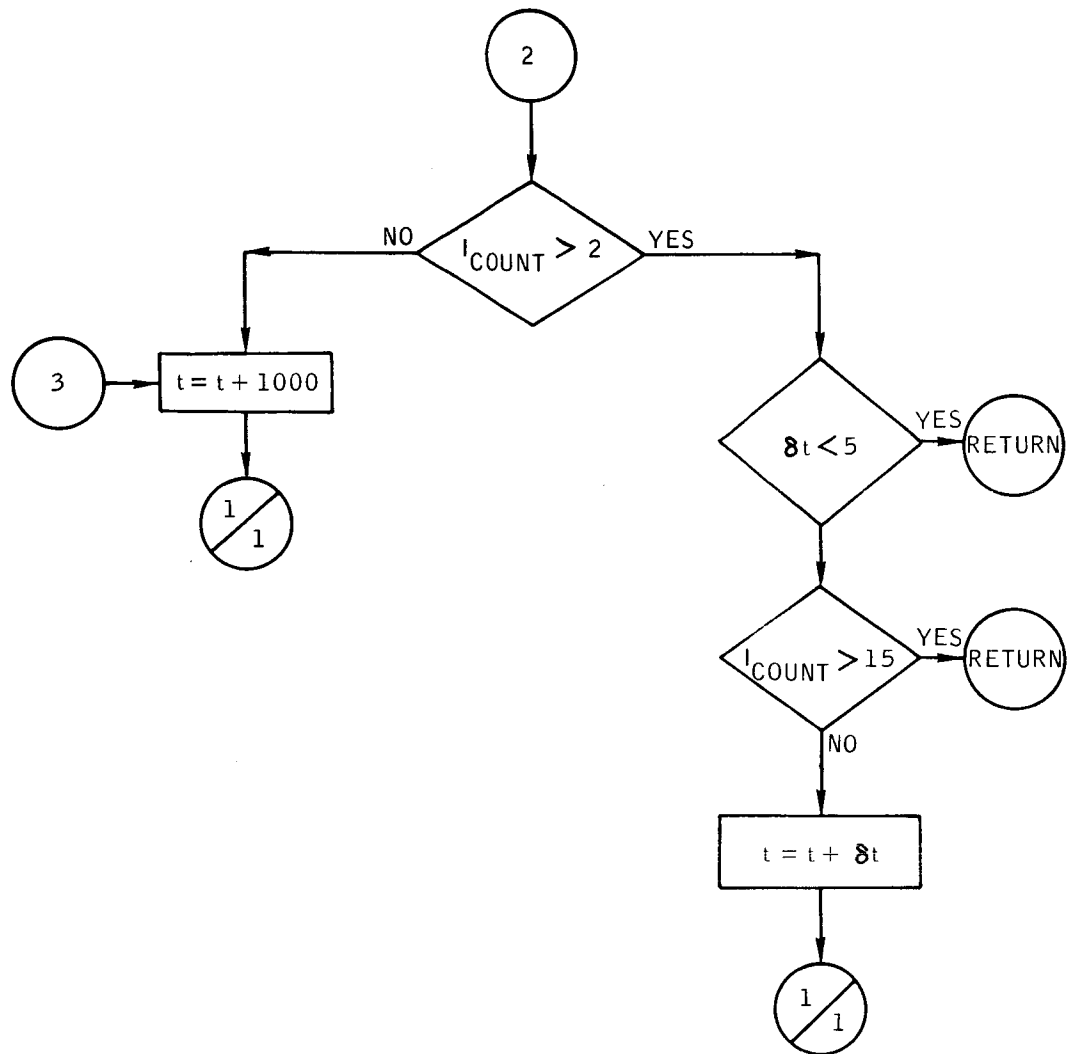


Figure B-64.- Concluded.

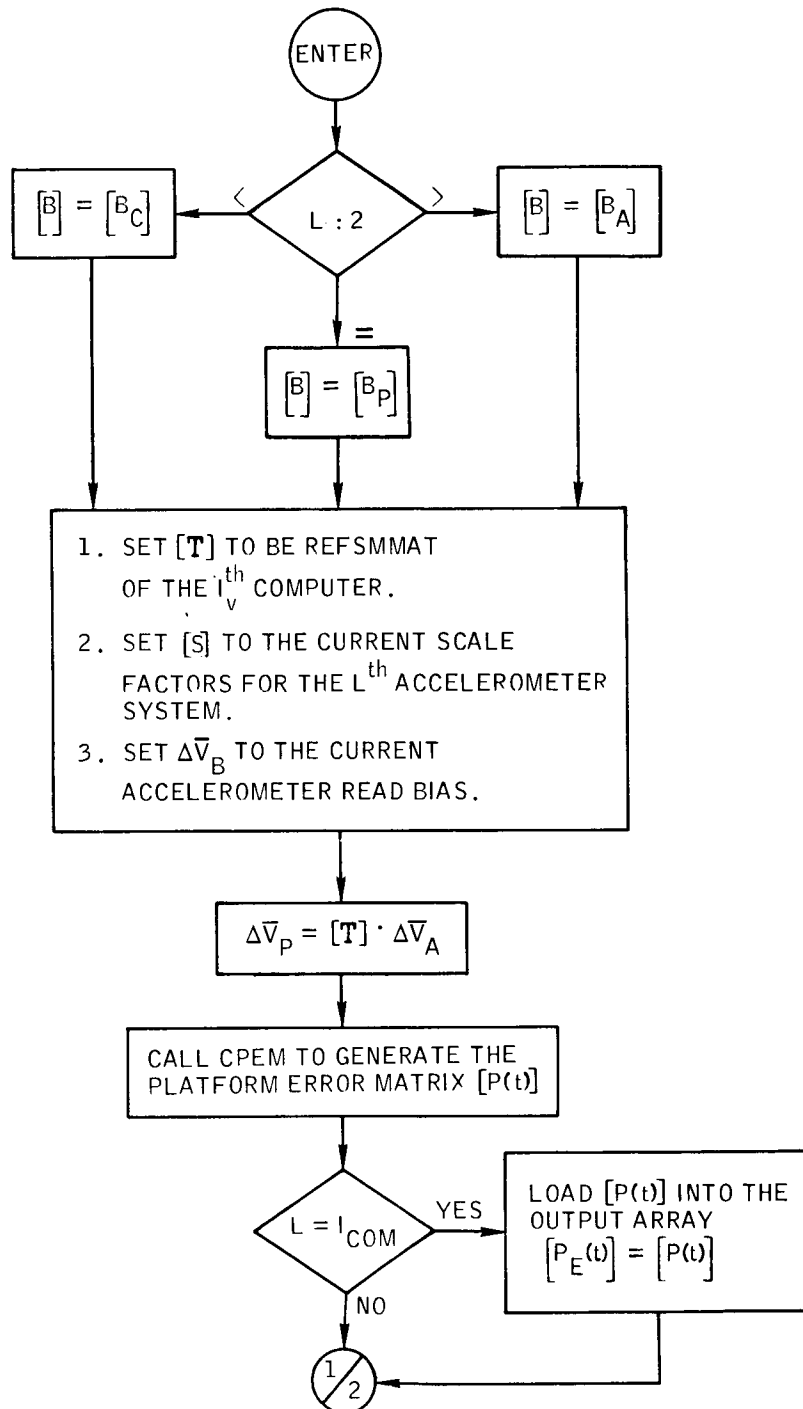


Figure B-65.- Flow chart of subroutine PERRO.

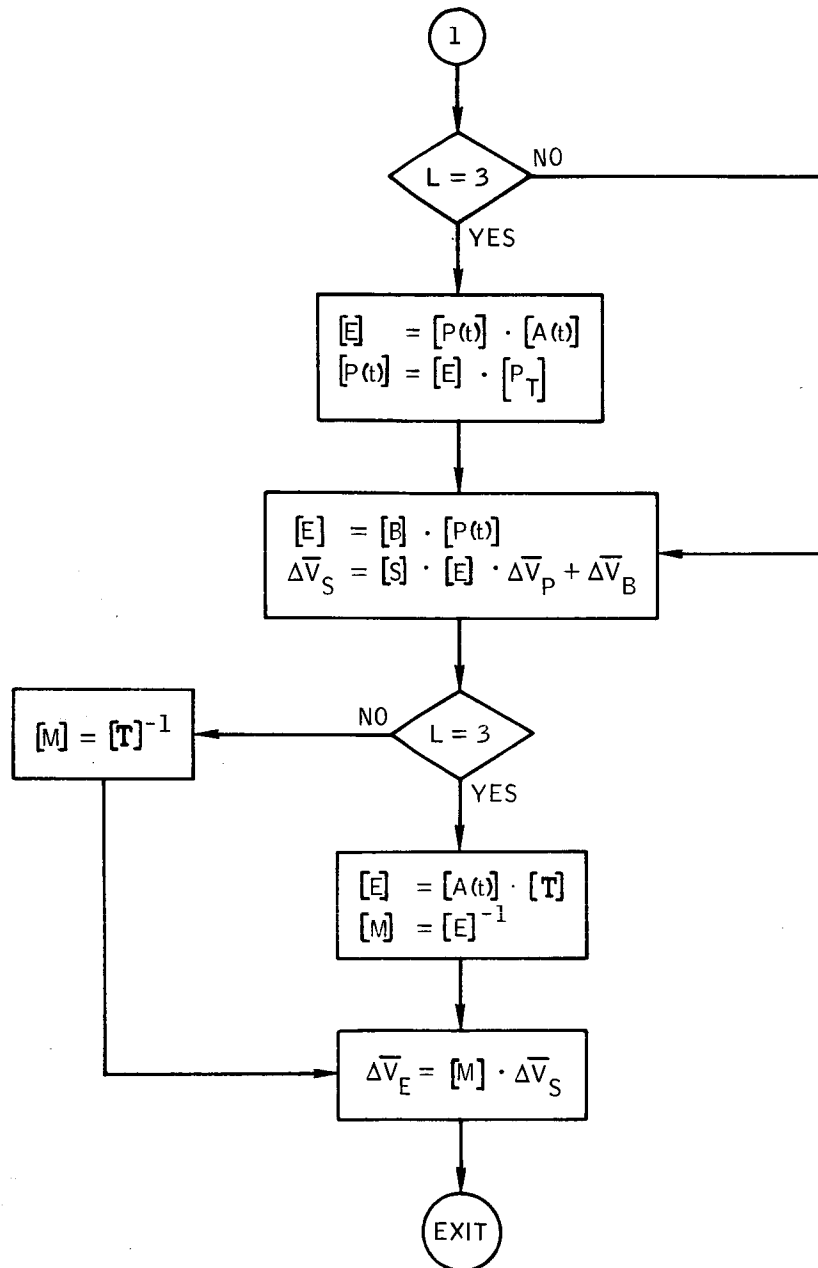


Figure B-65.- Concluded.



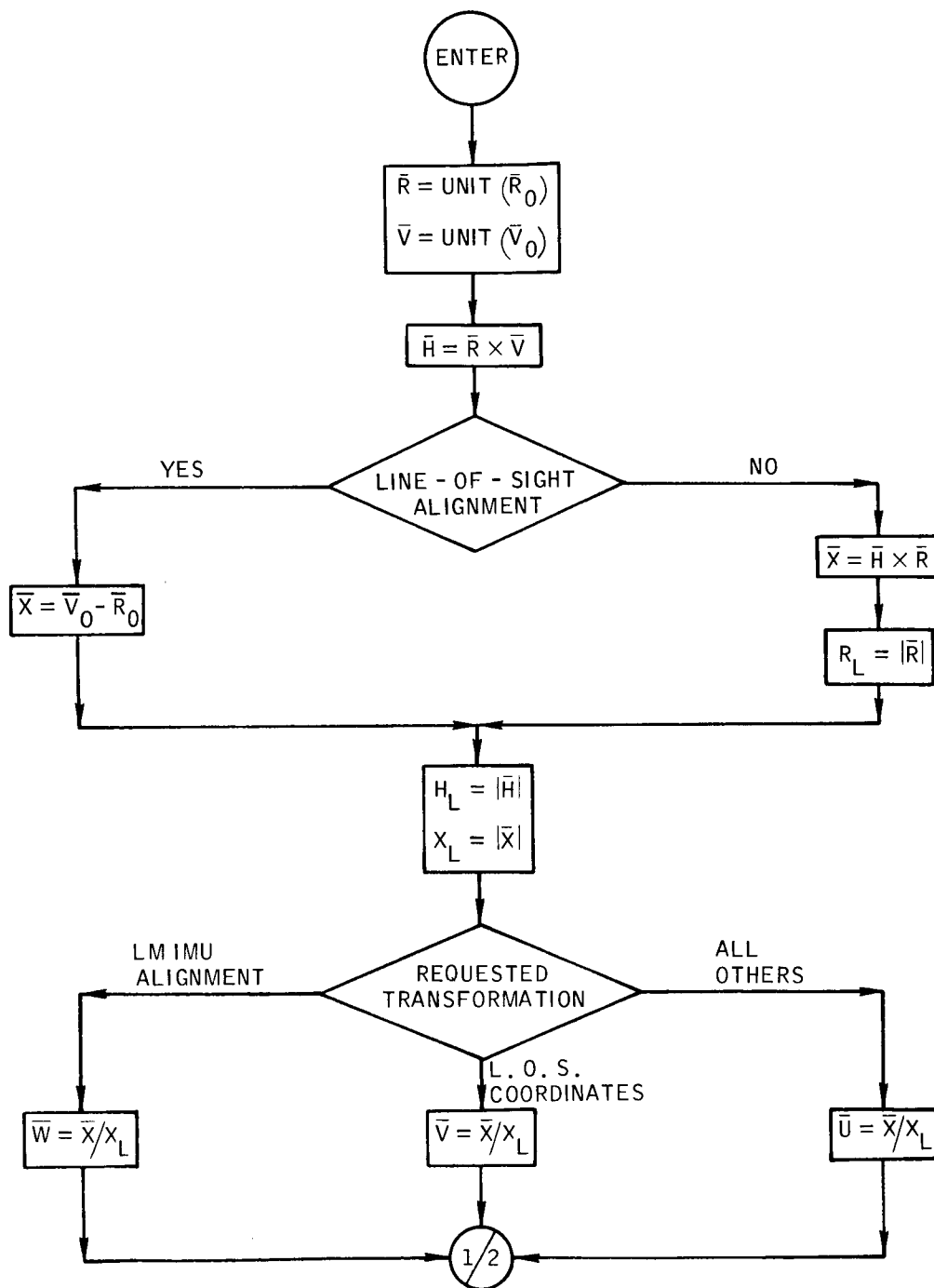


Figure B-66.- Flow chart of subroutine PMATRIX.

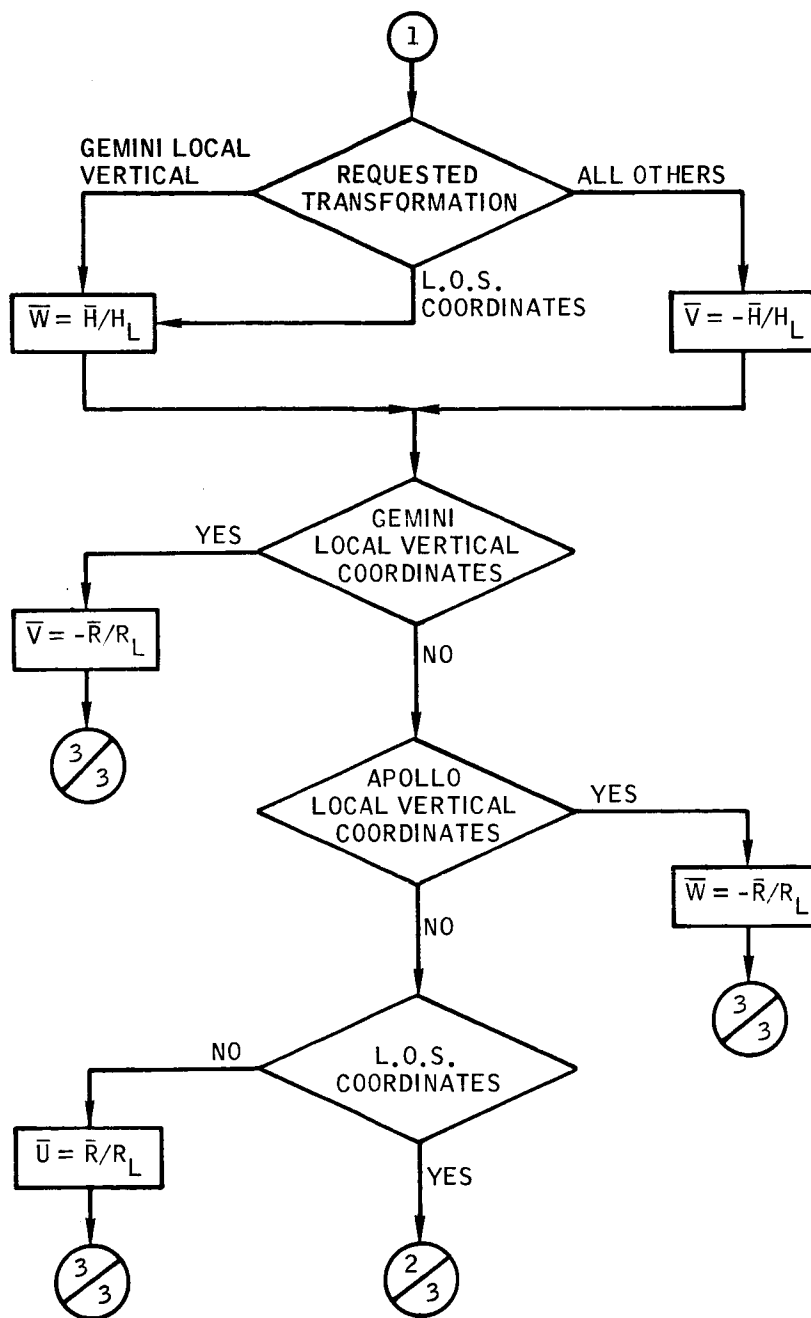


Figure B-66.- Continued.

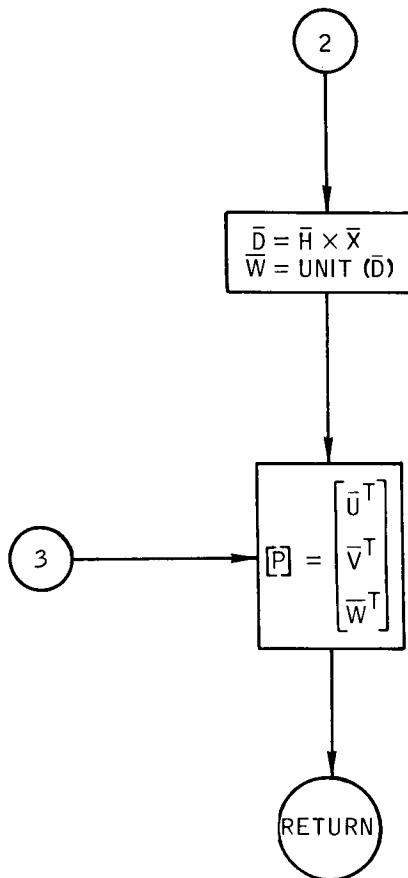


Figure B-66.- Concluded.

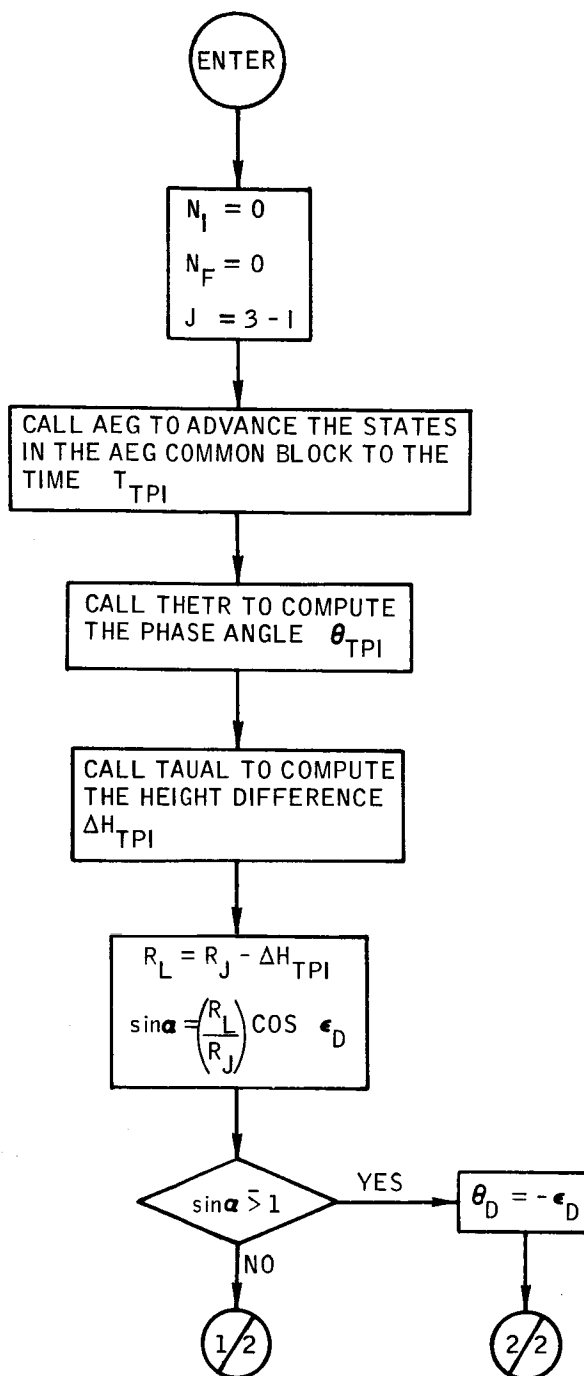


Figure B-67.- Flow chart of subroutine PMISS.

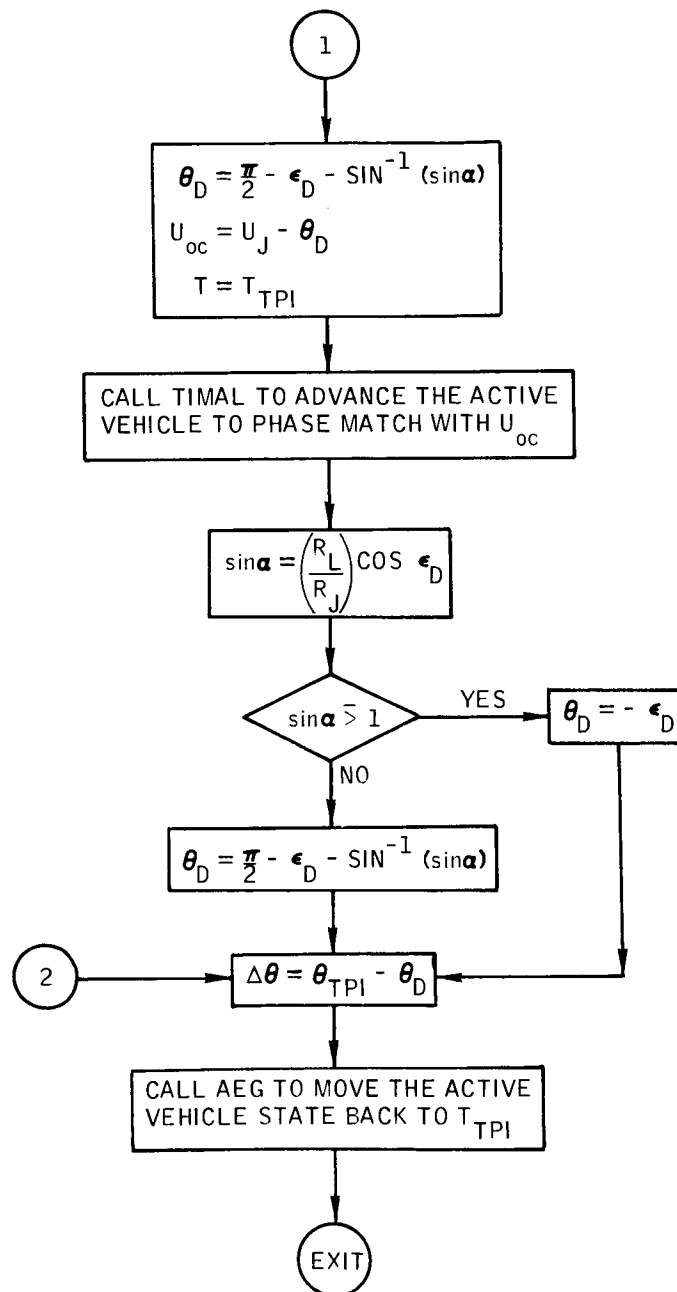


Figure B-67.- Concluded.

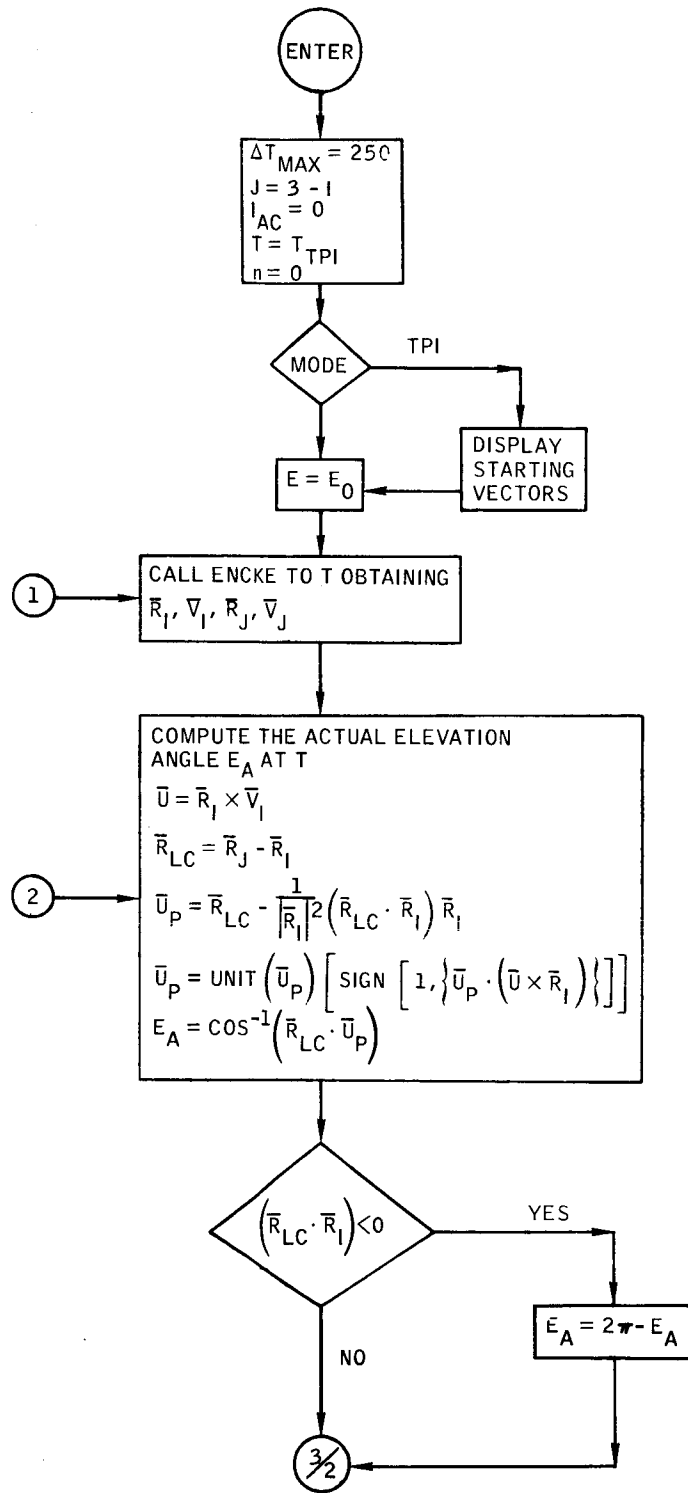


Figure B-68. - Flow chart of subroutine PRETPI.

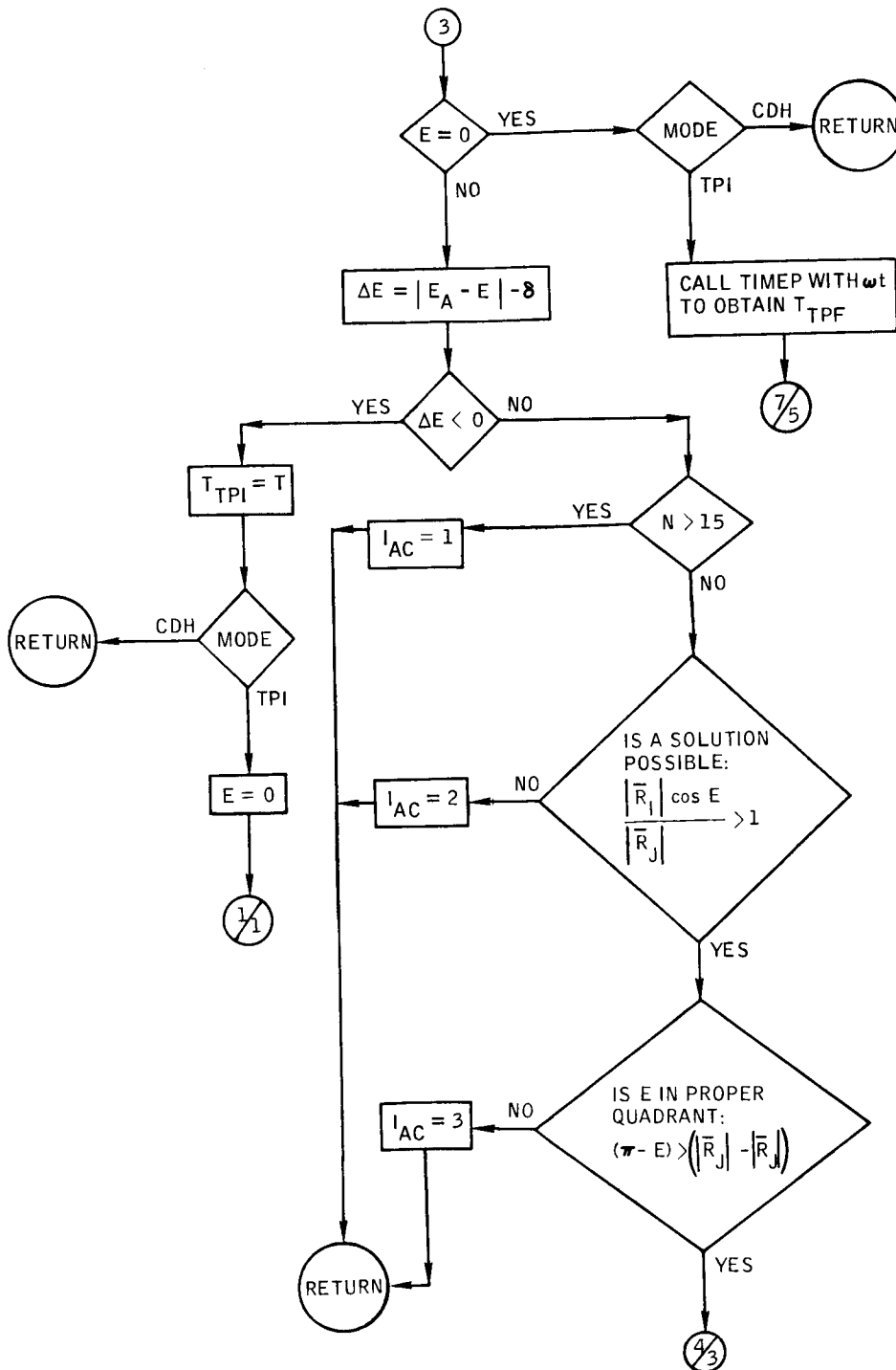


Figure B-68.- Continued.

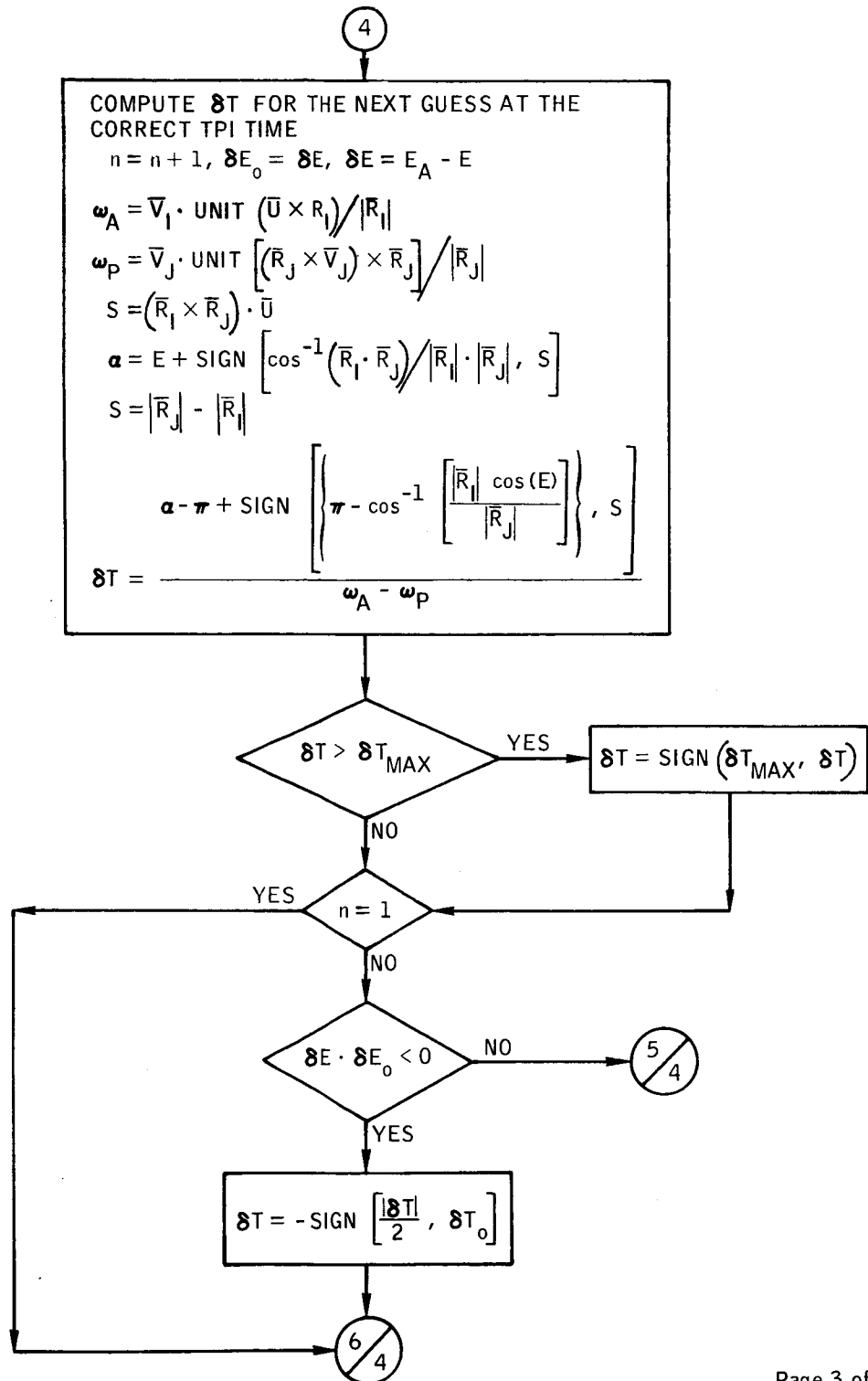


Figure B-68. - Continued.



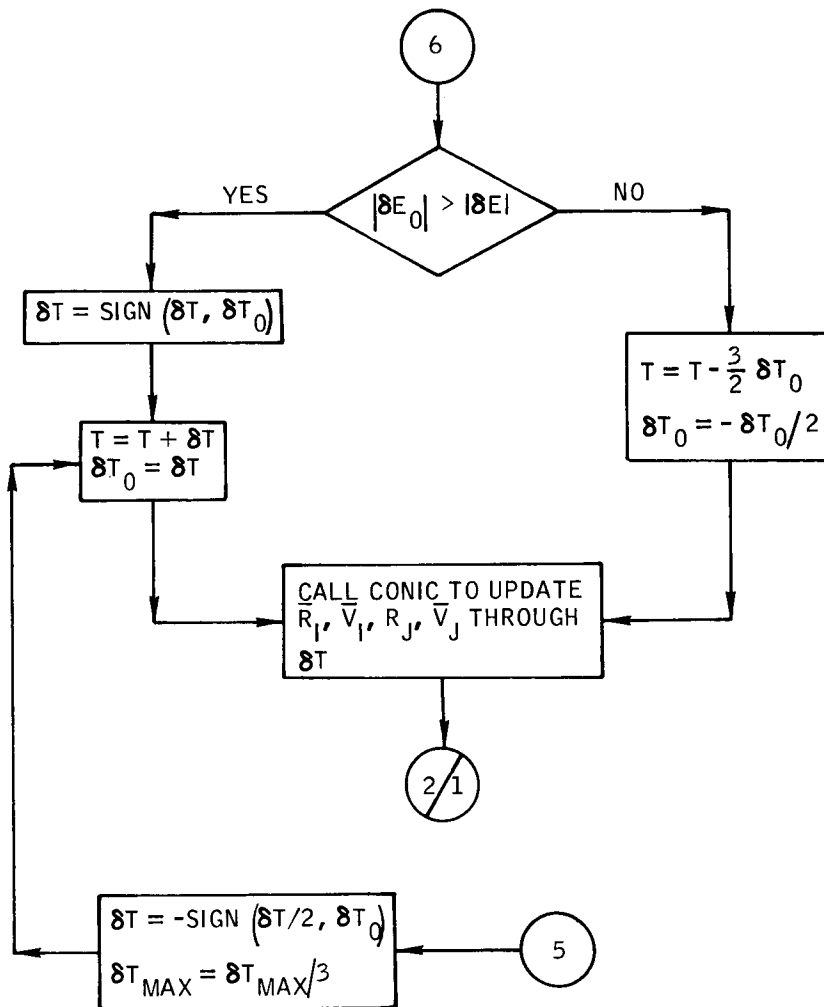


Figure B-68.- Continued.

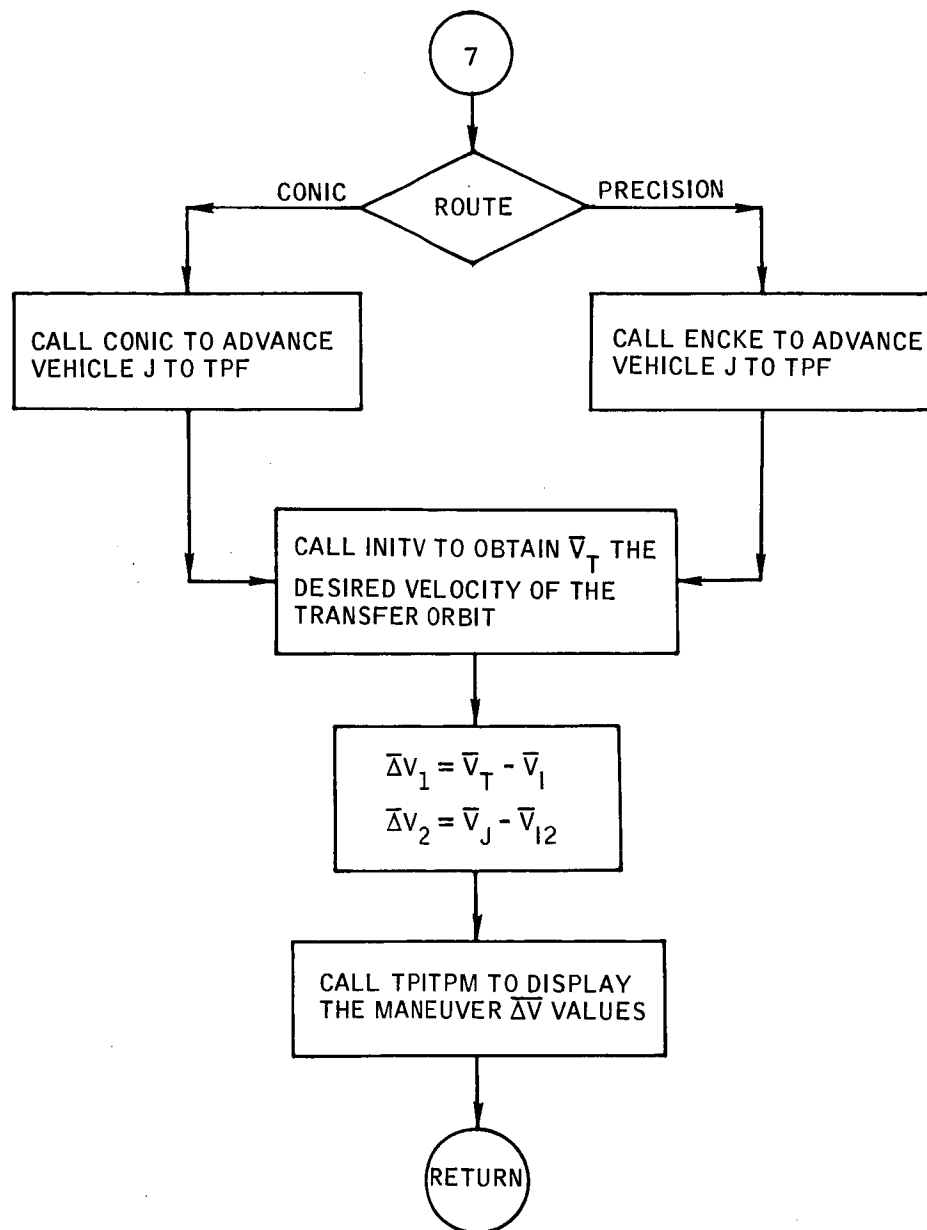


Figure B-68. - Concluded.

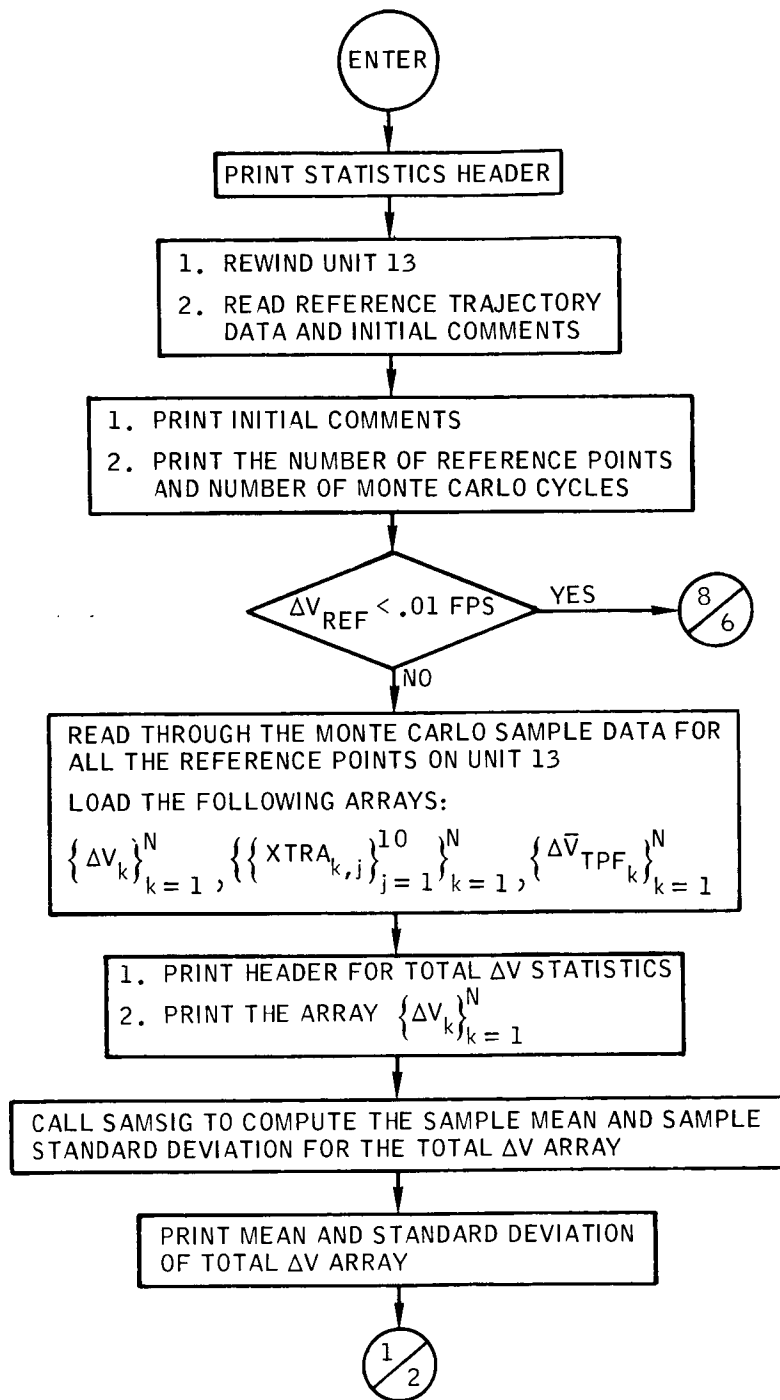


Figure B-69.- Flow chart of subroutine PROCES.

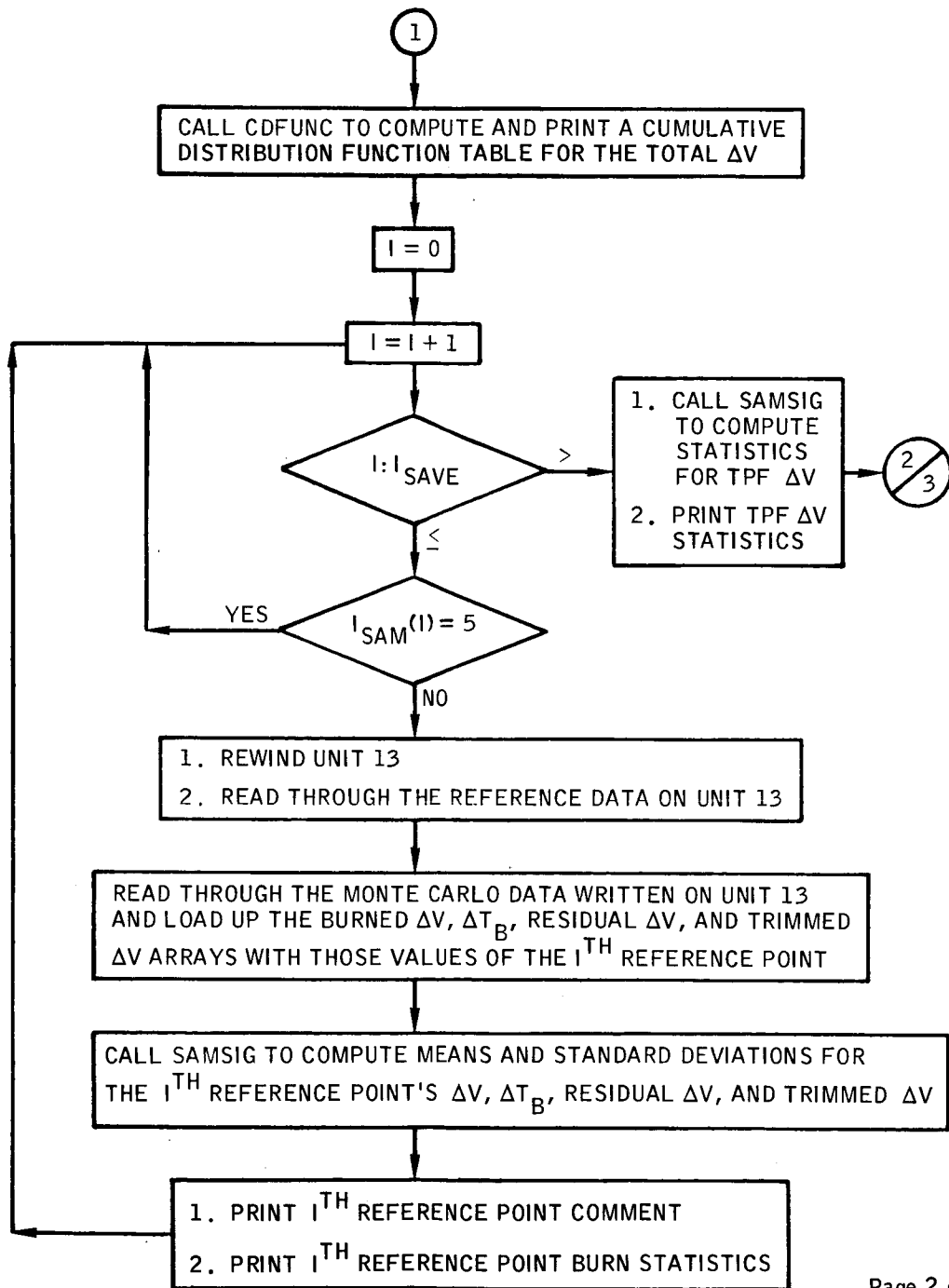


Figure B-69.- Continued.

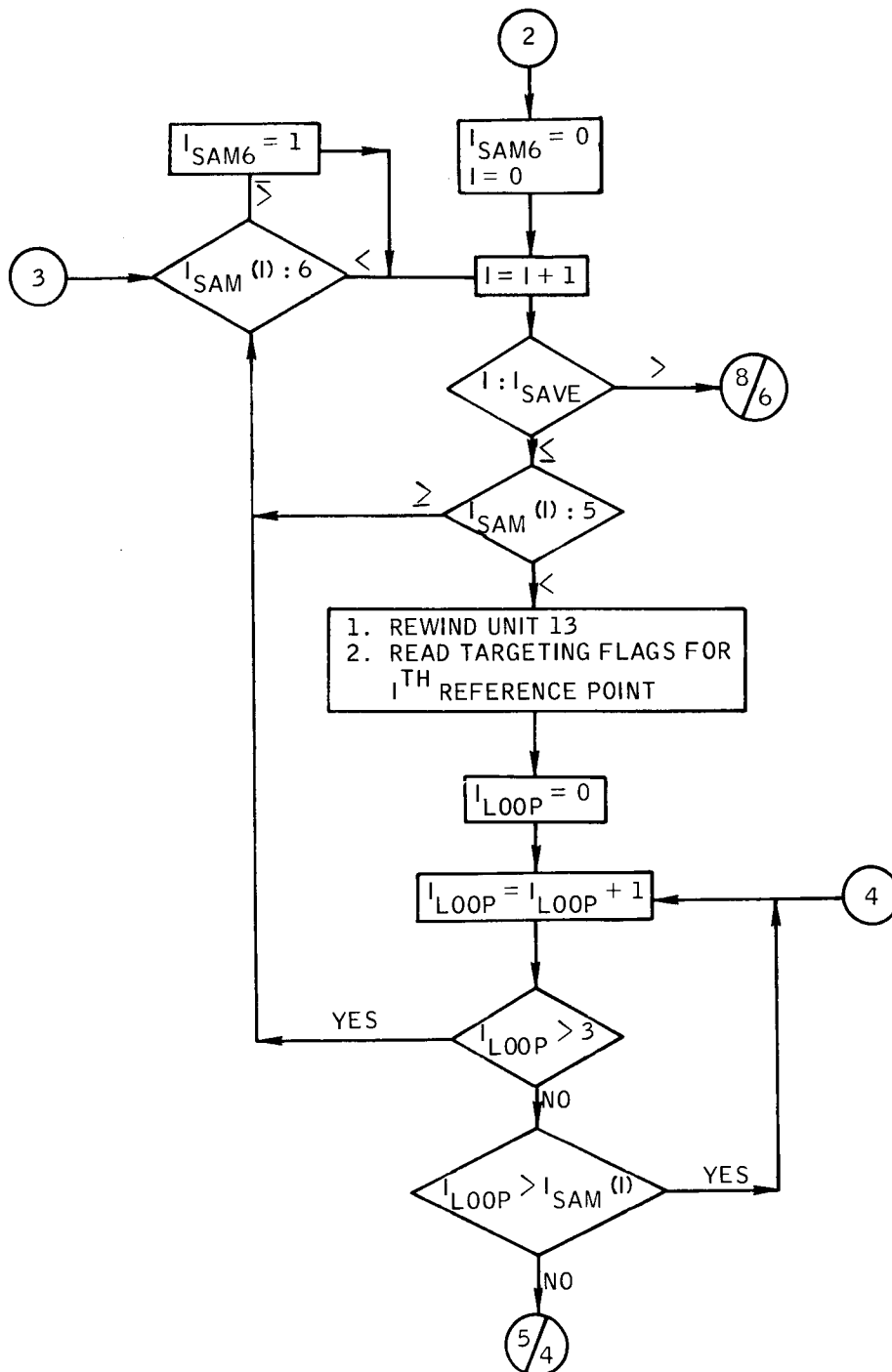


Figure B-69.- Continued.

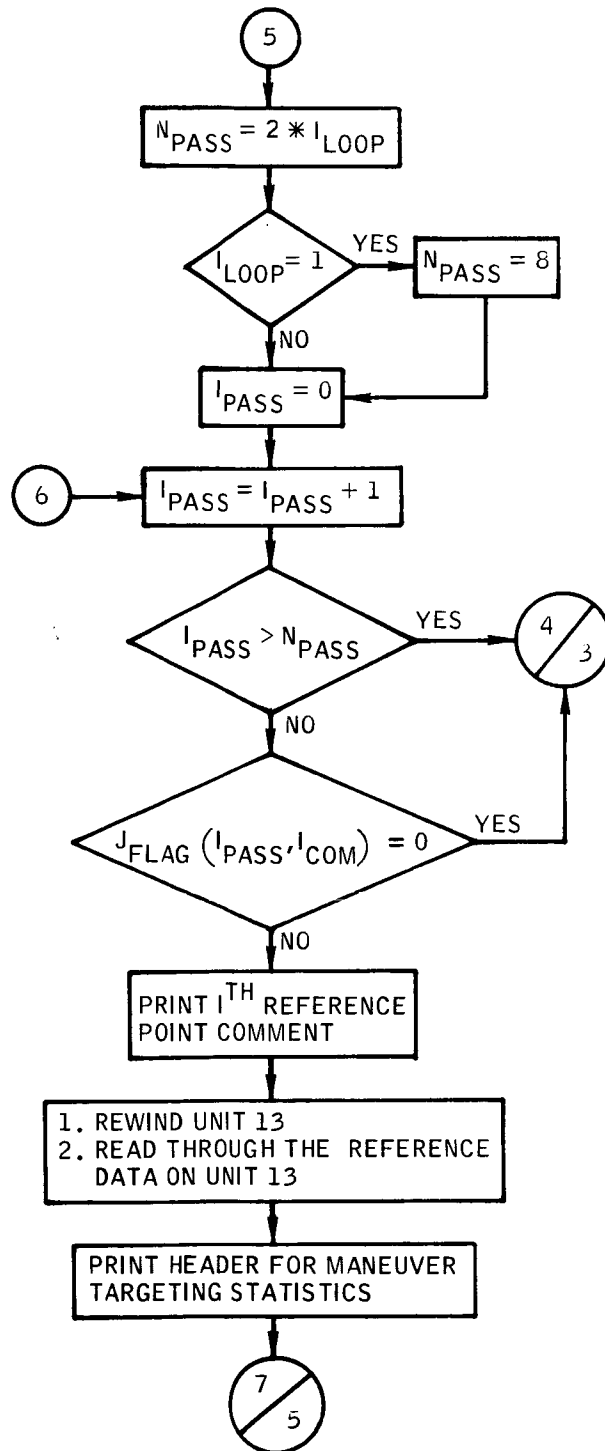


Figure B-69.- Continued.

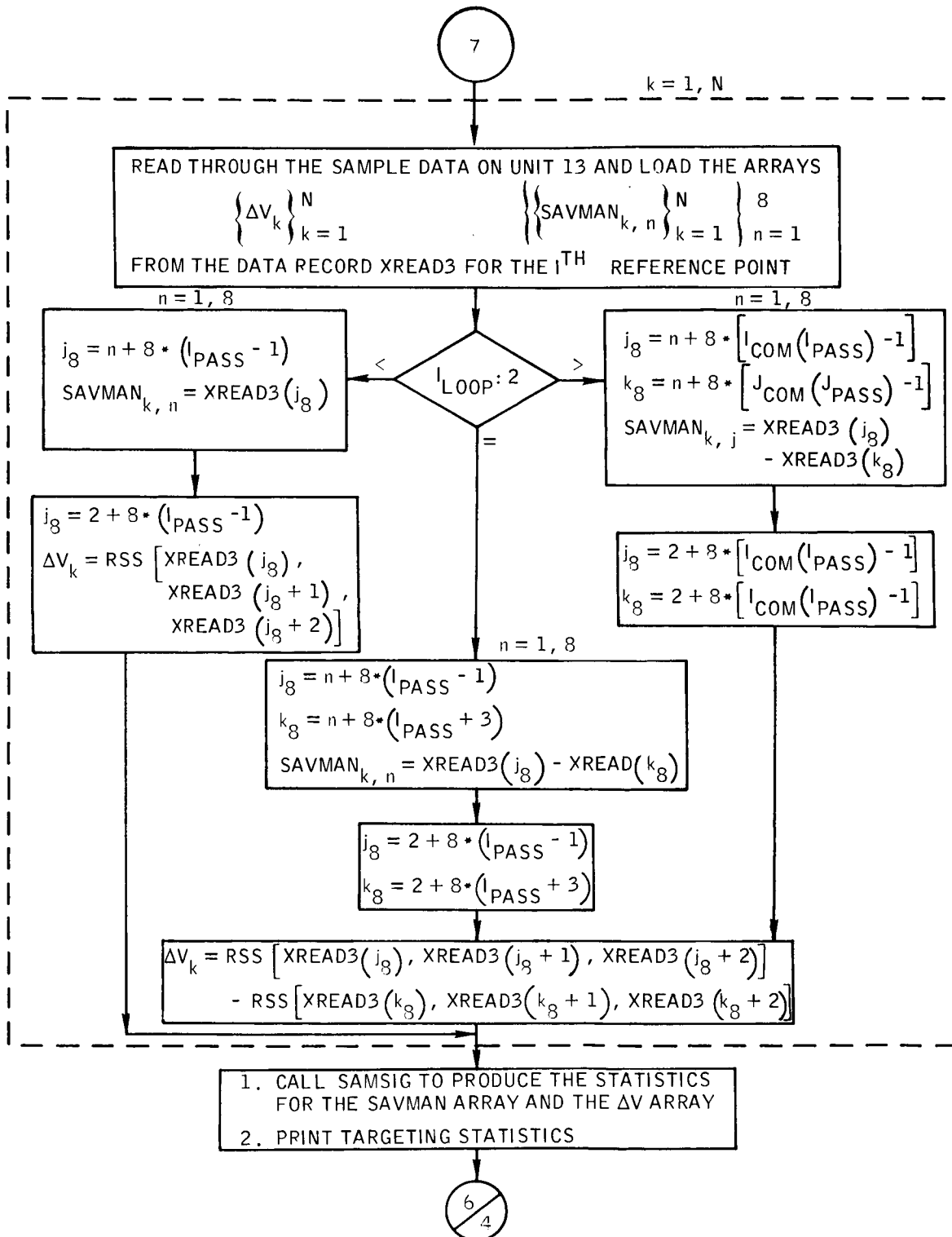
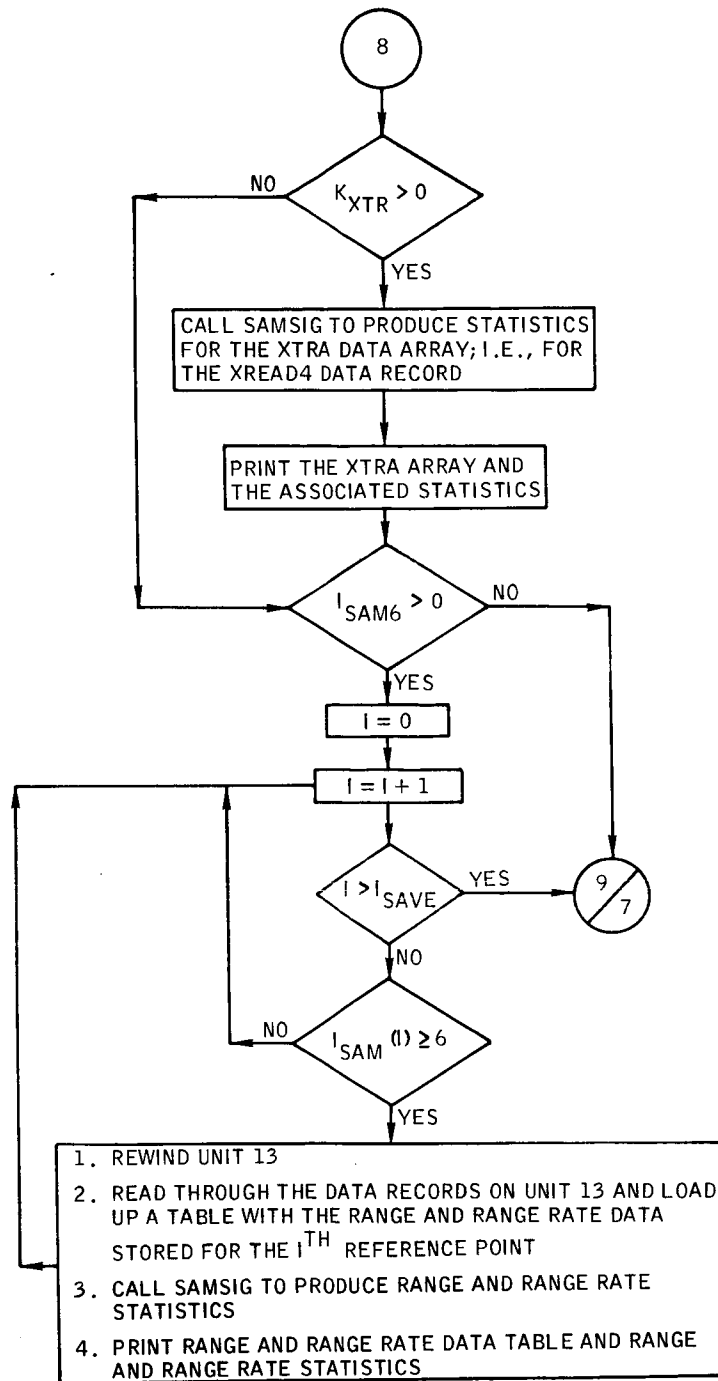


Figure B-69.- Continued.





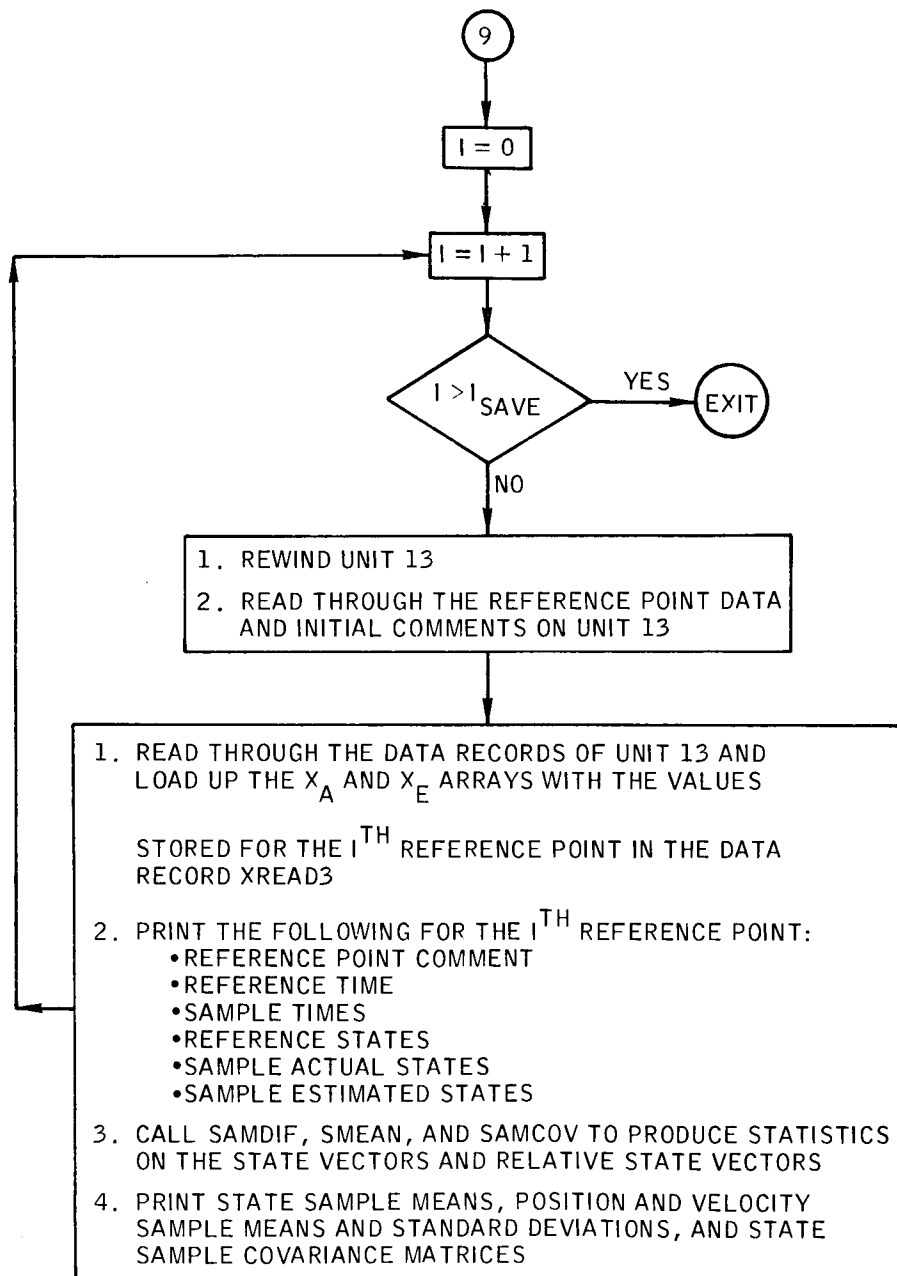


Figure B-69.- Concluded.

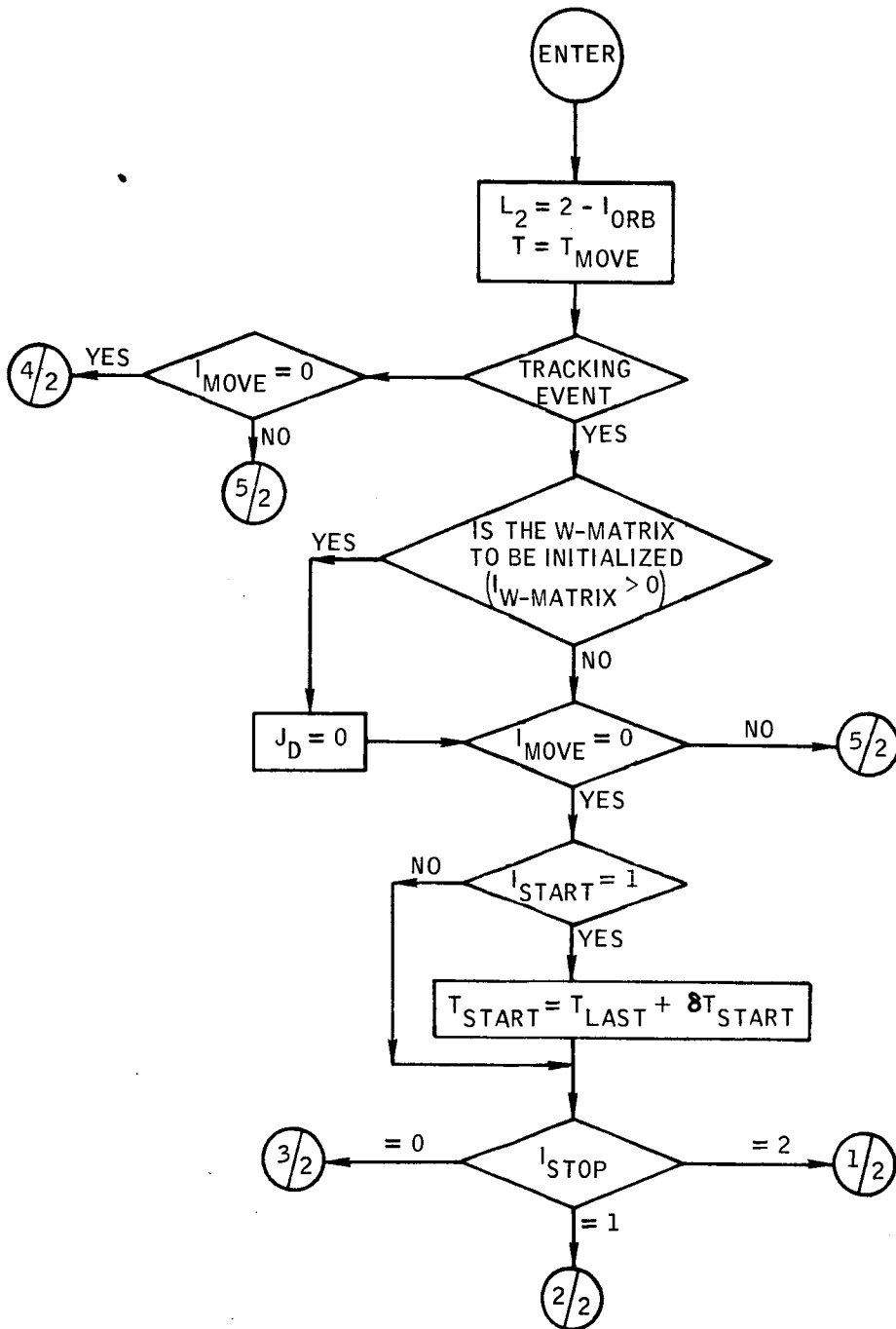
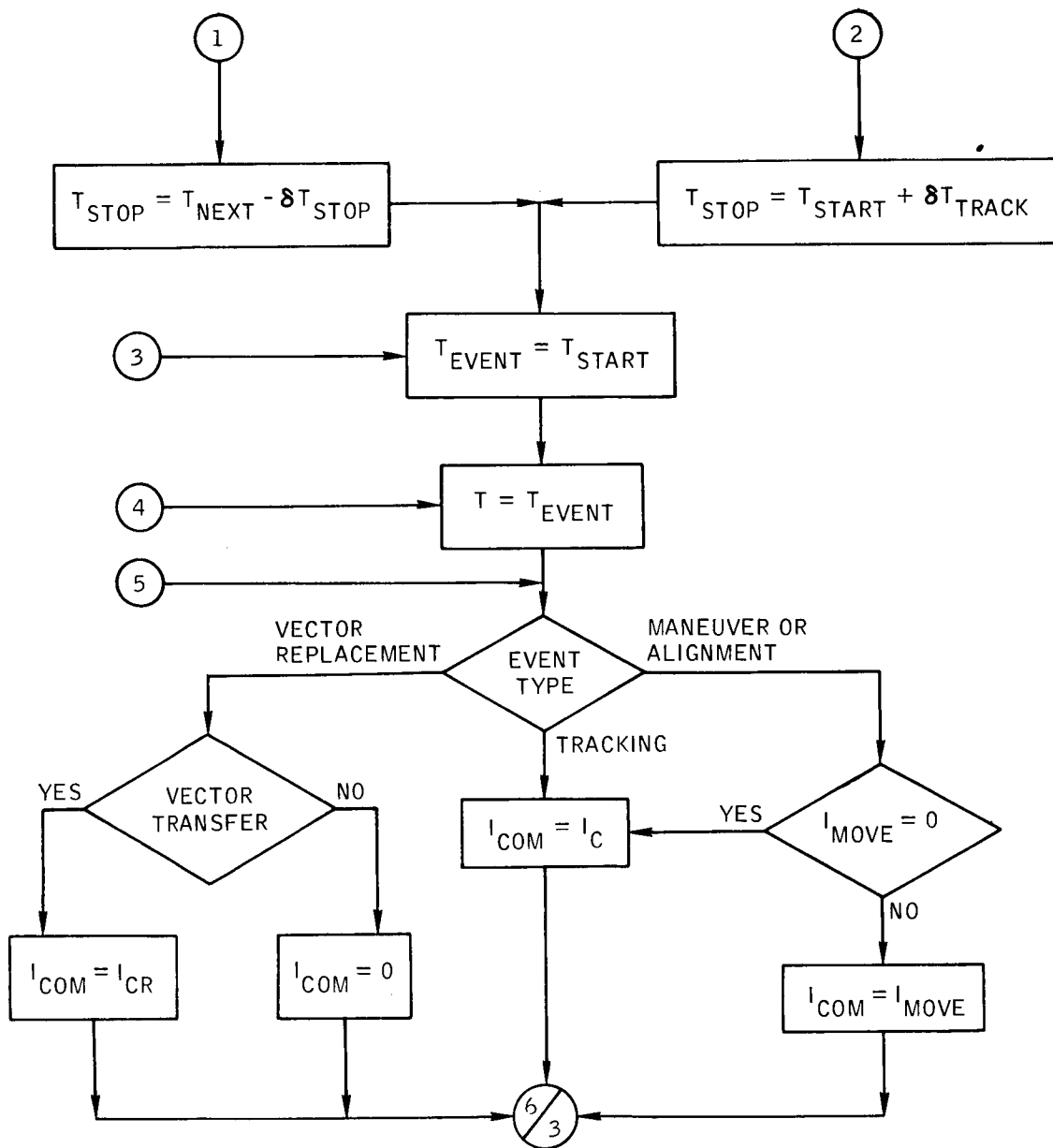


Figure B-70.- Flow chart of subroutine PROPAG.



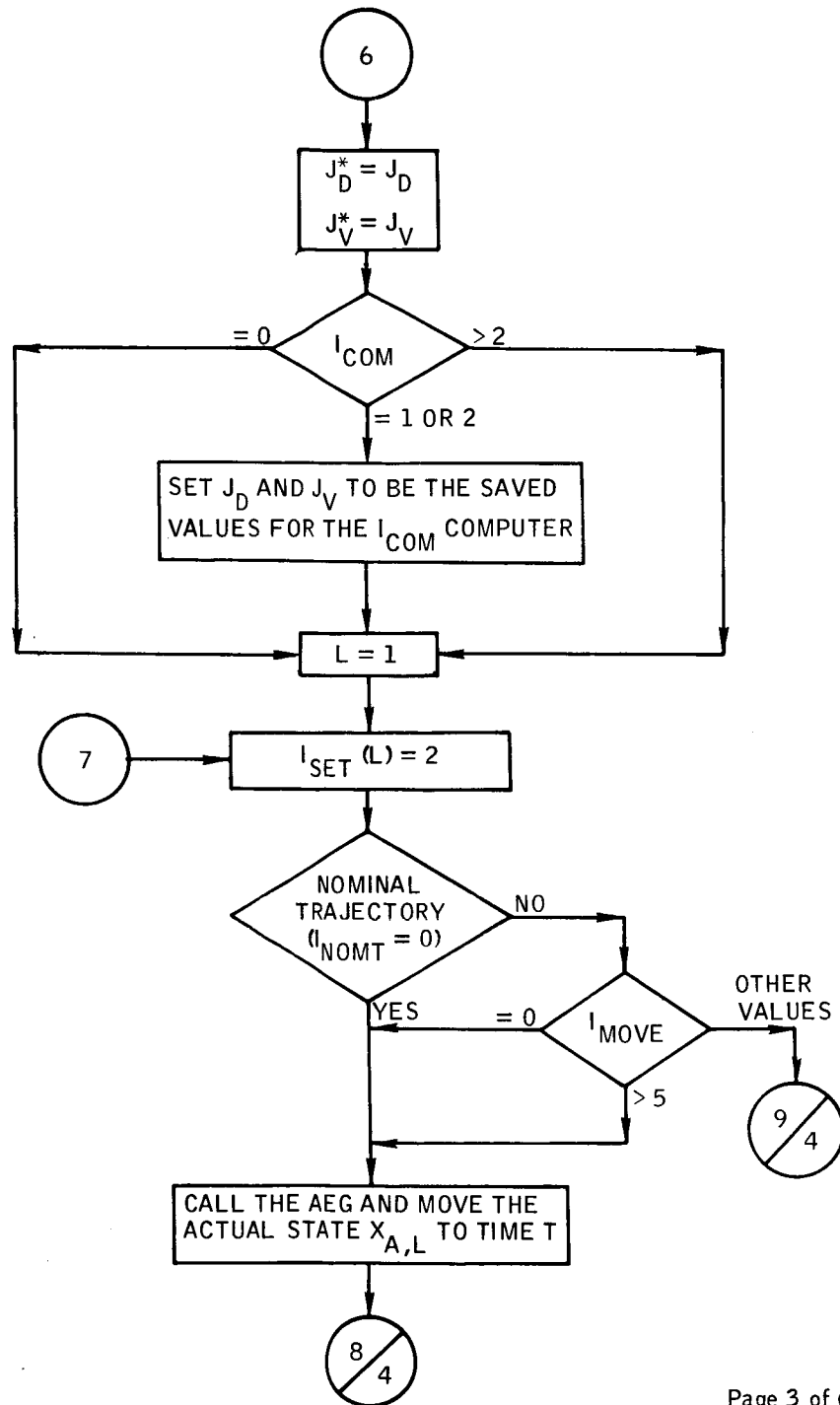


Figure B-70. - Continued.

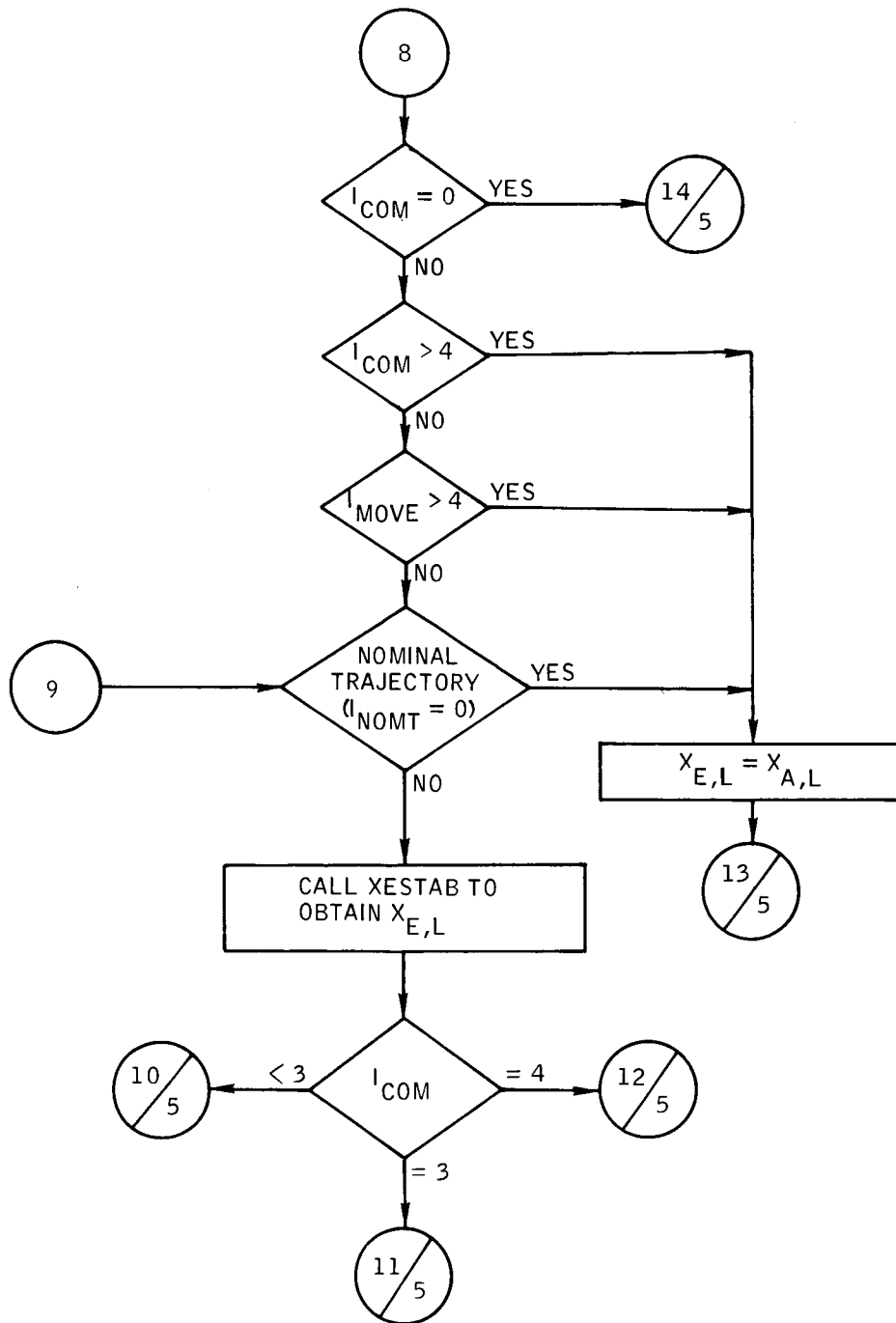


Figure B-70.- Continued.

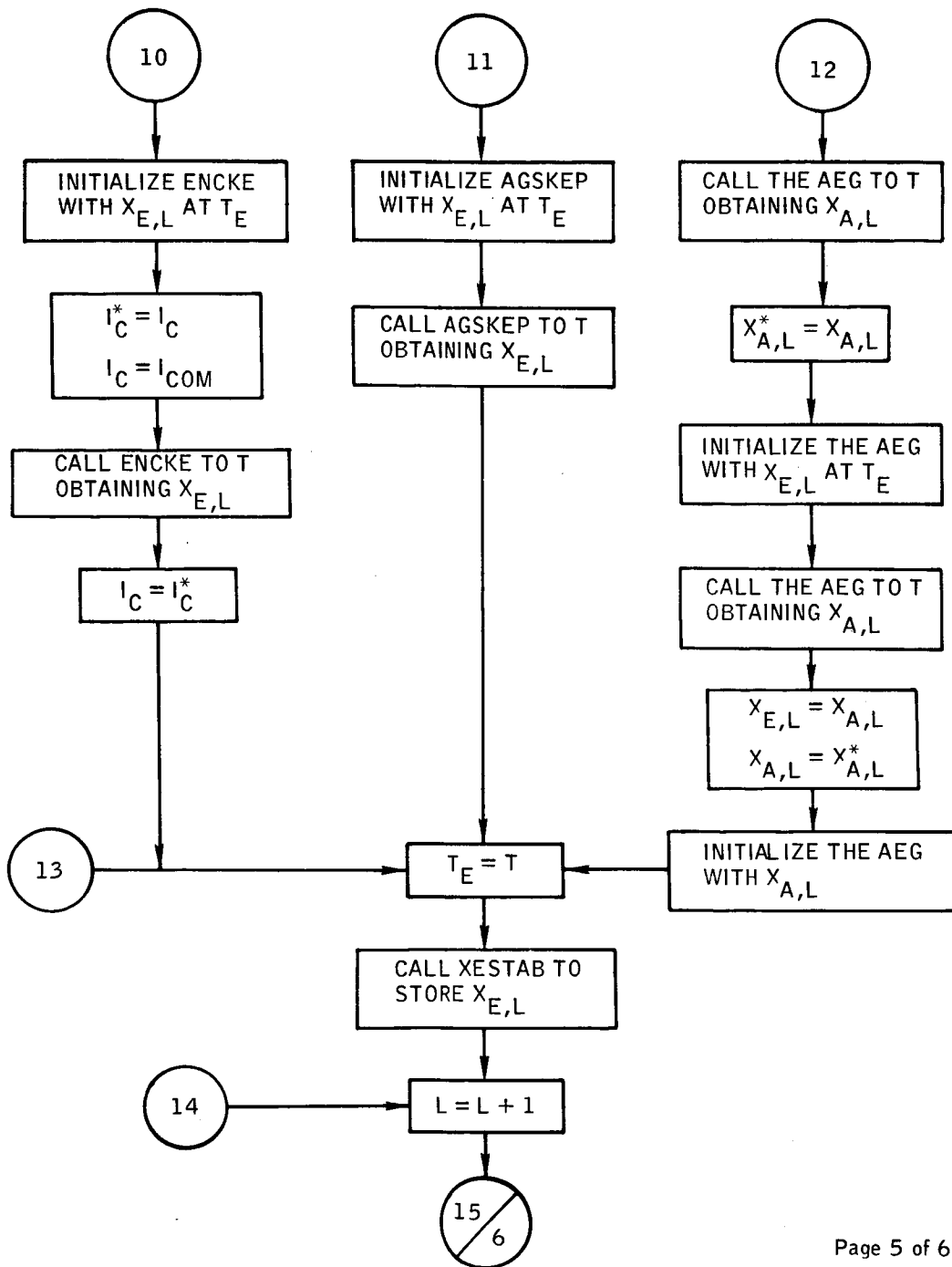
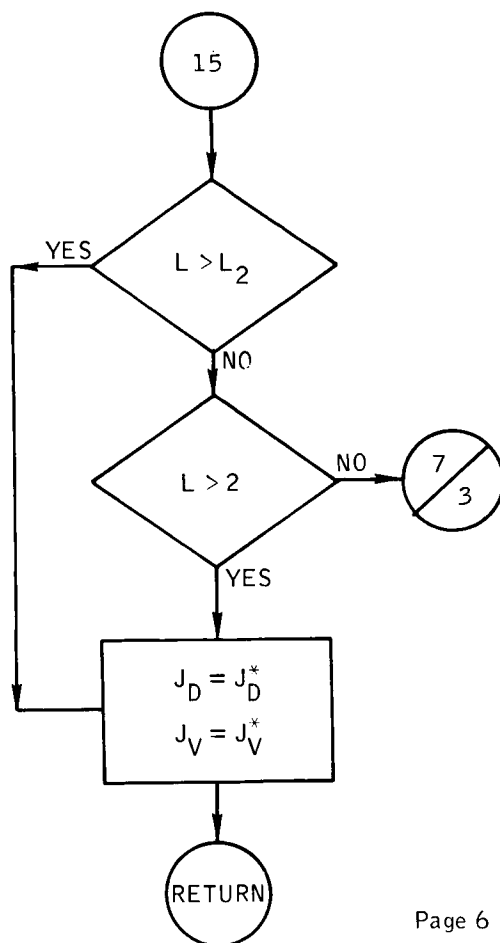


Figure B-70. - Continued.



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Figure B-70.- Concluded.

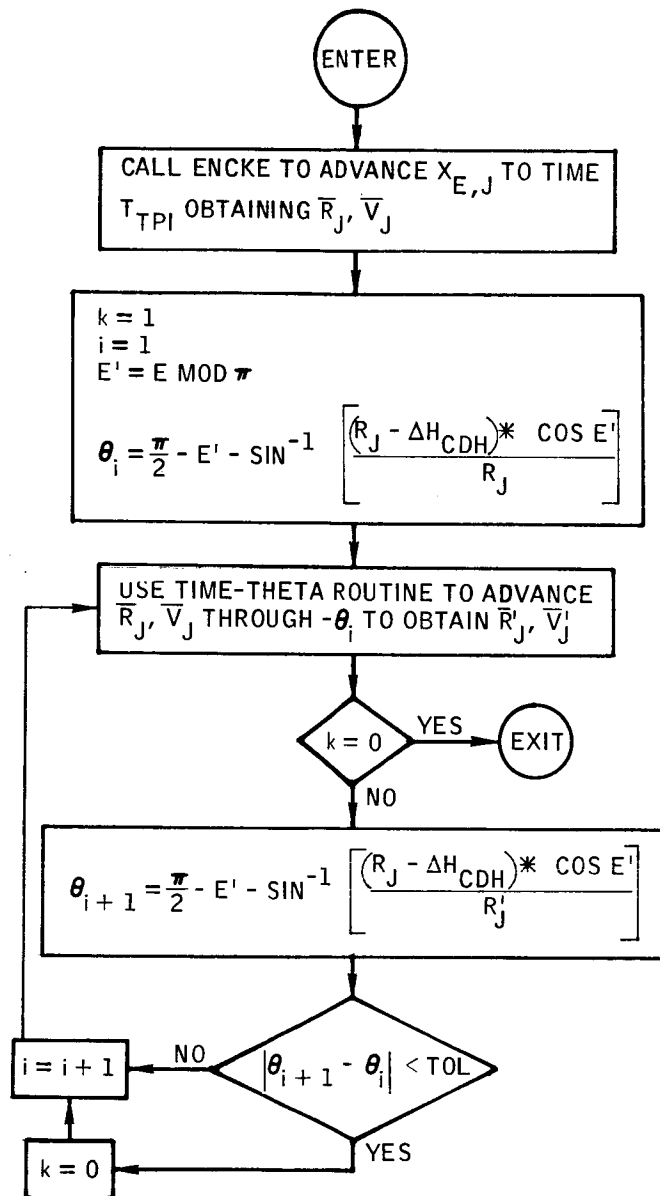


Figure B-71.- Flow chart of subroutine QRDTPI.



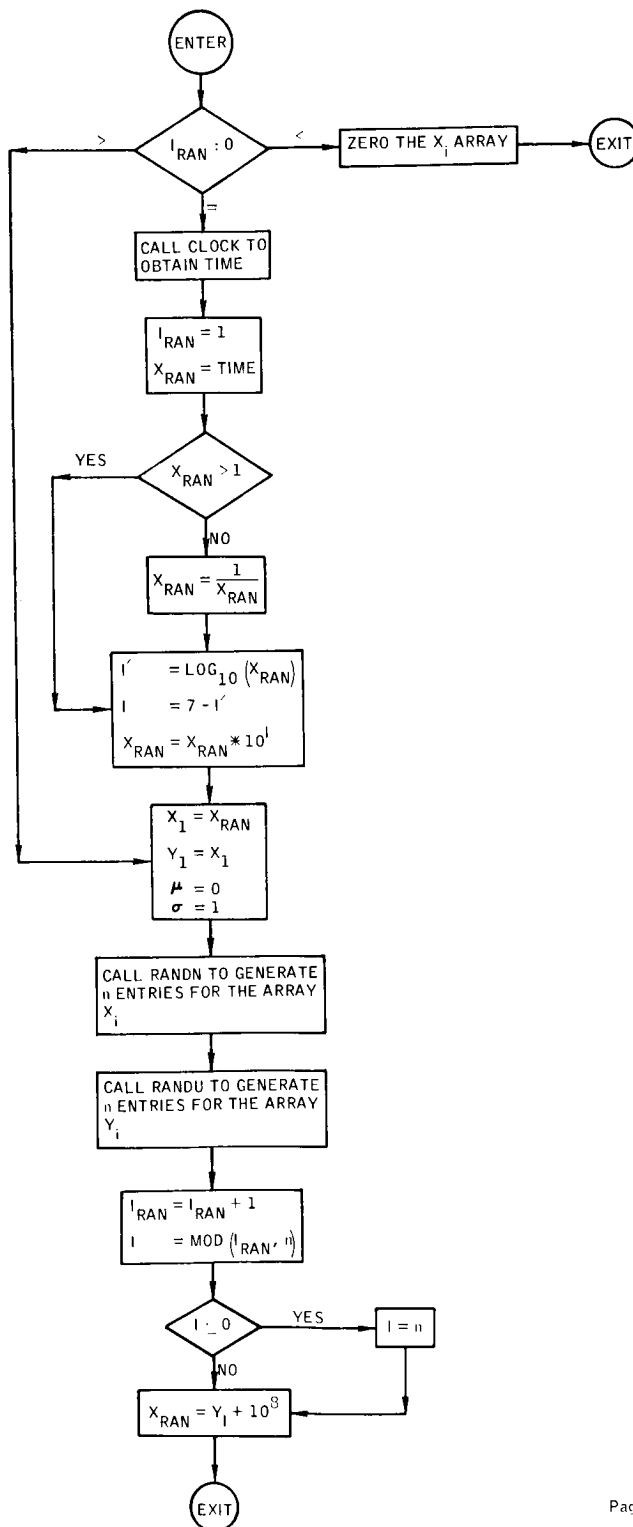


Figure B-72.- Flow chart of subroutine RANNO.

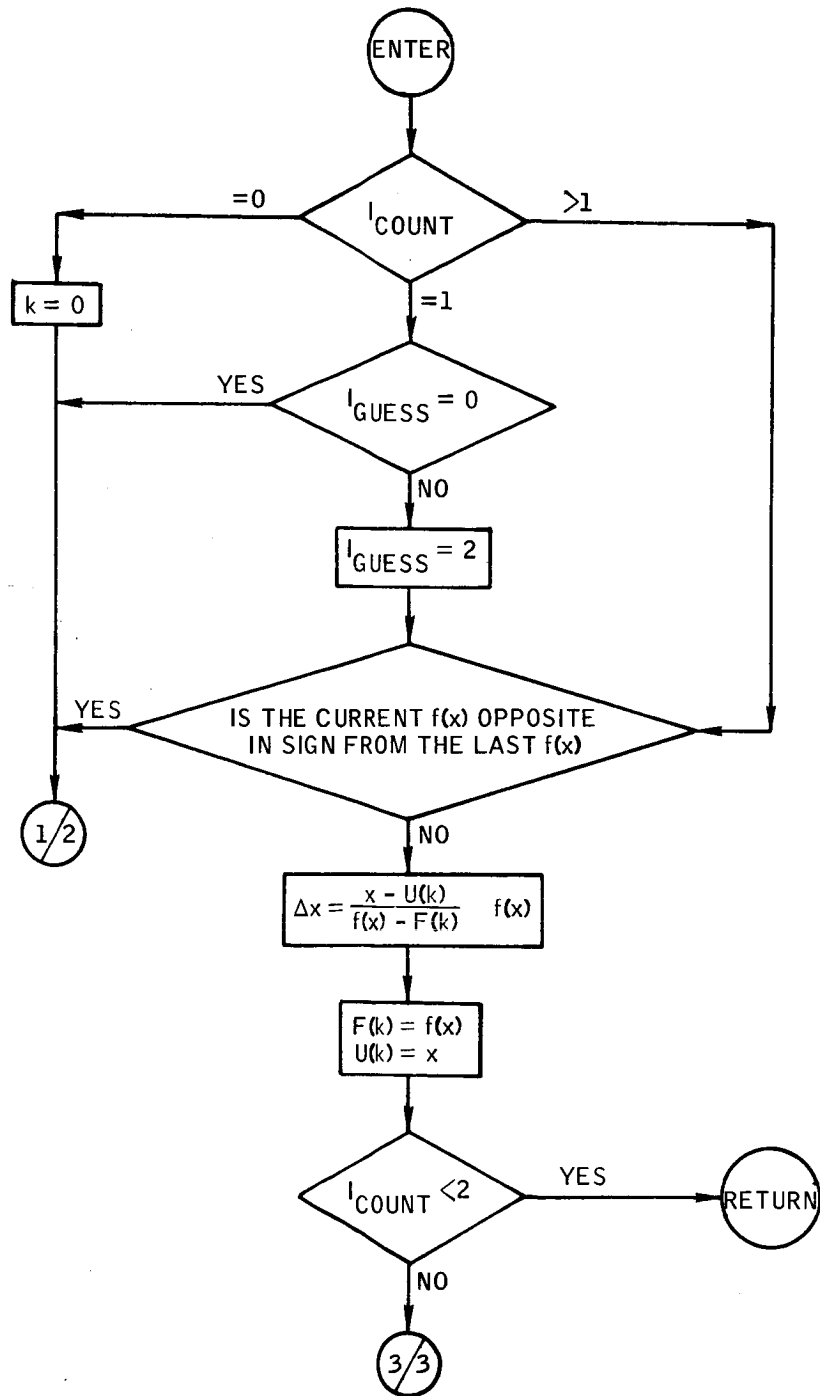


Figure B-73.- Flow chart for subroutine REGFAL.

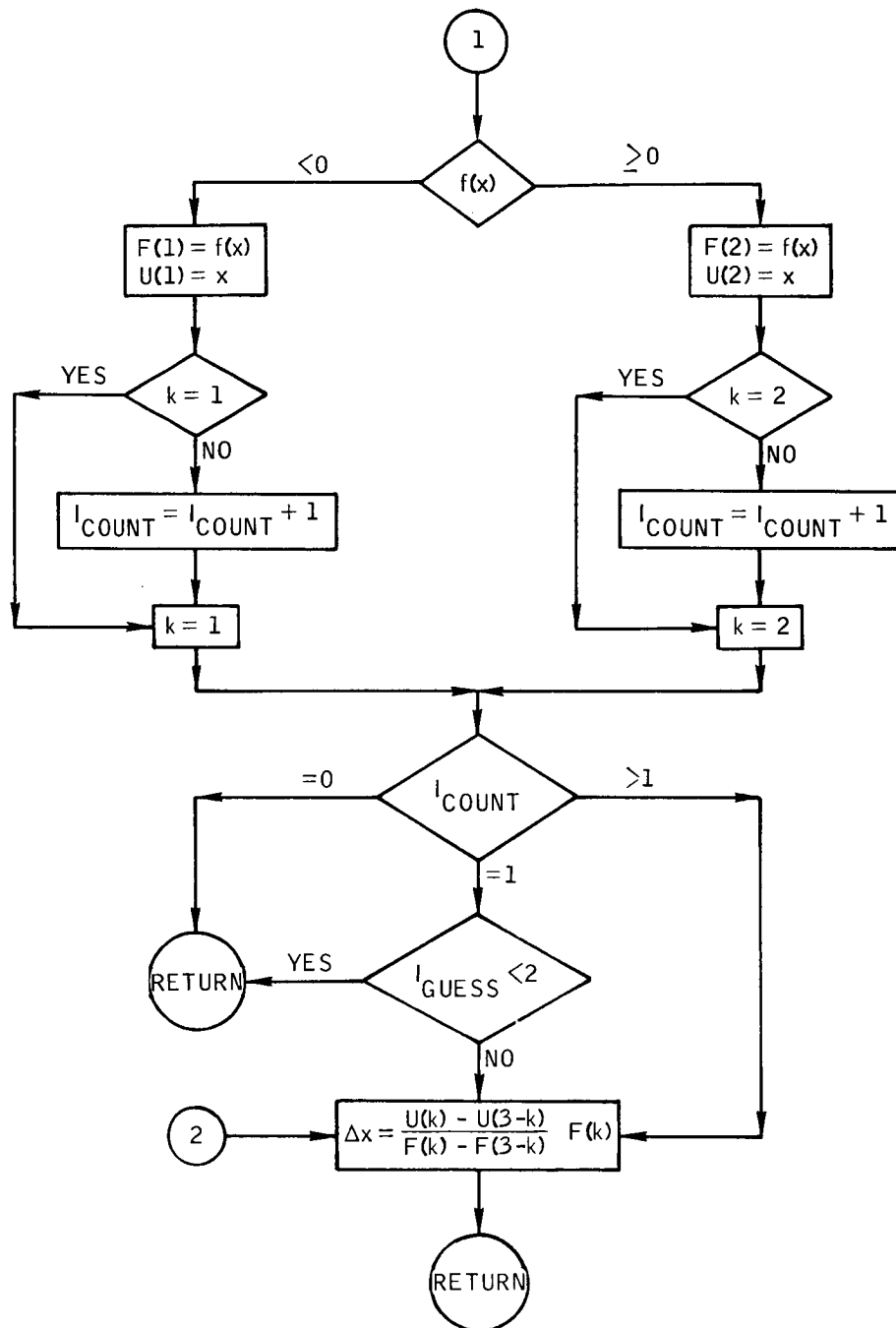


Figure B-73.- Continued.

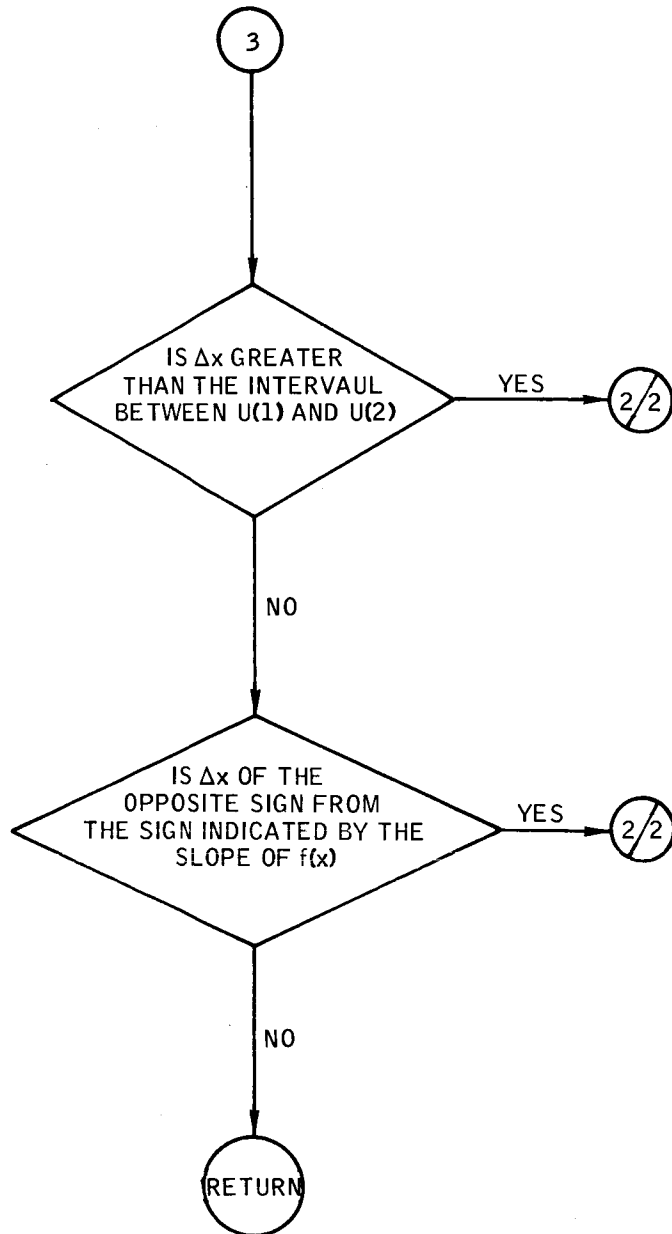


Figure B-73.- Concluded.

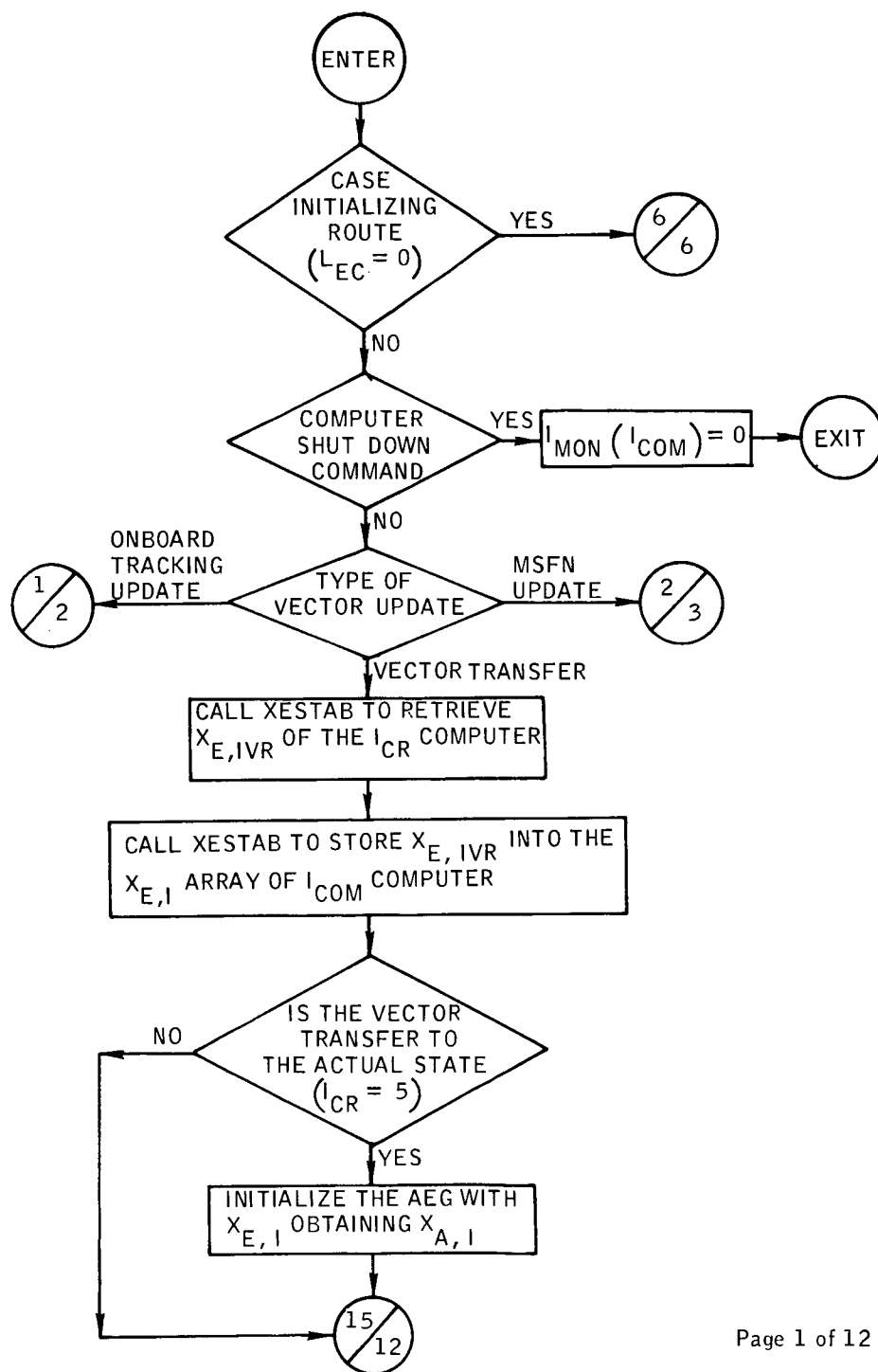


Figure B-74. - Flow chart of subroutine REPLAC.

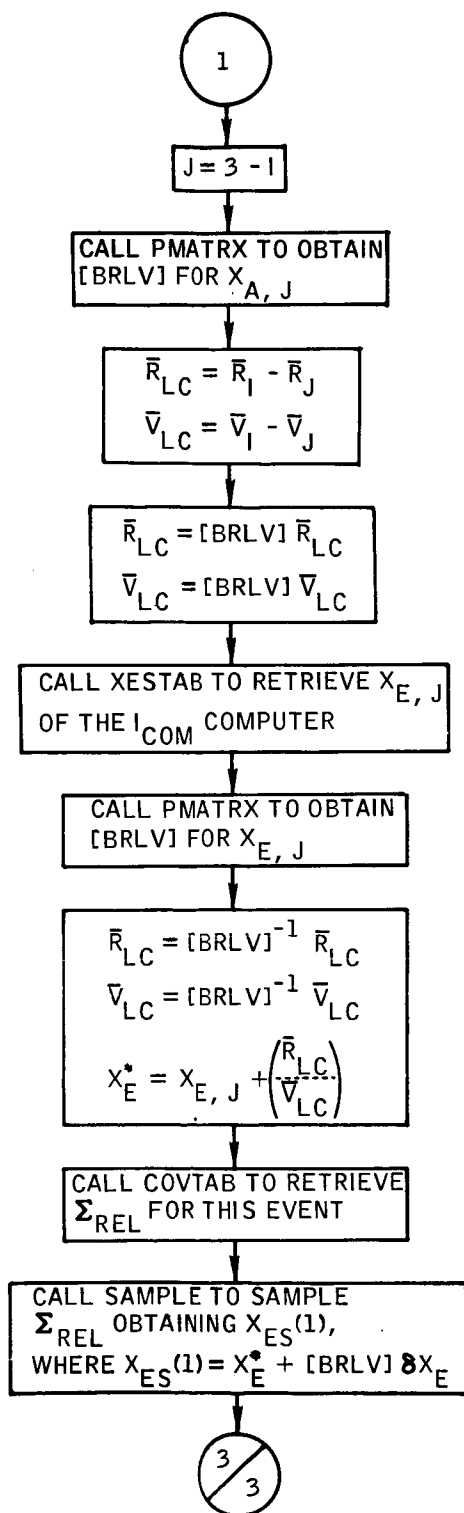


Figure B-74. - Continued.

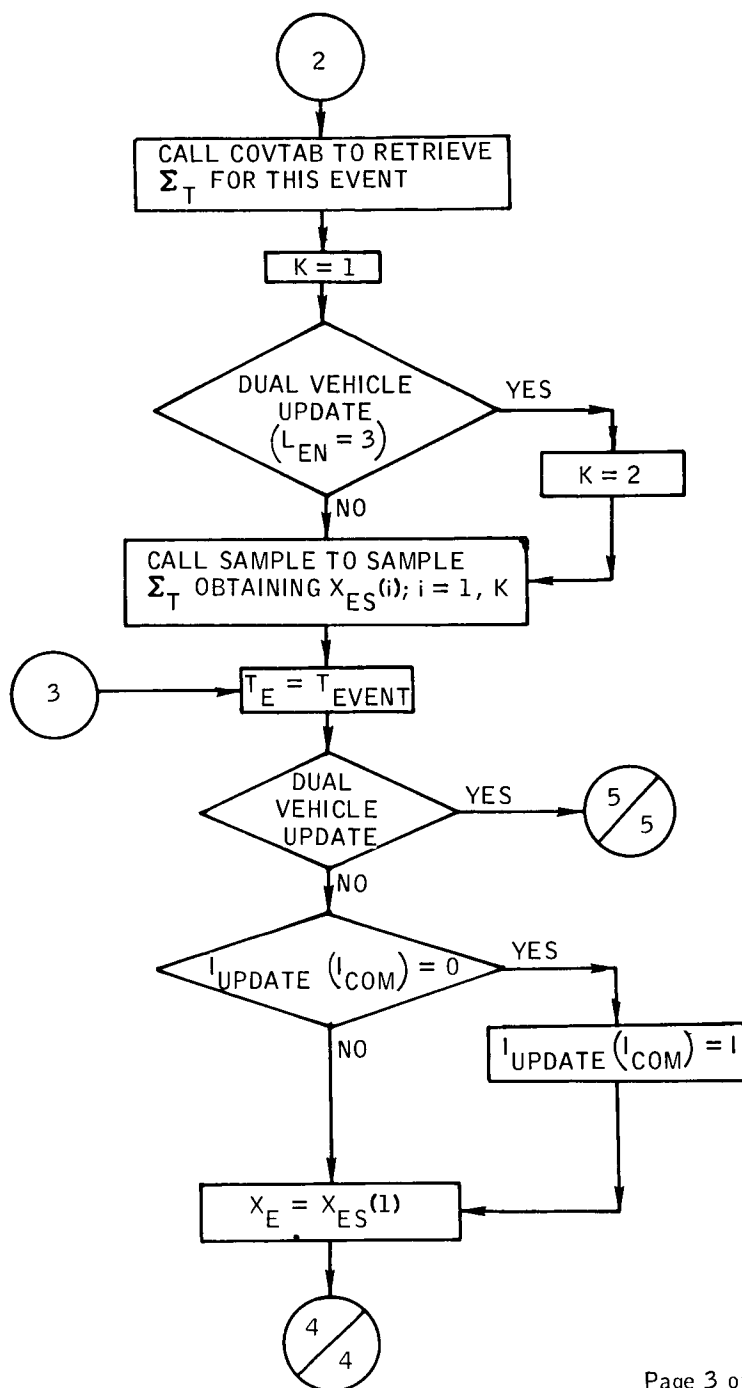


Figure B-74. - Continued.

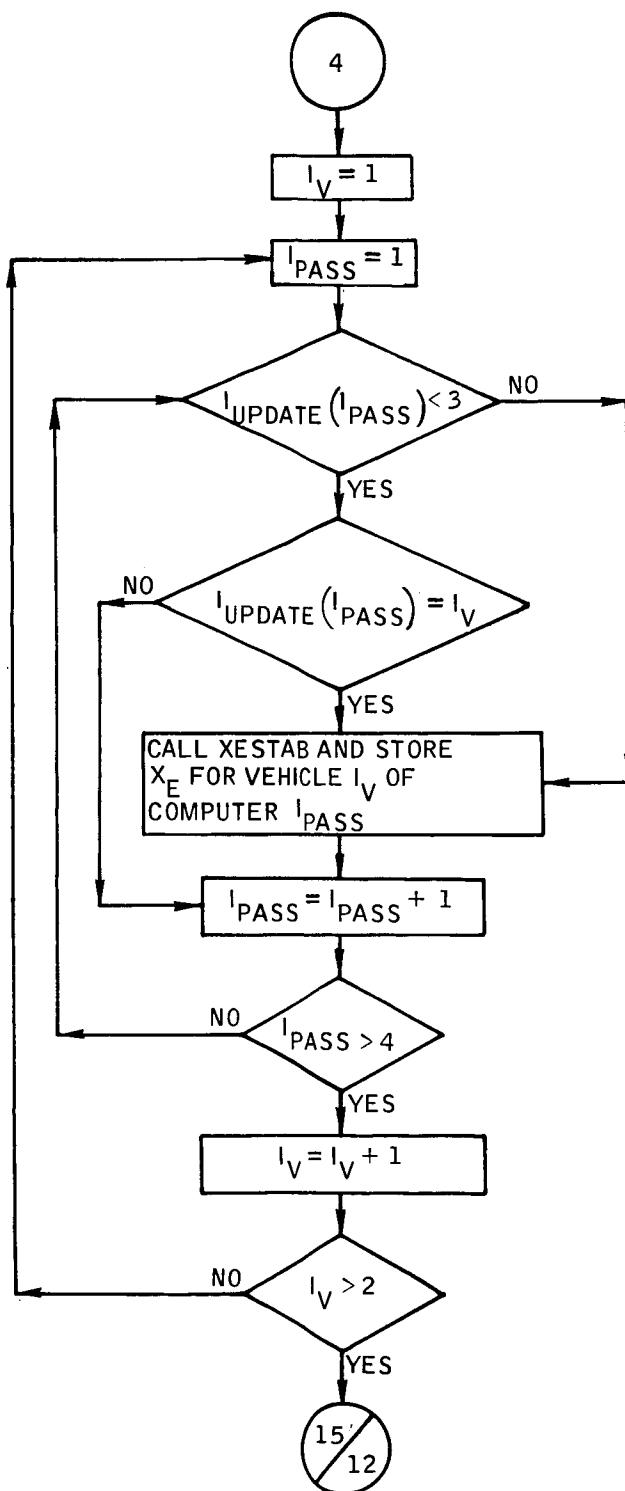


Figure B-74.- Continued.



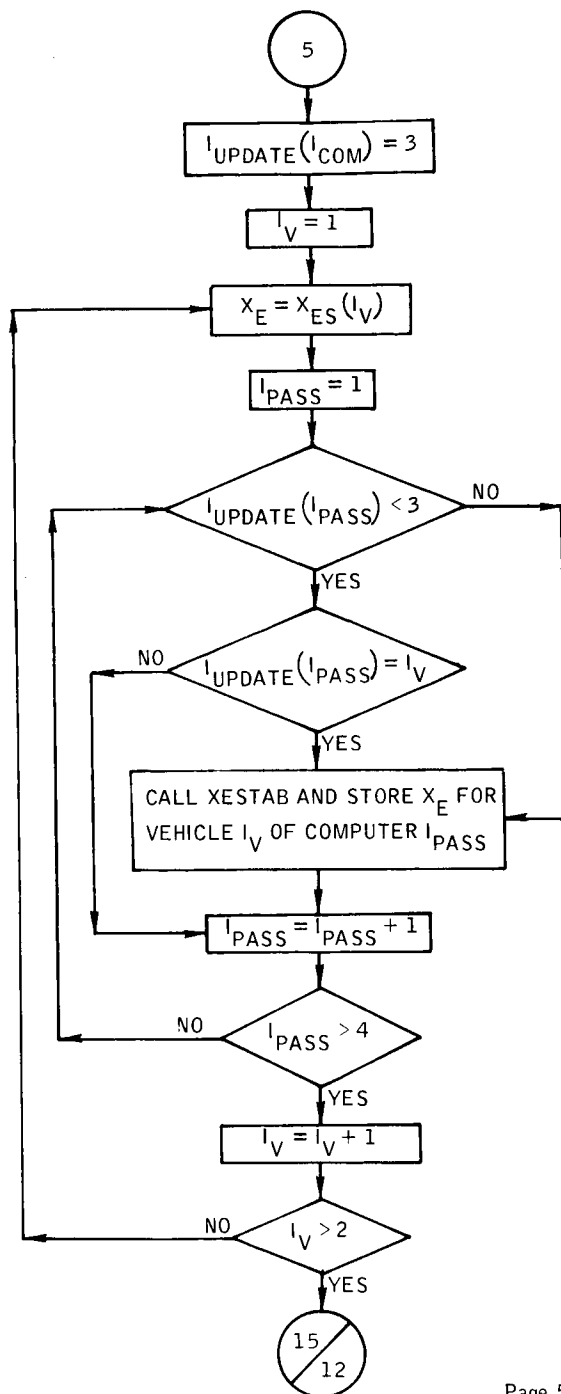
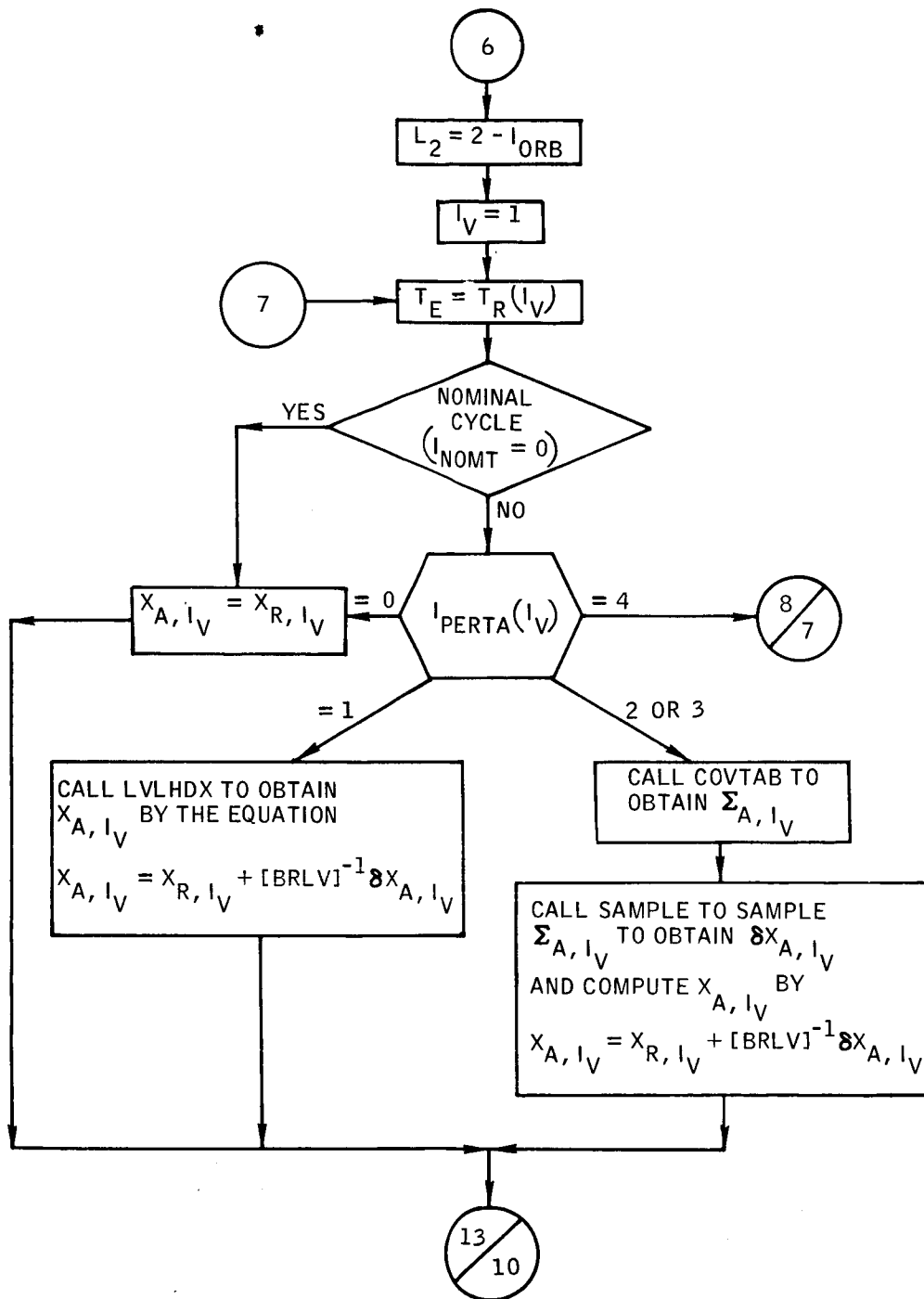


Figure B-74. - Continued.



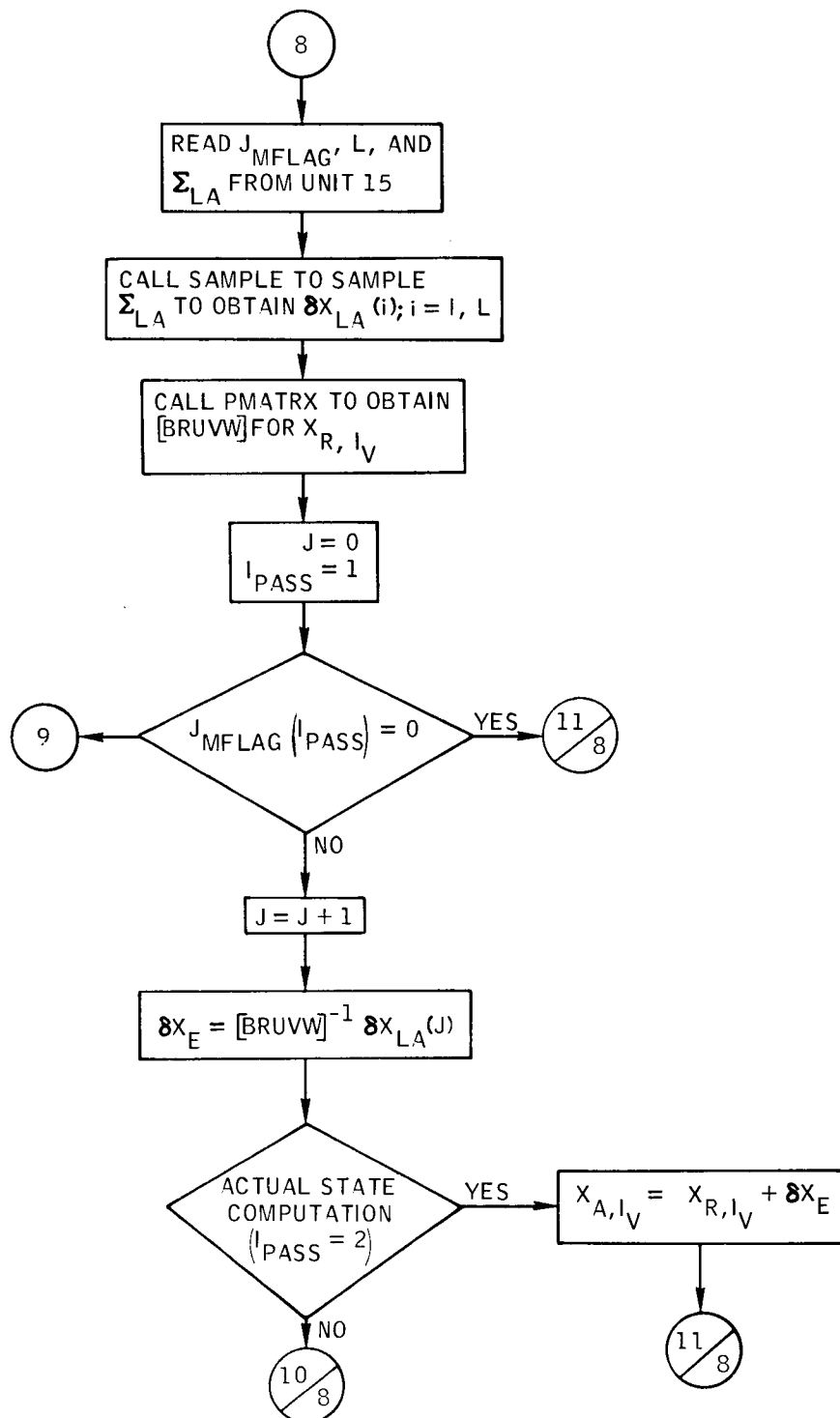


Figure B-74.- Continued.

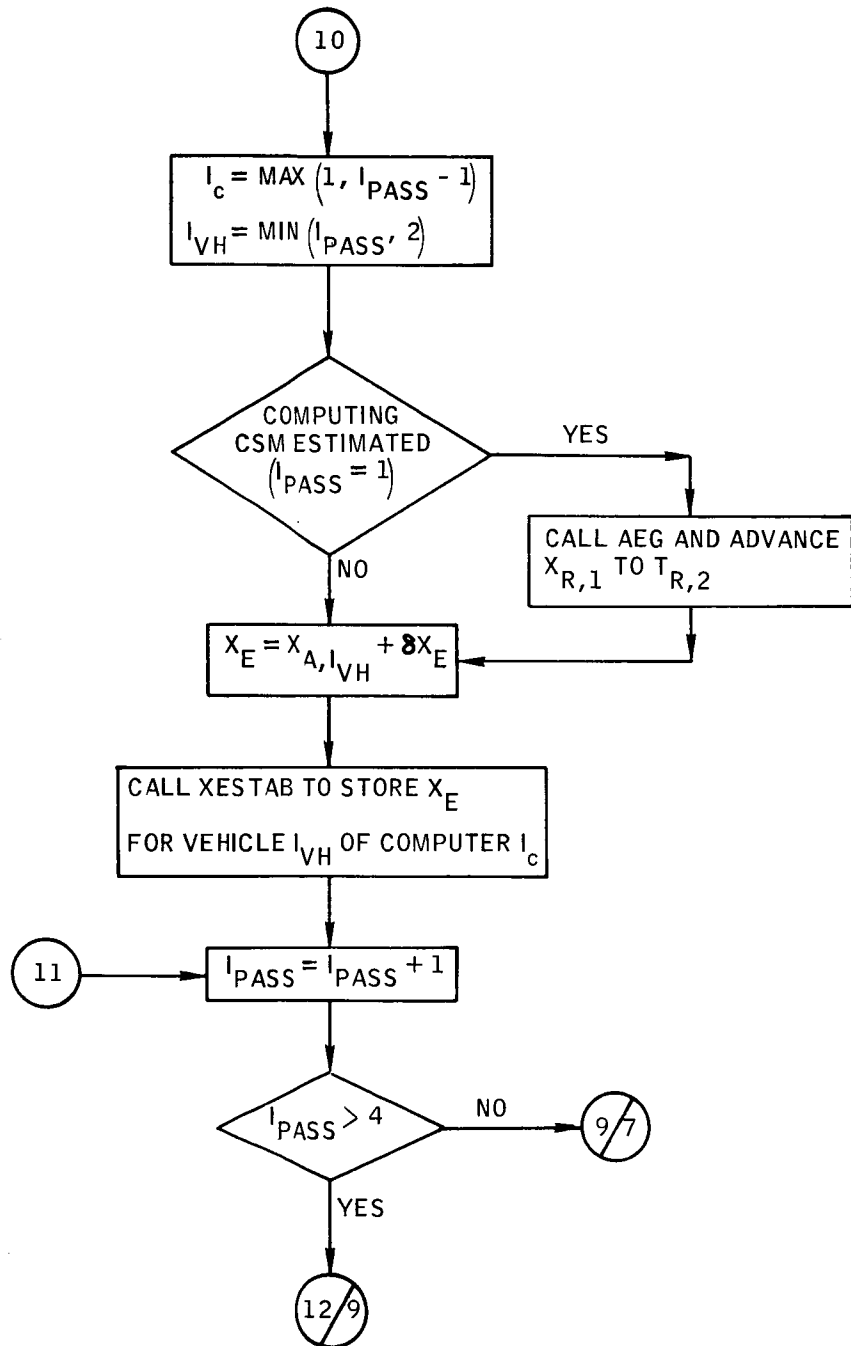


Figure B-74.- Continued.

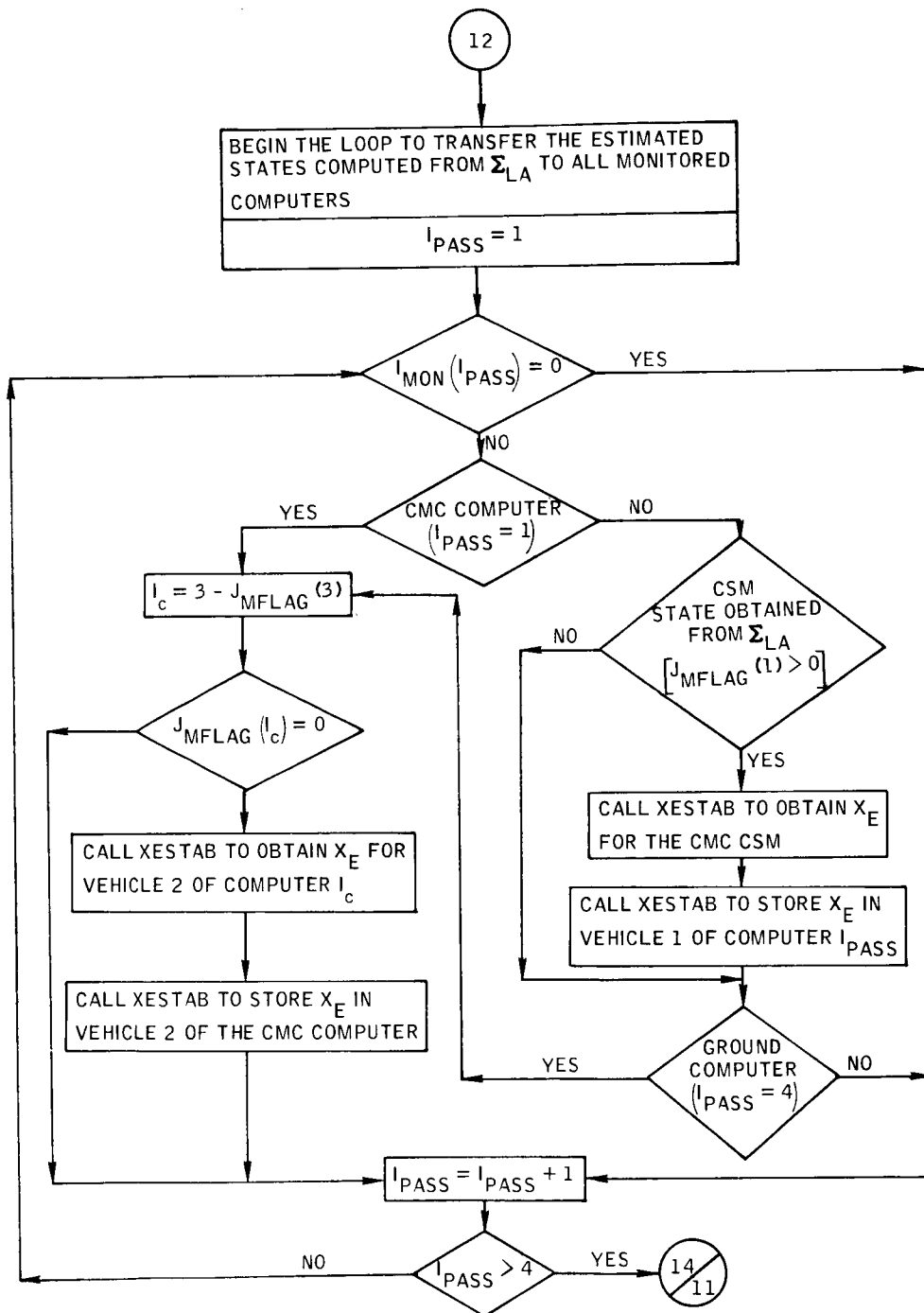


Figure B-74.- Continued.

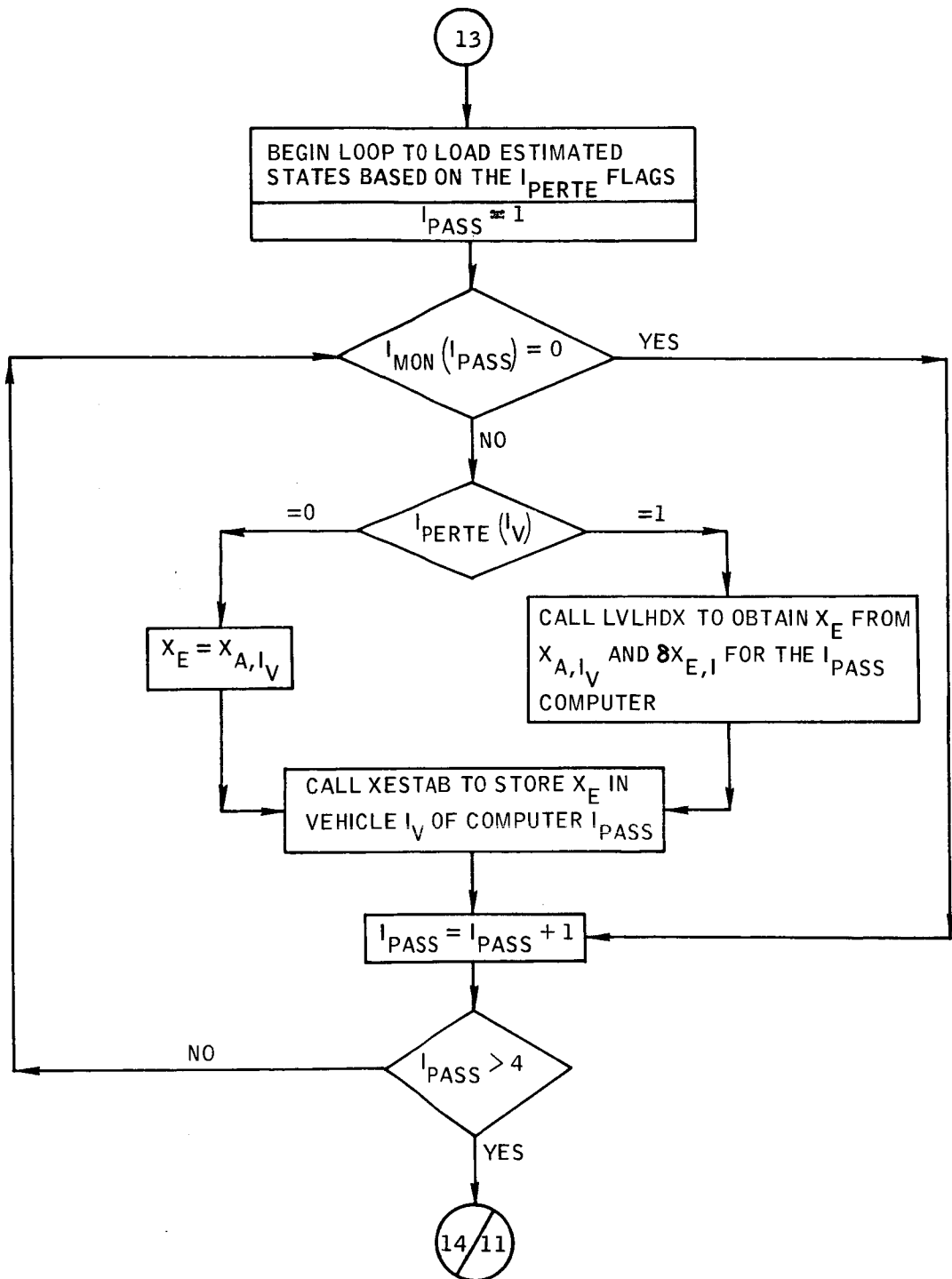


Figure B-74.- Continued.

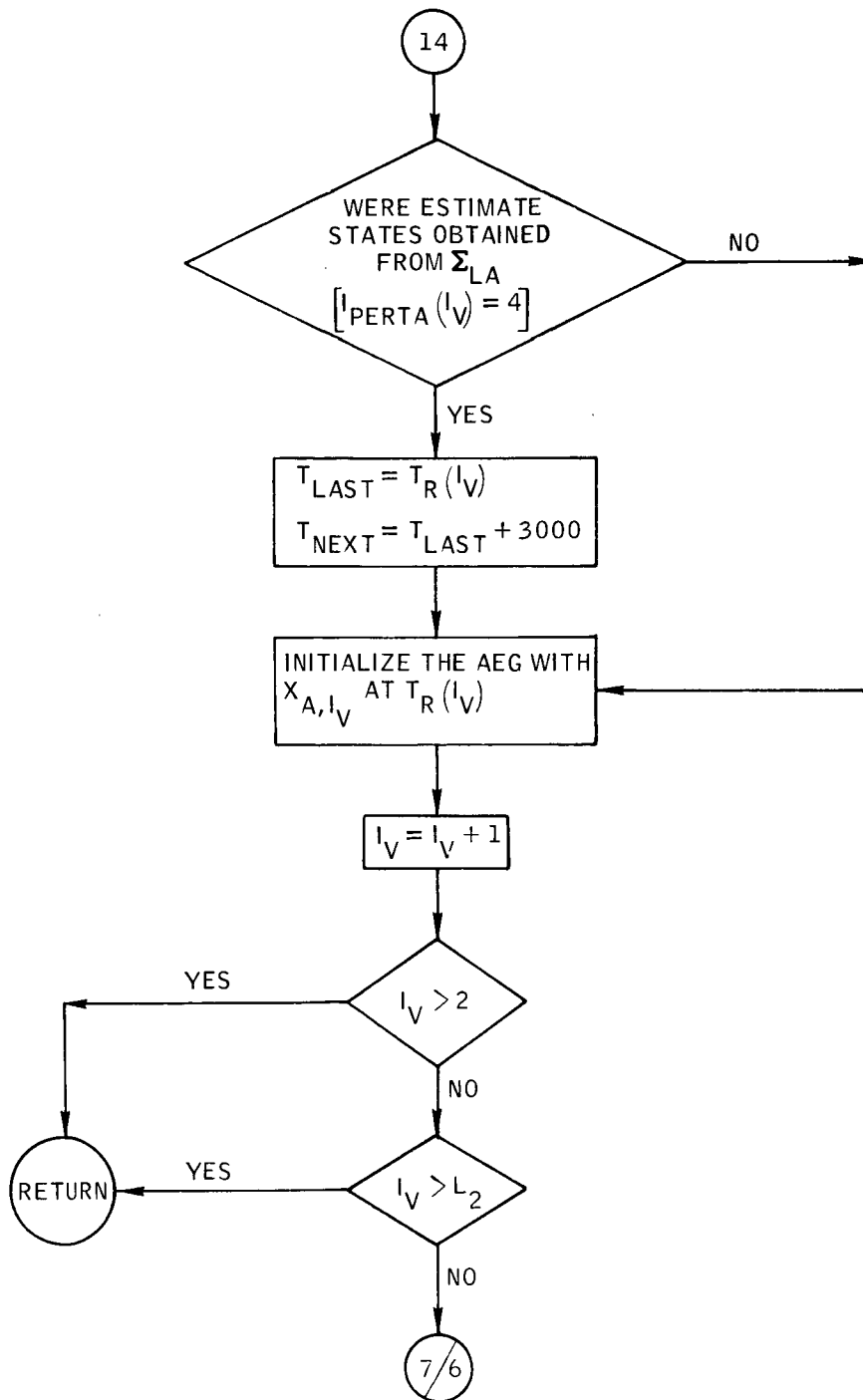


Figure 74.- Continued.

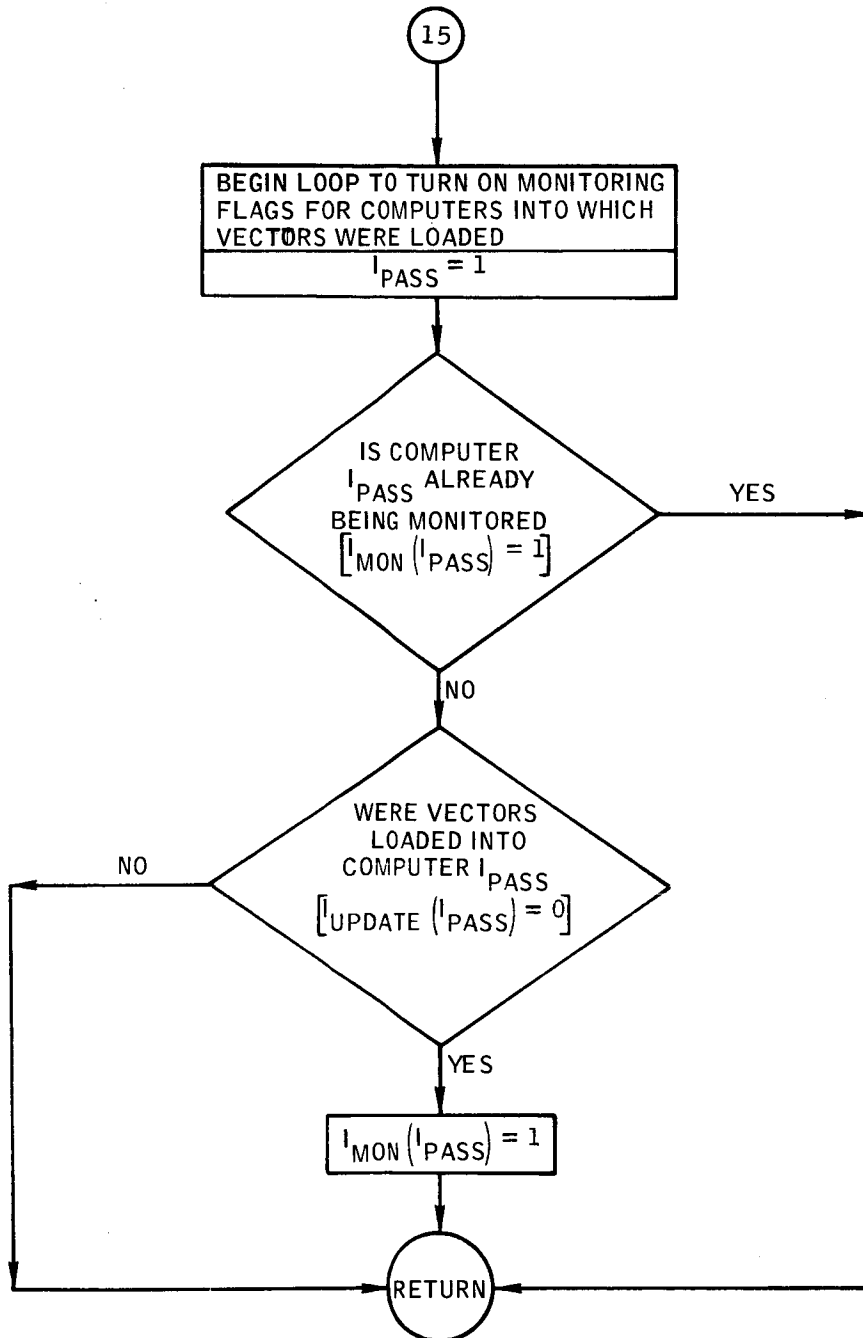


Figure B-74.- Concluded.



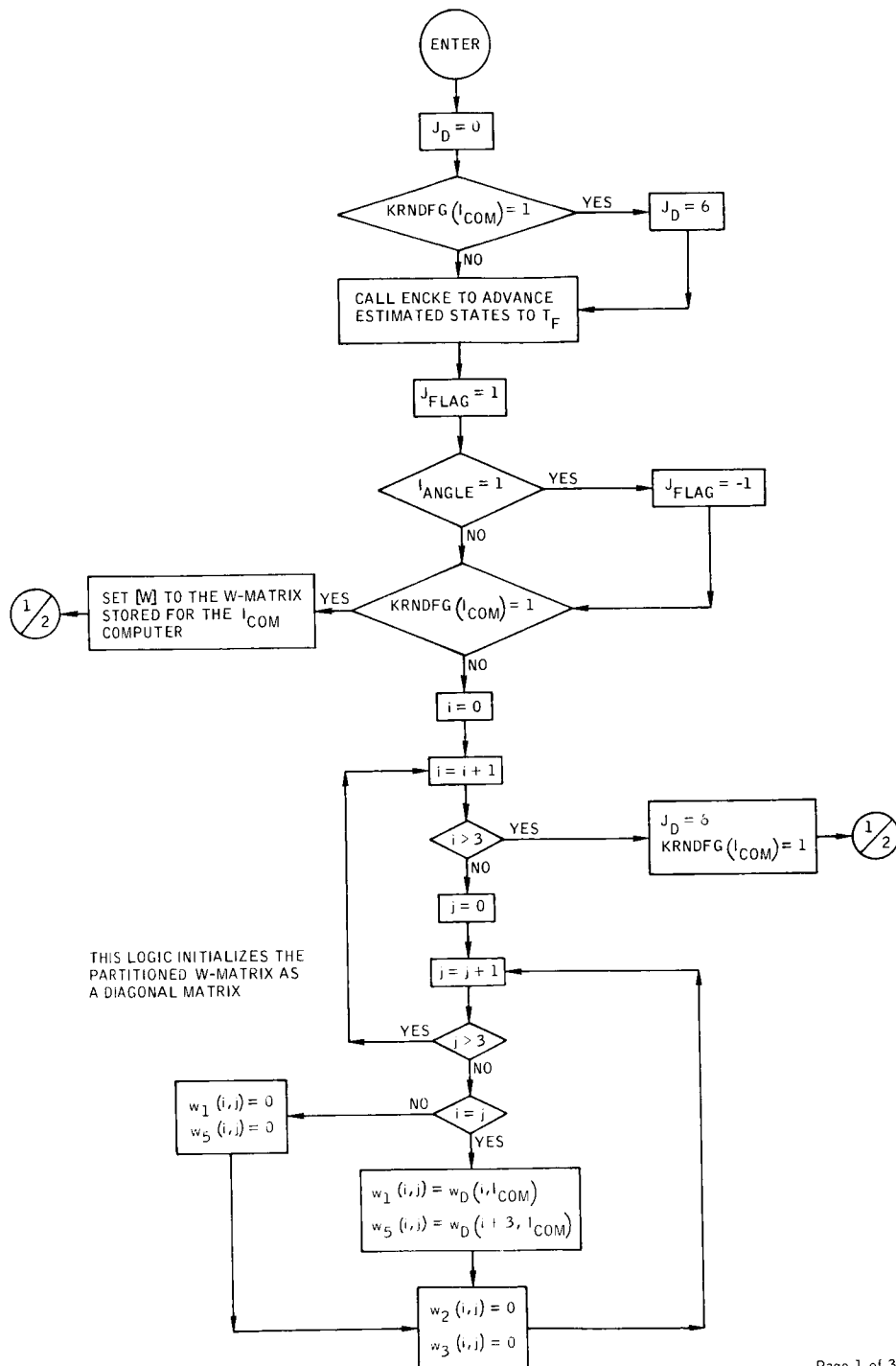


Figure B-75.- Flow chart of subroutine RNR.

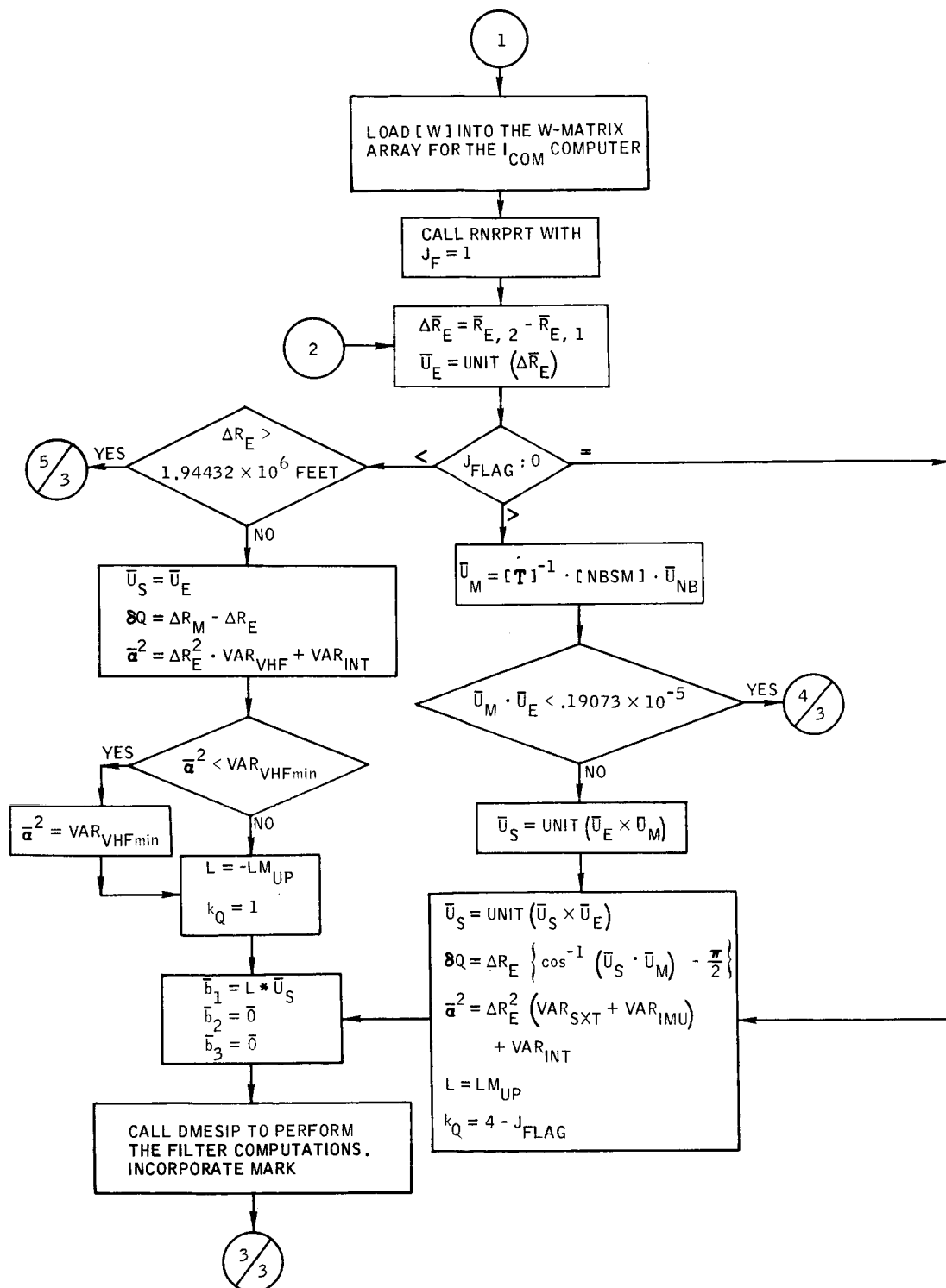
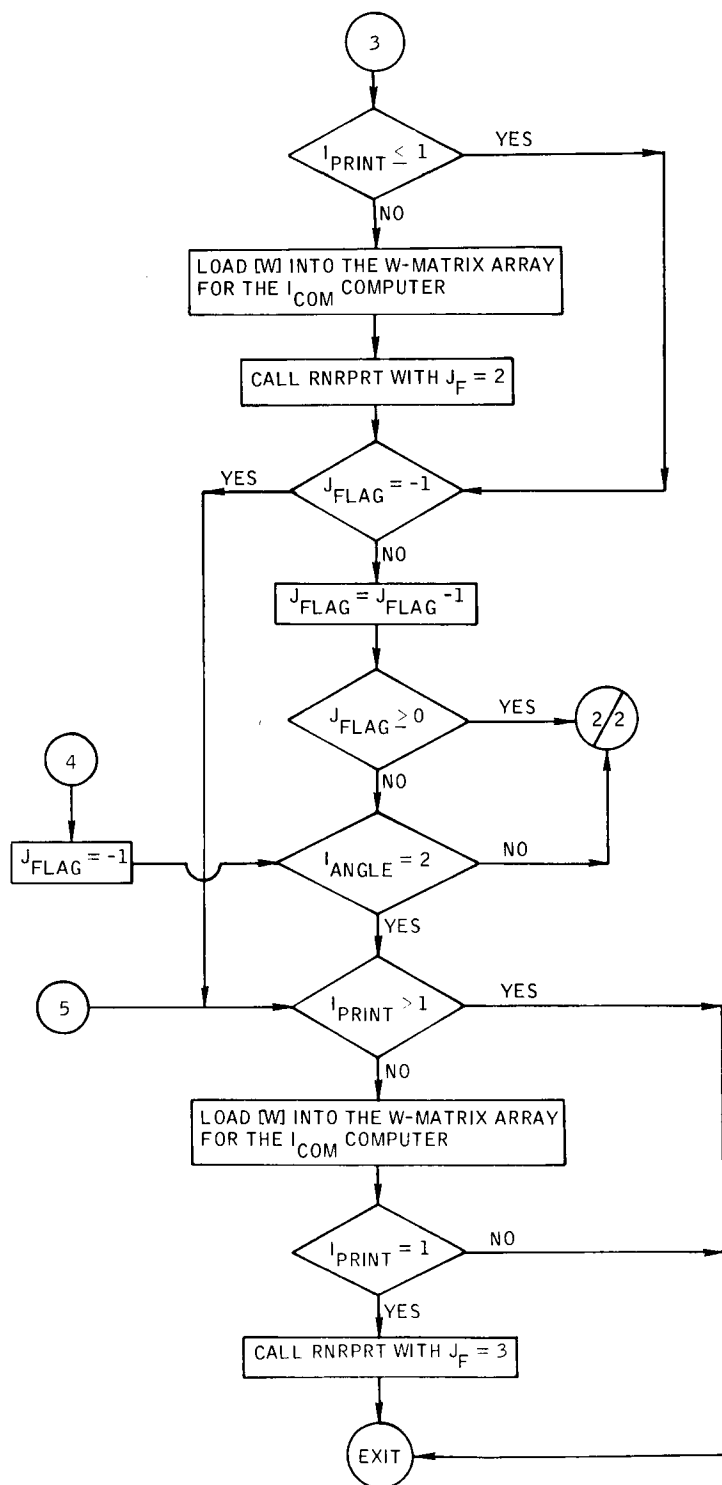


Figure B-75.- Continued.



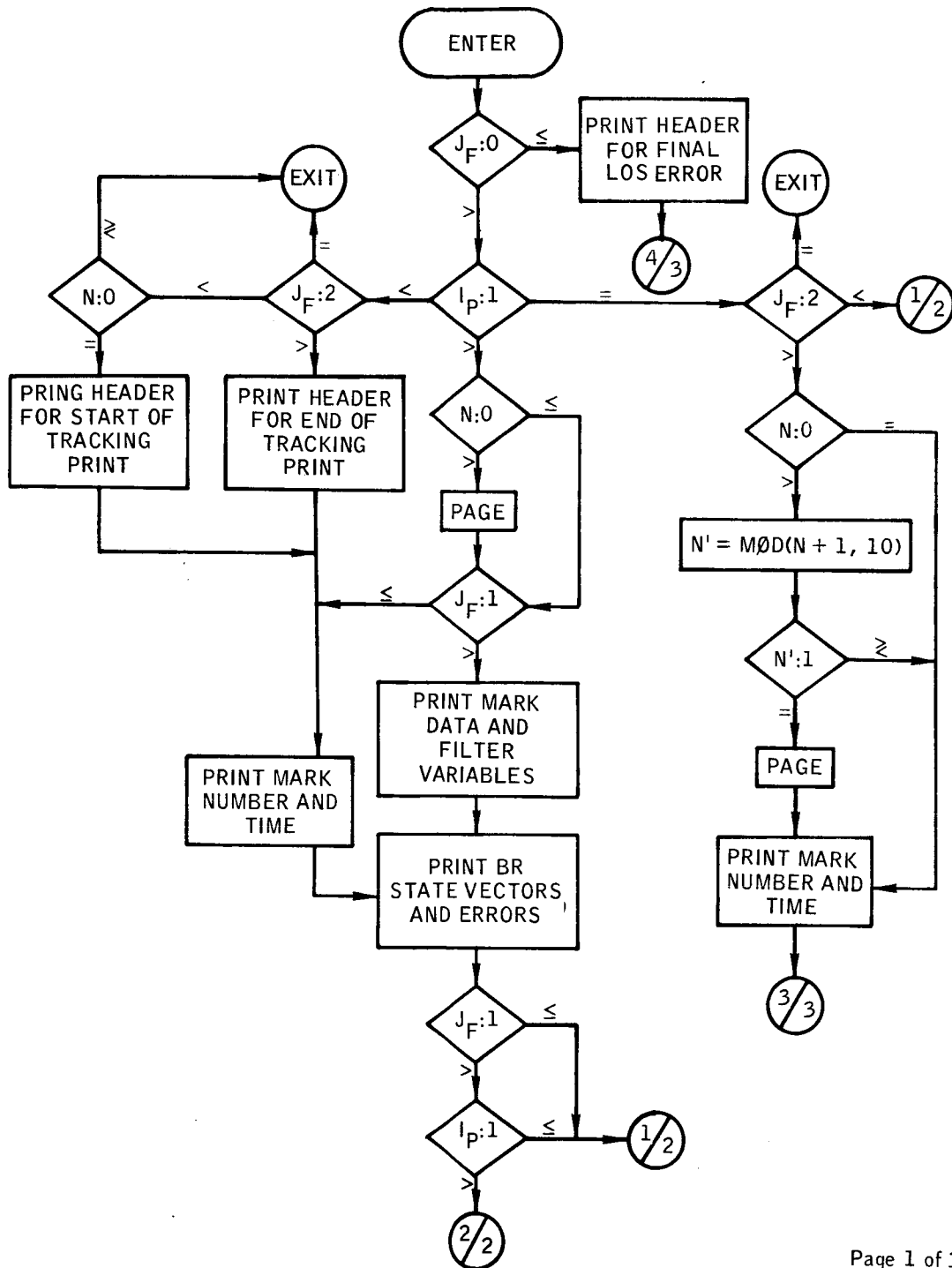
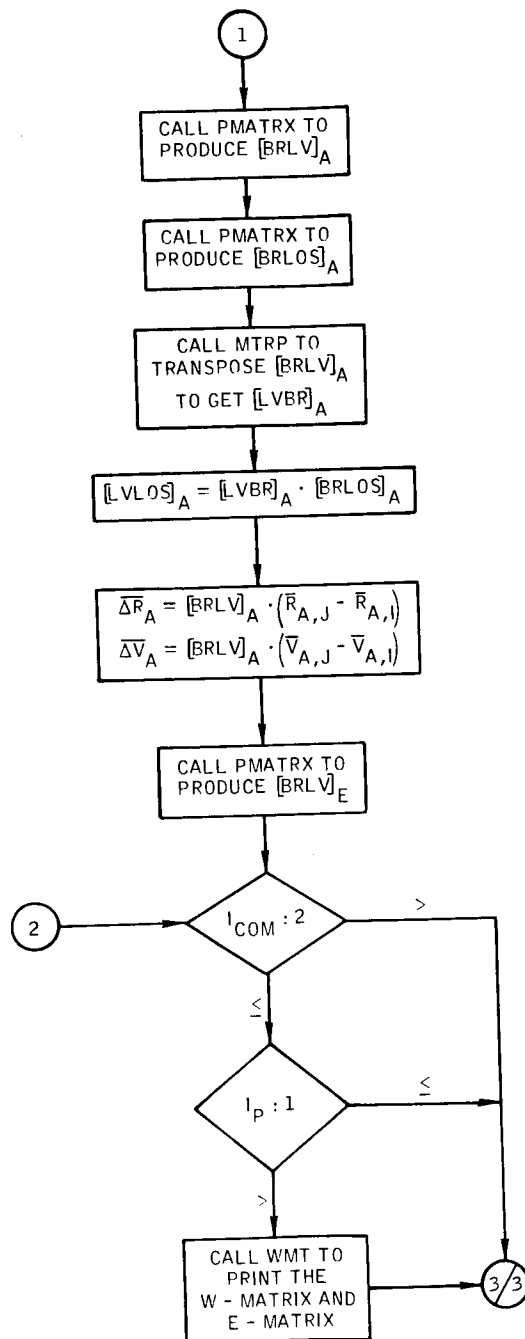


Figure B-76.- Flow chart of subroutine RNRPRT.



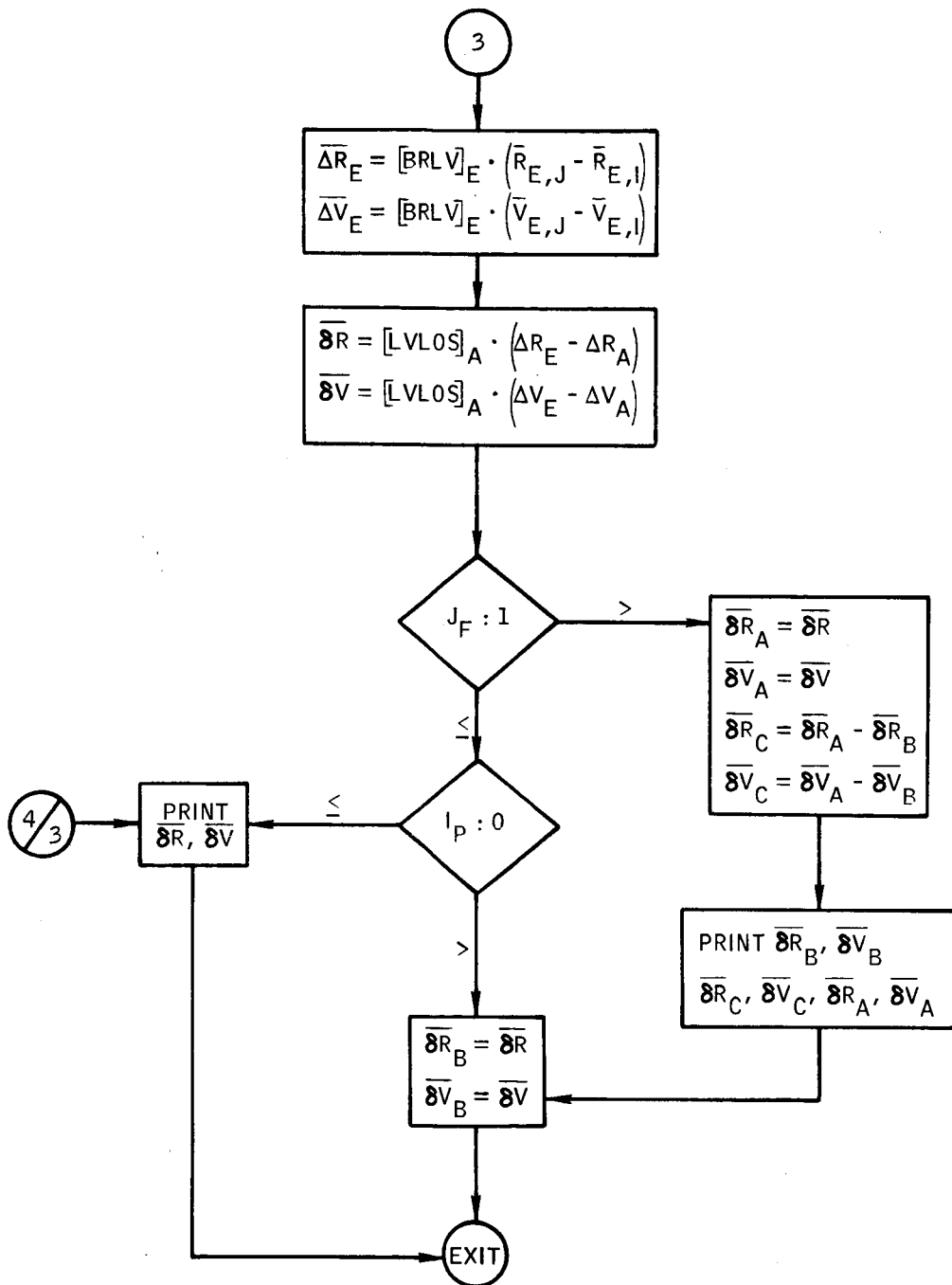


Figure B-76.- Concluded.

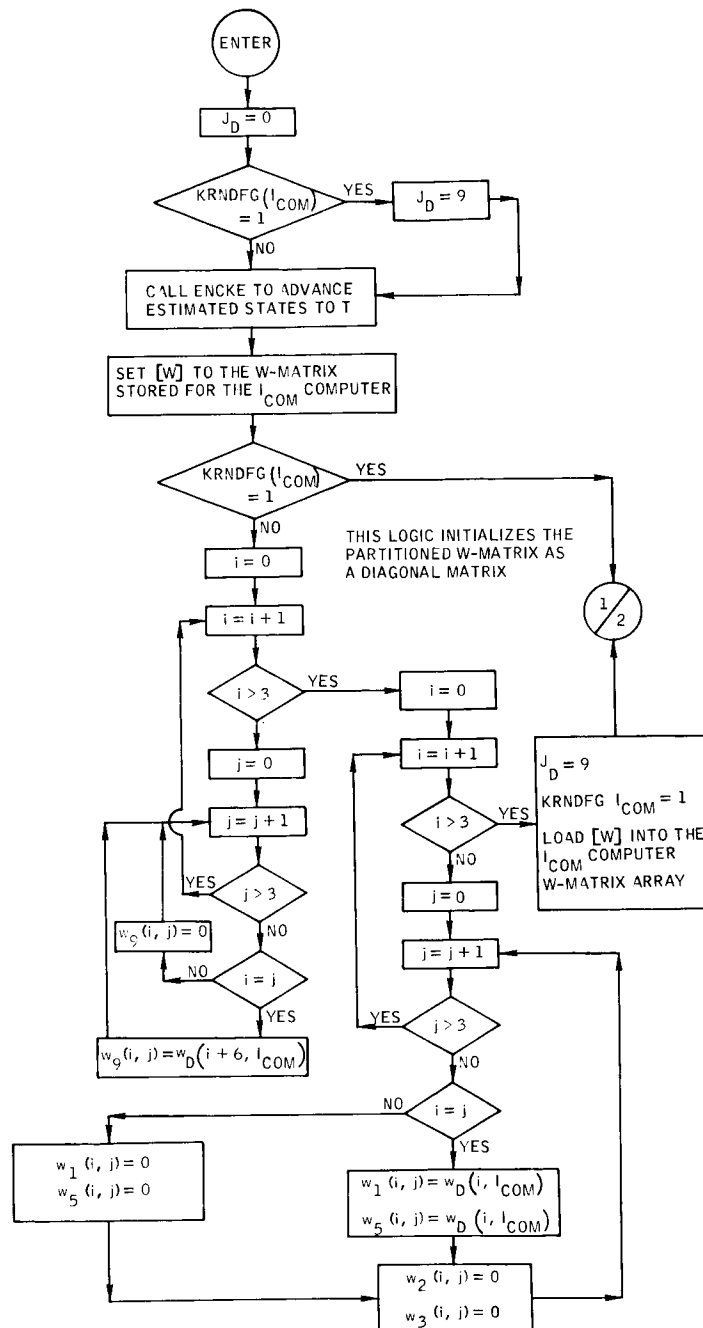


Figure B-77.- Flow chart of subroutine RR.

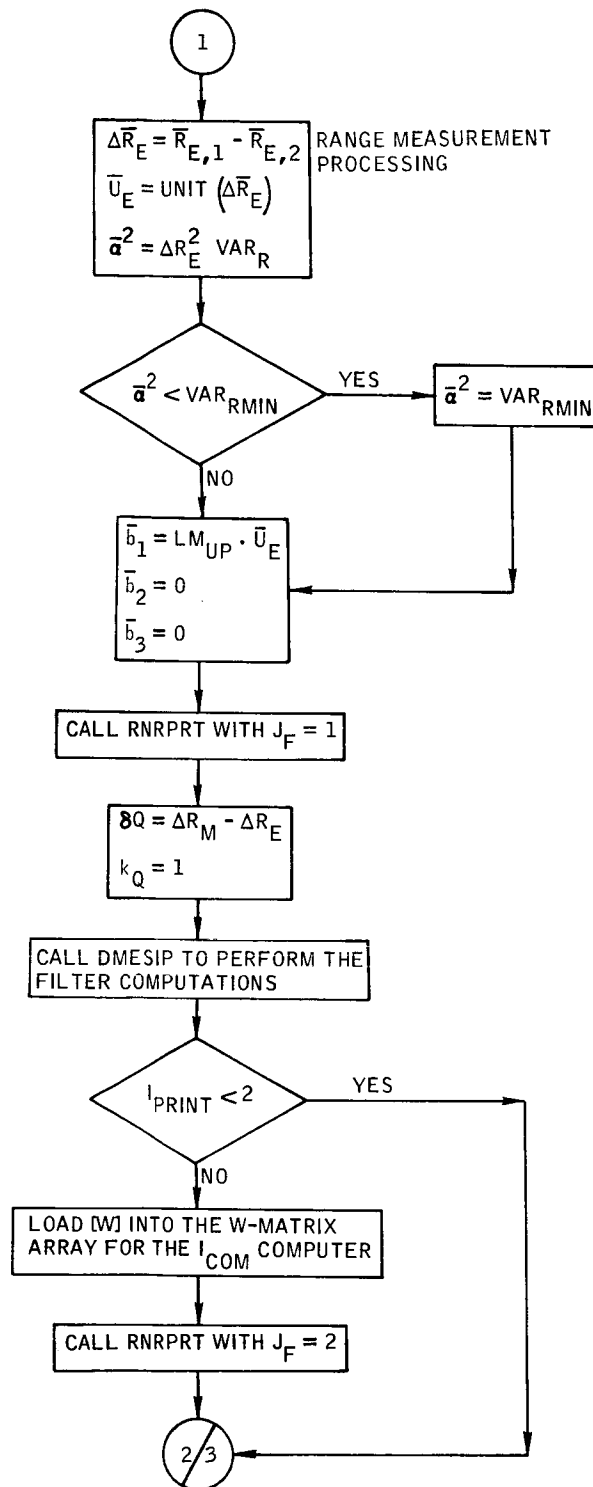
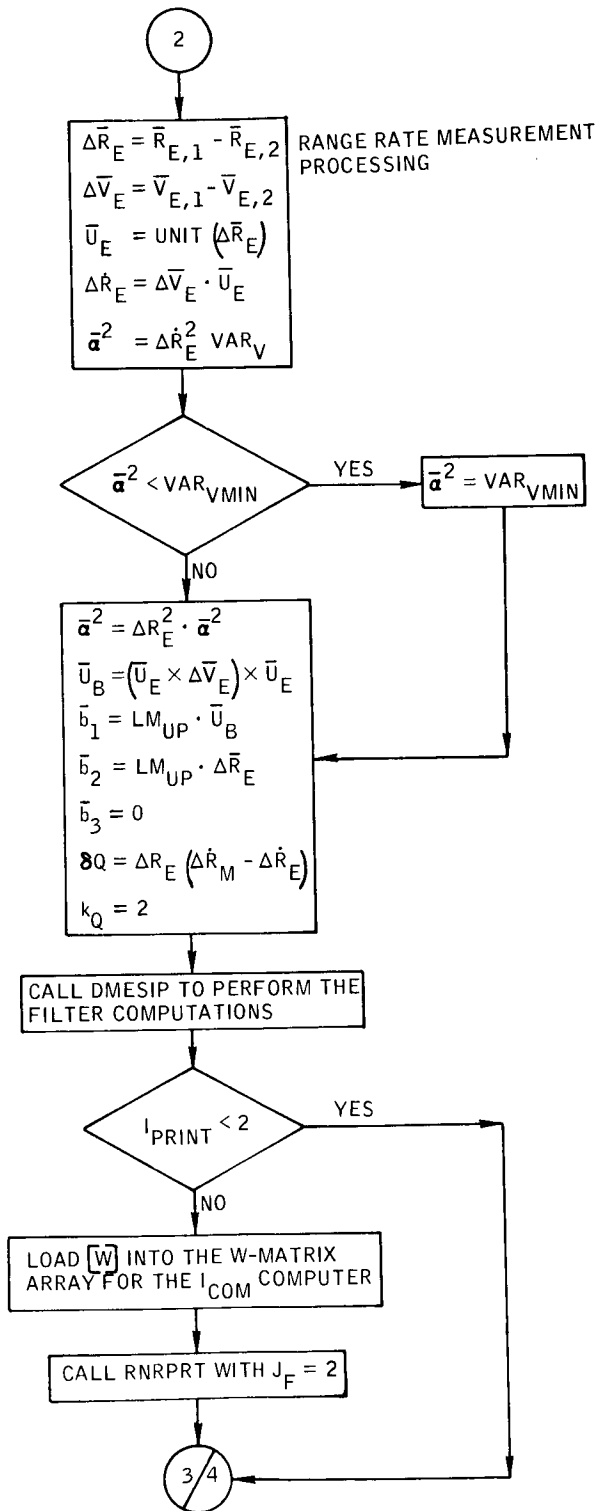
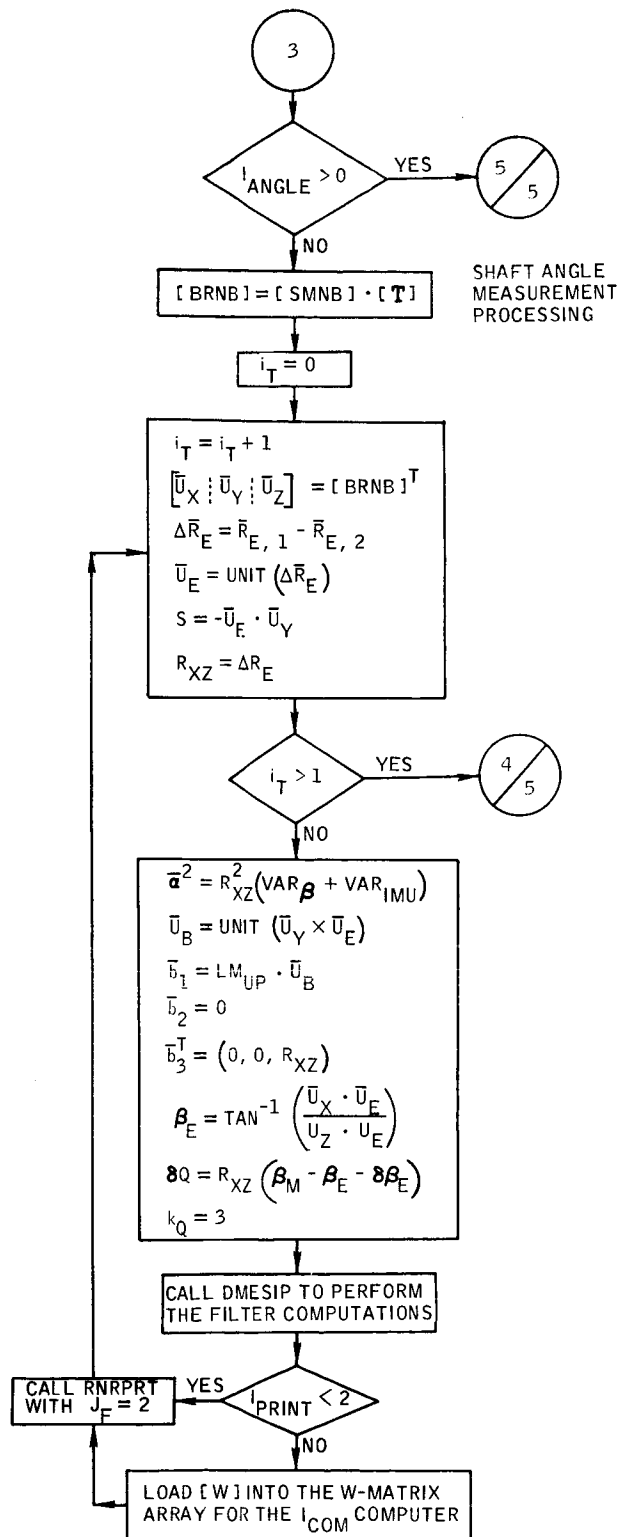


Figure B-77.- Continued.





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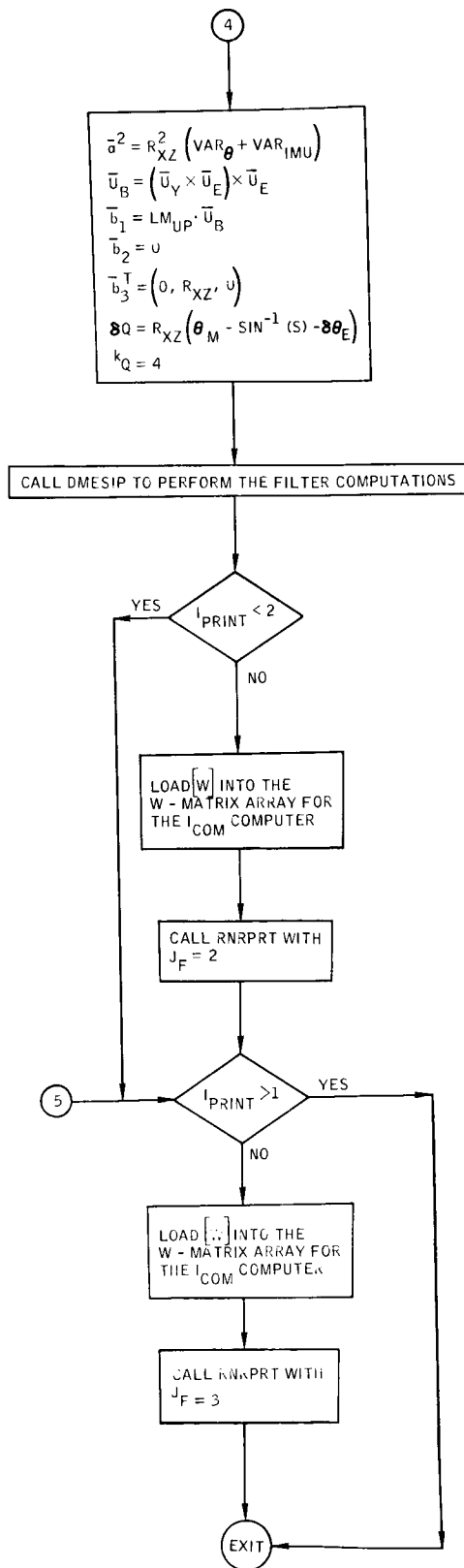


Figure B-77.- Concluded.

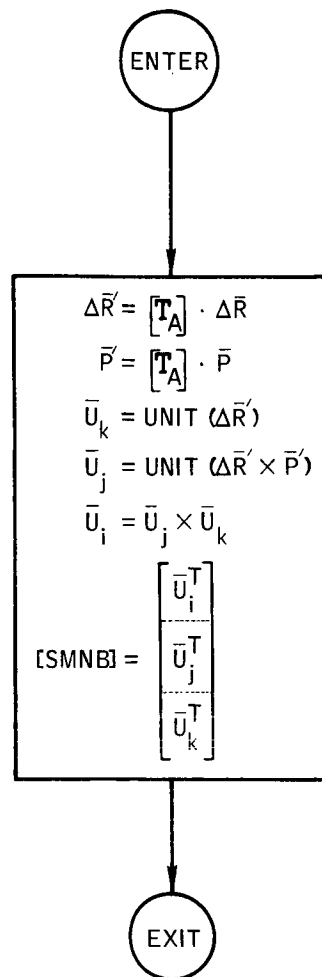


Figure B-78.- Flow chart of subroutine PRSMNB.

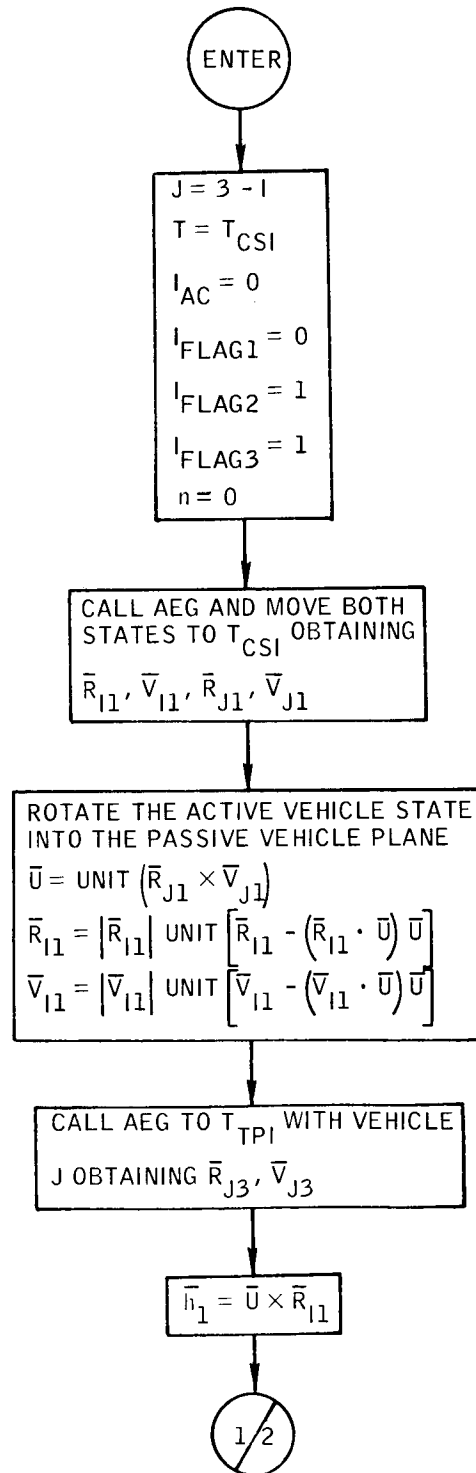


Figure B-79. - Flow chart of subroutine RTCCSI.

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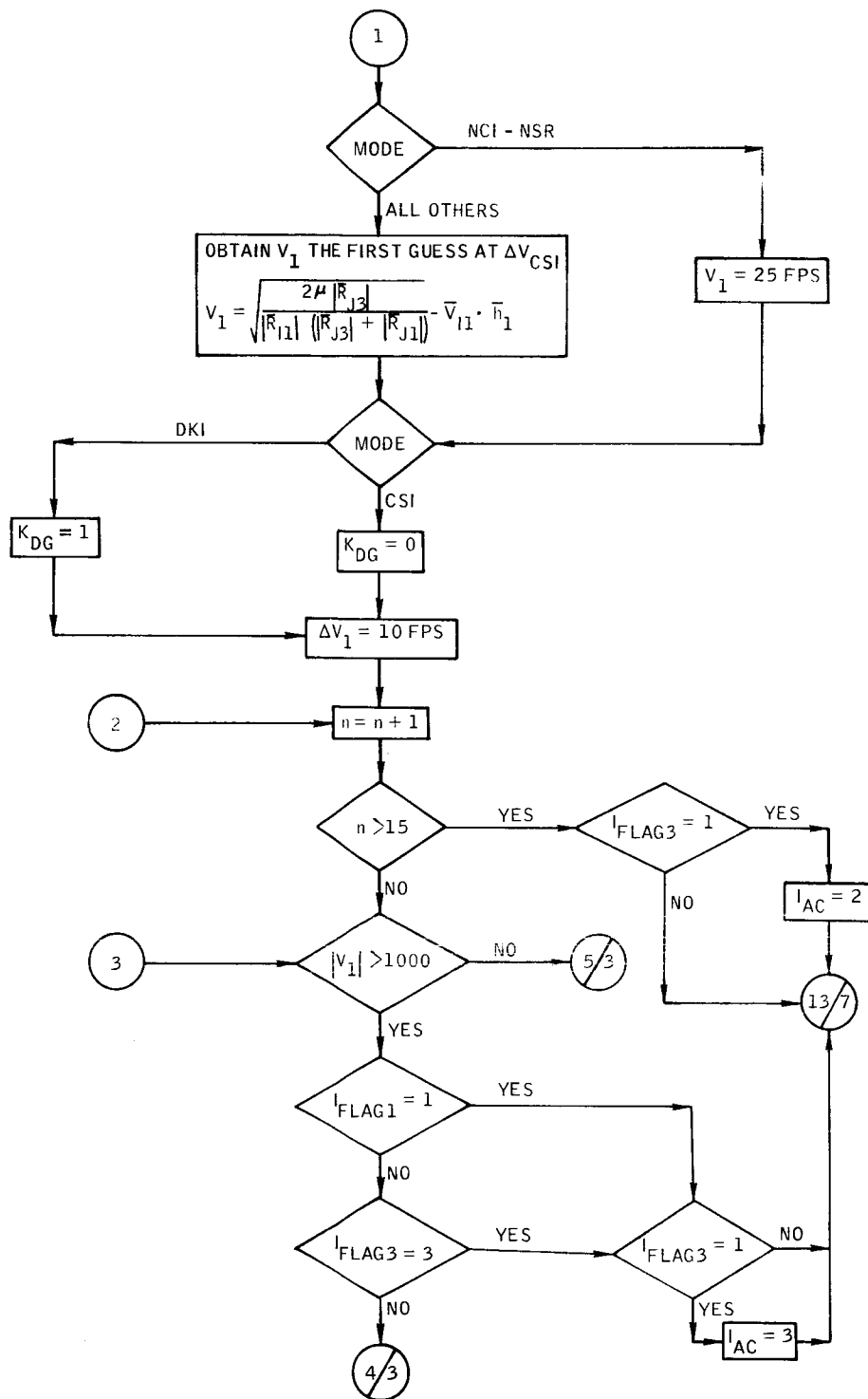


Figure B-79. - Continued.

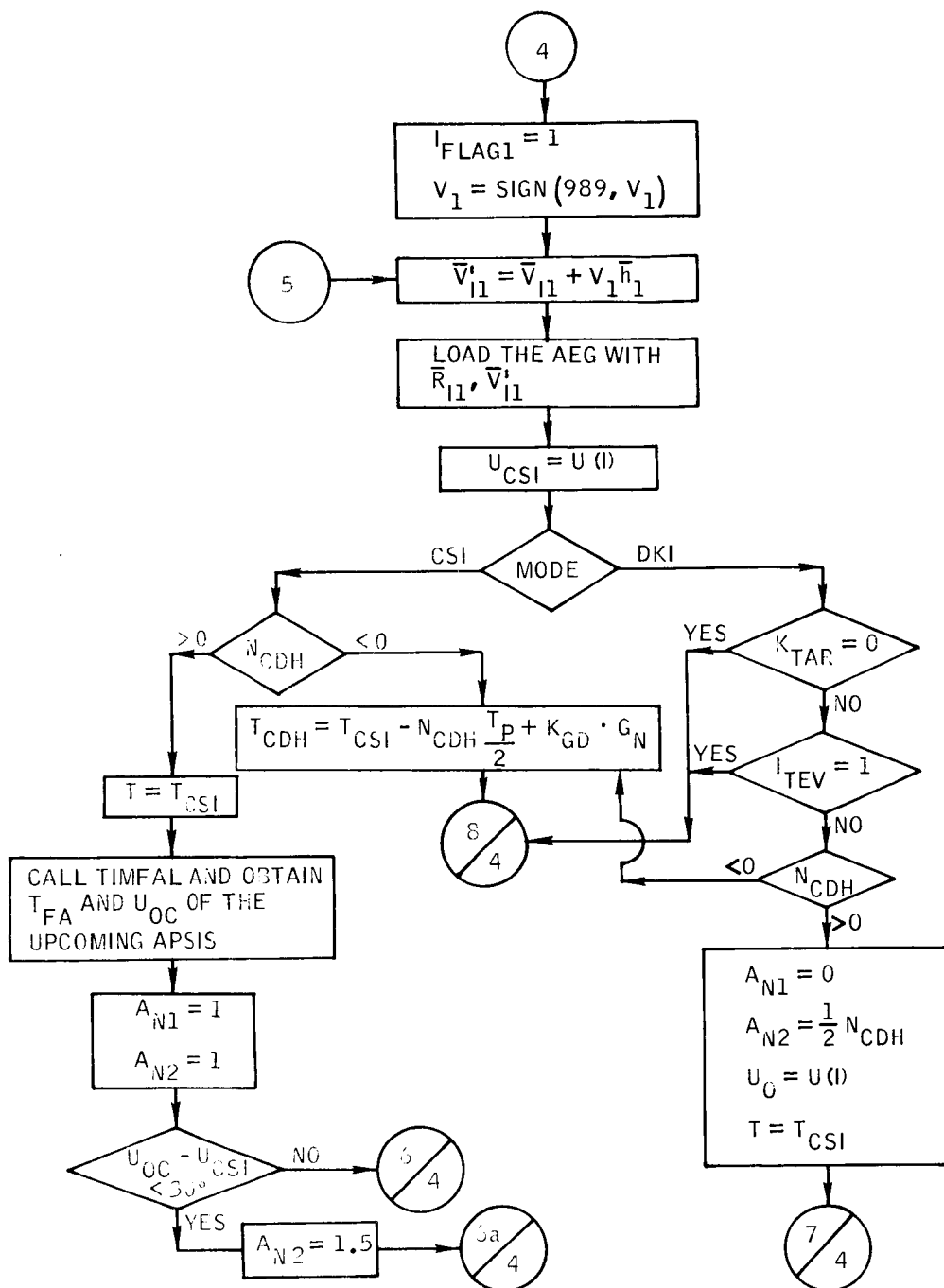


Figure B-79. - Continued.

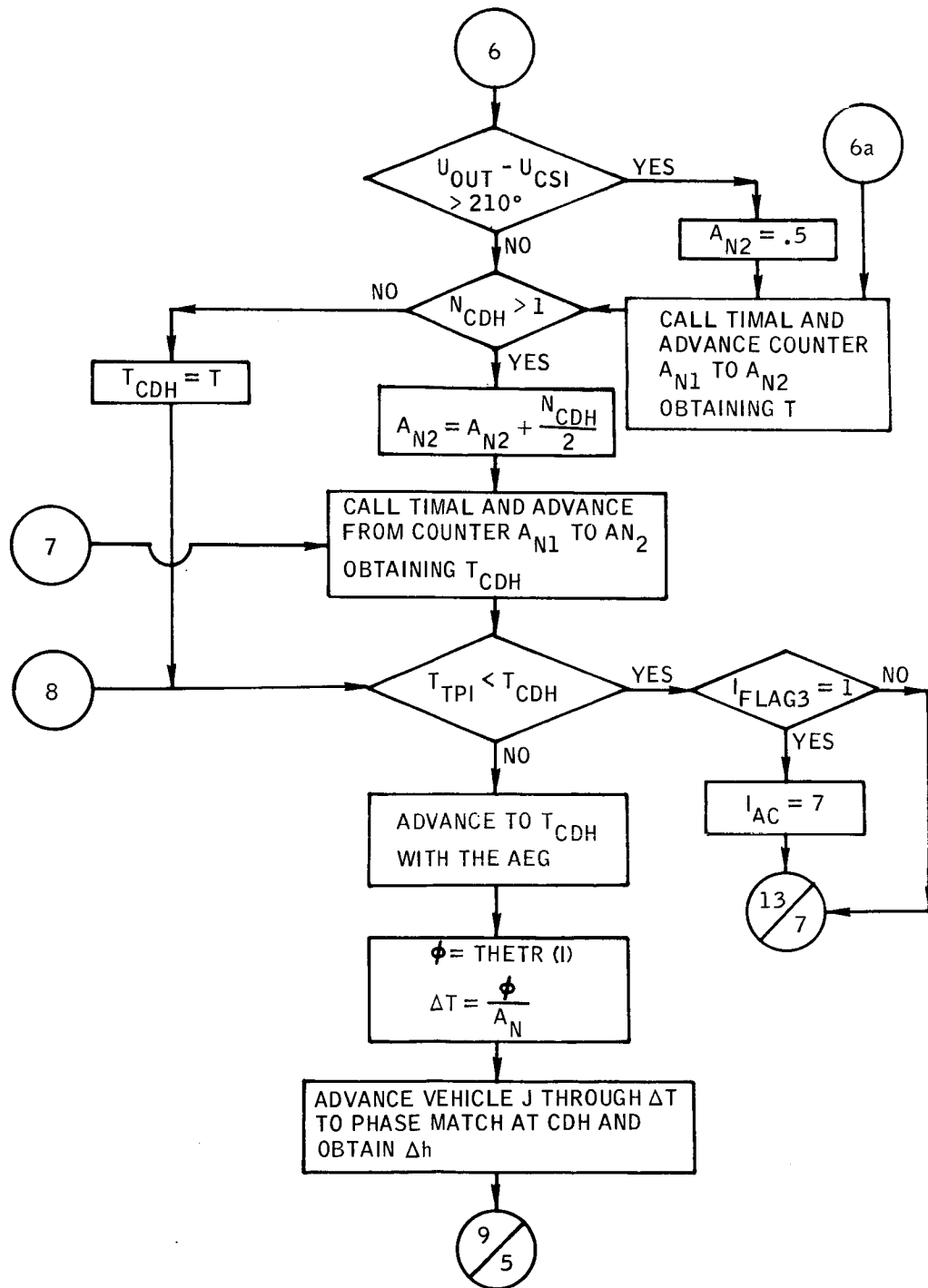


Figure B-79. - Continued.



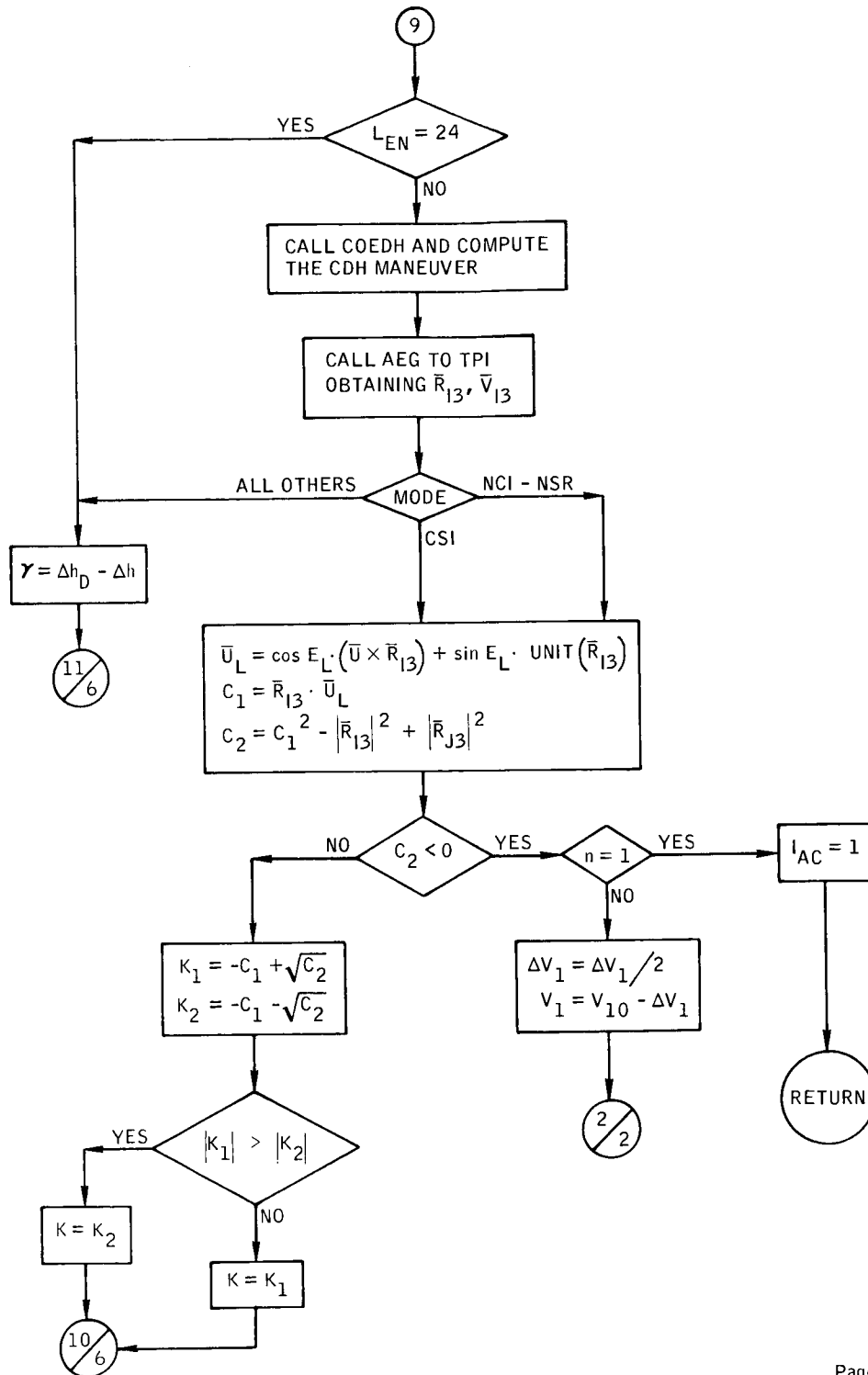


Figure B-79.- Continued.

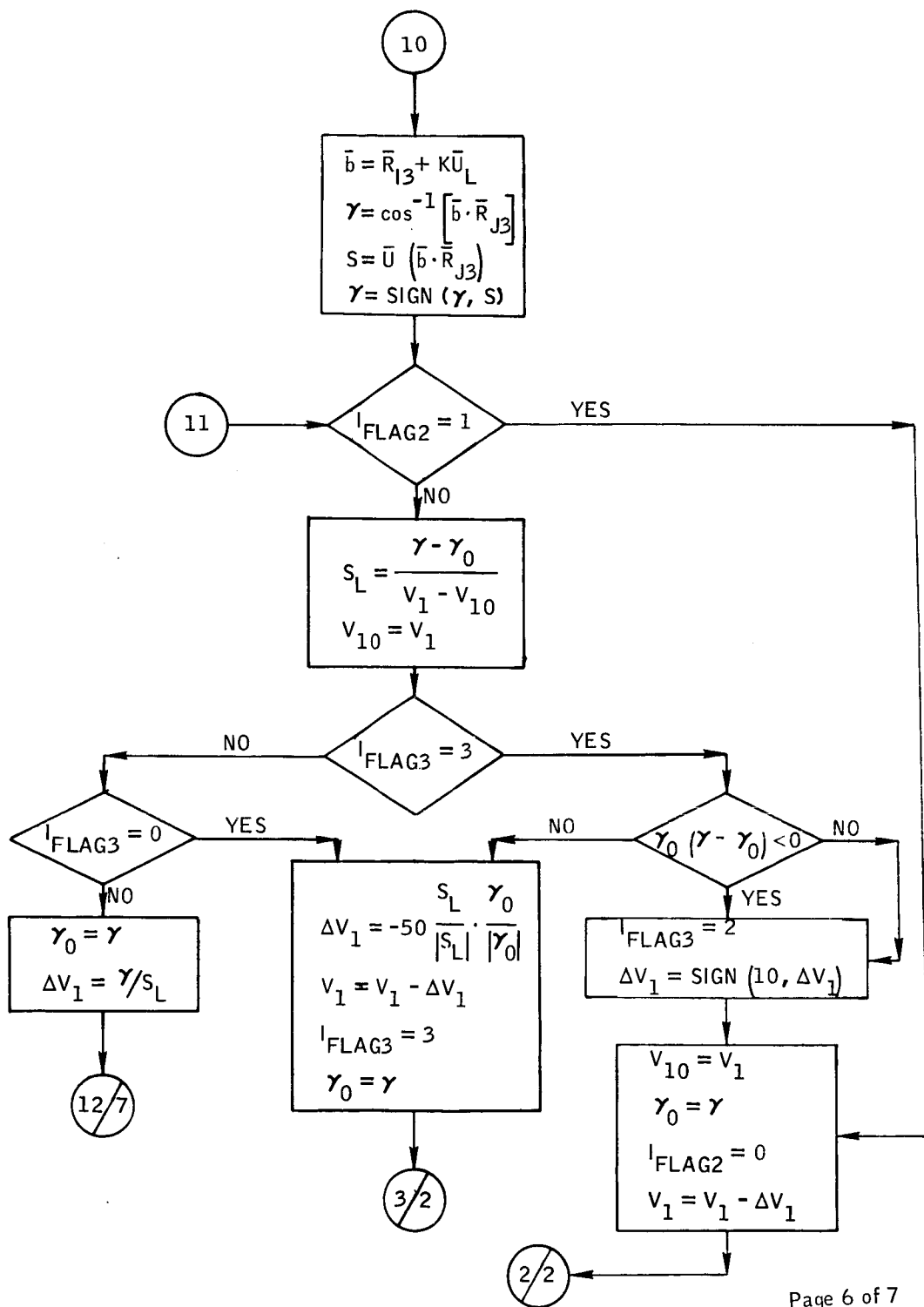


Figure B-79. - Continued.

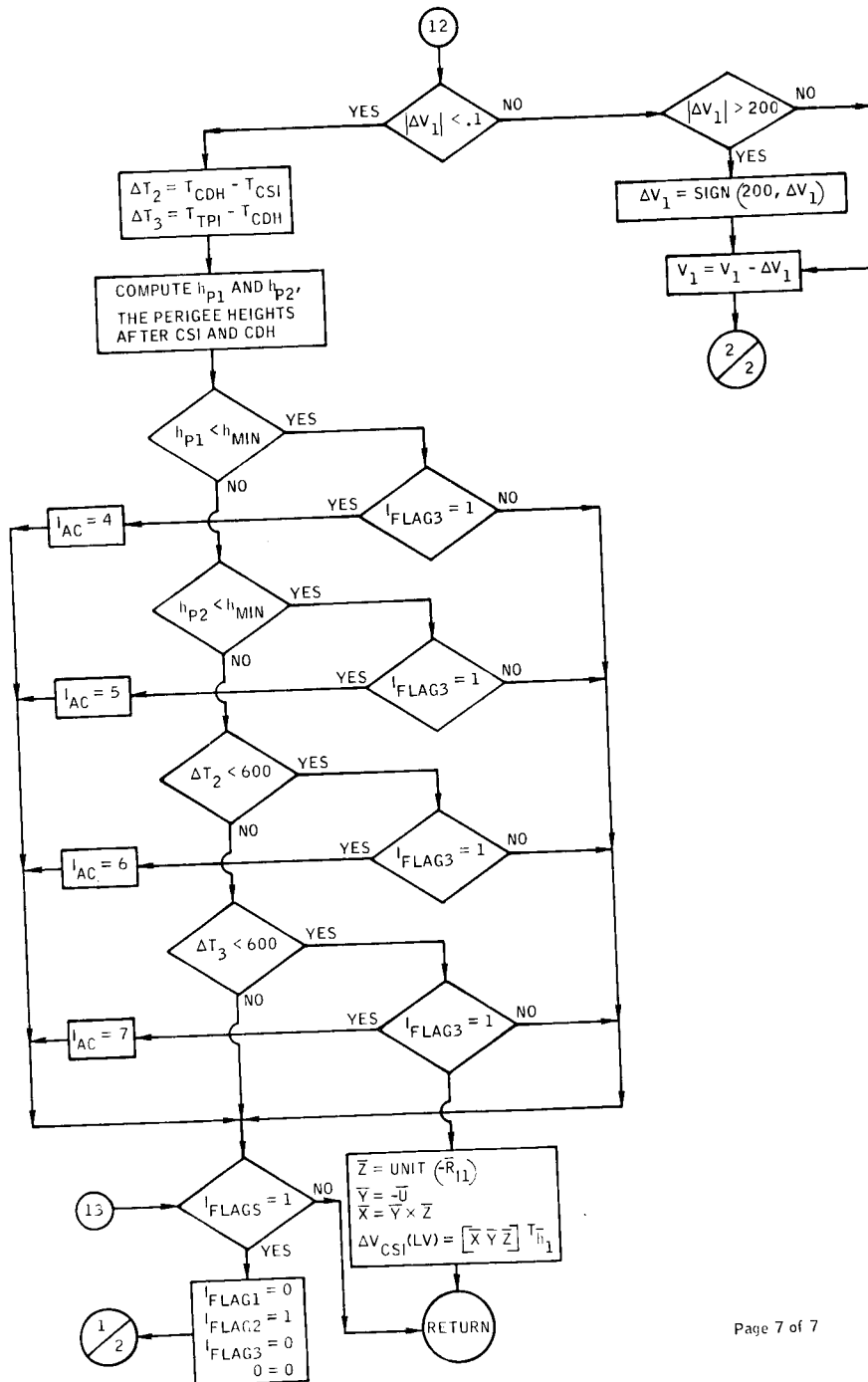


Figure B-79. - Concluded.

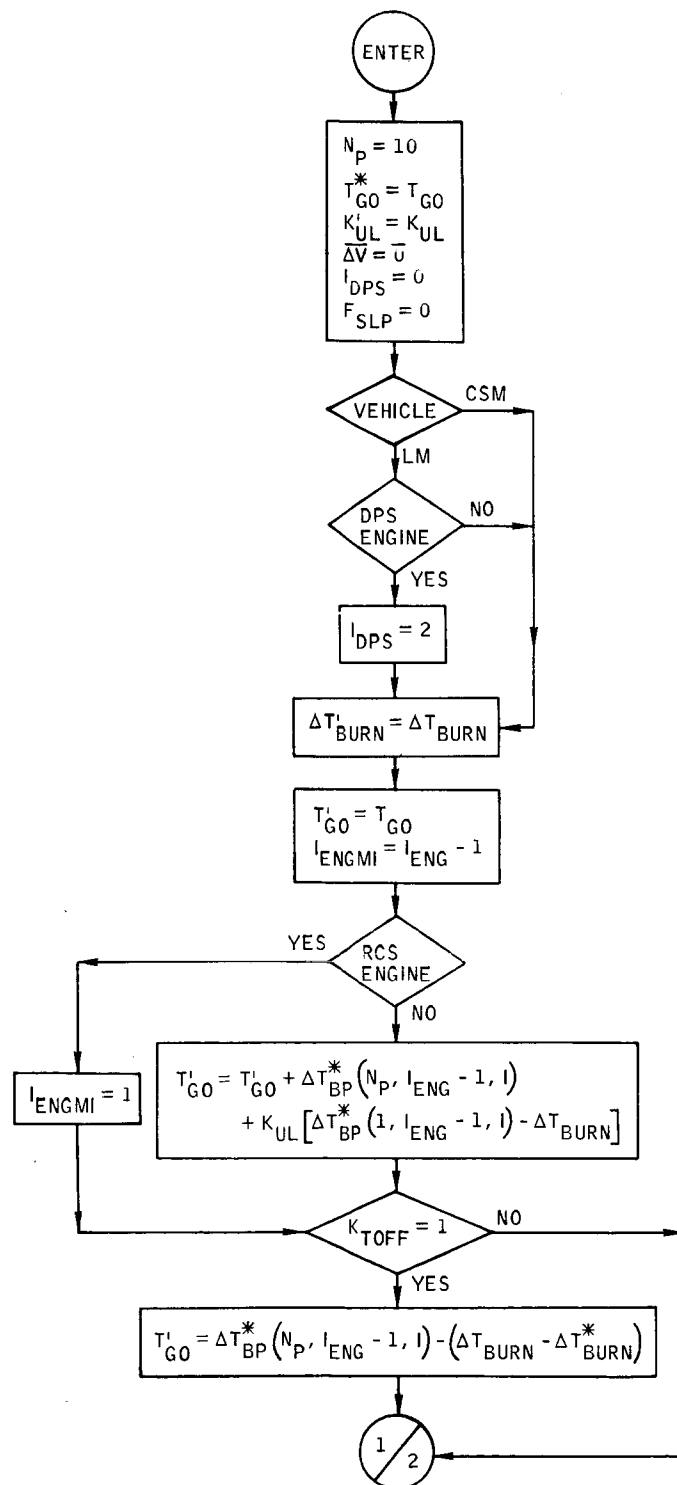
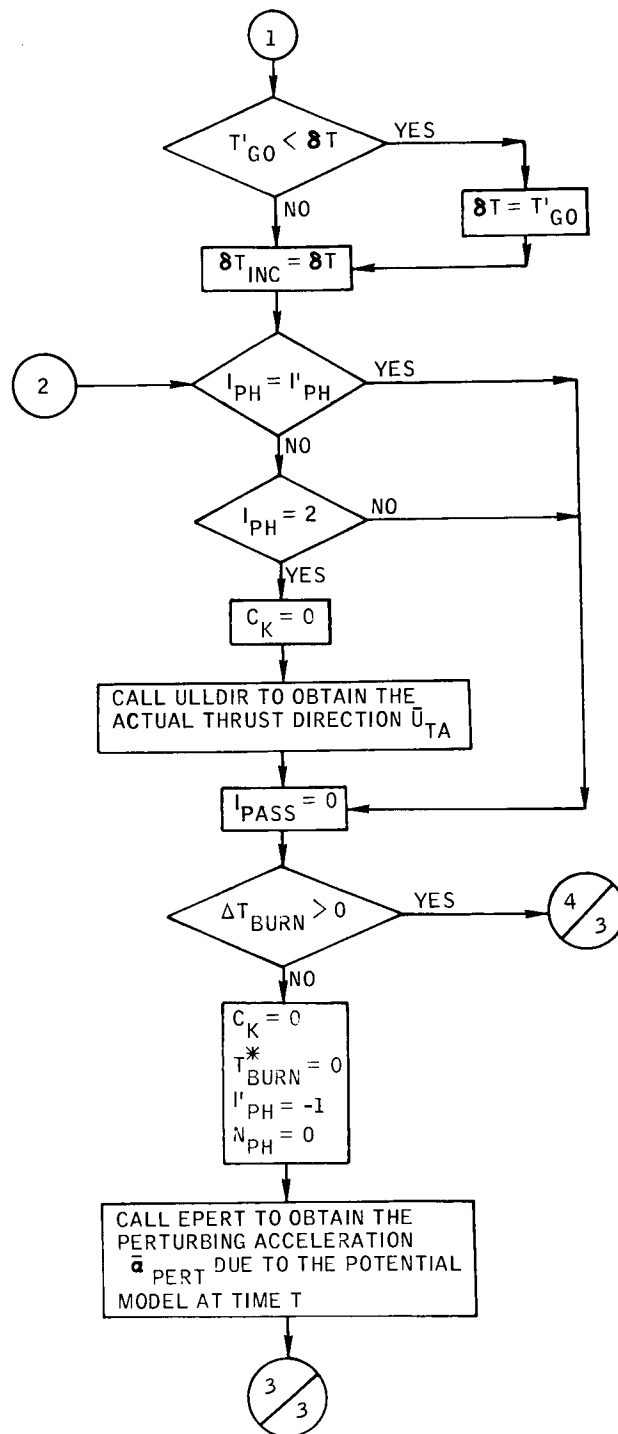


Figure B-80. - Flow chart of subroutine RUNGA.



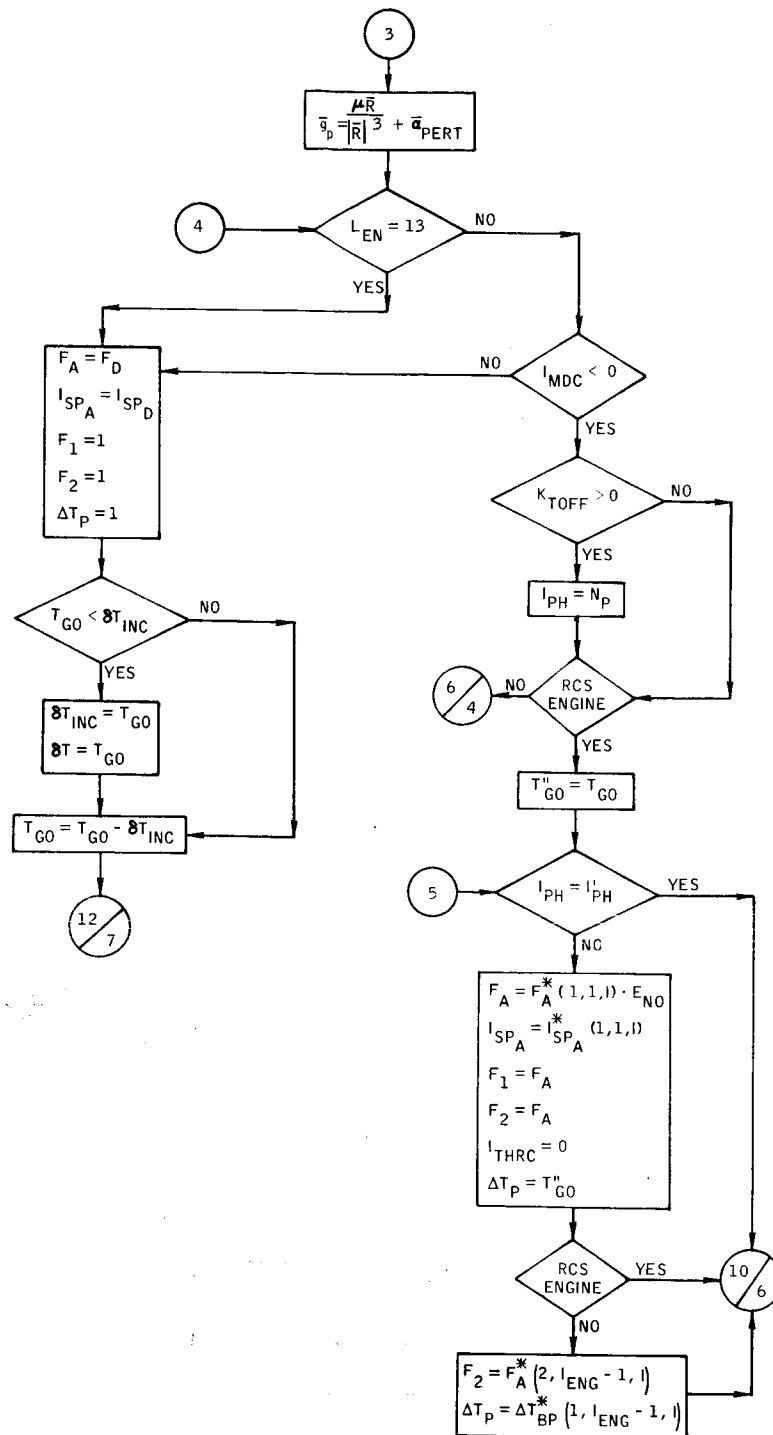
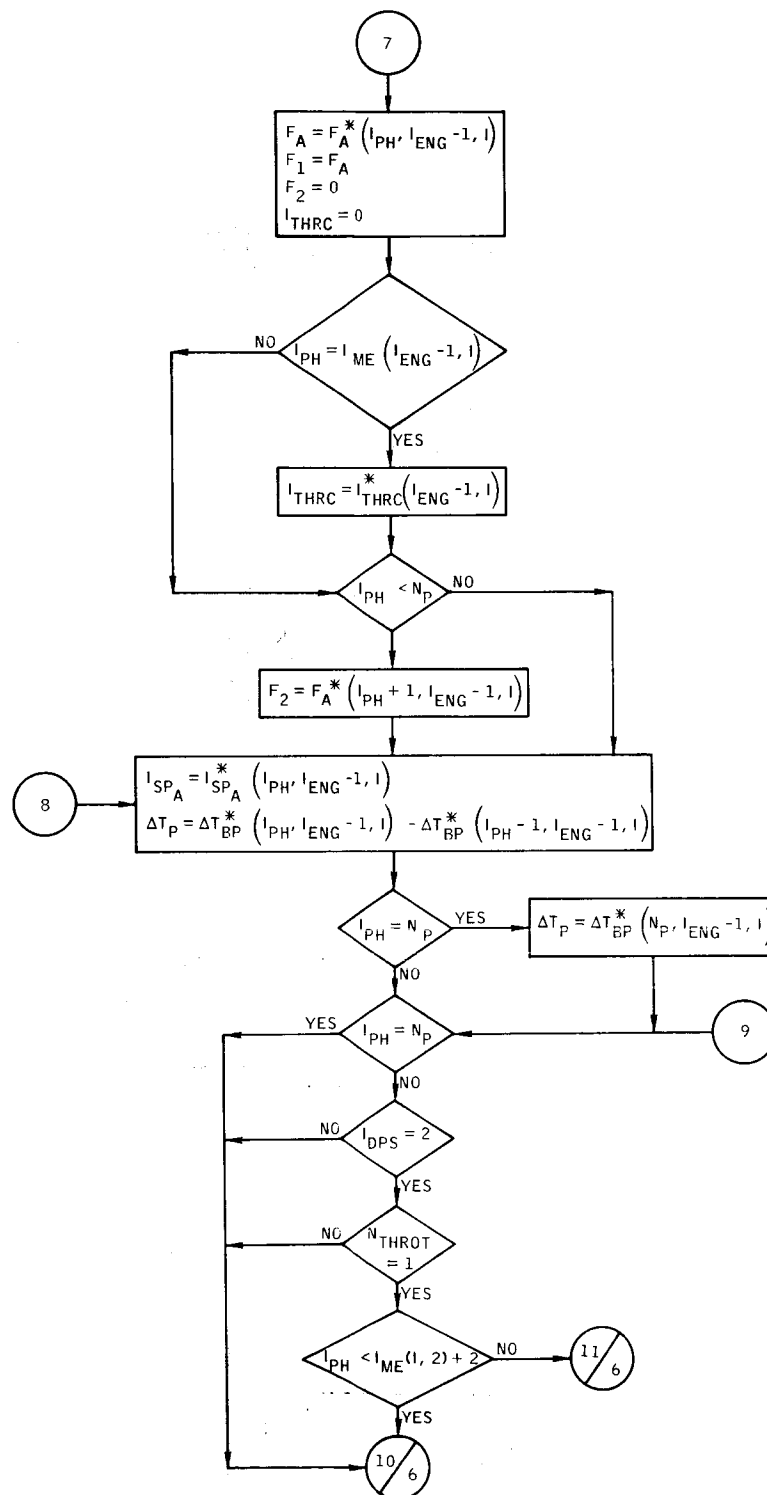
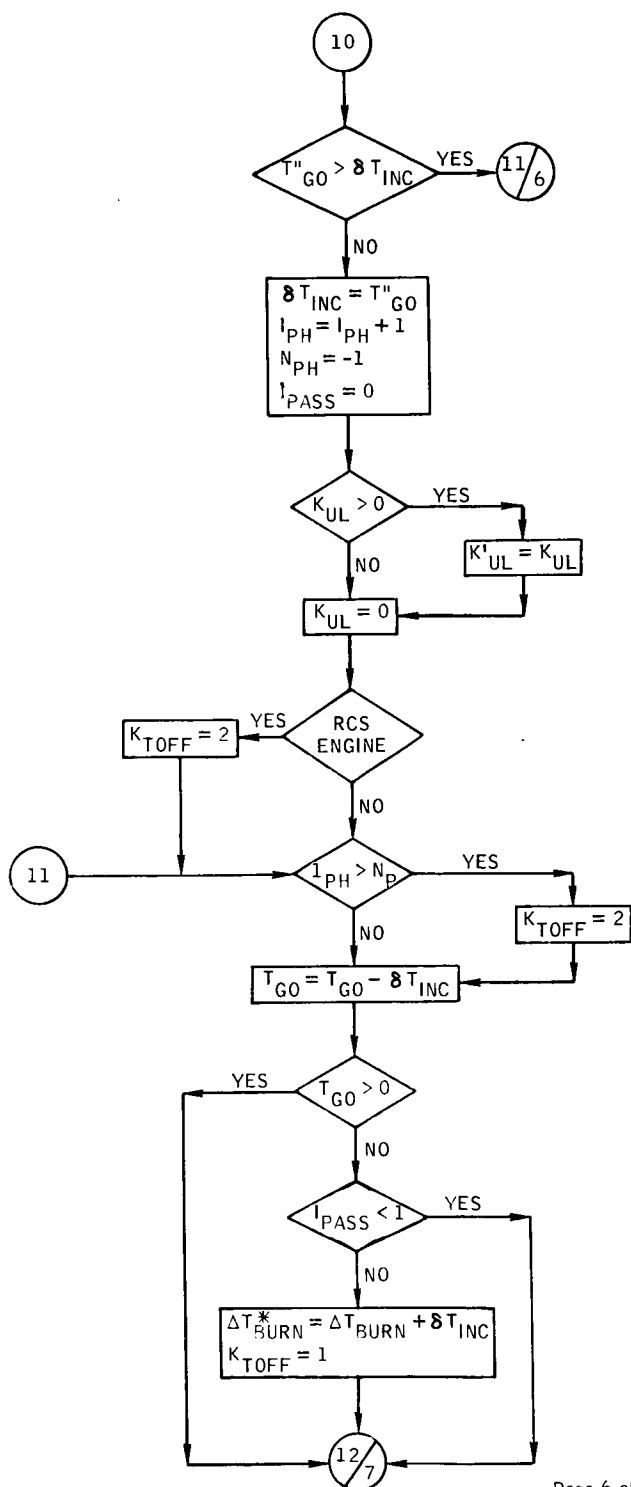


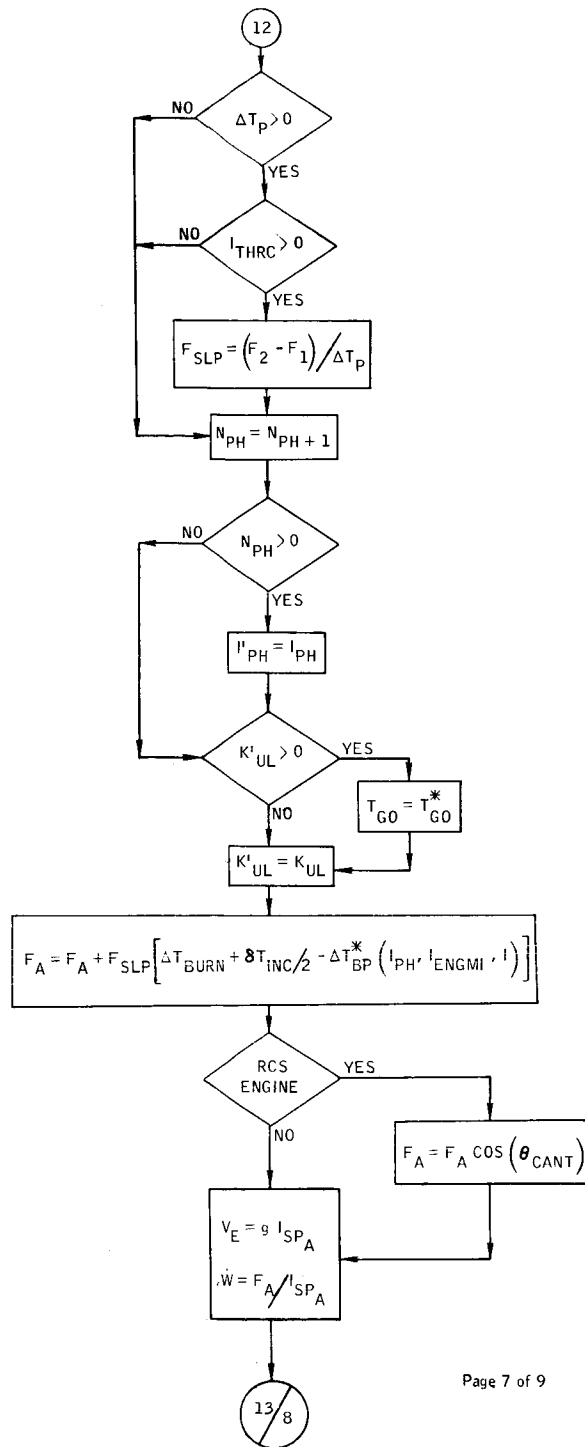
Figure B-80. - Continued.

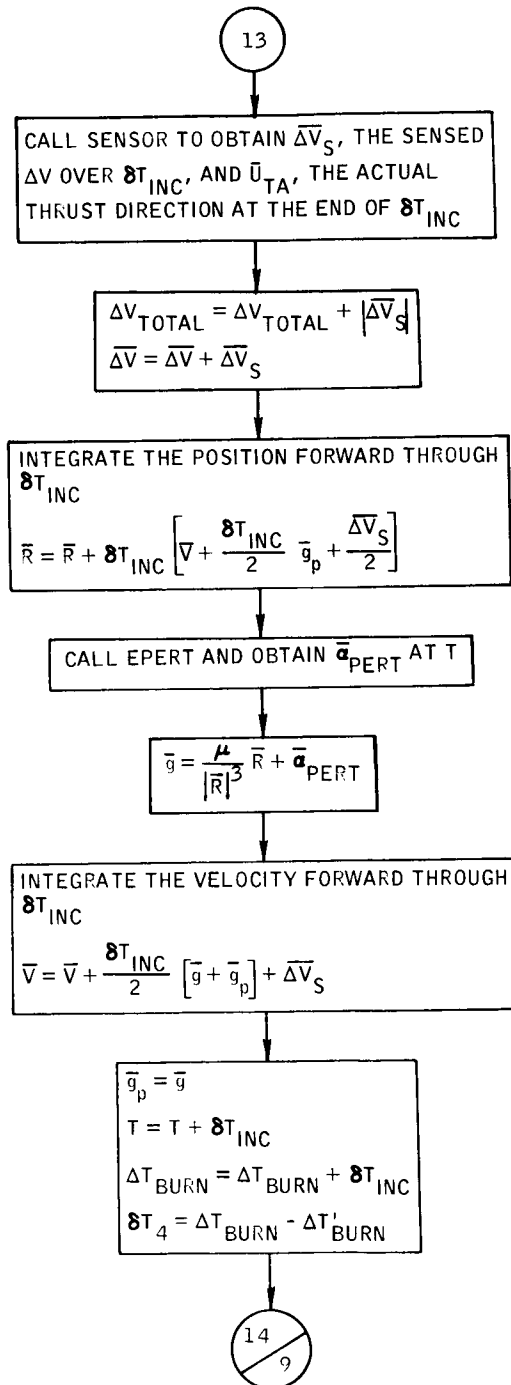












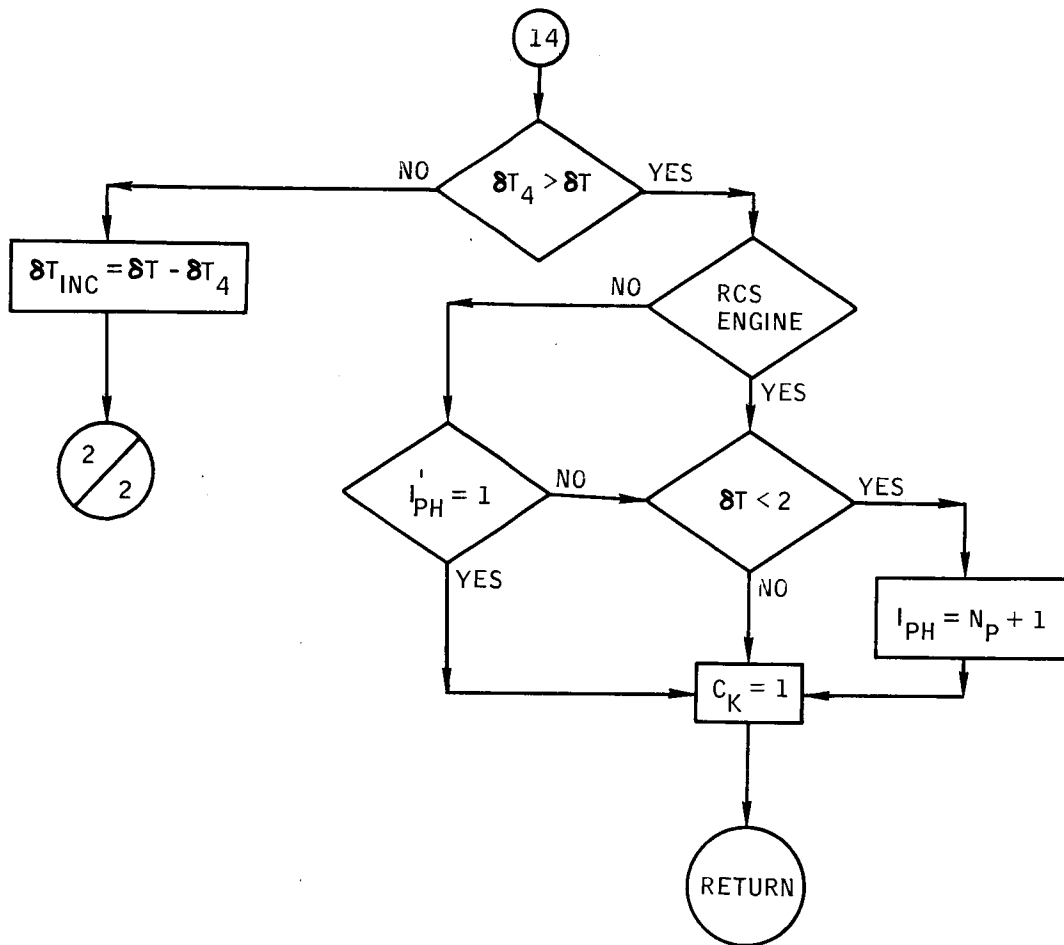


Figure B-80.- Concluded.

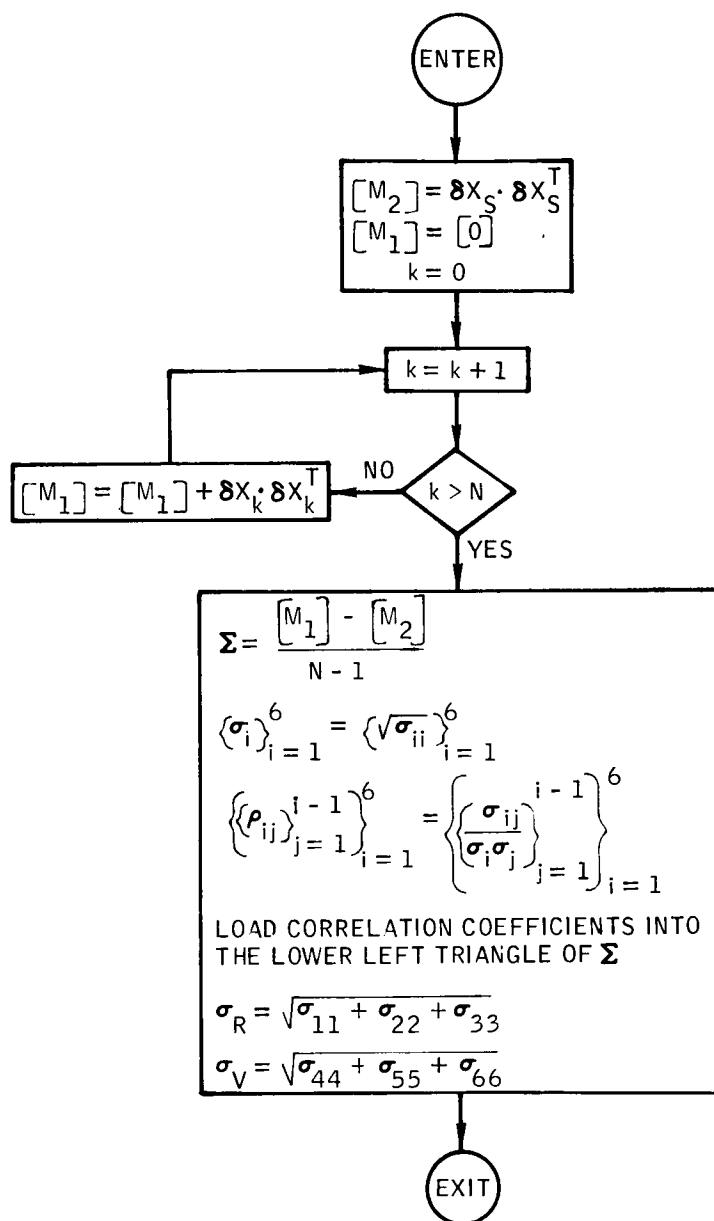


Figure B-81.- Flow chart of subroutine SAMCOV.

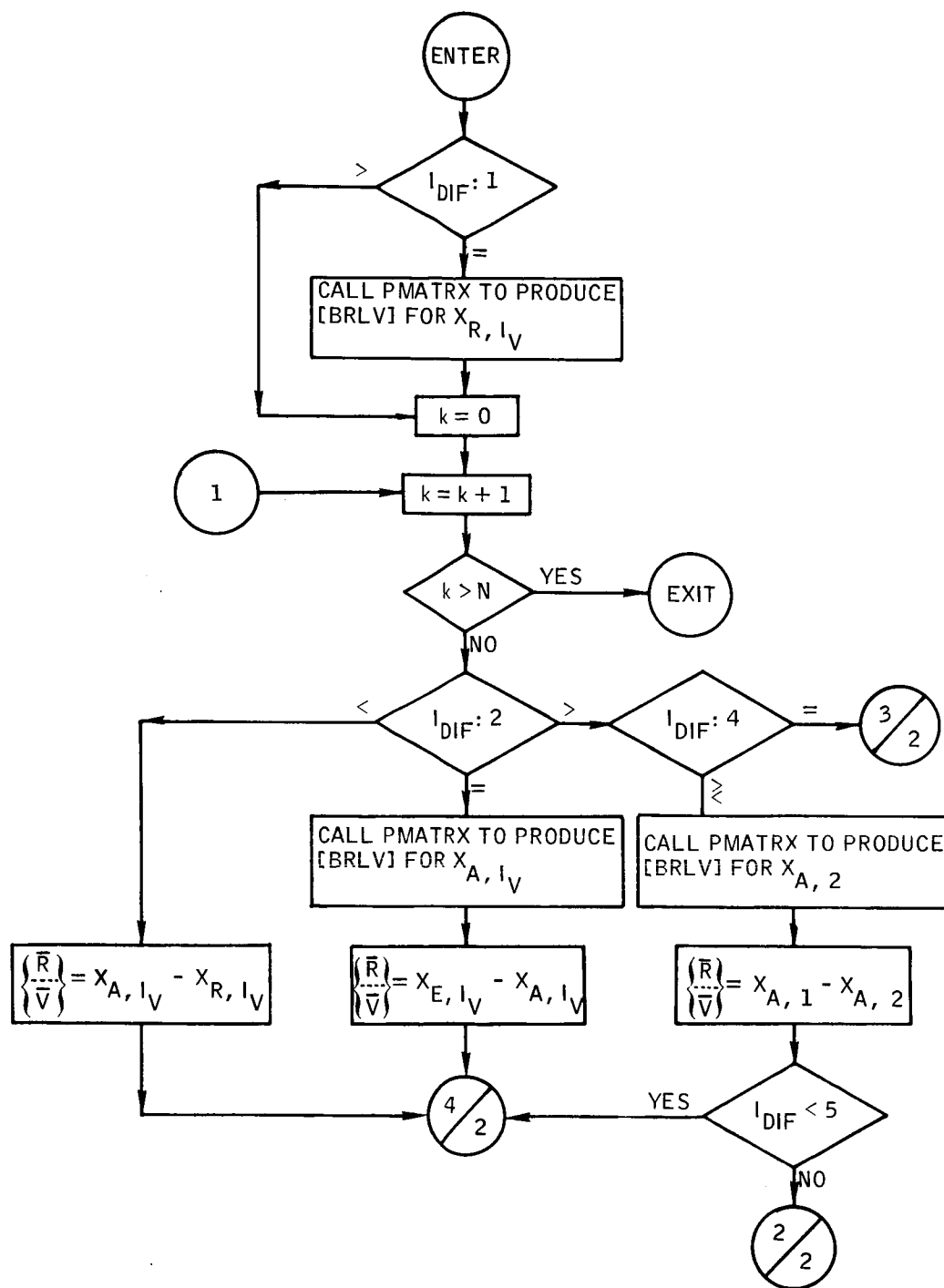


Figure B-82. - Flow chart of subroutine SAMDIF.

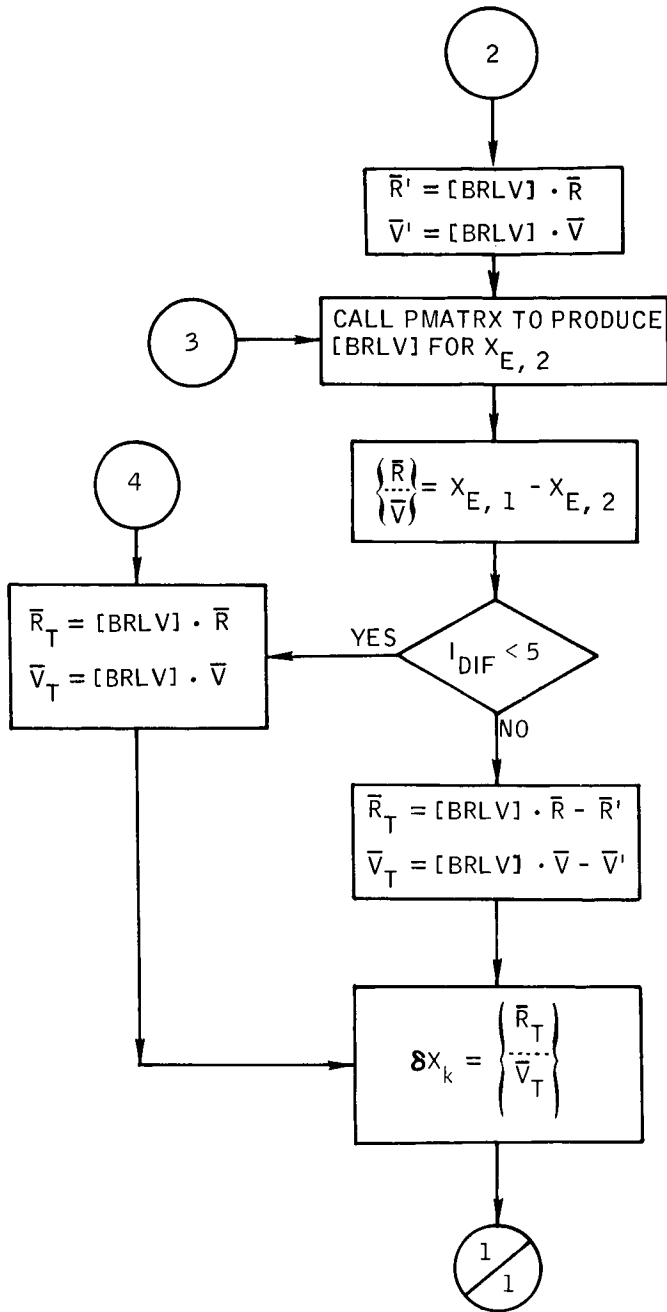


Figure B-82. - Concluded.

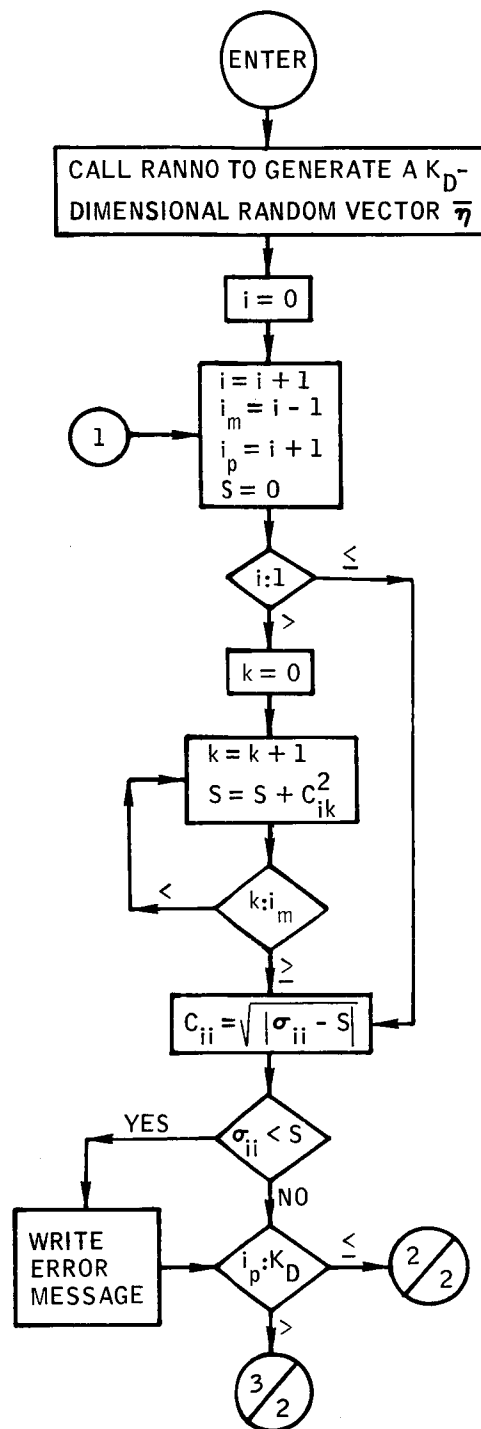


Figure B-83.- Flow chart of subroutine SAMPLE.



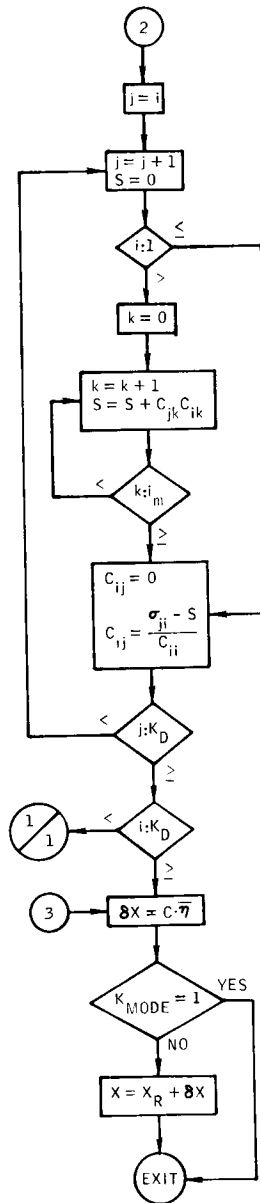


Figure B-33. - Concluded.

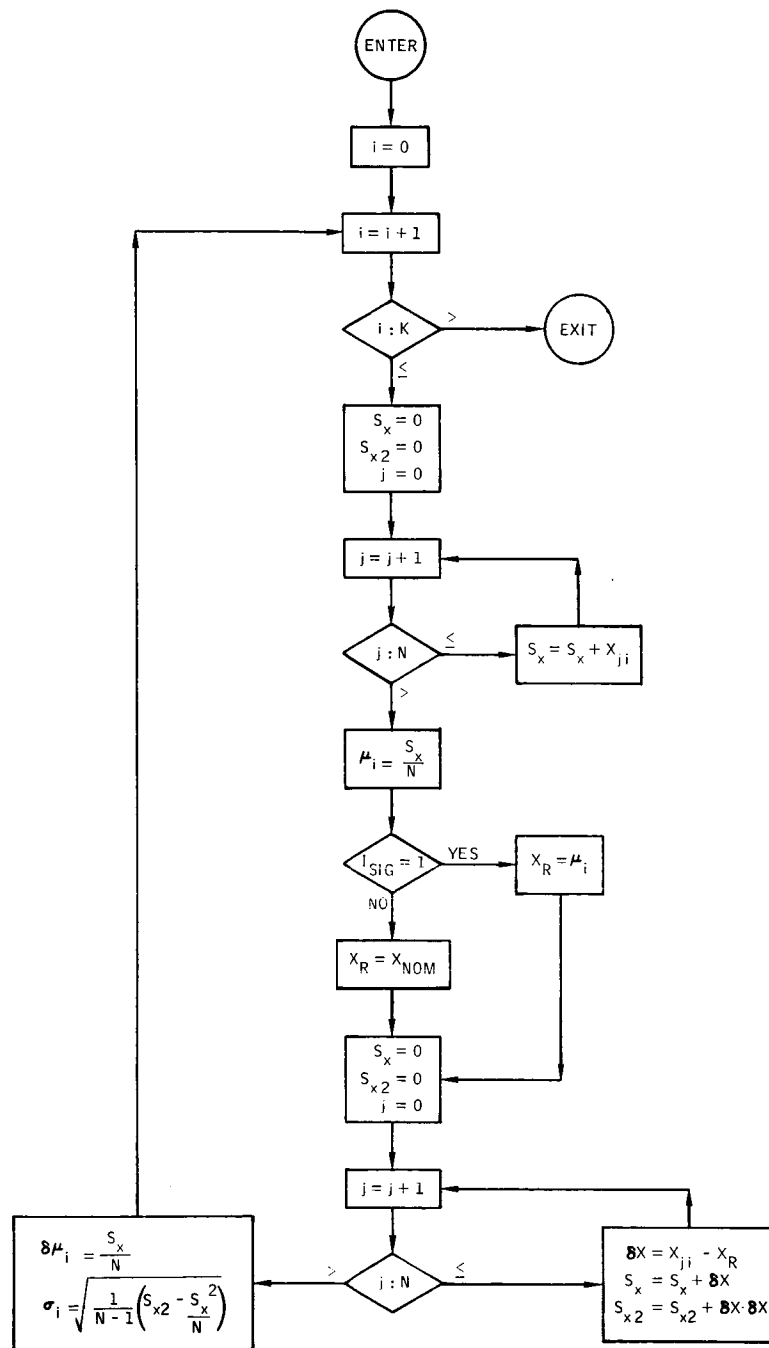


Figure B-34.- Flow chart of subroutine SAMSIG.

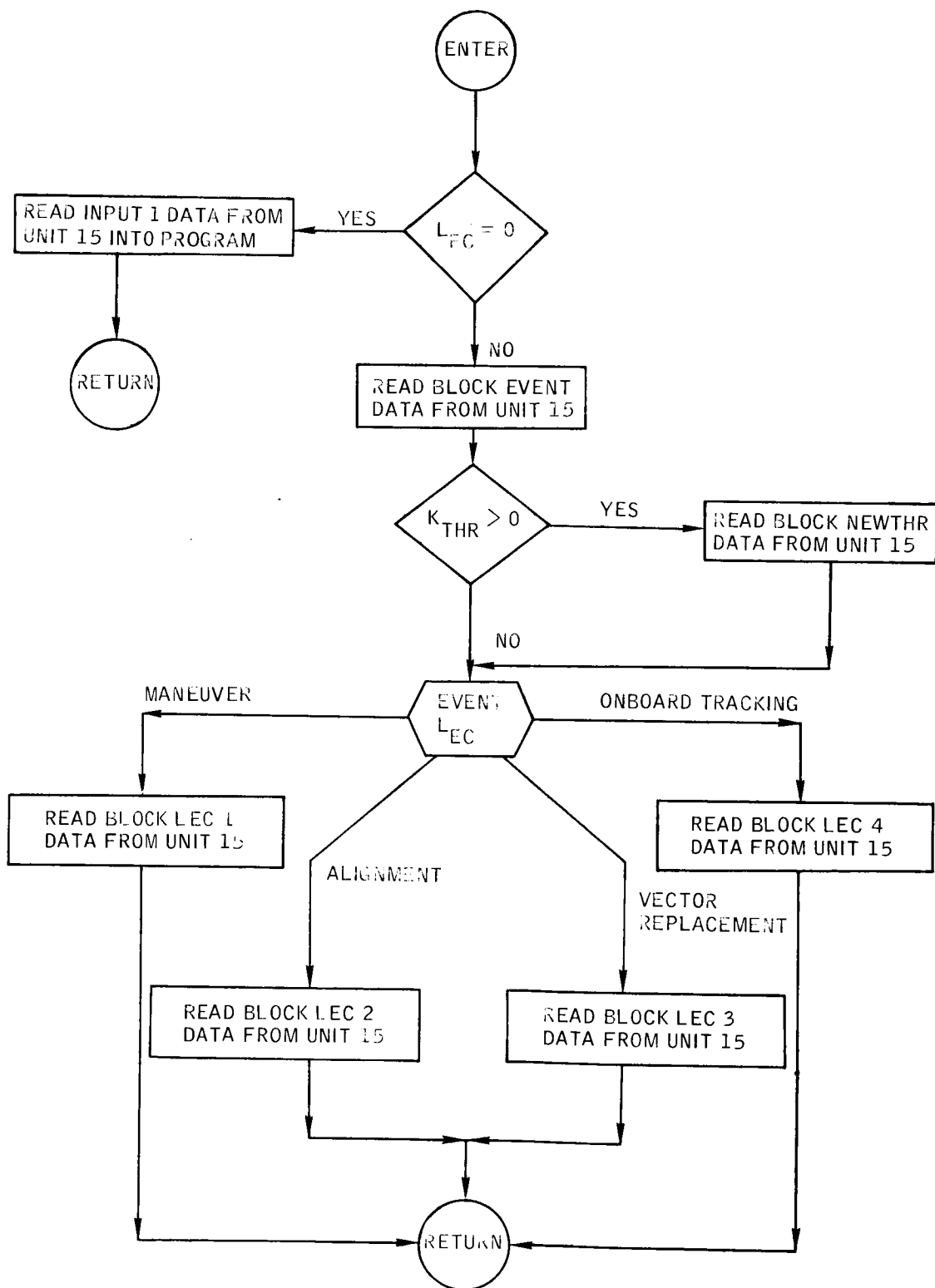


Figure B-35.- Flow chart of subroutine SAVIP 2.

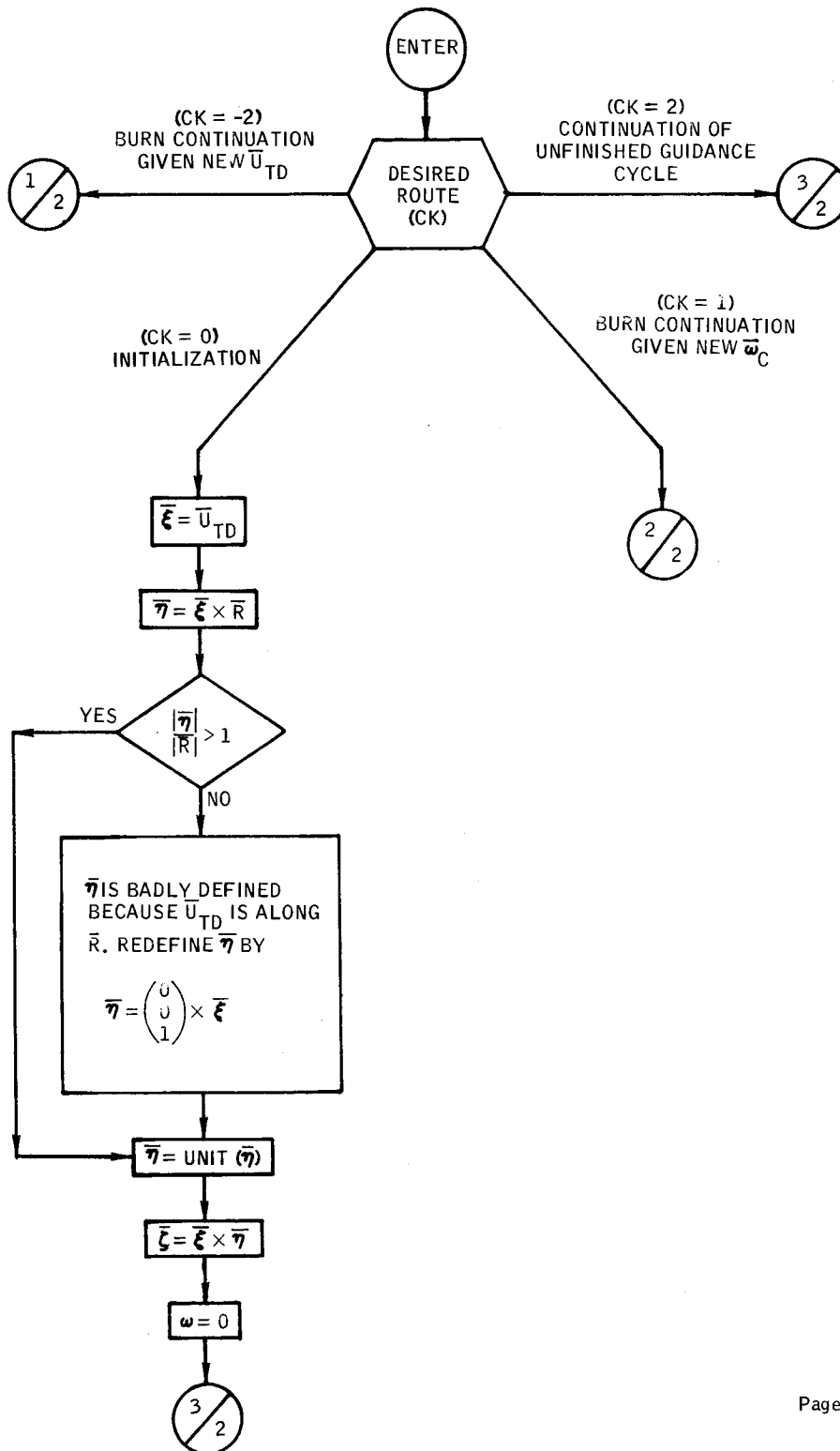
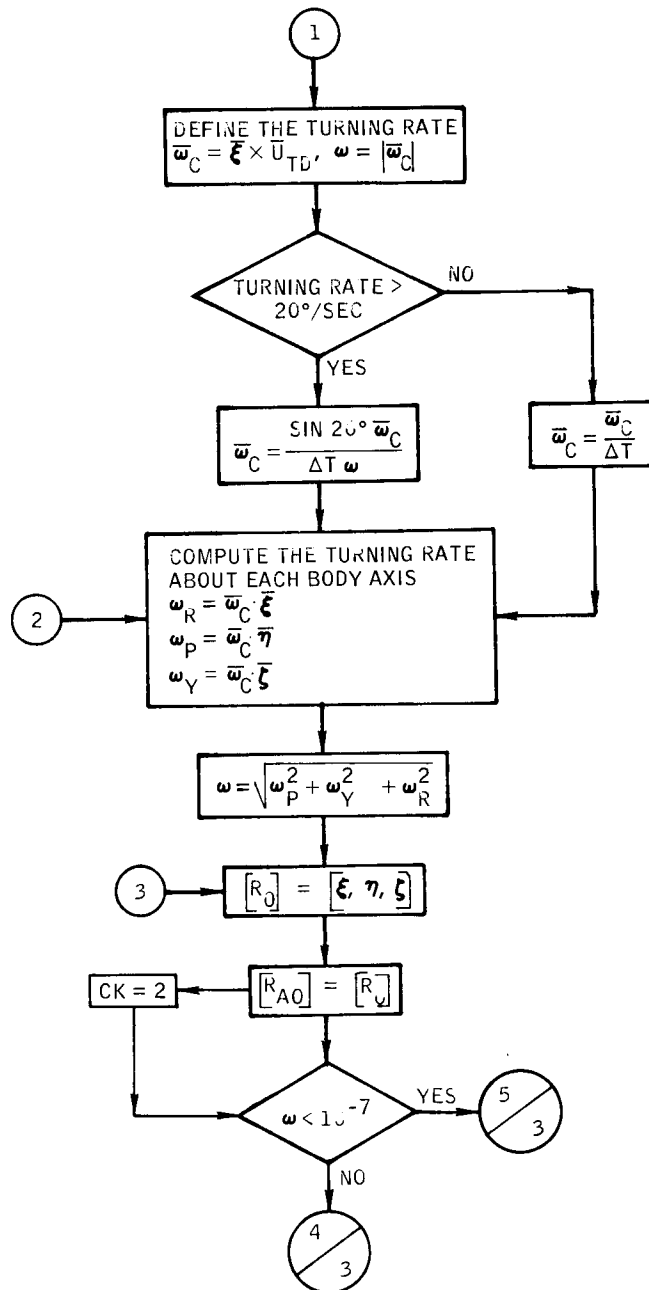


Figure B-86.- Flow chart of subroutine SENSOR.



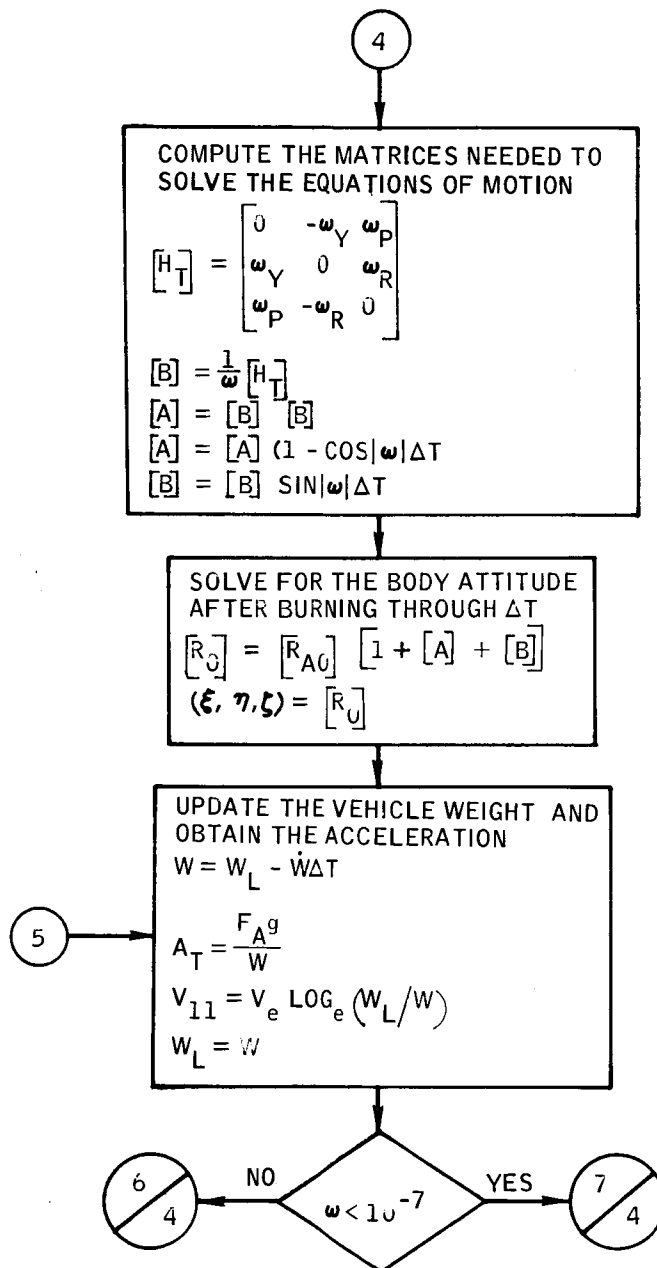
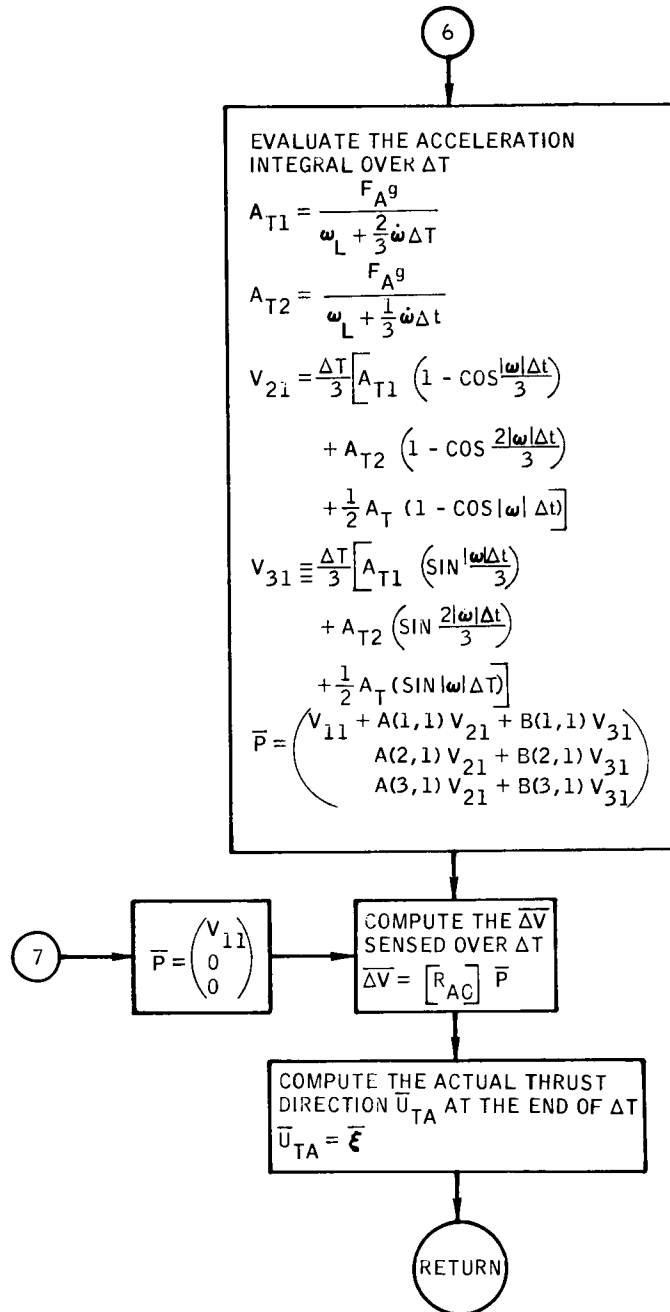


Figure B-86.- Continued.



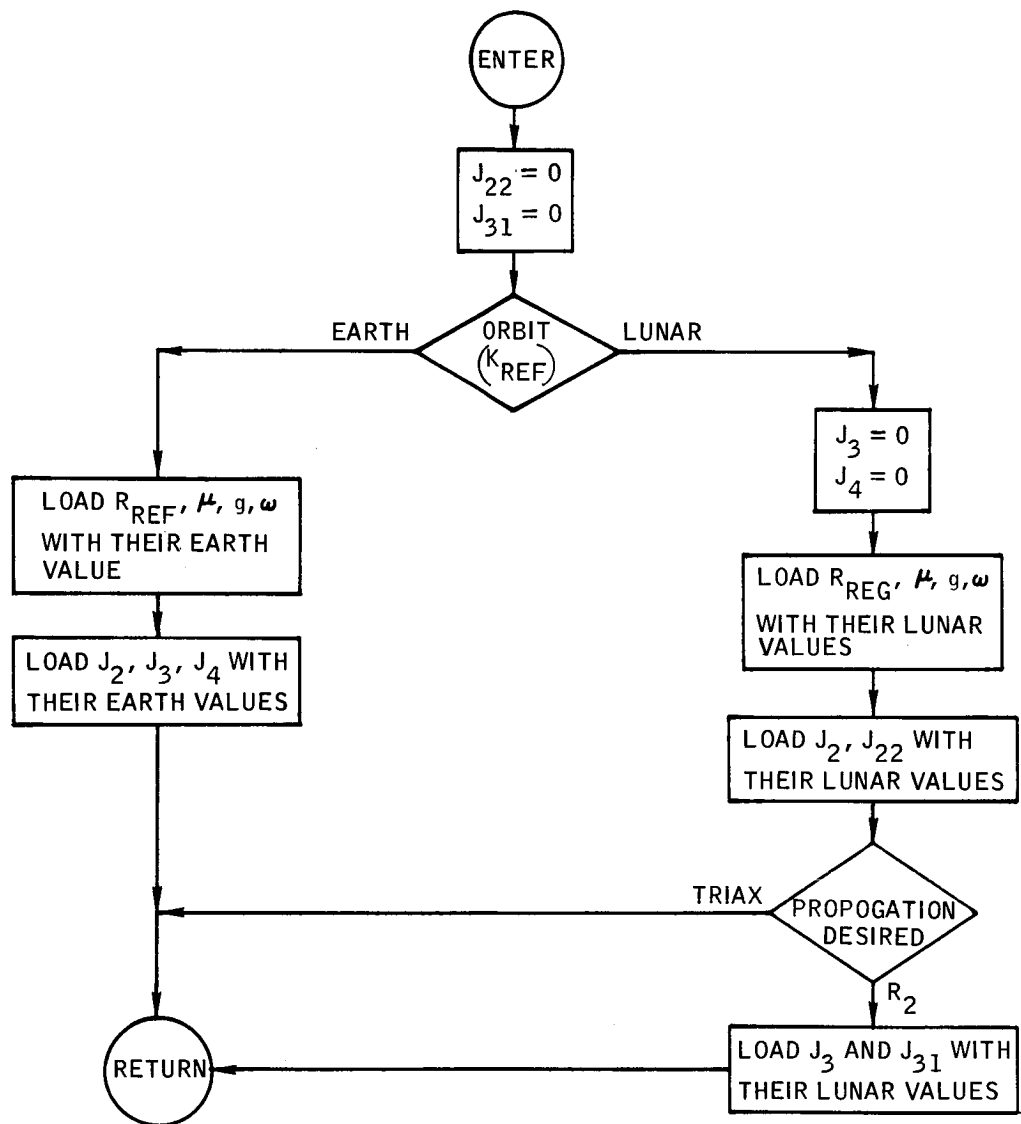


Figure B-87.- Flow chart of subroutine SETPC.



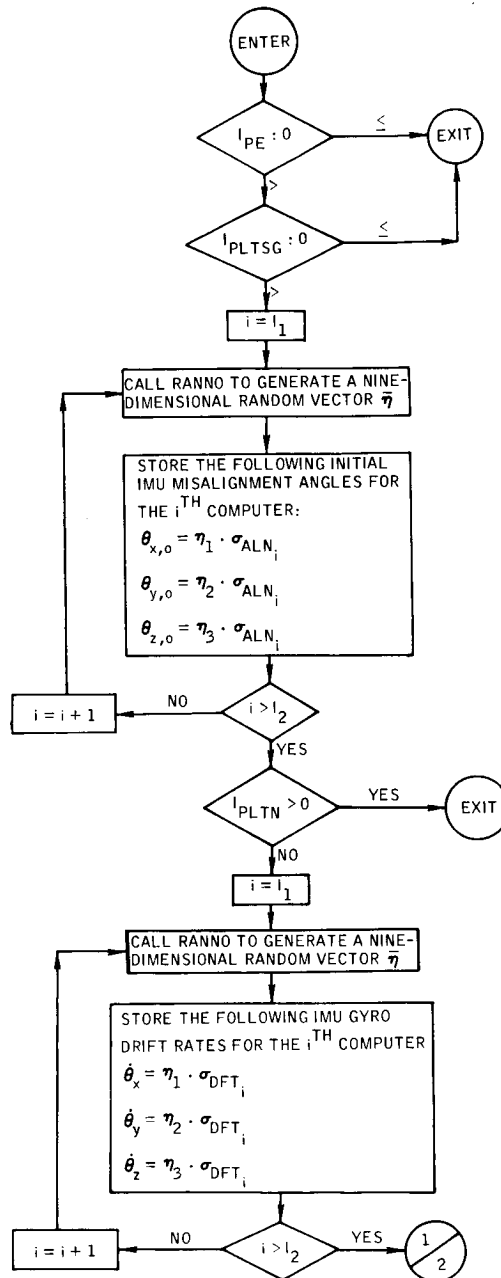
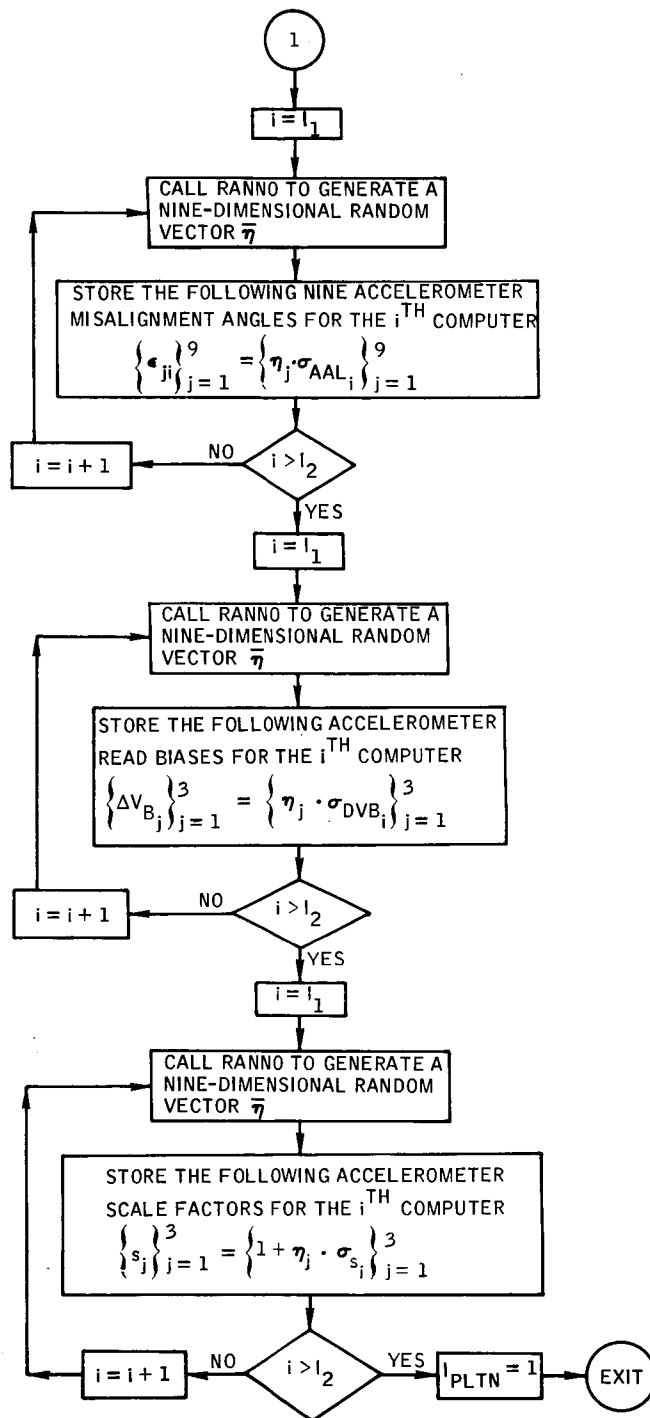


Figure B-93.- Flow chart of subroutine SETPLT.



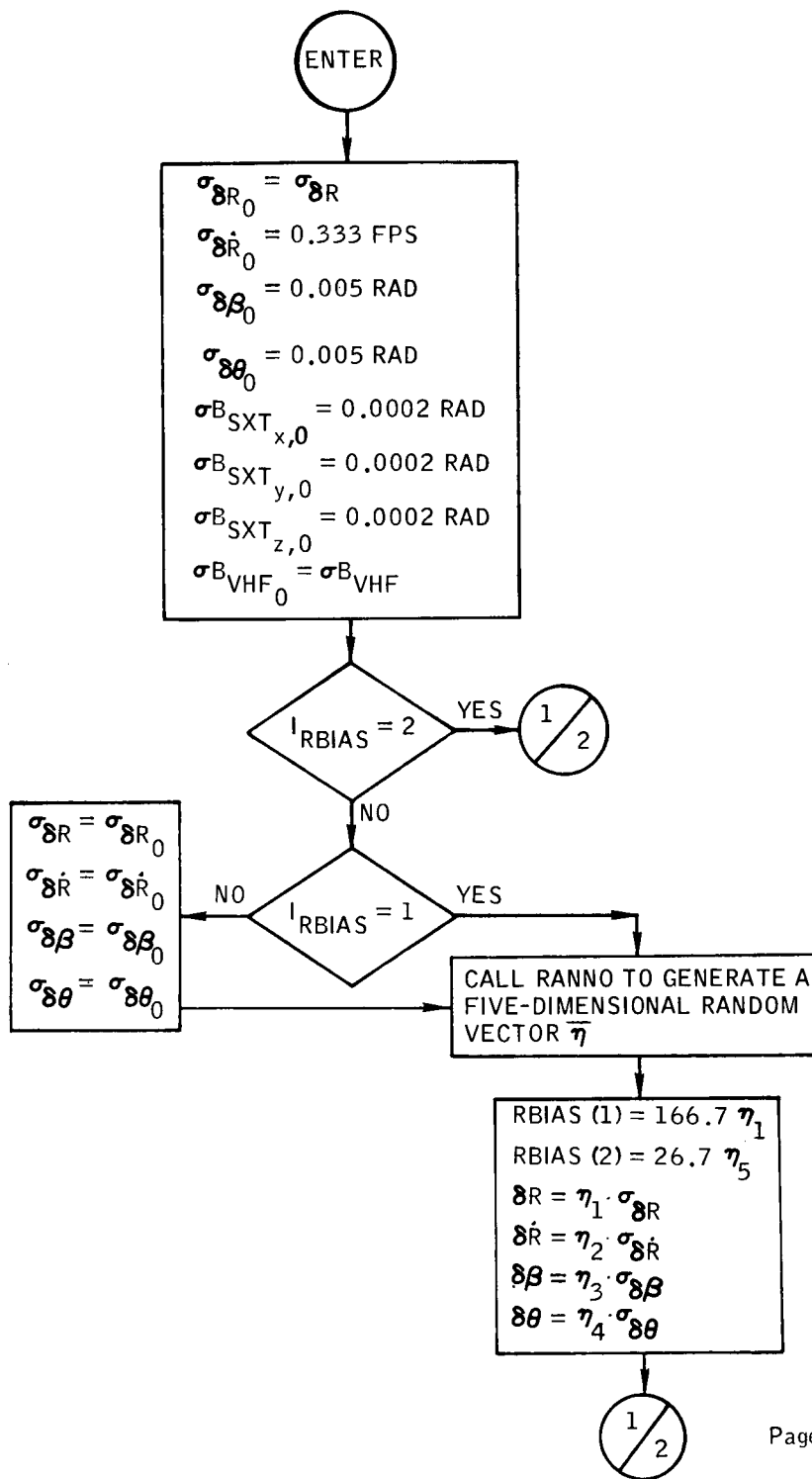


Figure B-89.- Flow chart of subroutine SETRBS.

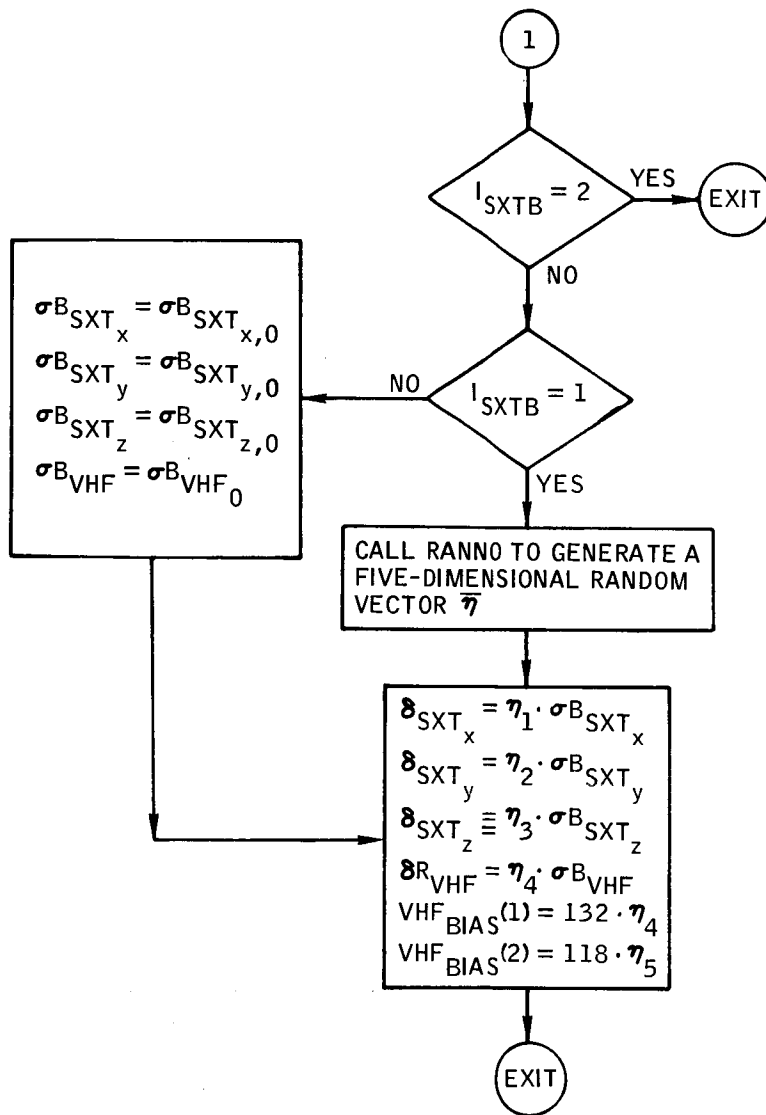


Figure B-89.- Concluded.

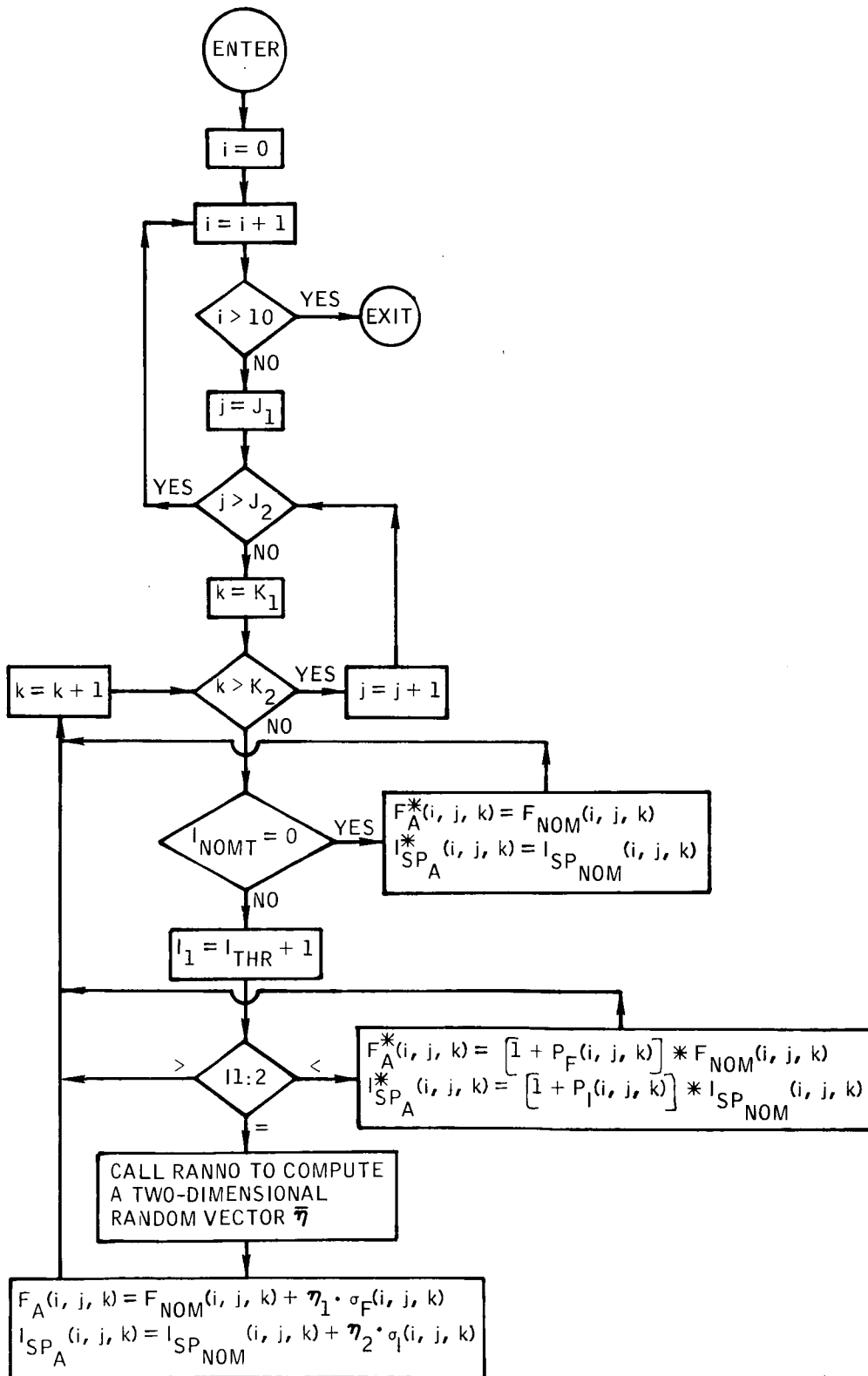


Figure B-90. Flow chart of subroutine SETTHR.

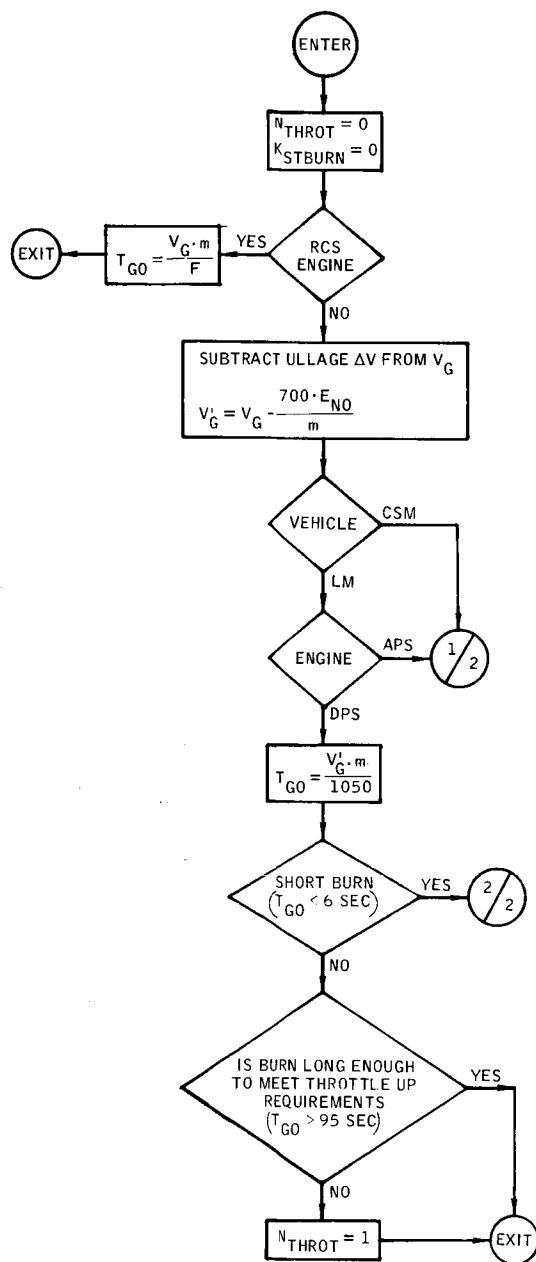


Figure B-91.- Flow chart of subroutine SHORTB.

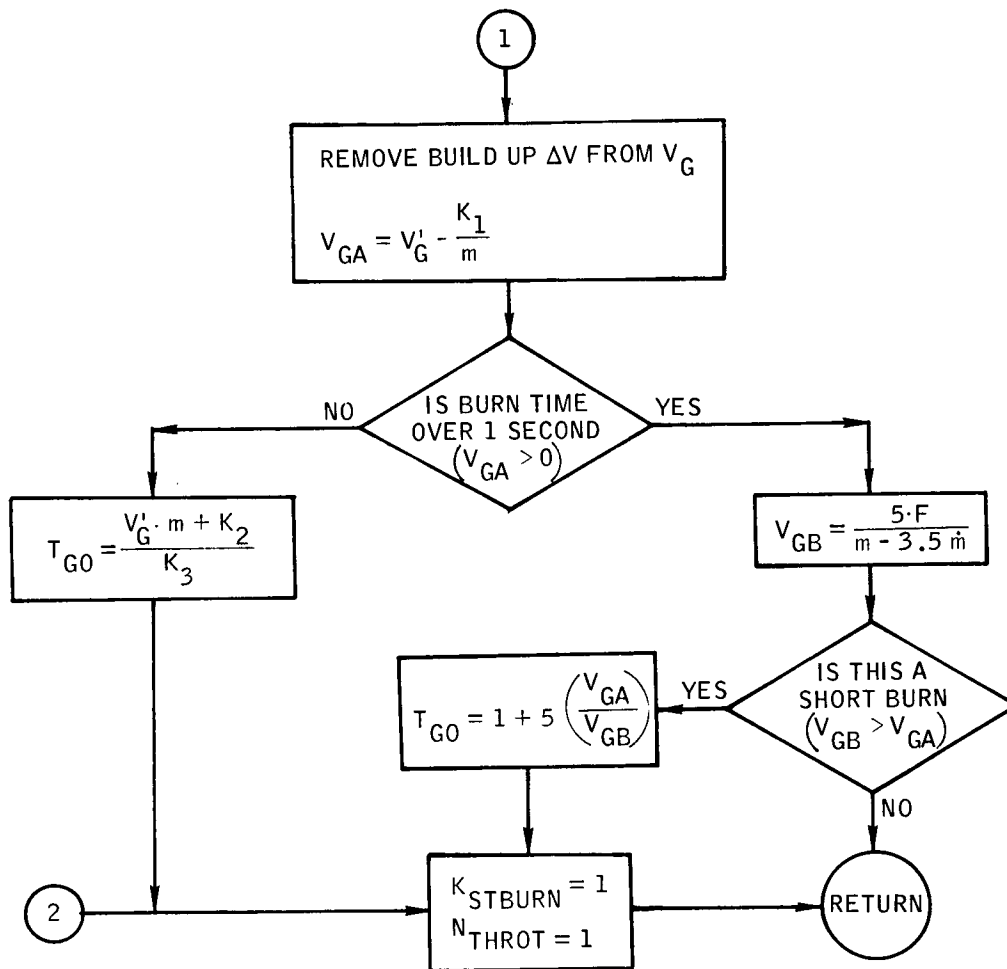


Figure B-91.- Concluded.

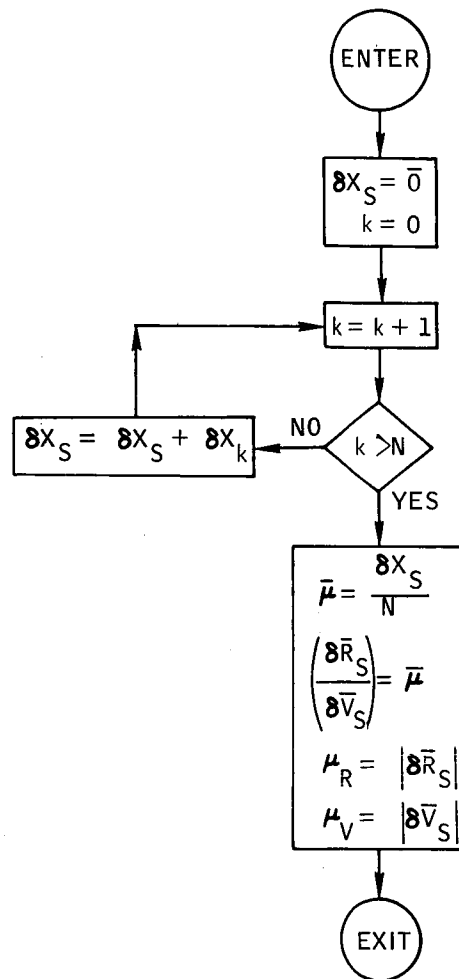


Figure B-92. - Flow chart of subroutine SMEAN.



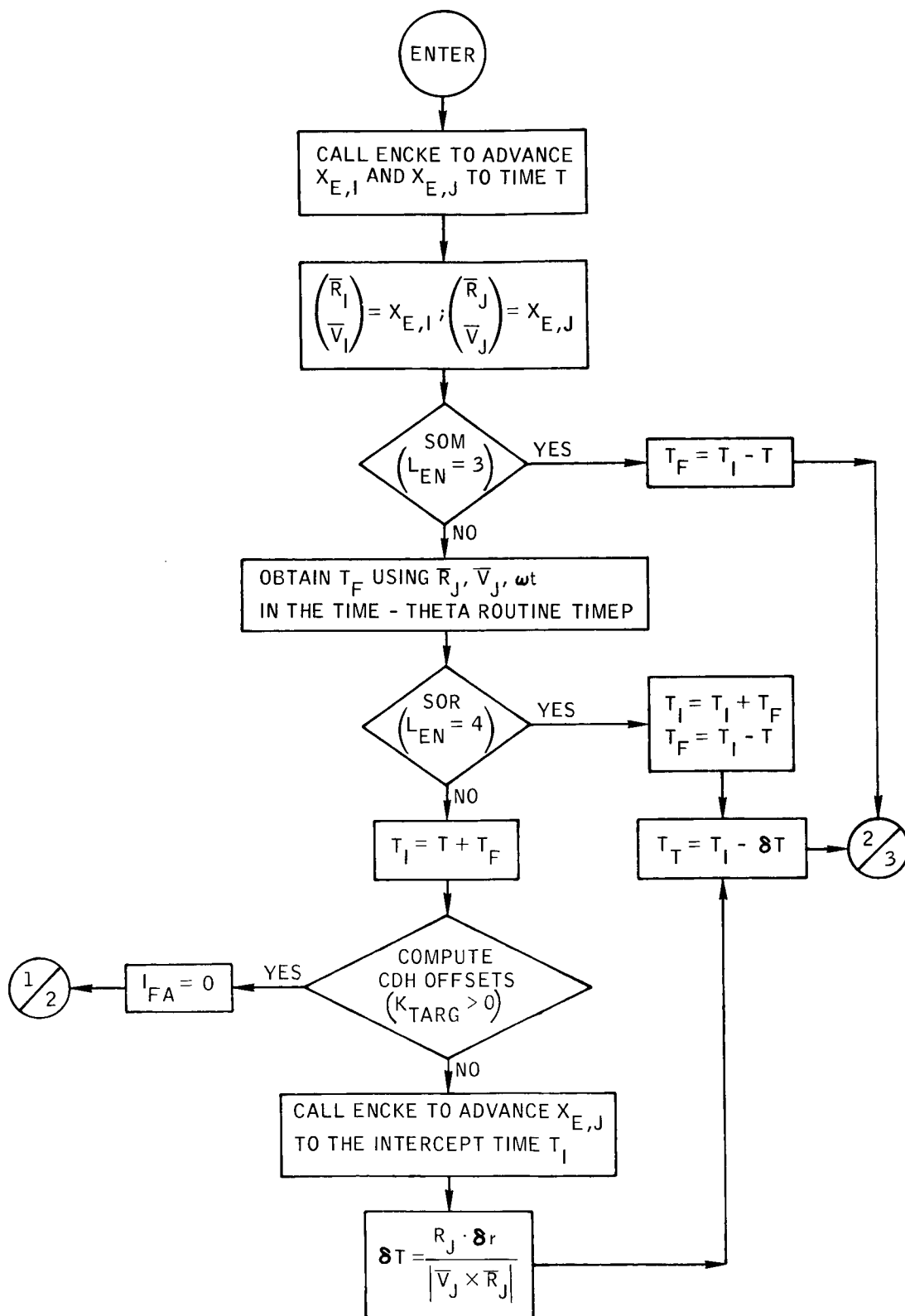


Figure B-93.- Flow chart of subroutine SOR.

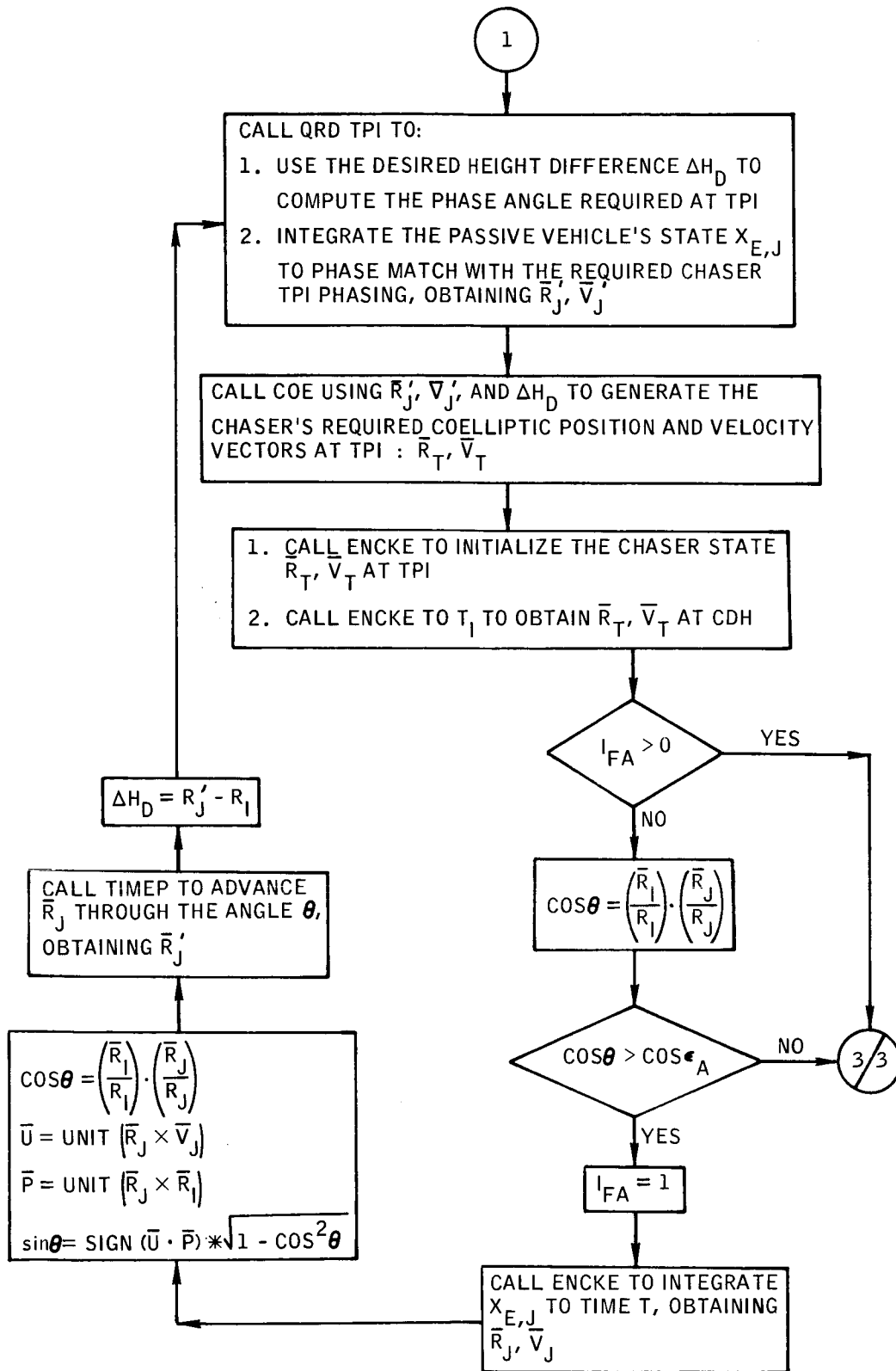


Figure B-93.- Continued.

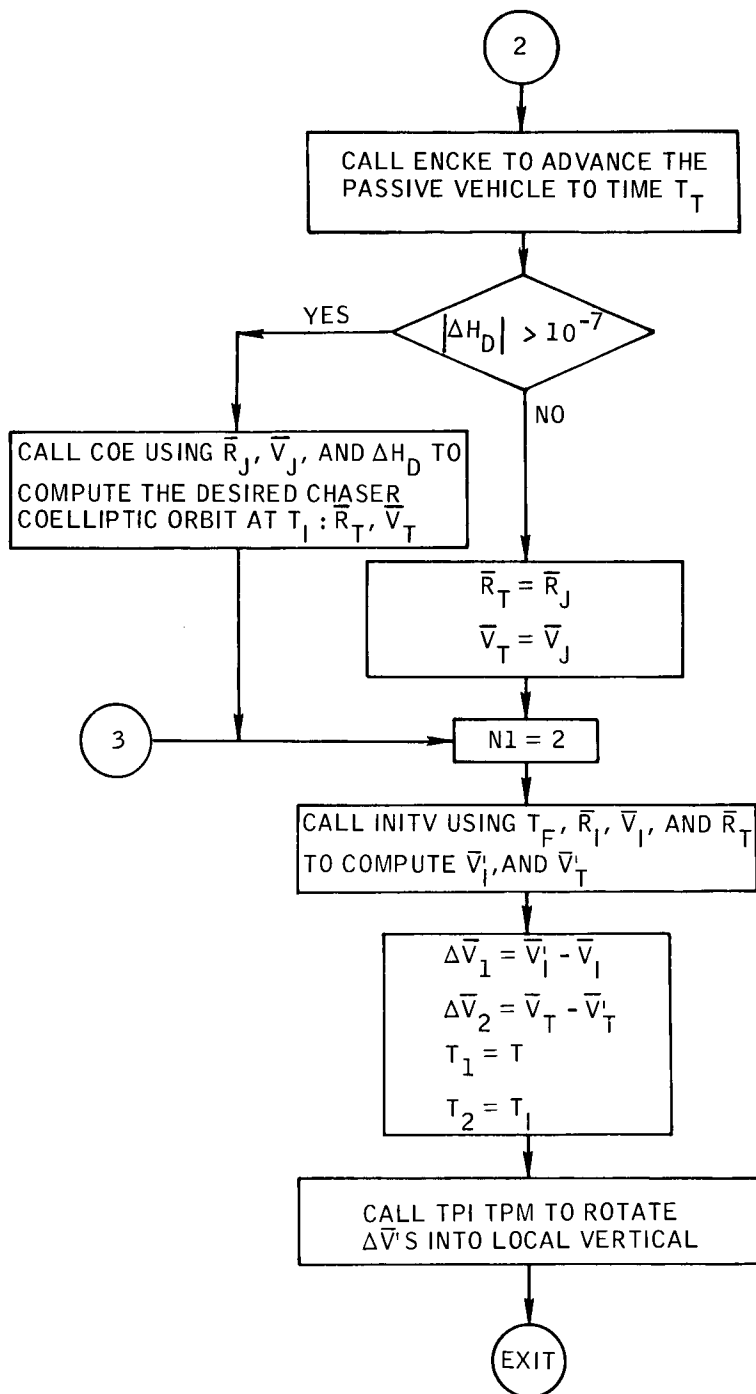


Figure B-73.- Concluded.

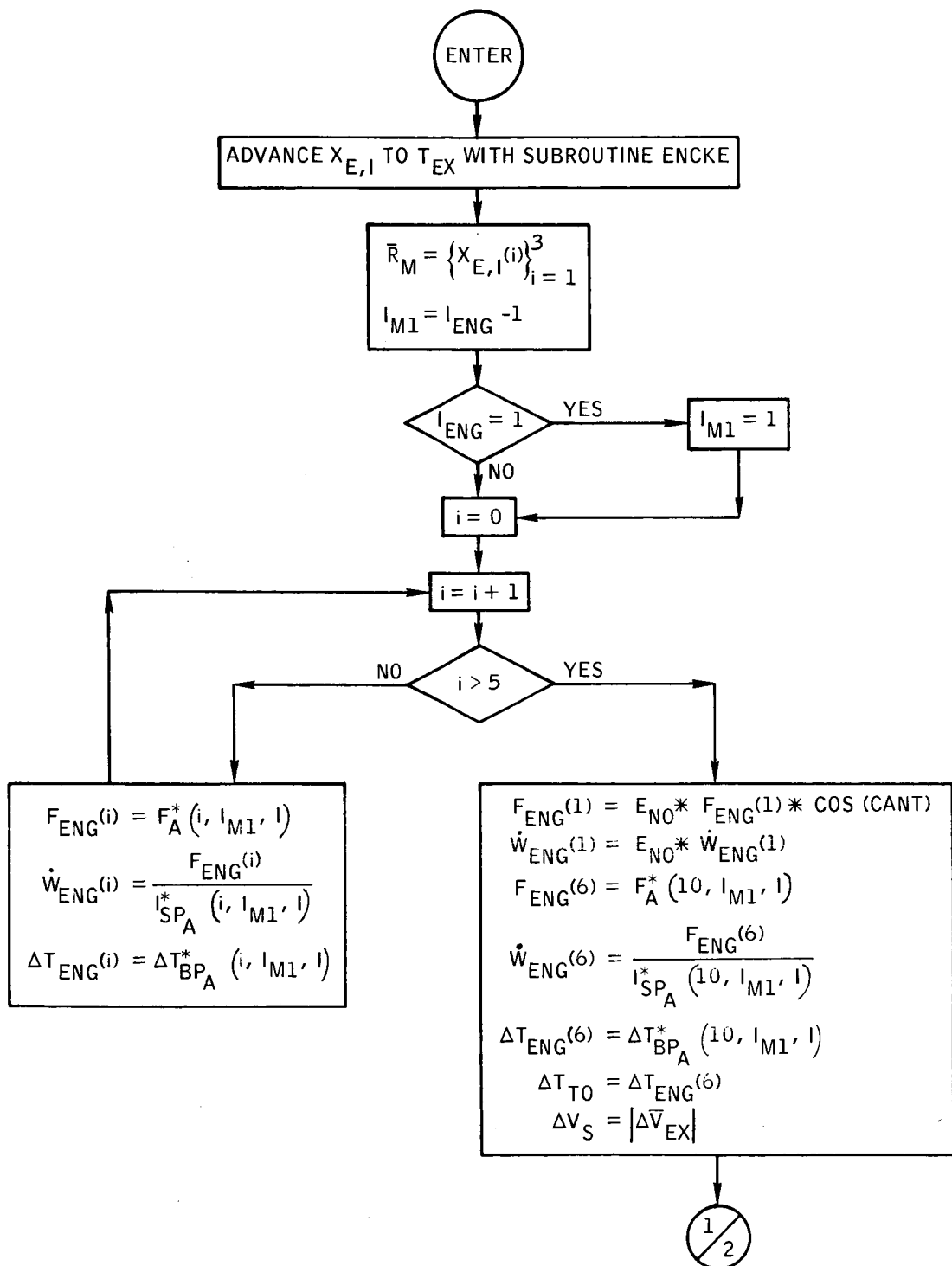


Figure B-94. - Flow chart of subroutine SPLIT.

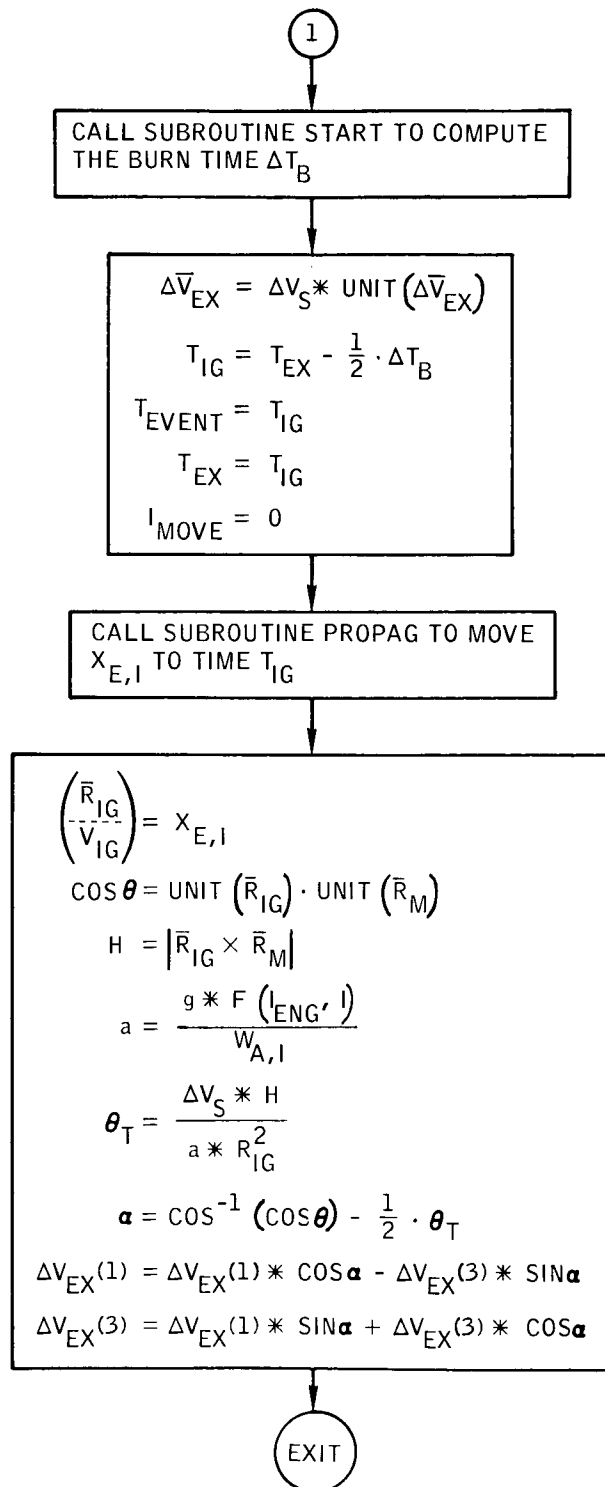


Figure B-94.- Concluded.

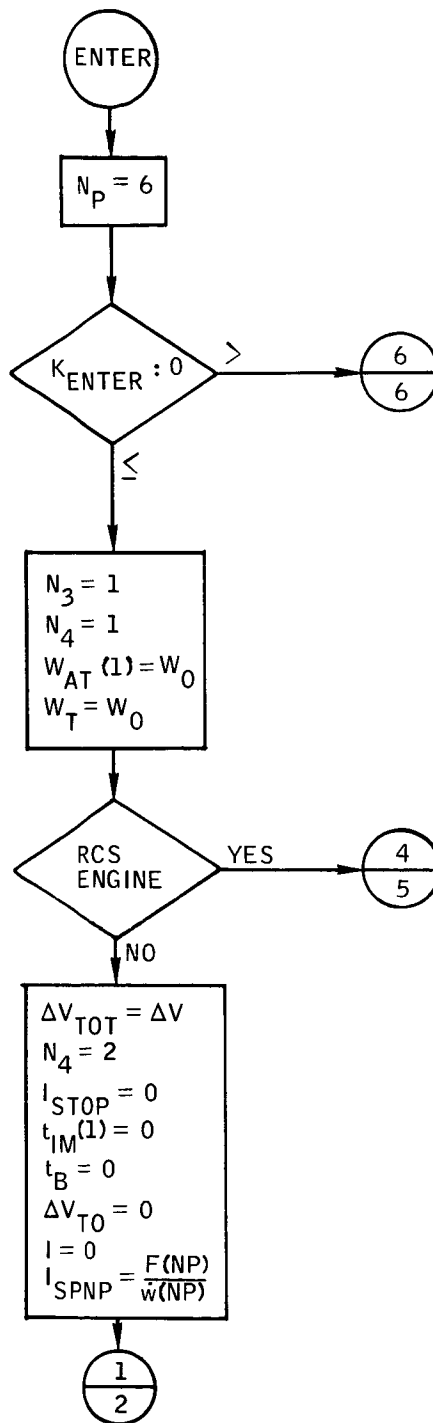


Figure B-95. - Flow chart of subroutine START.

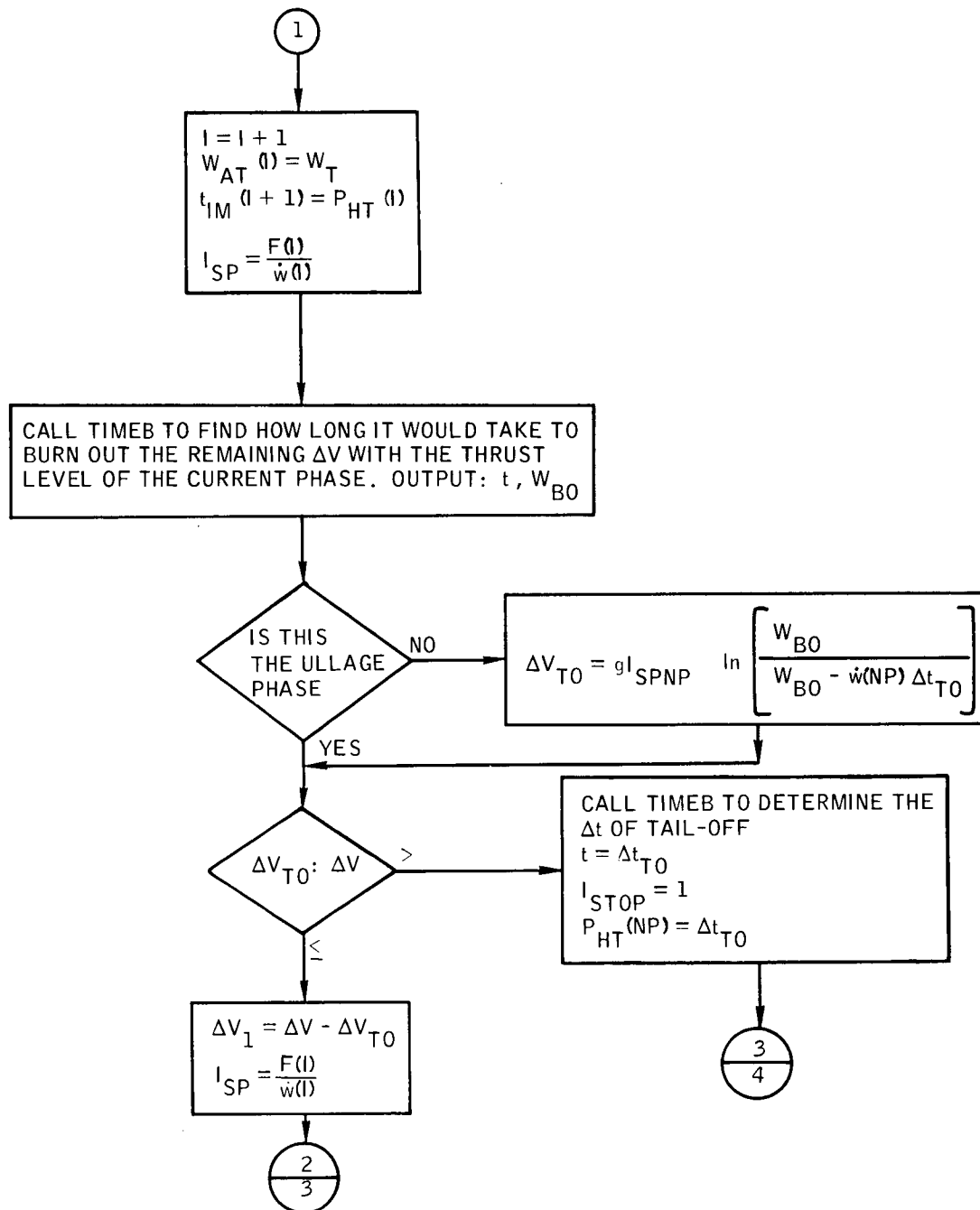


Figure B-95.- Continued.

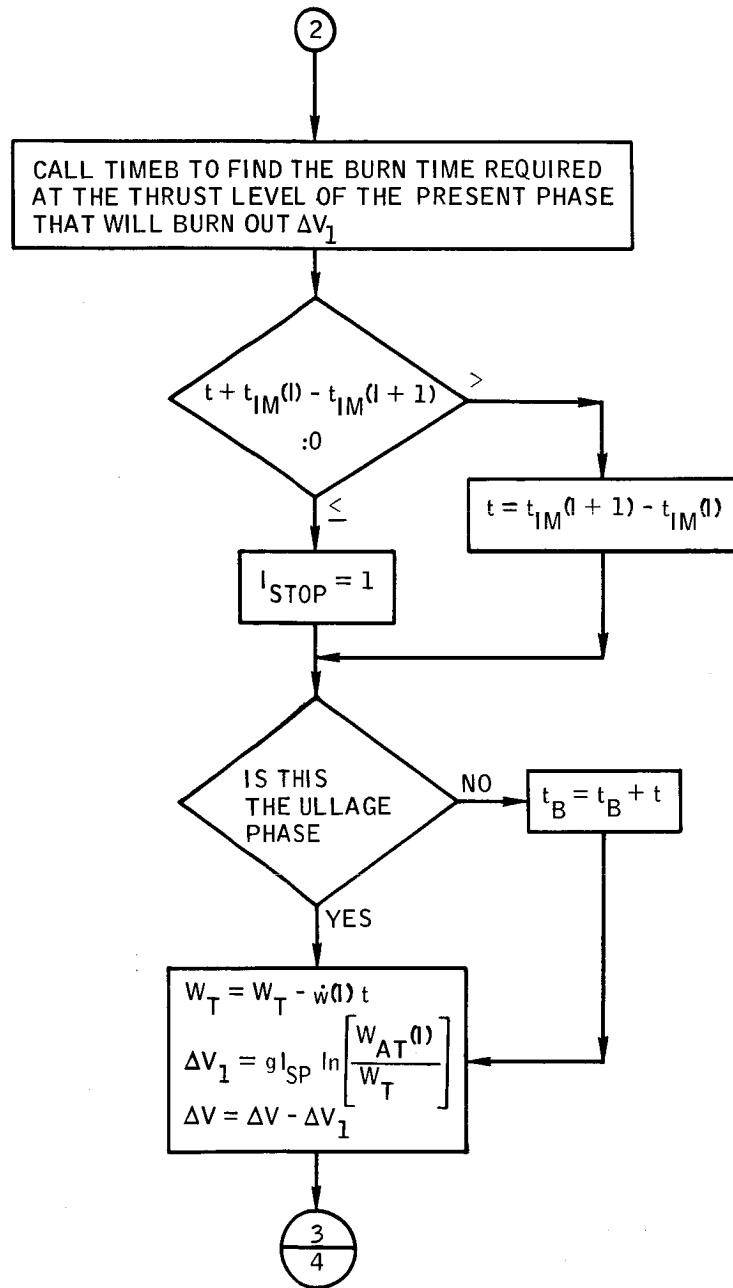


Figure B-95.- Continued.



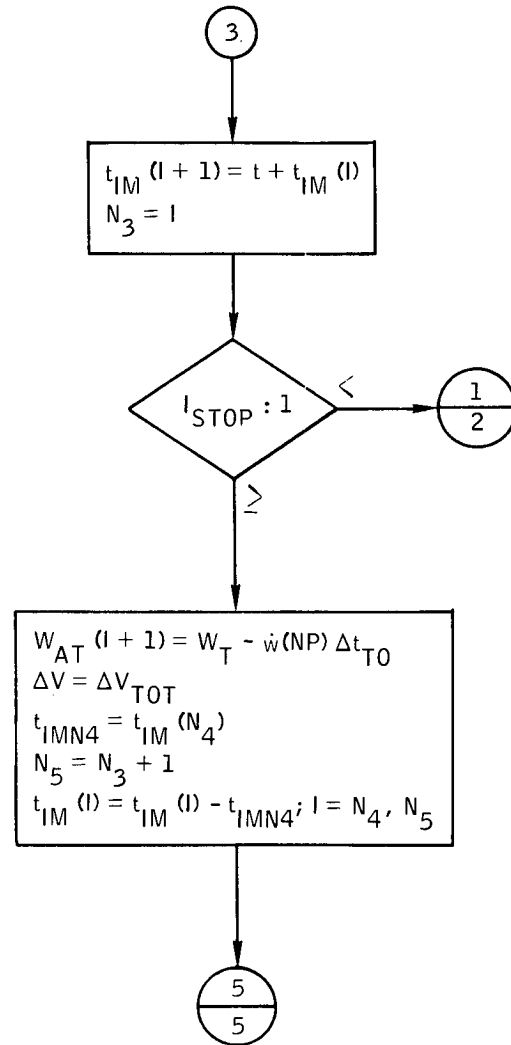


Figure B-95.- Continued.

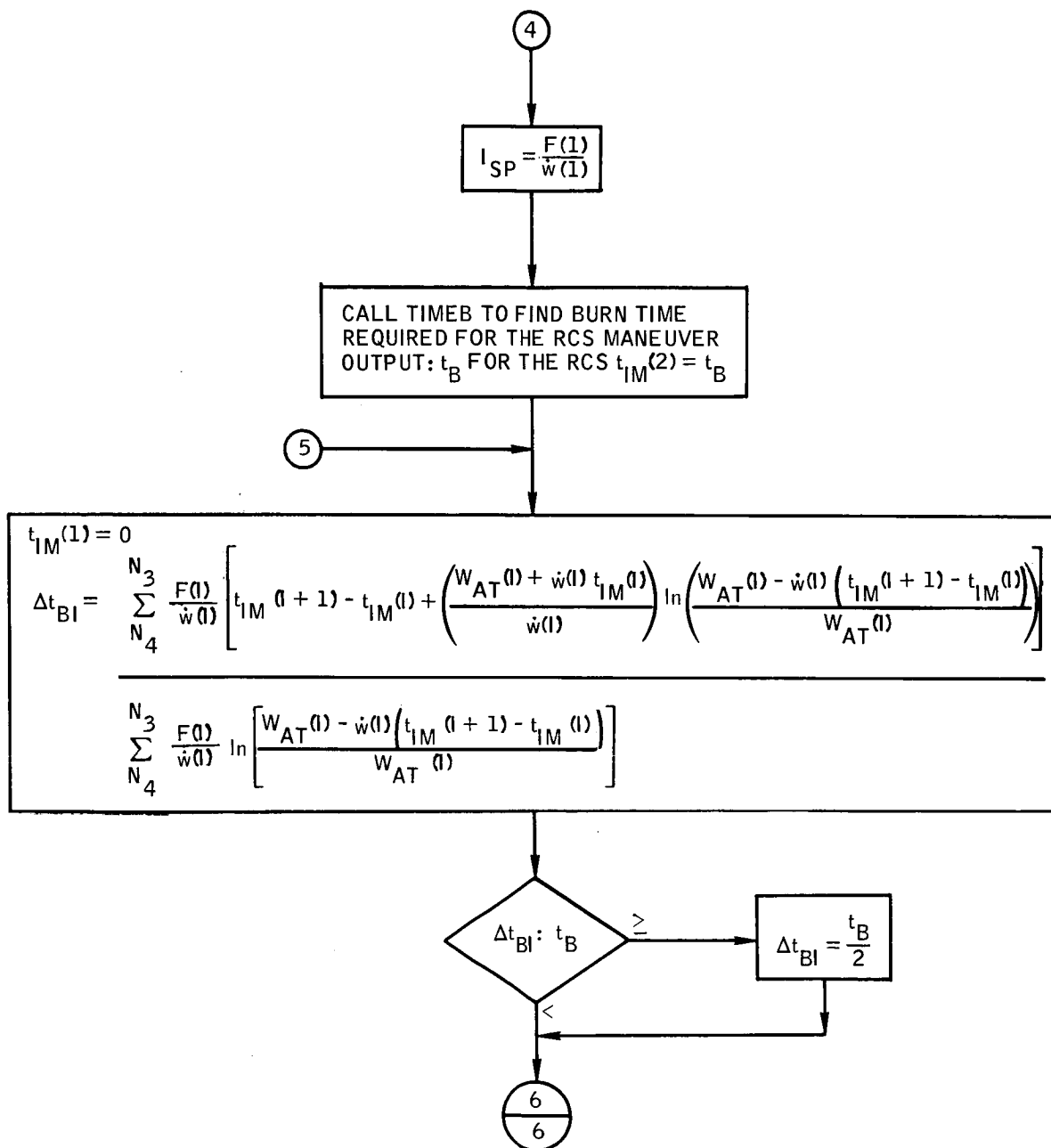


Figure B-95. - Continued.

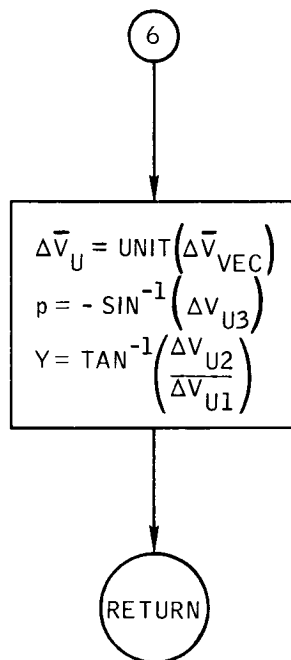
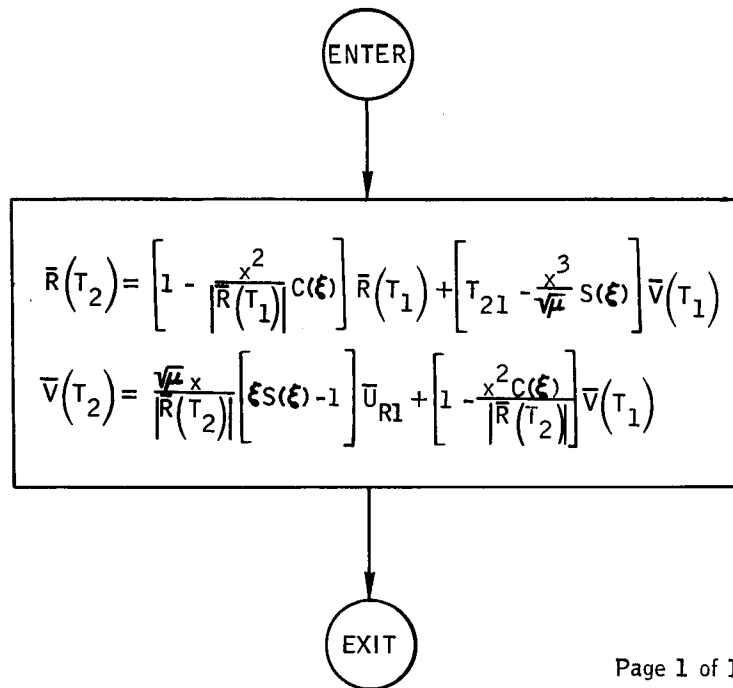


Figure B-95. - Concluded.



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Figure B-96.- Flow chart of subroutine STAYT.

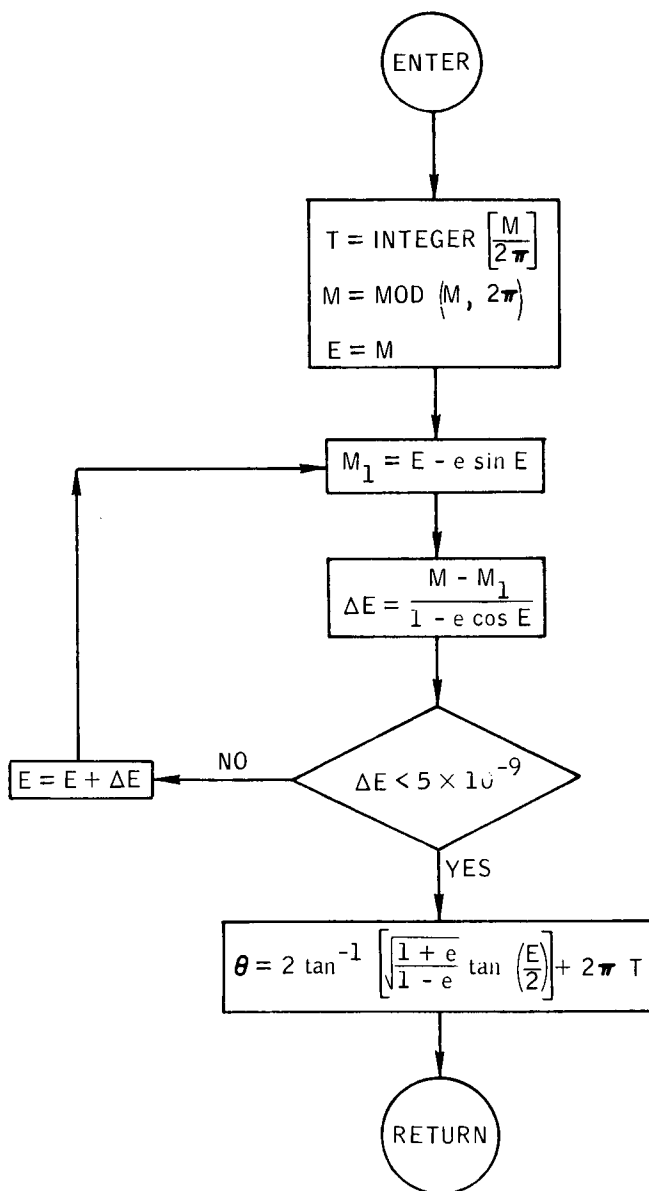


Figure B-97. - Flow chart of function TA.

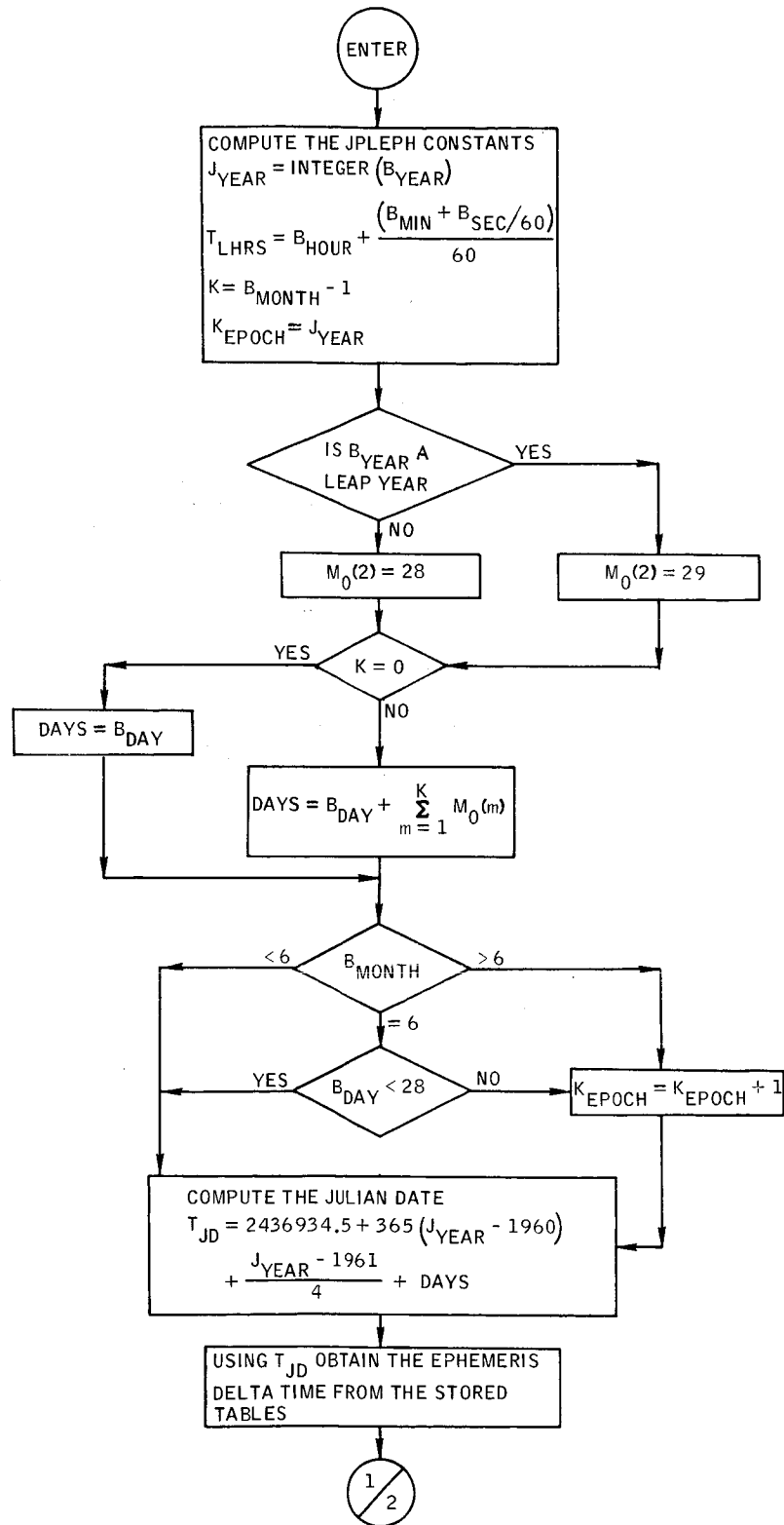
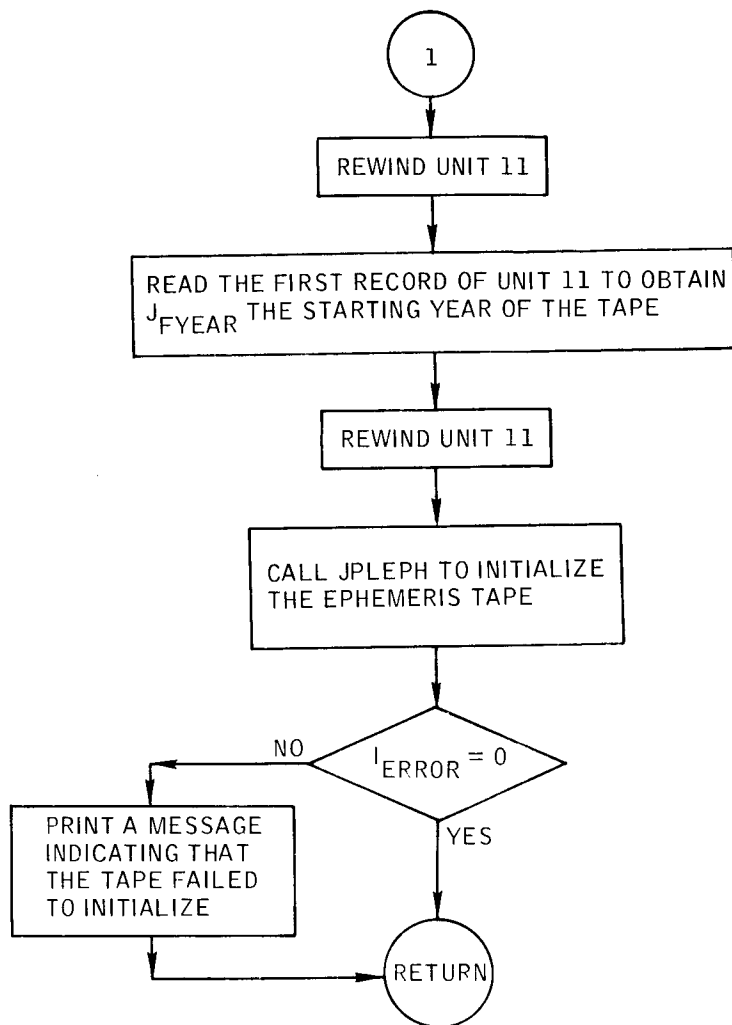


Figure B-98.- Flow chart of subroutine TAPEUP.



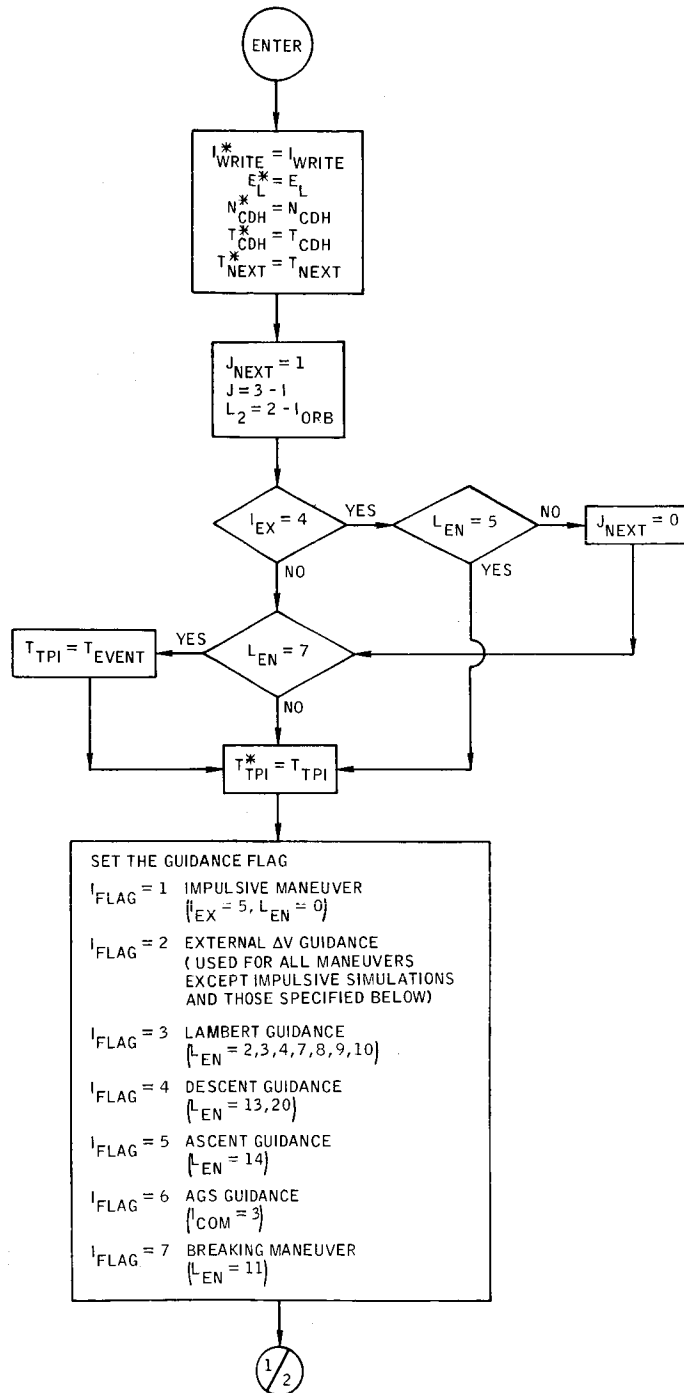


Figure B-99. - Flow chart of subroutine TARGET.



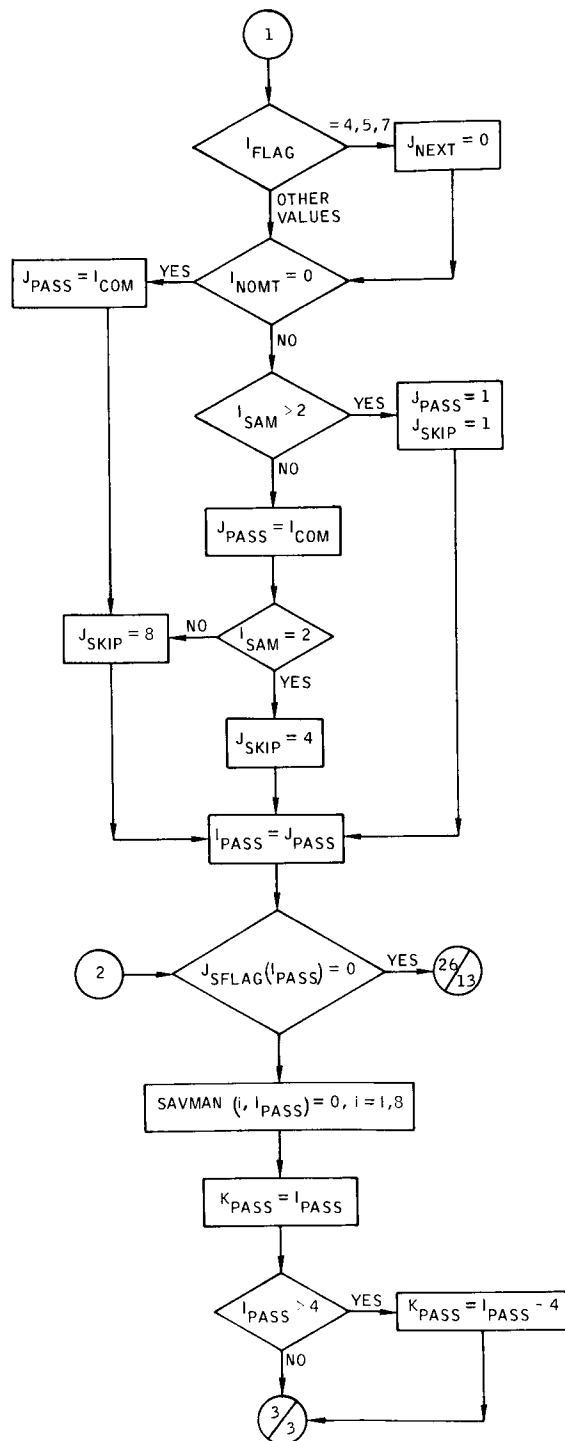


Figure B-99. - Continued.

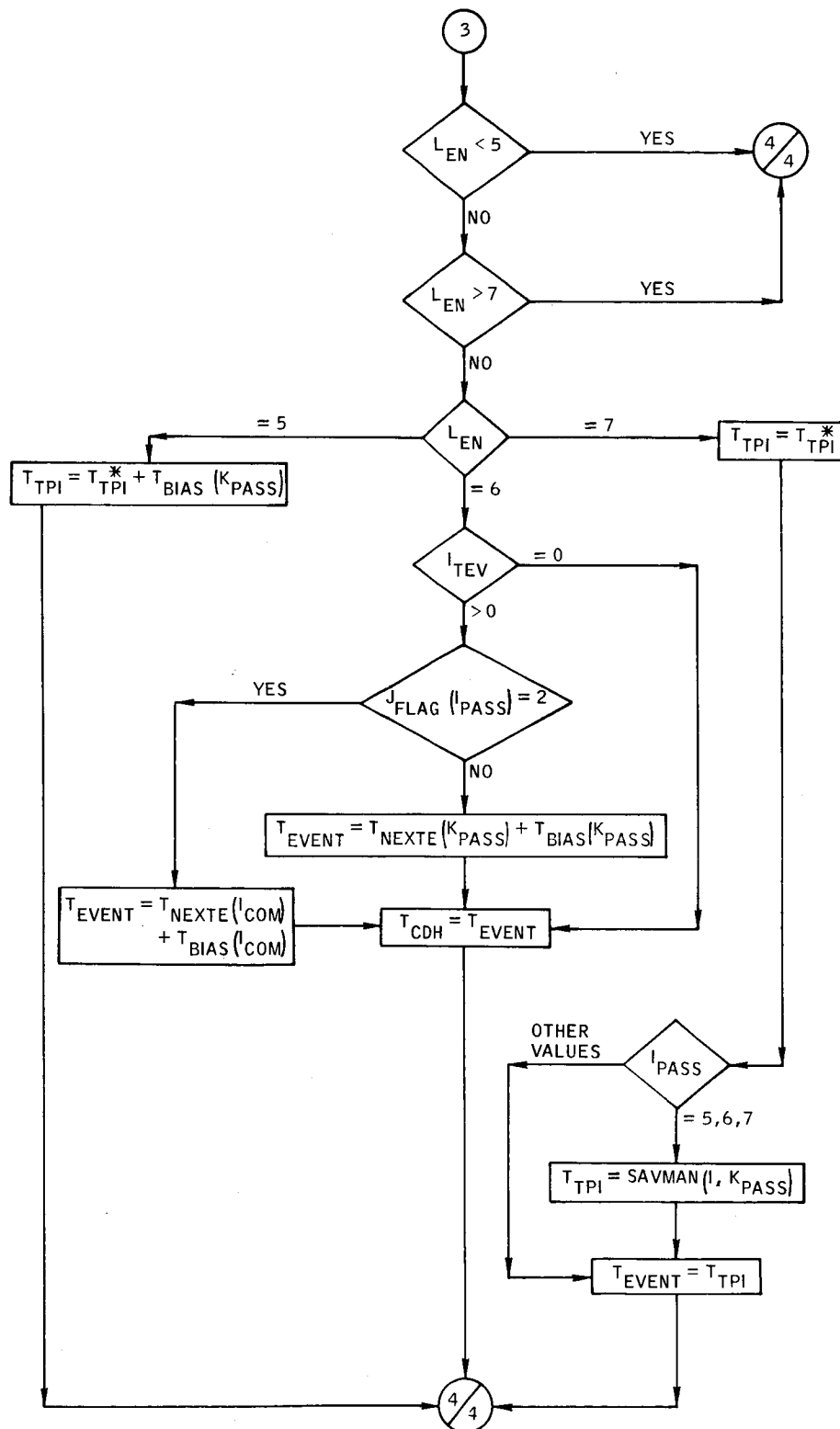


Figure B-99.- Continued.

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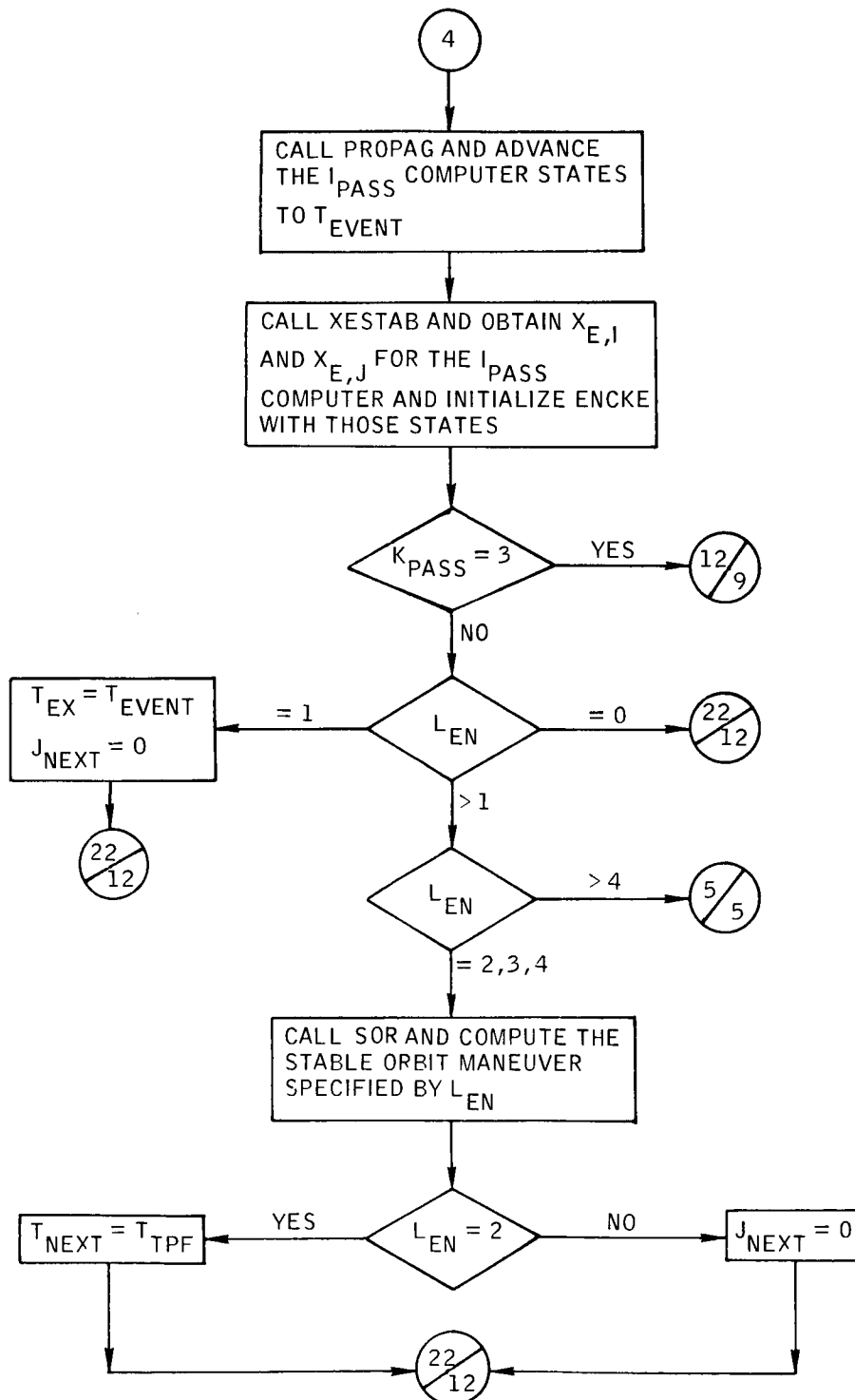


Figure B-99. - Continued.

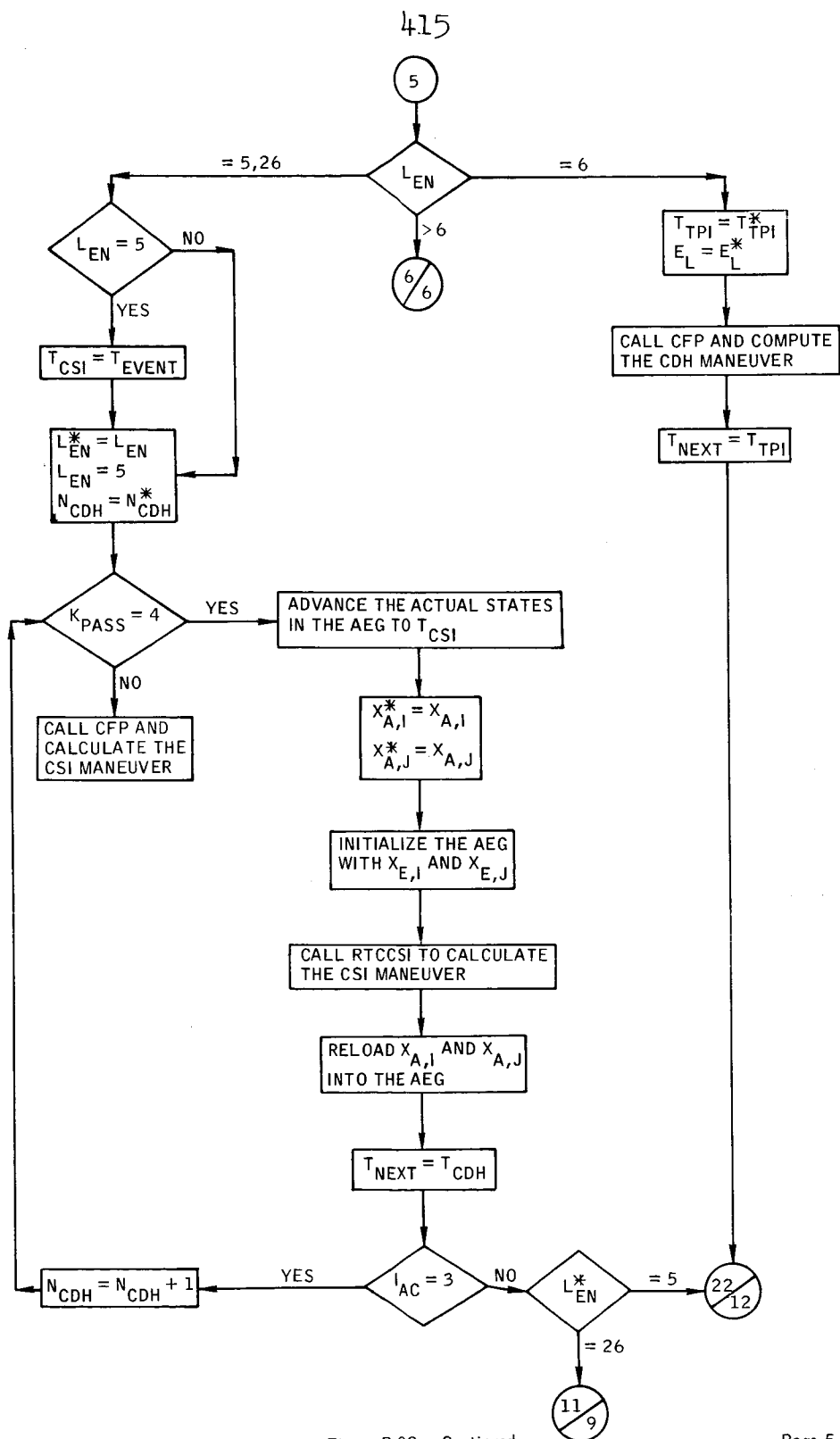


Figure B-99. - Continued.

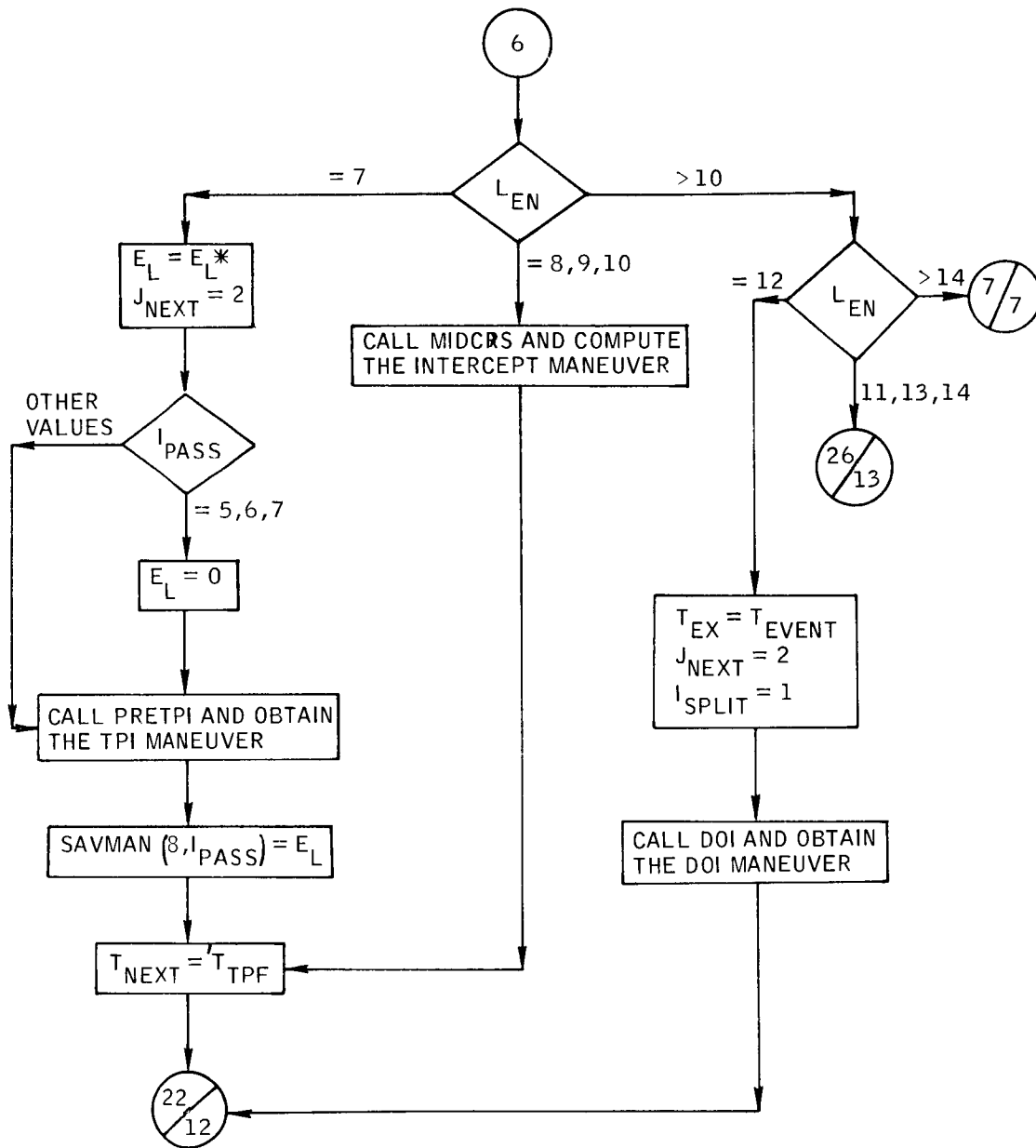
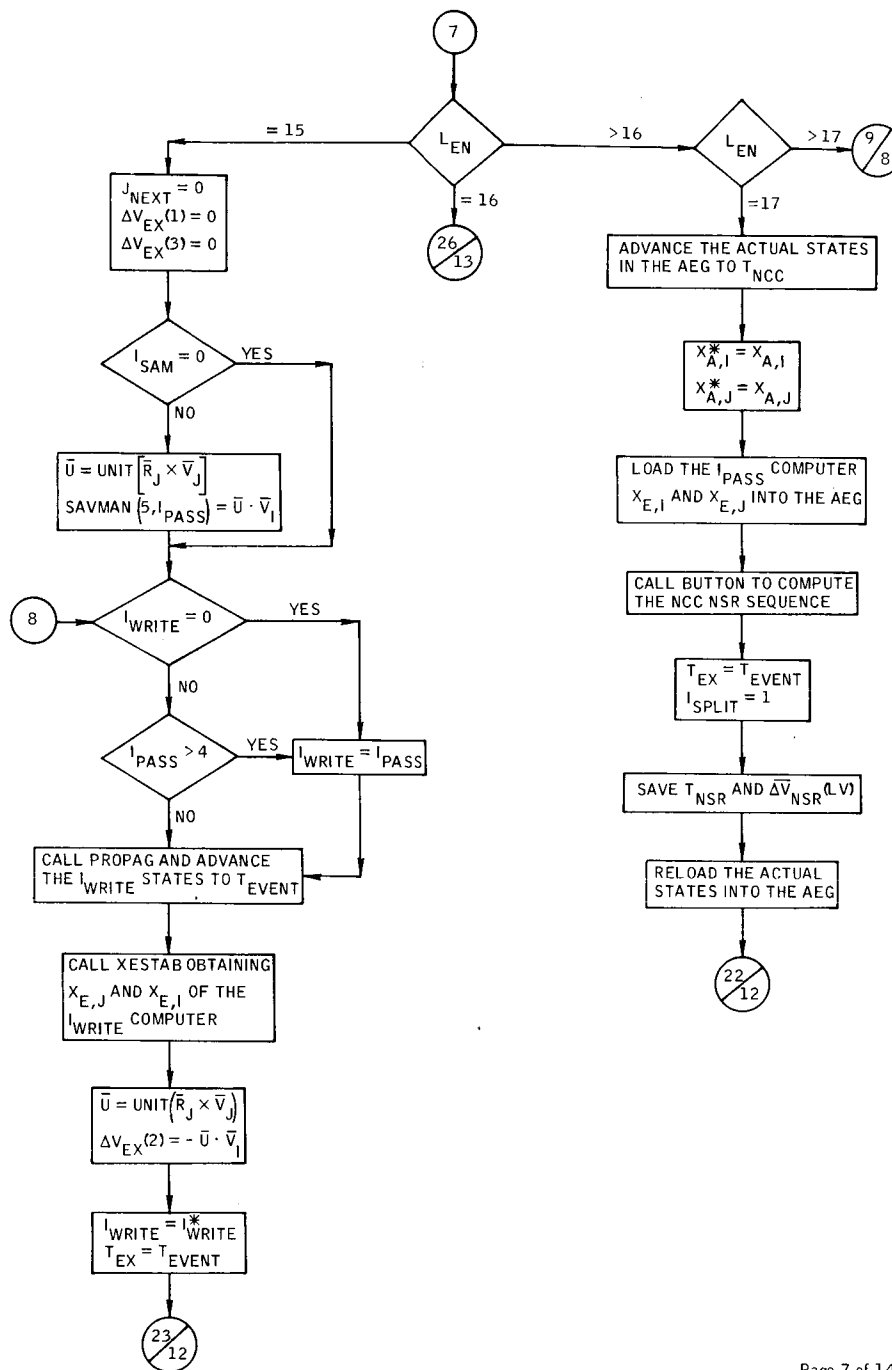


Figure B-99. - Continued.



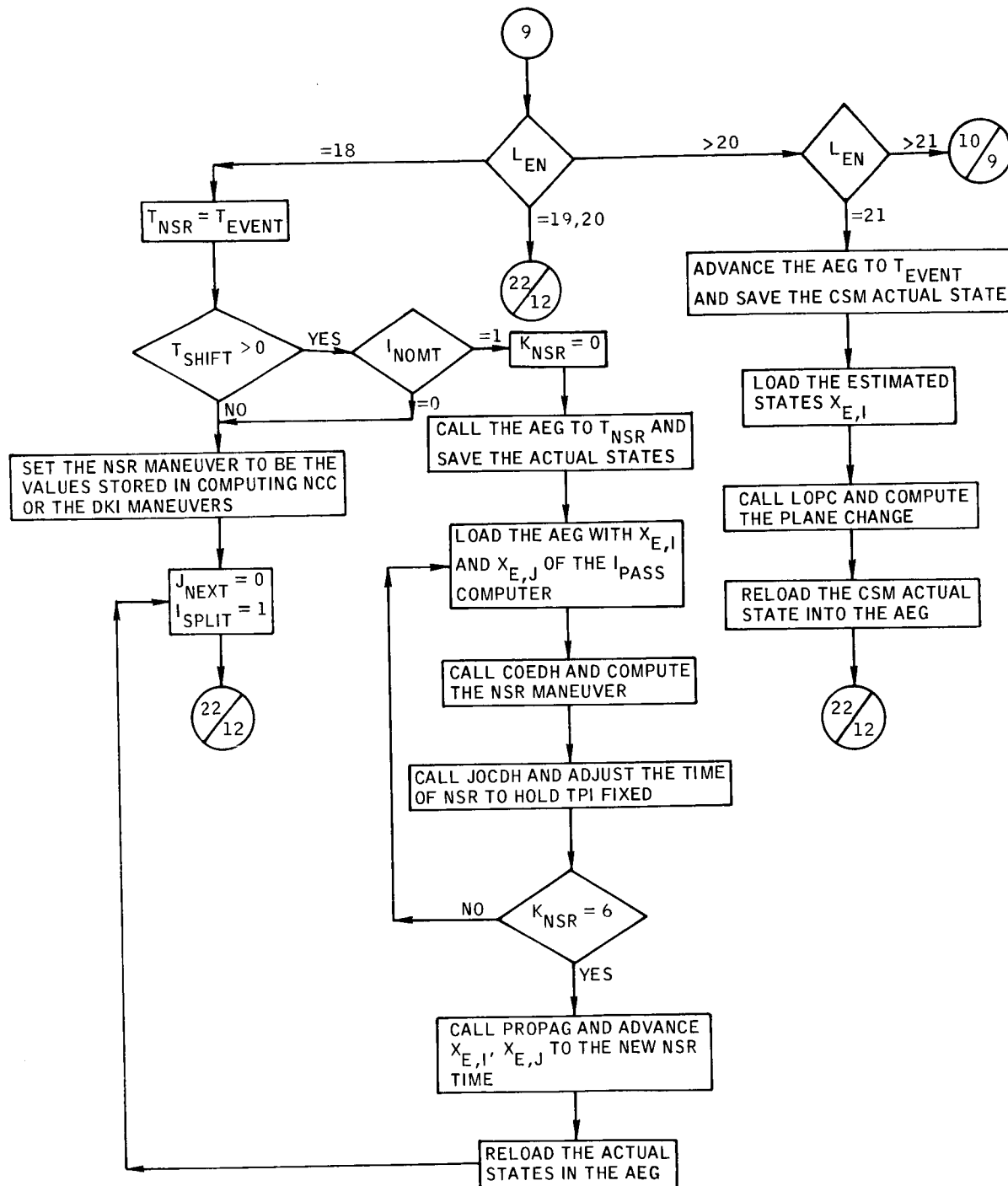


Figure B-99.- Continued.

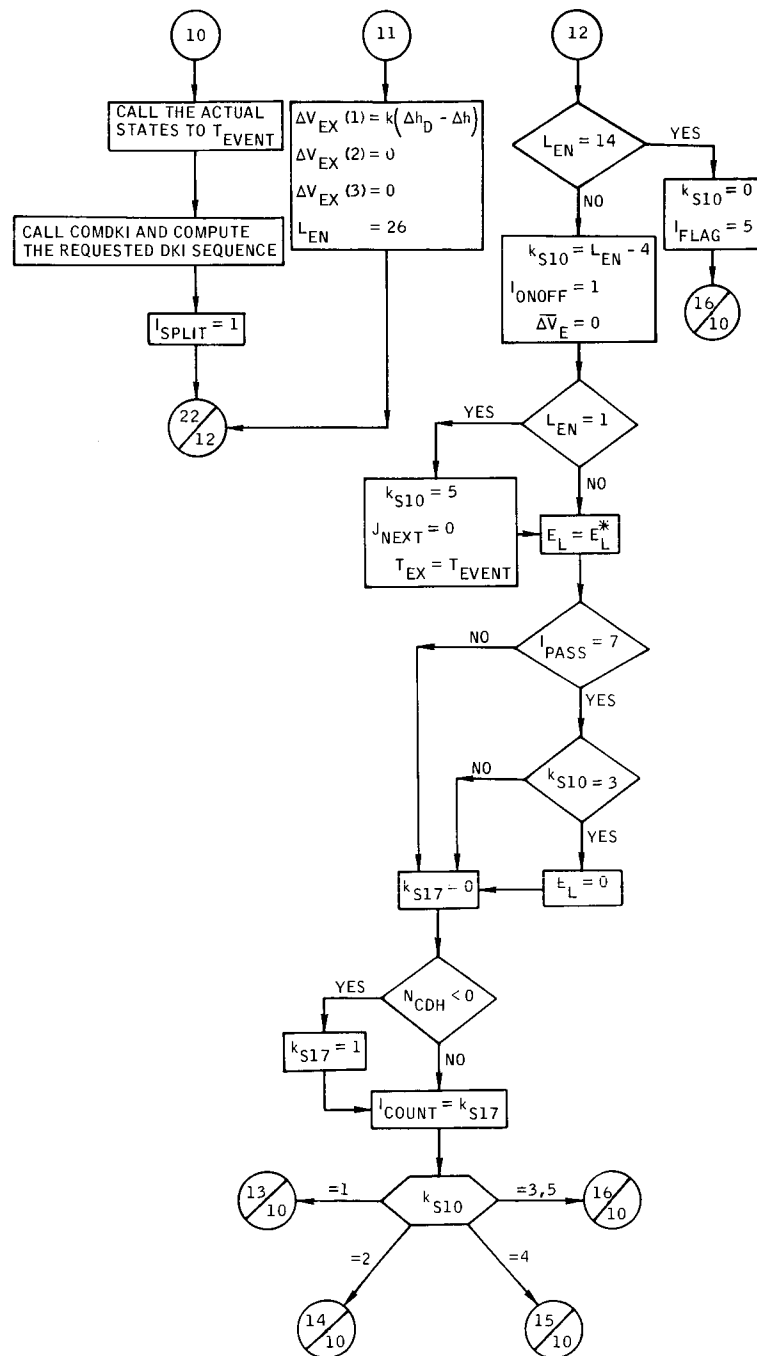


Figure B-99. - Continued.



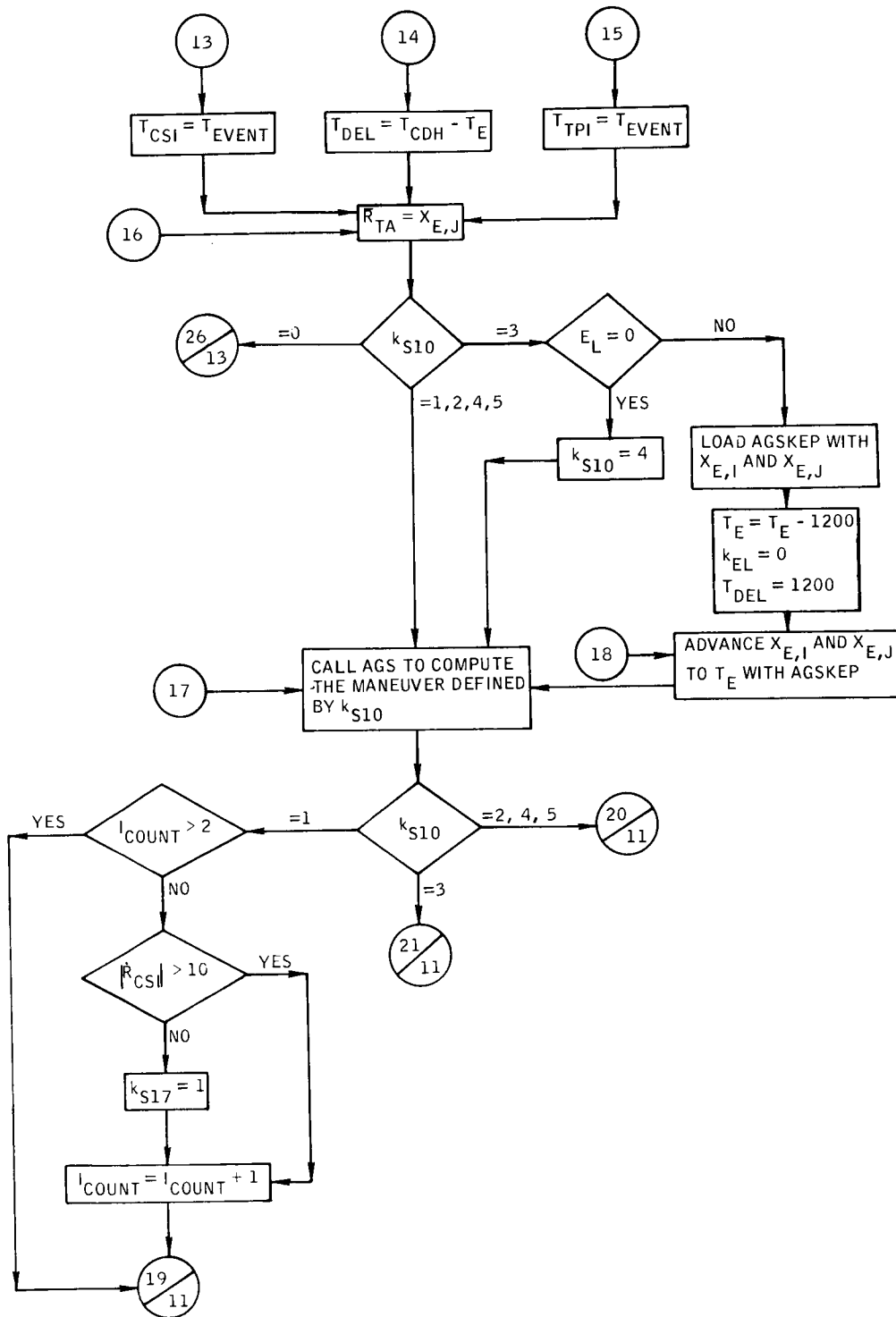


Figure B-99. - Continued.

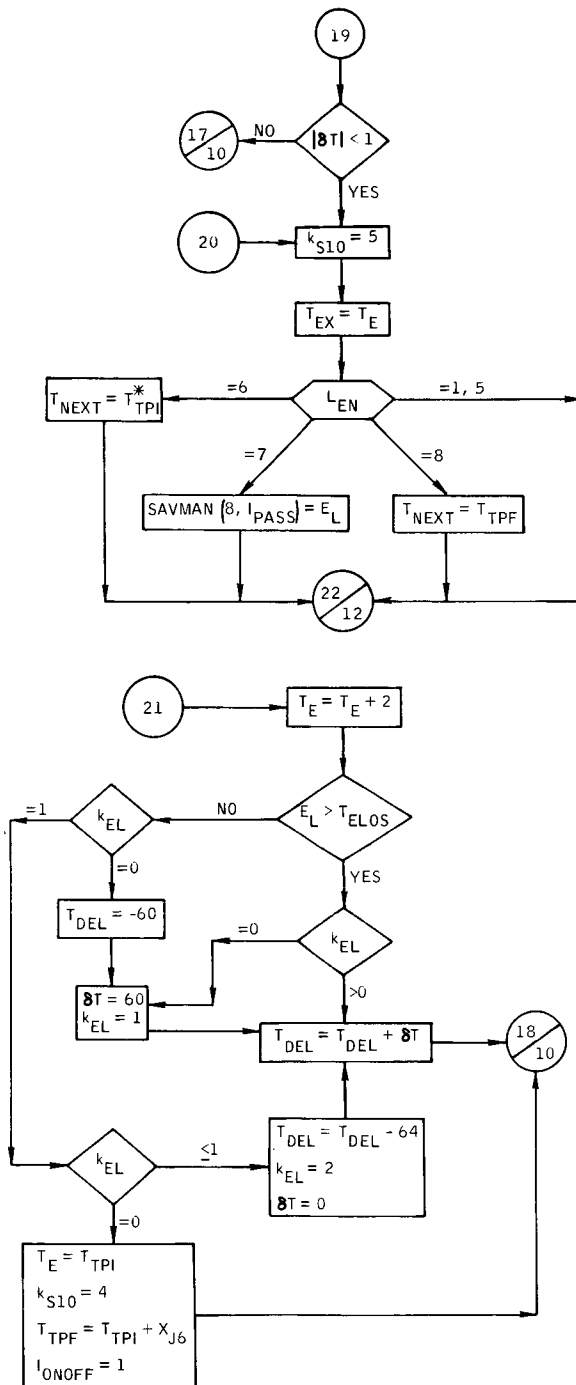


Figure B-99. - Continued.

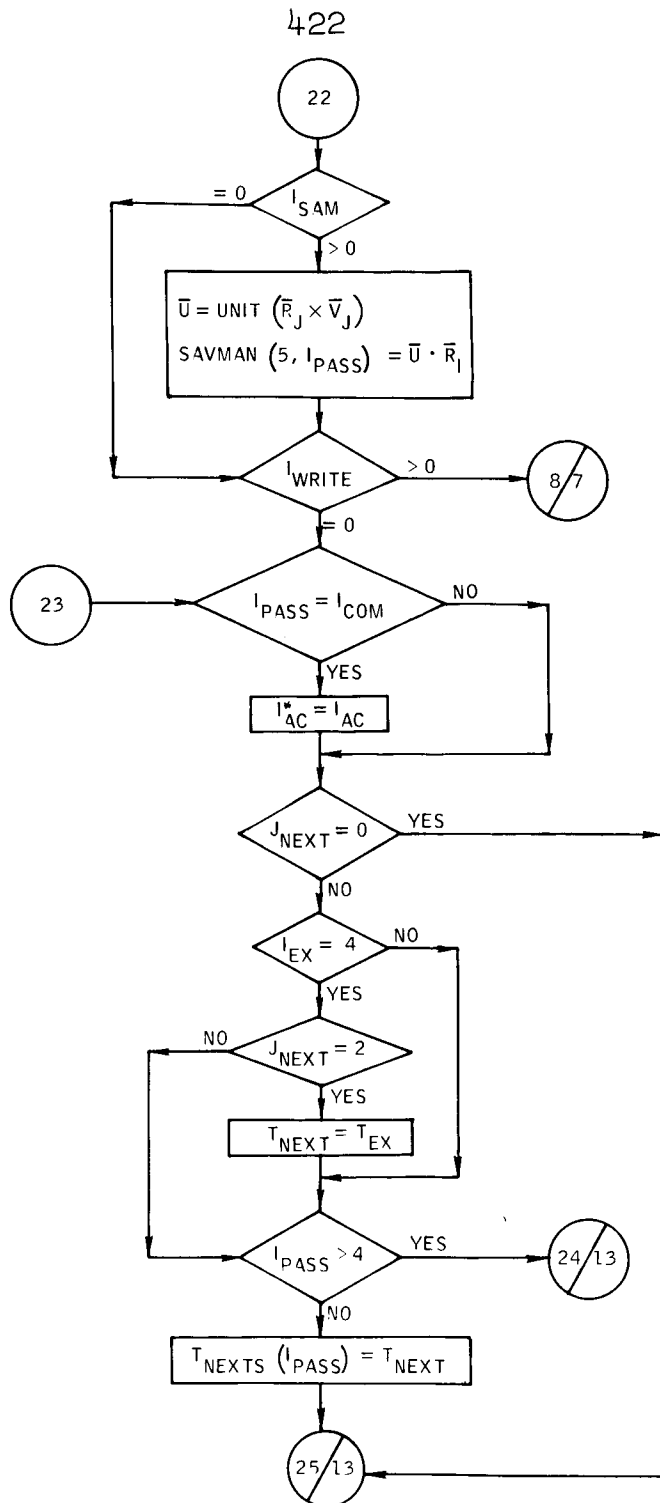
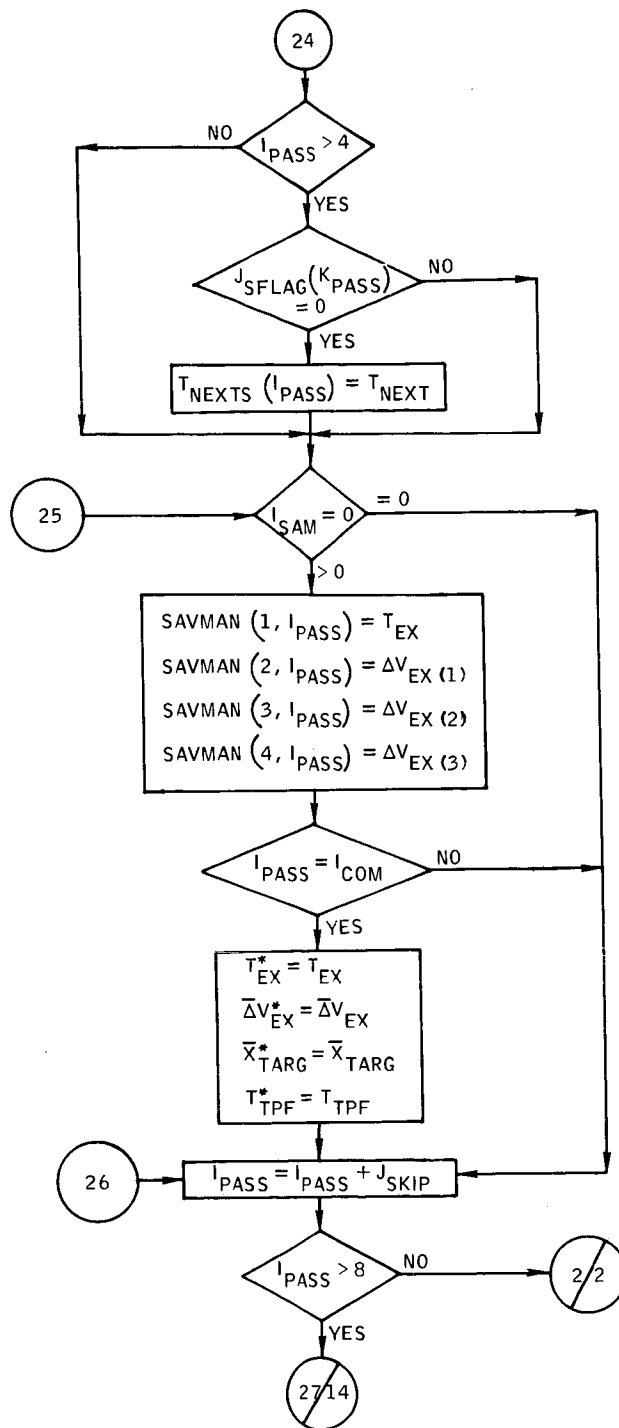


Figure B-99. - Continued.



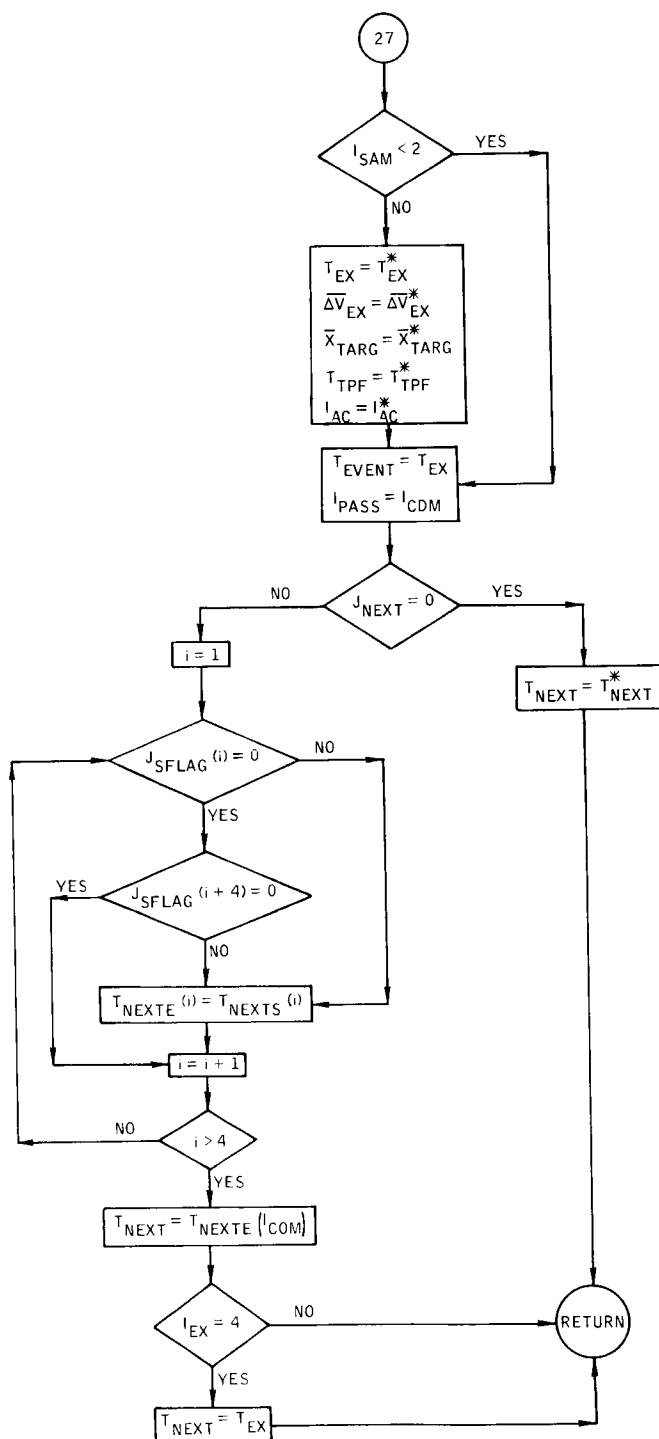


Figure B-99. - Concluded.

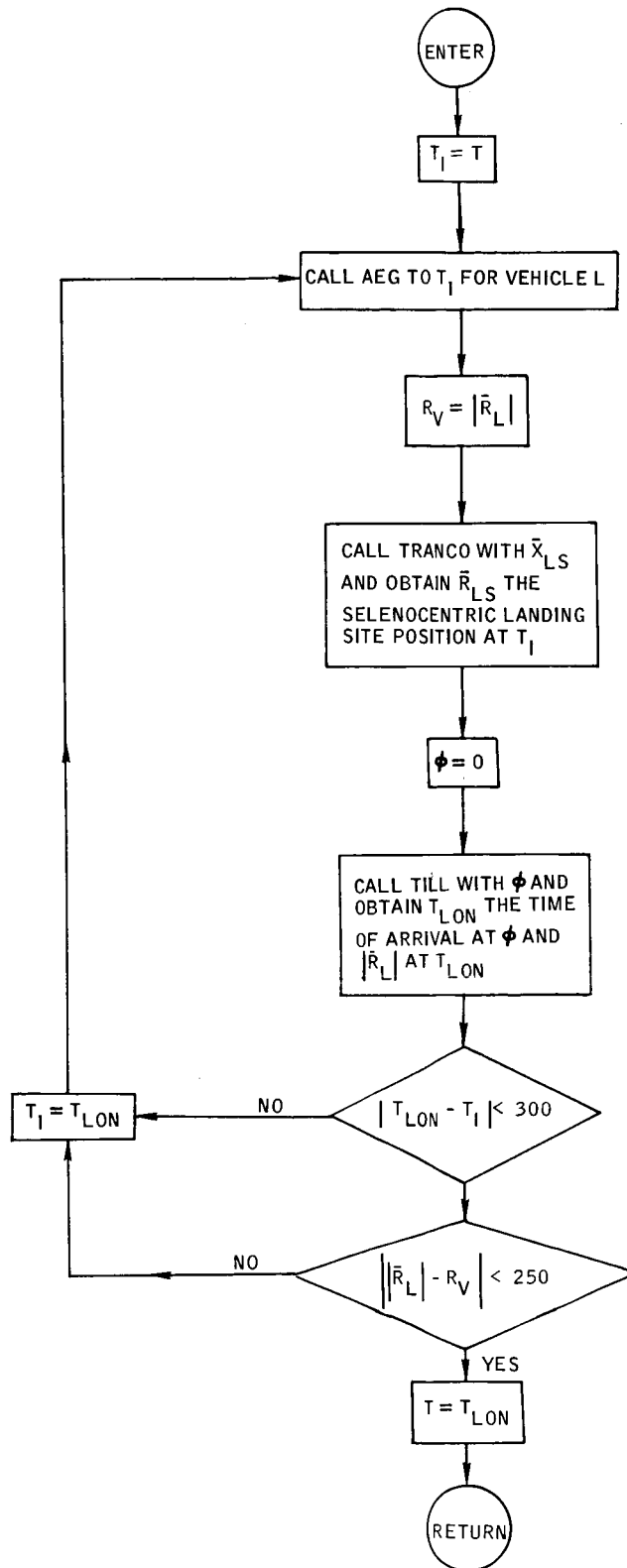


Figure B-100.- Flow chart of subroutine TCONE.

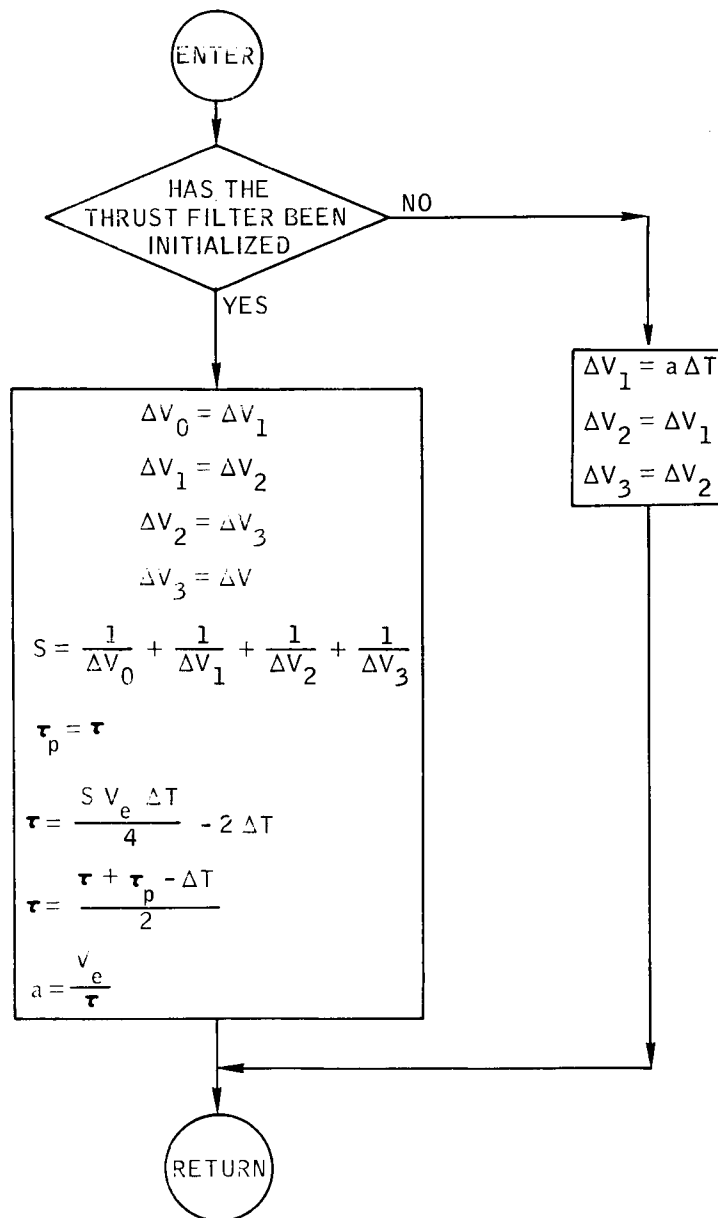


Figure B-101.- Flow chart of subroutine THRFIL.

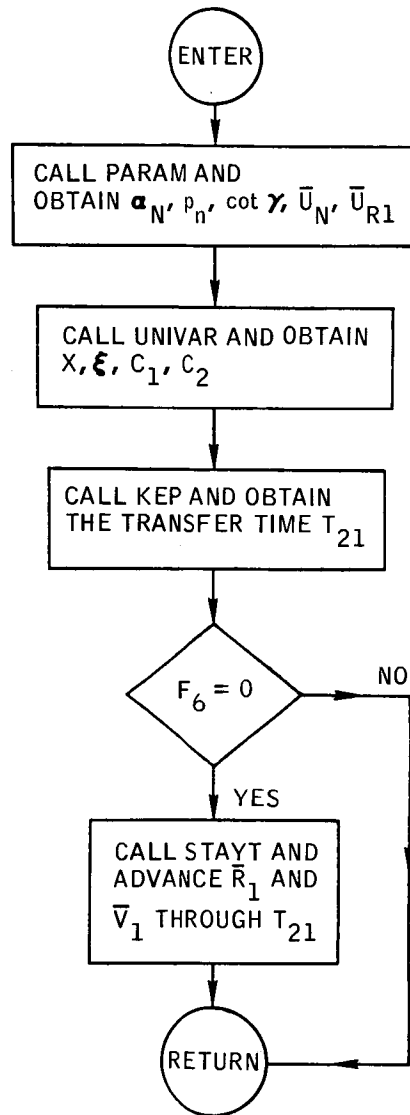


Figure B-102.- Flow chart of subroutine TIMEP.



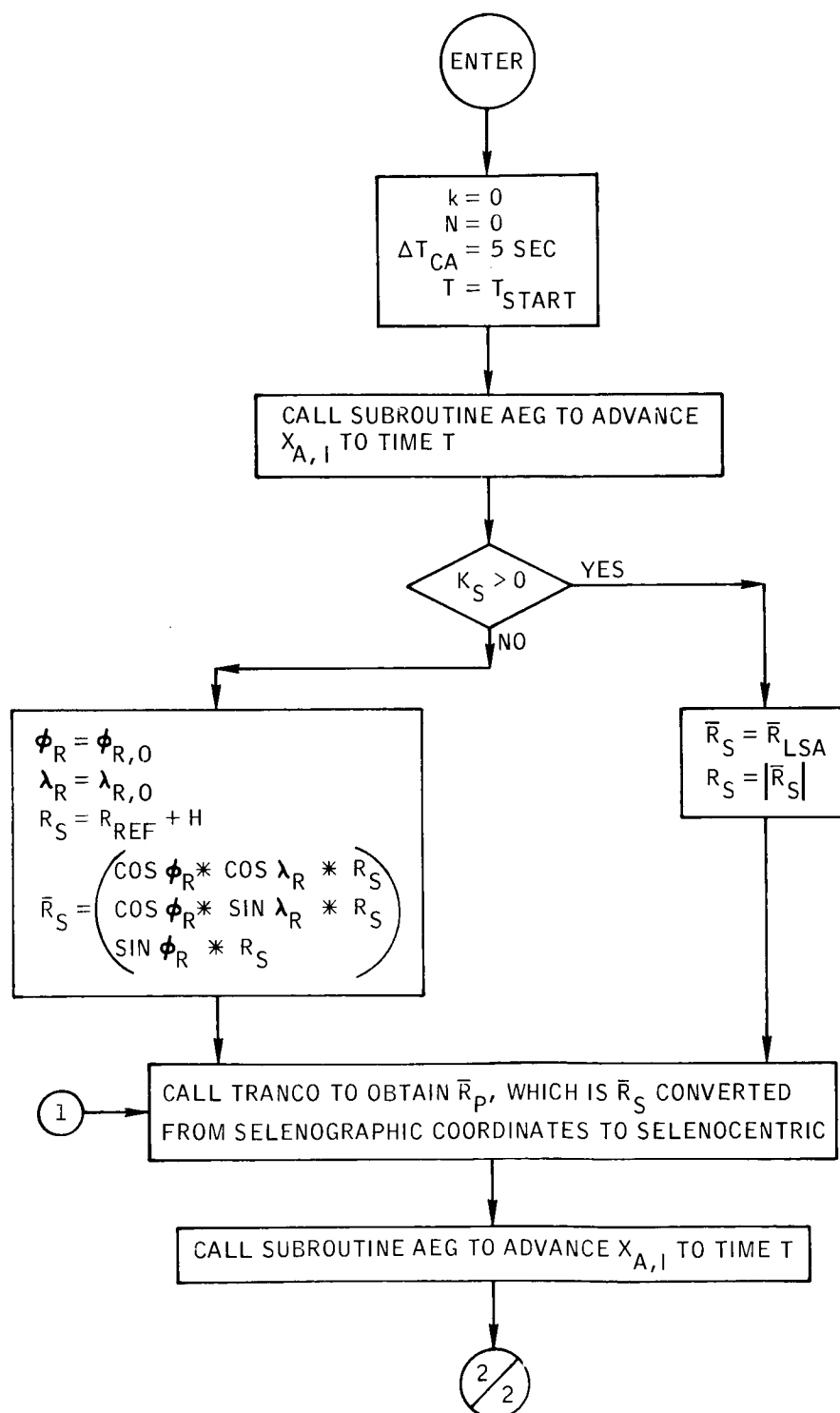


Figure B-103. - Flow chart of subroutine TPASS.

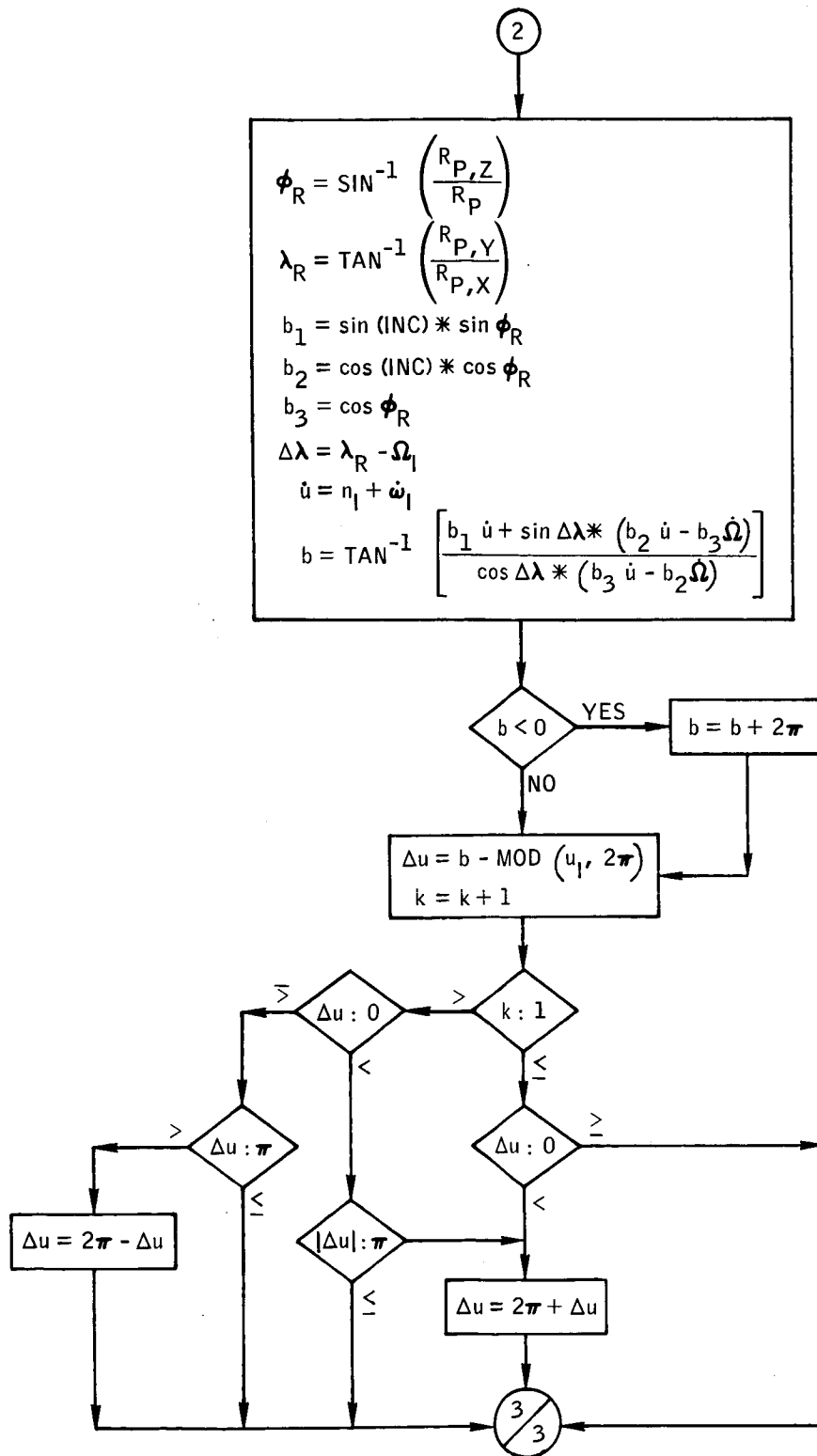


Figure B-103.- Continued.

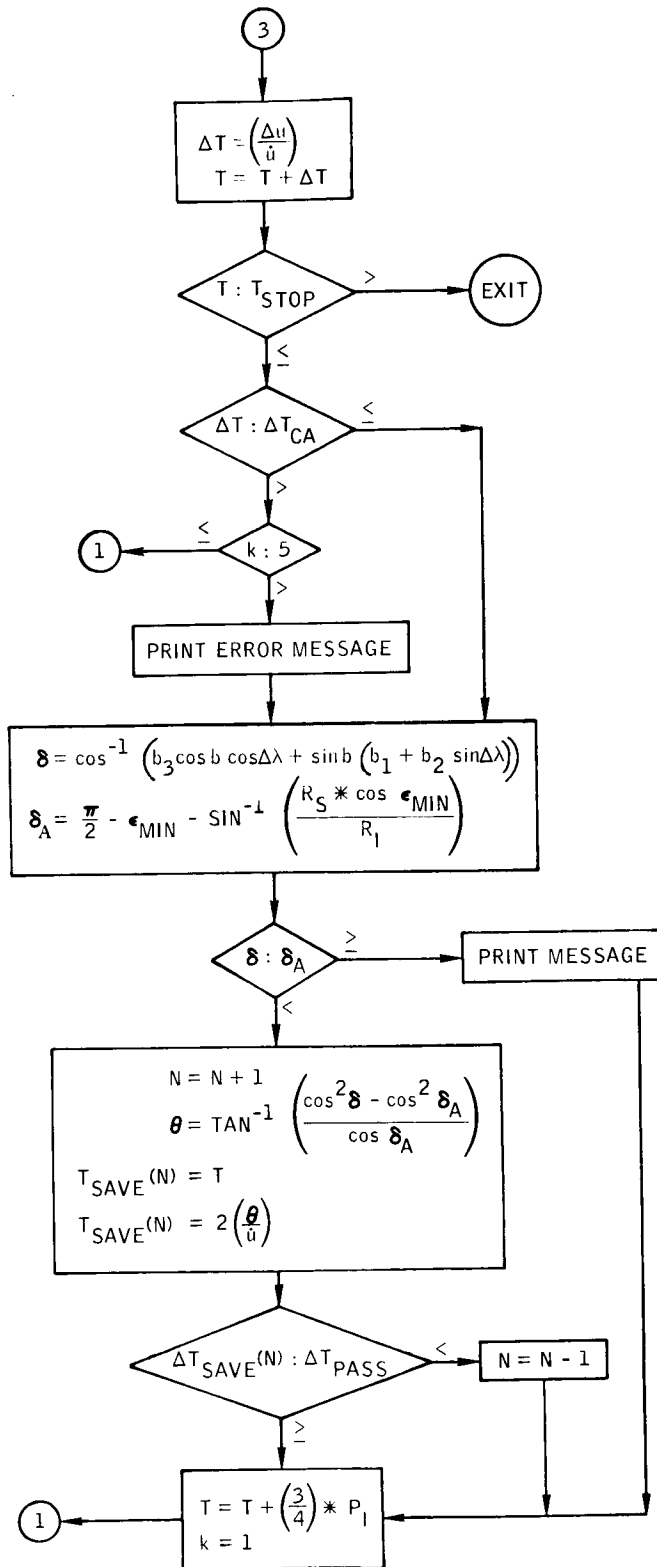


Figure B-103.- Concluded.

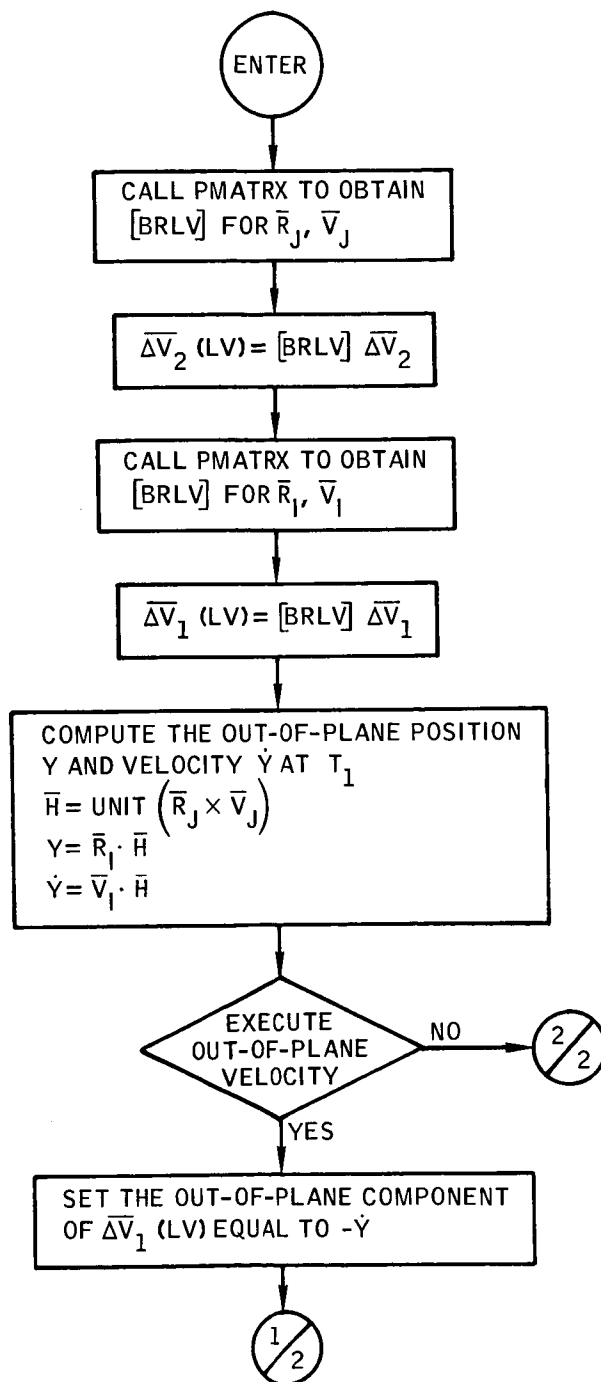


Figure B-104.- Flow chart of subroutine TPITPM.

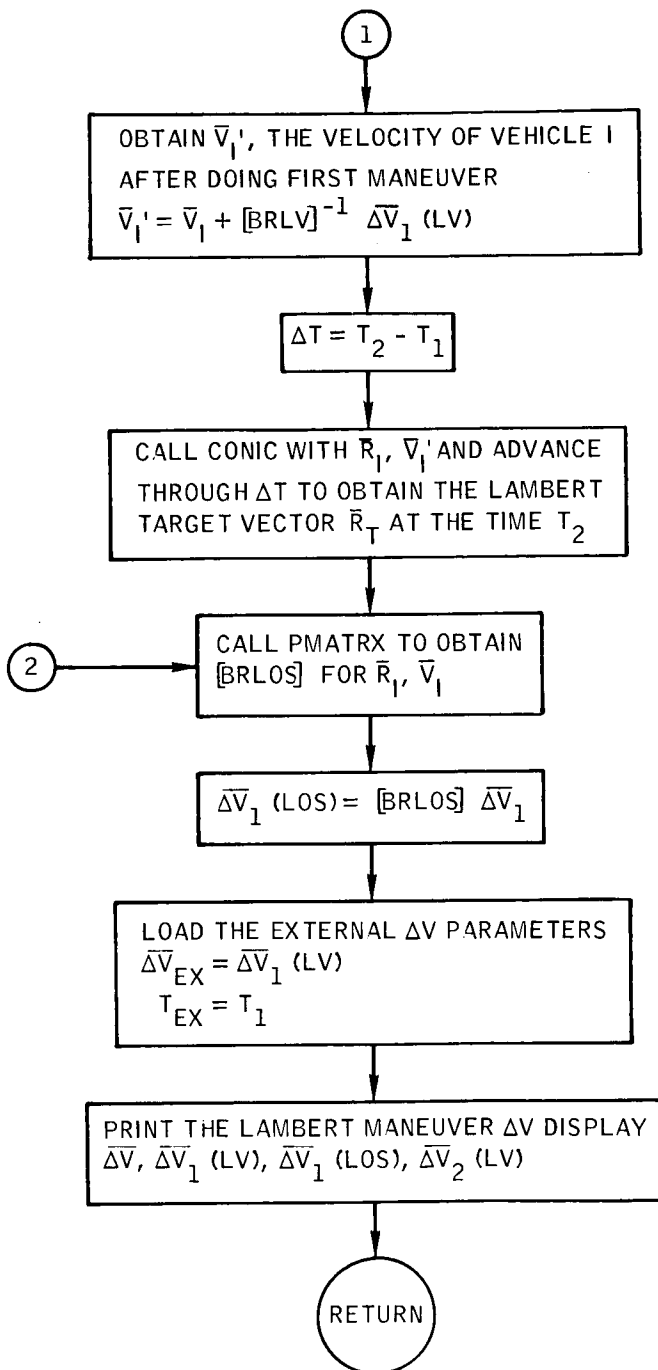


Figure B-104.- Concluded.

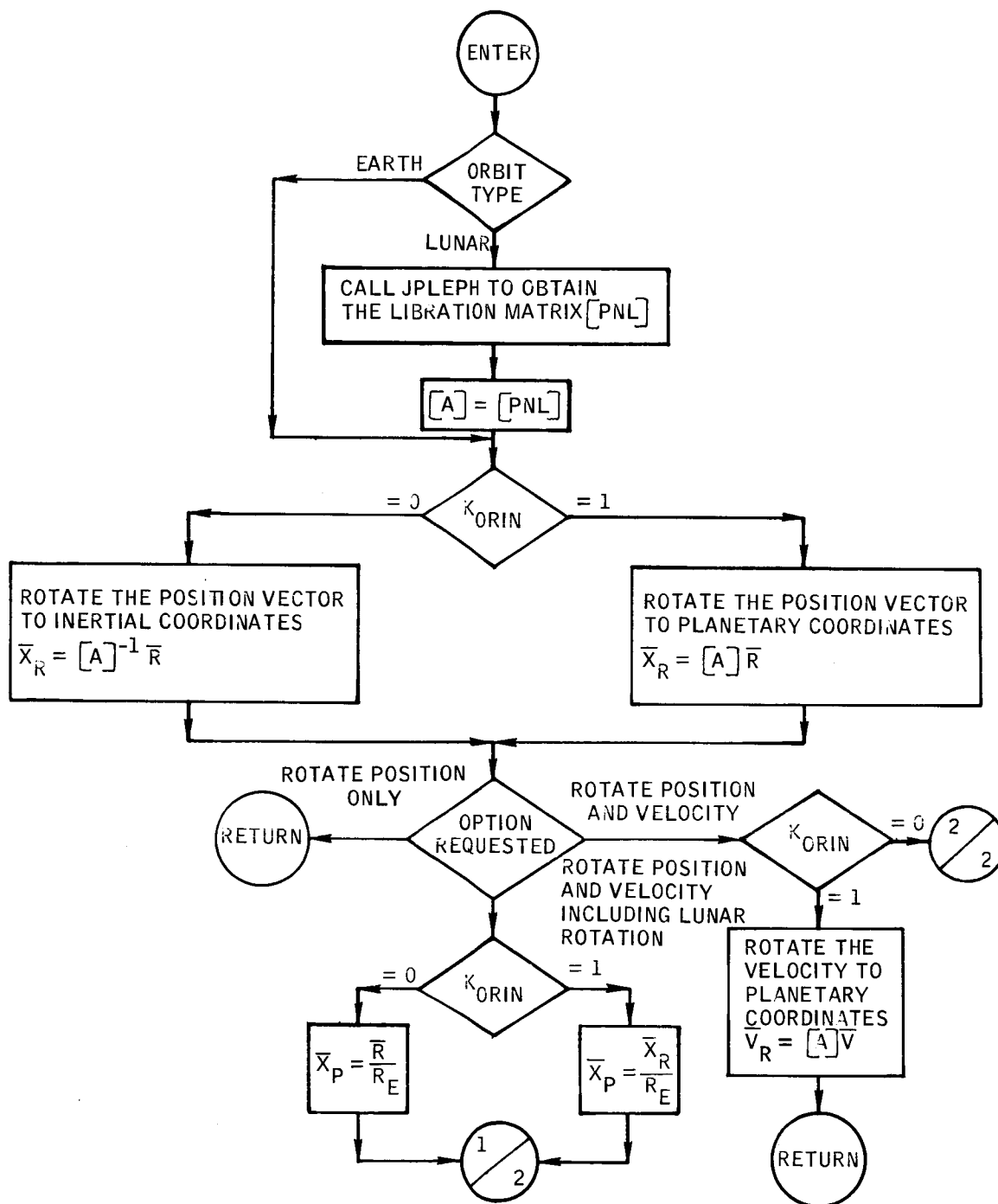


Figure B-105.- Flow chart of subroutine TRANC0.

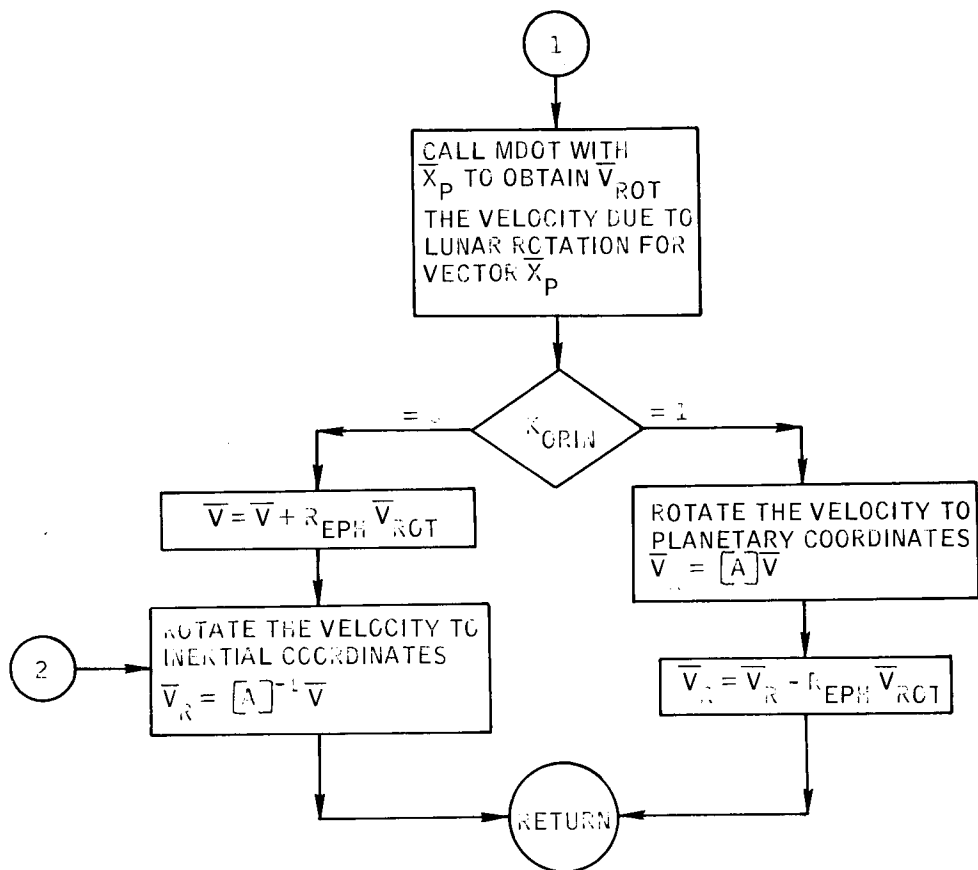


Figure B-105.- Concluded.

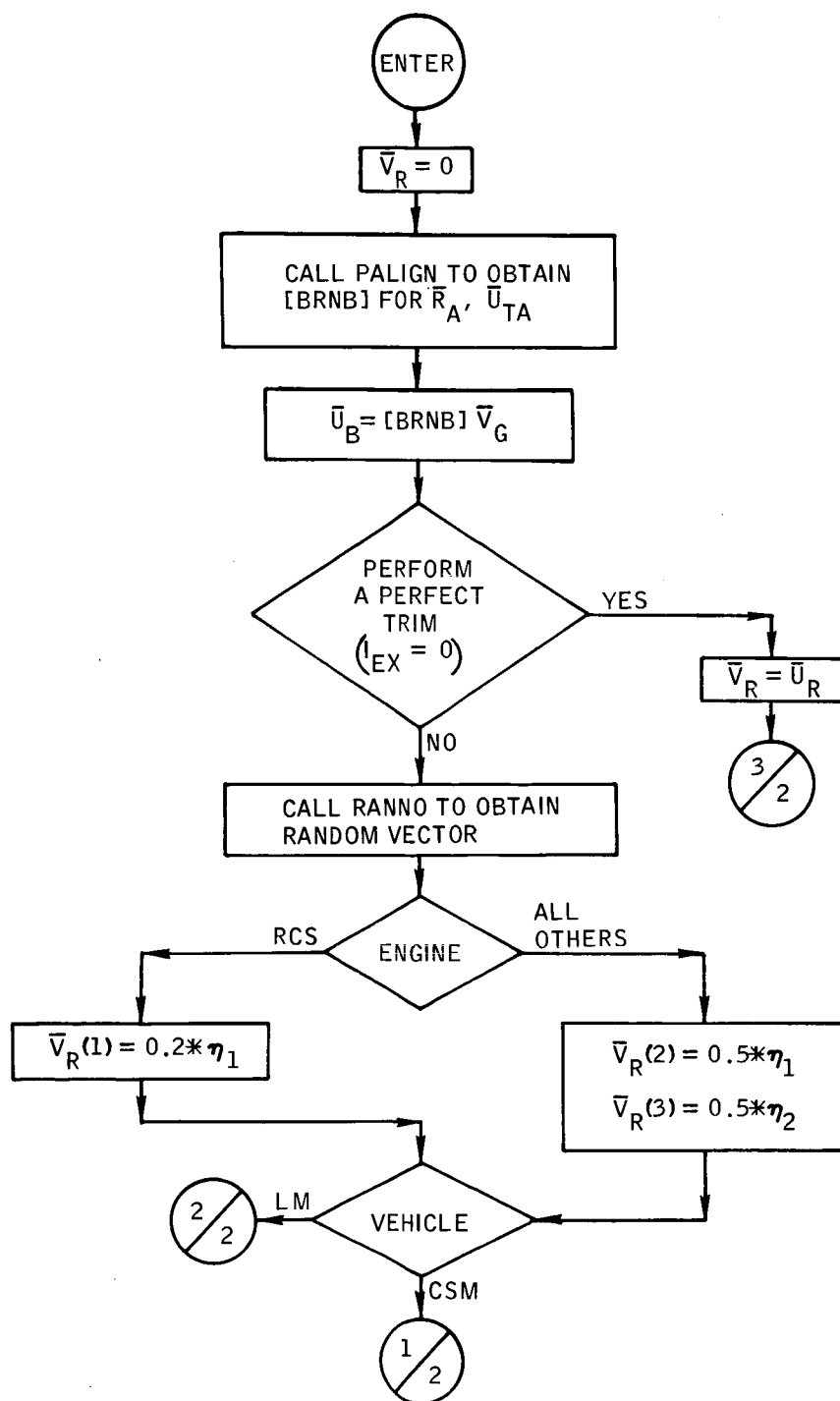


Figure B-106.- Flow chart of subroutine TRIM.



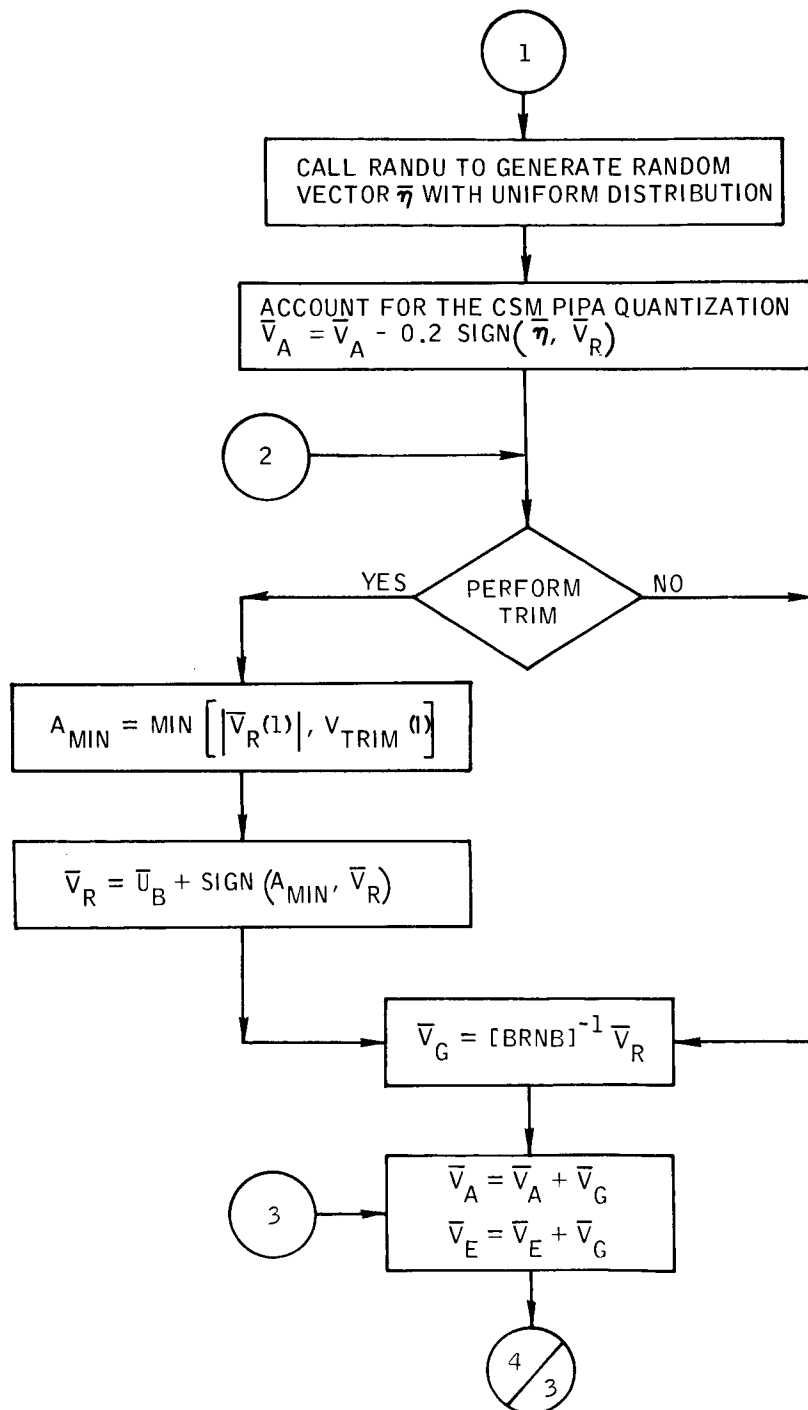


Figure B-106.- Continued.

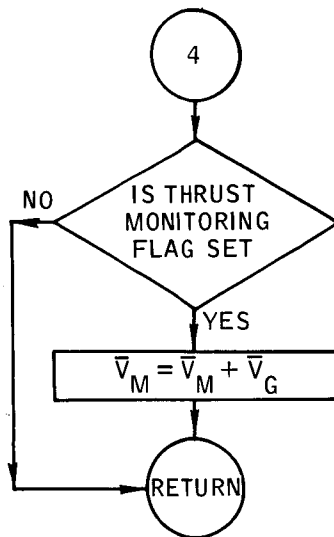


Figure B-106.- Concluded.

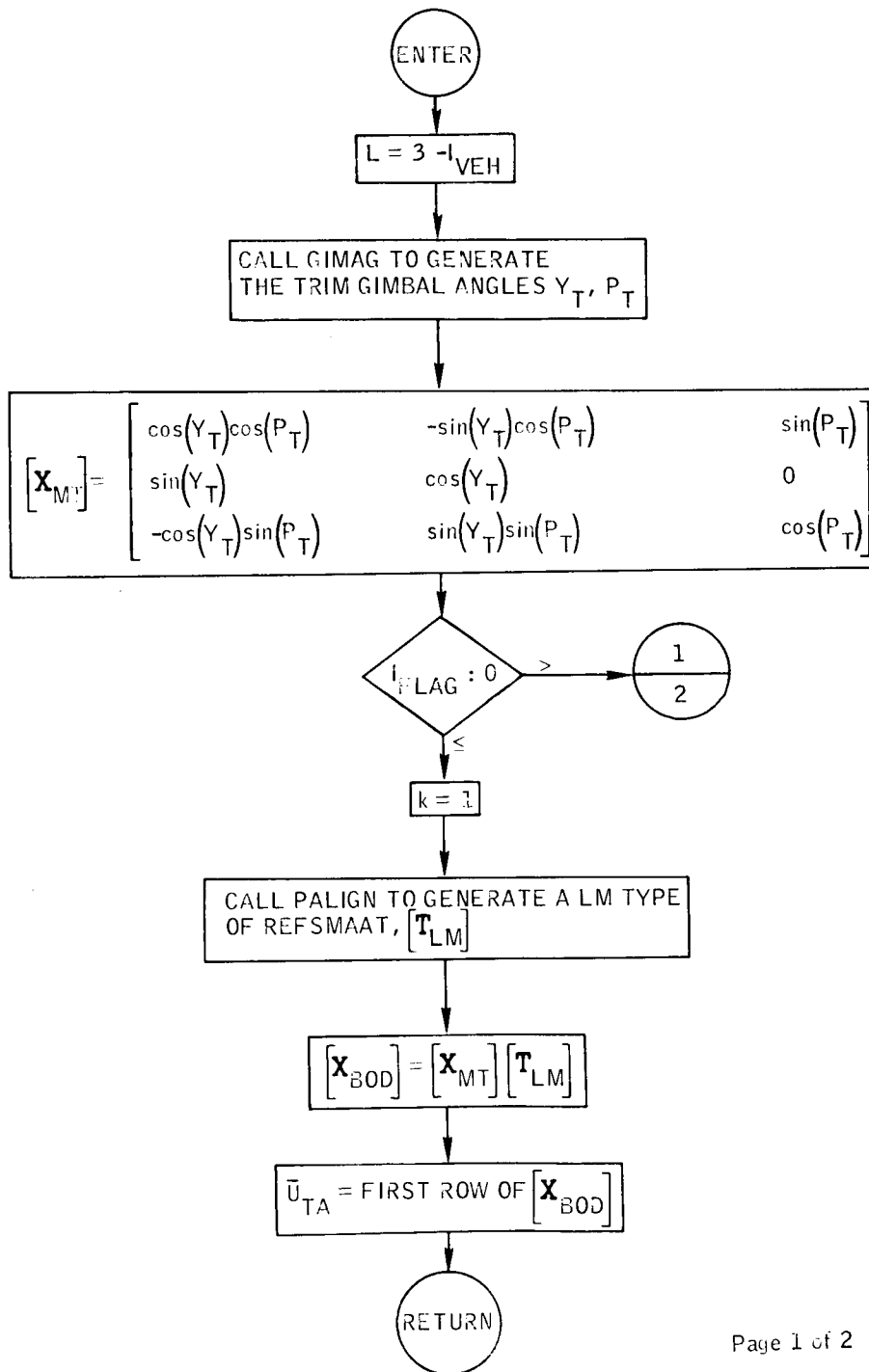


Figure B-107. - Flow chart of subroutine ULLDIR.

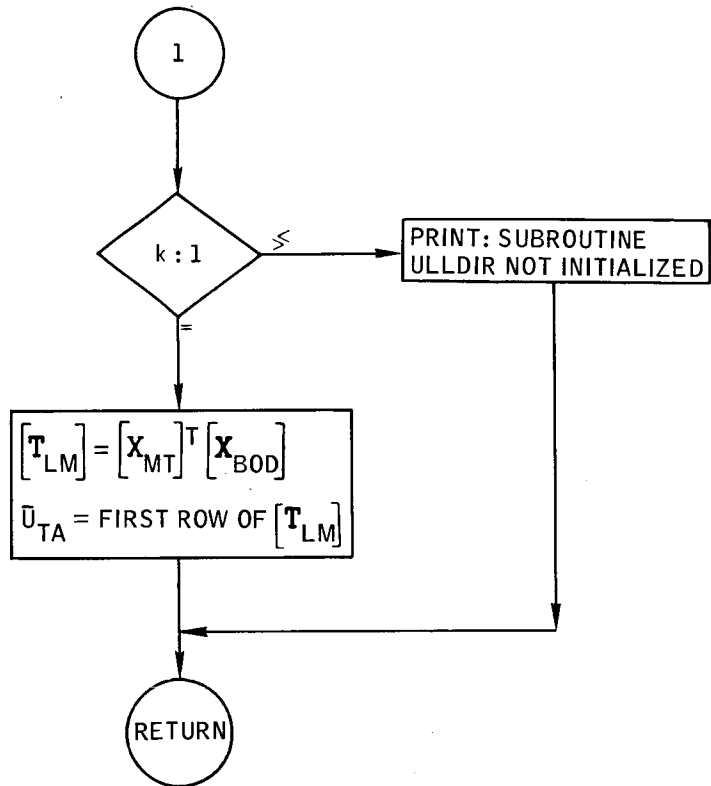


Figure B-107.- Concluded.

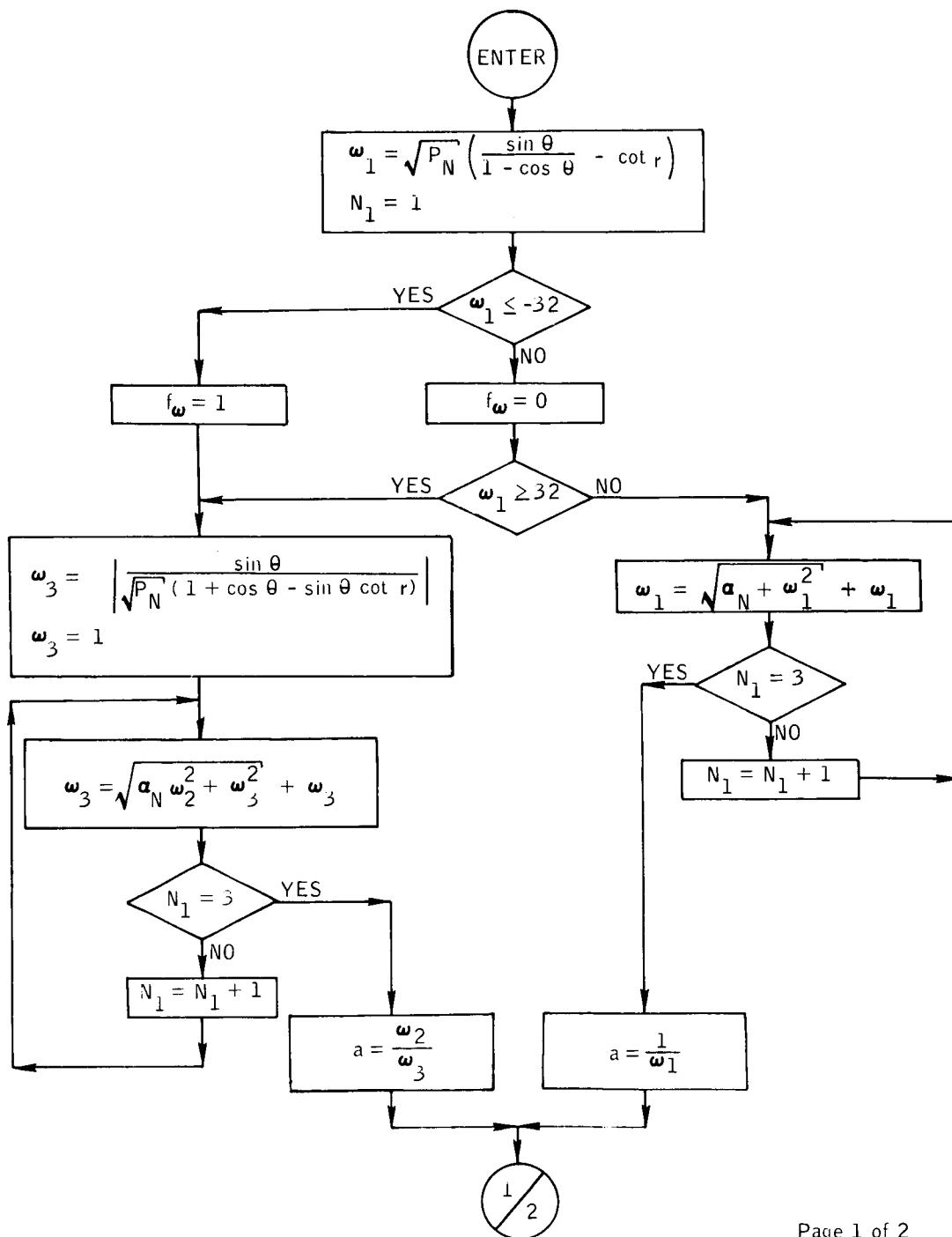


Figure B-108.- Flow chart of subroutine UNIVAR.

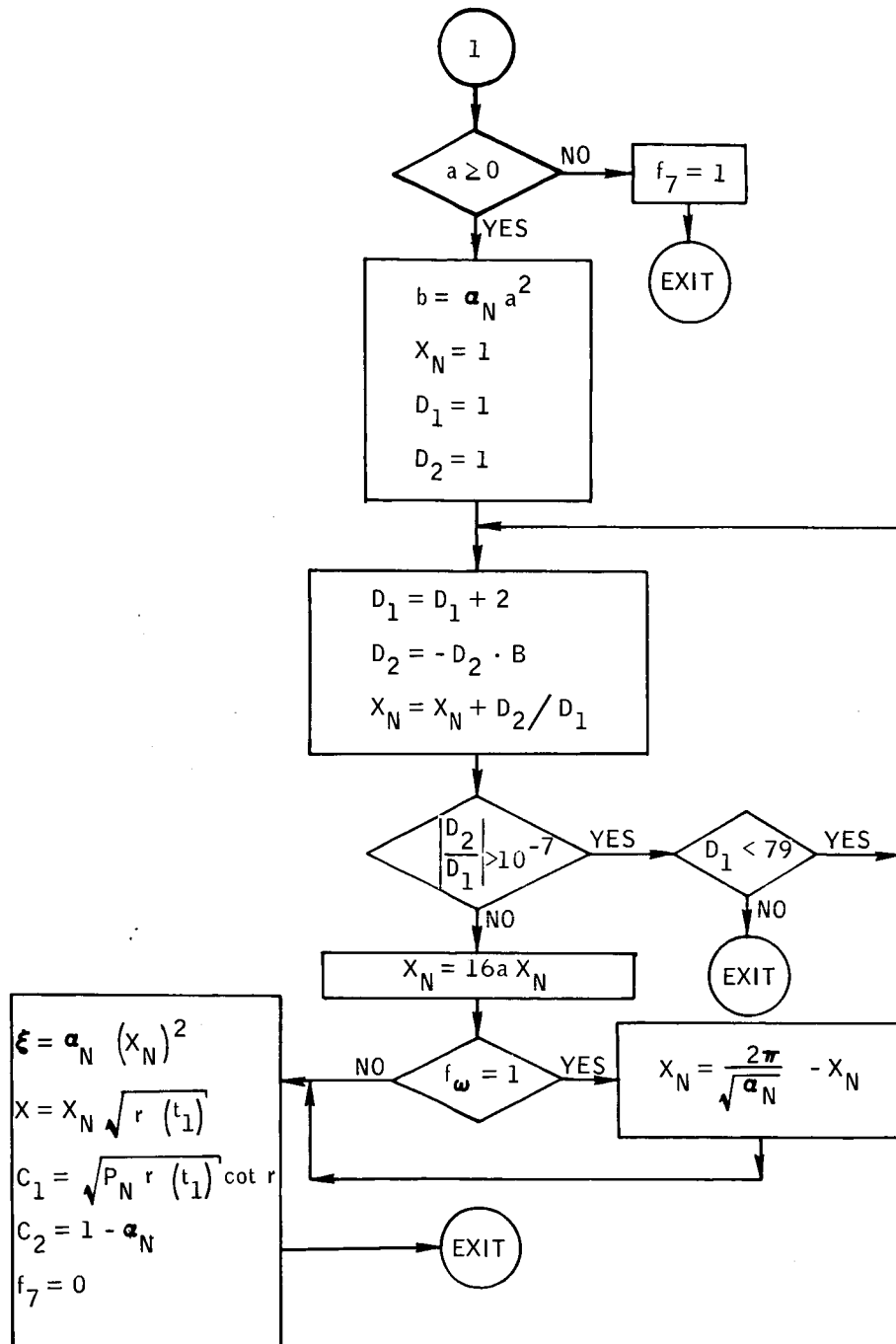


Figure B-108.- Concluded.

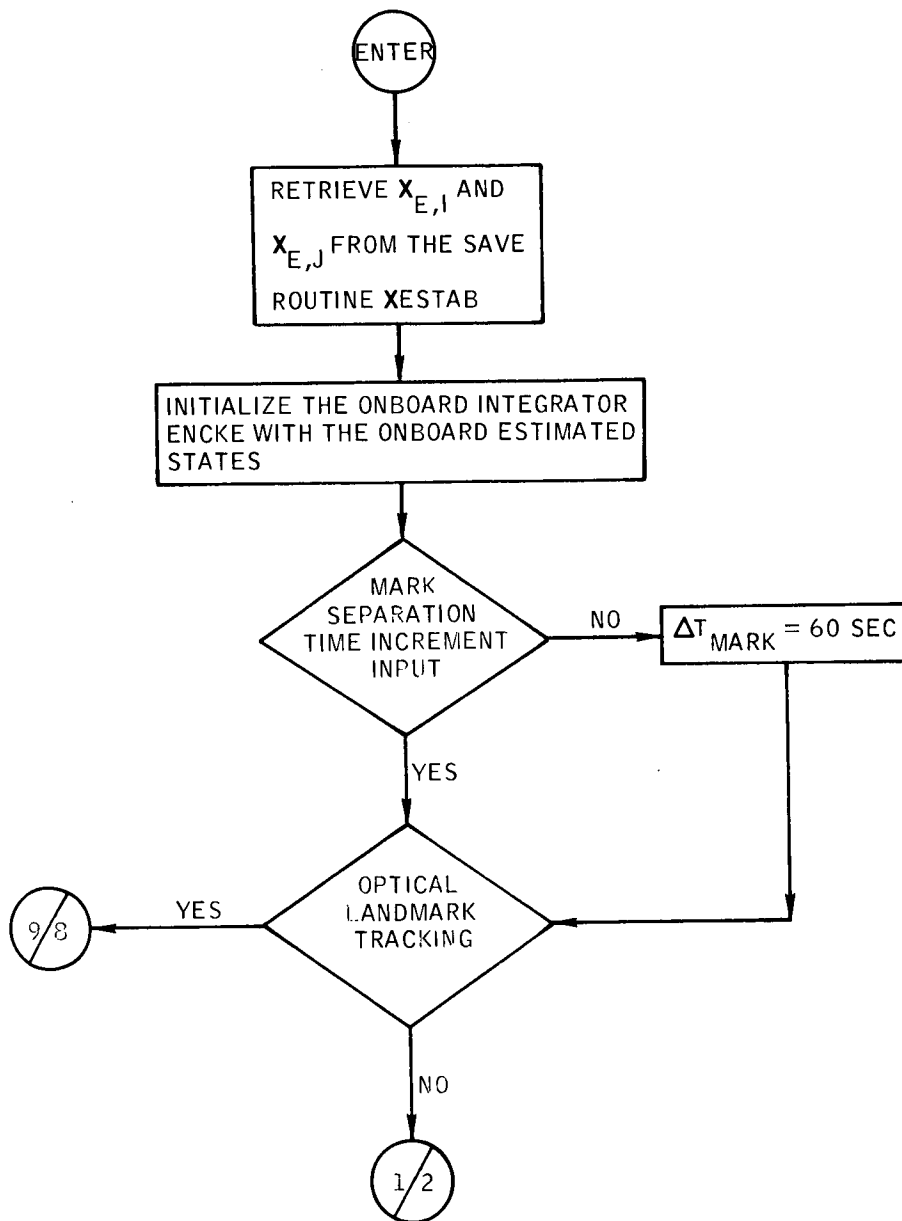


Figure B-109. - Flow chart of subroutine UPDATV.

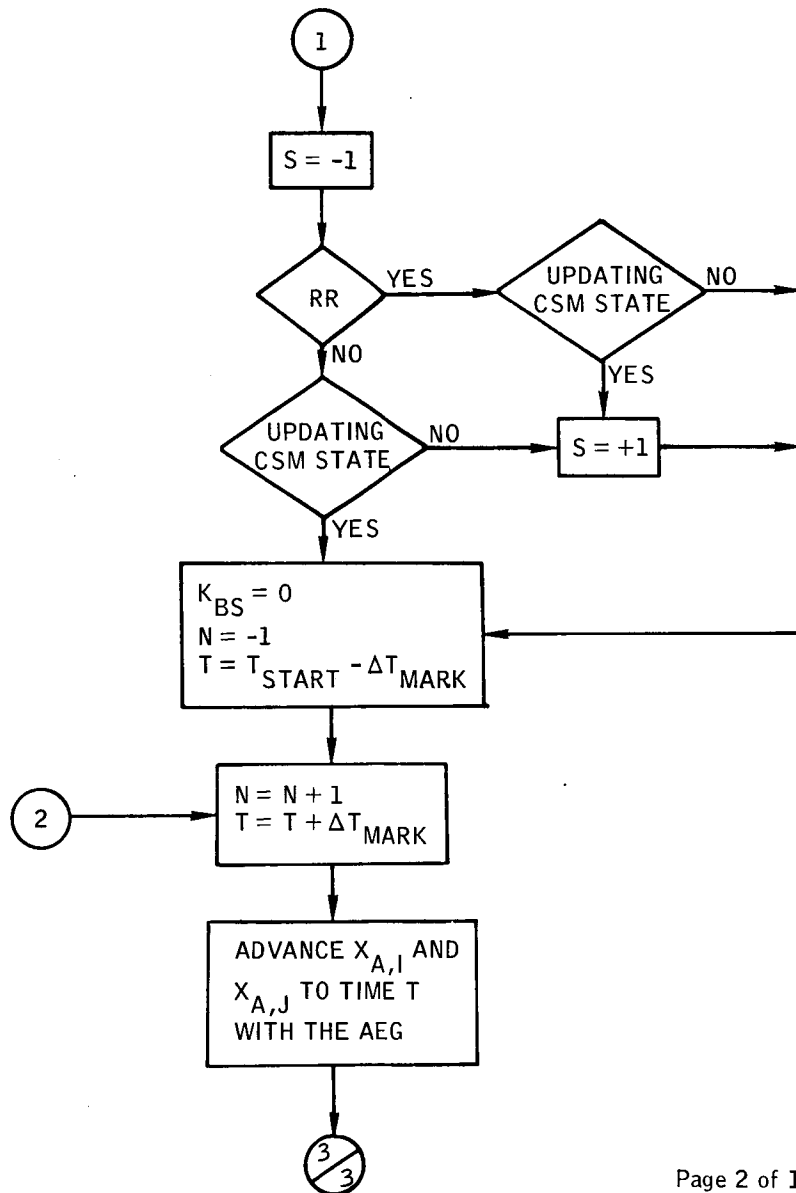


Figure B-109.- Continued.



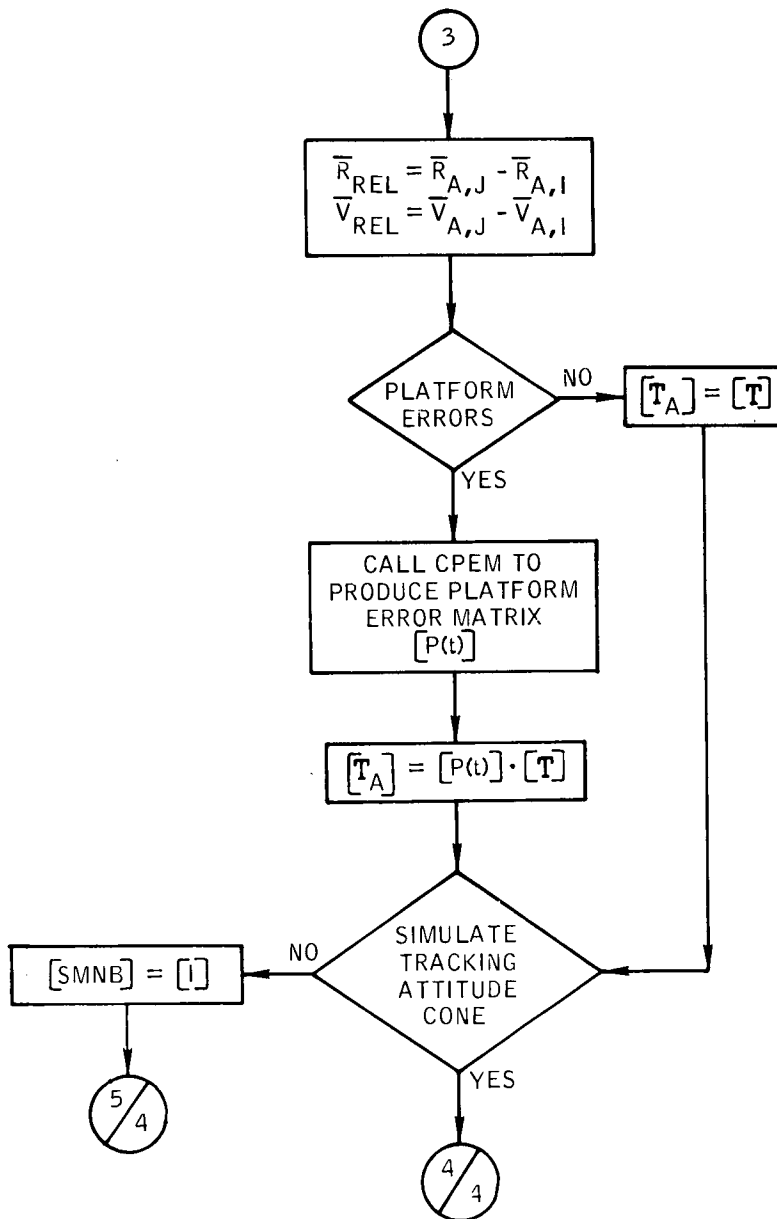


Figure B-109. - Continued.

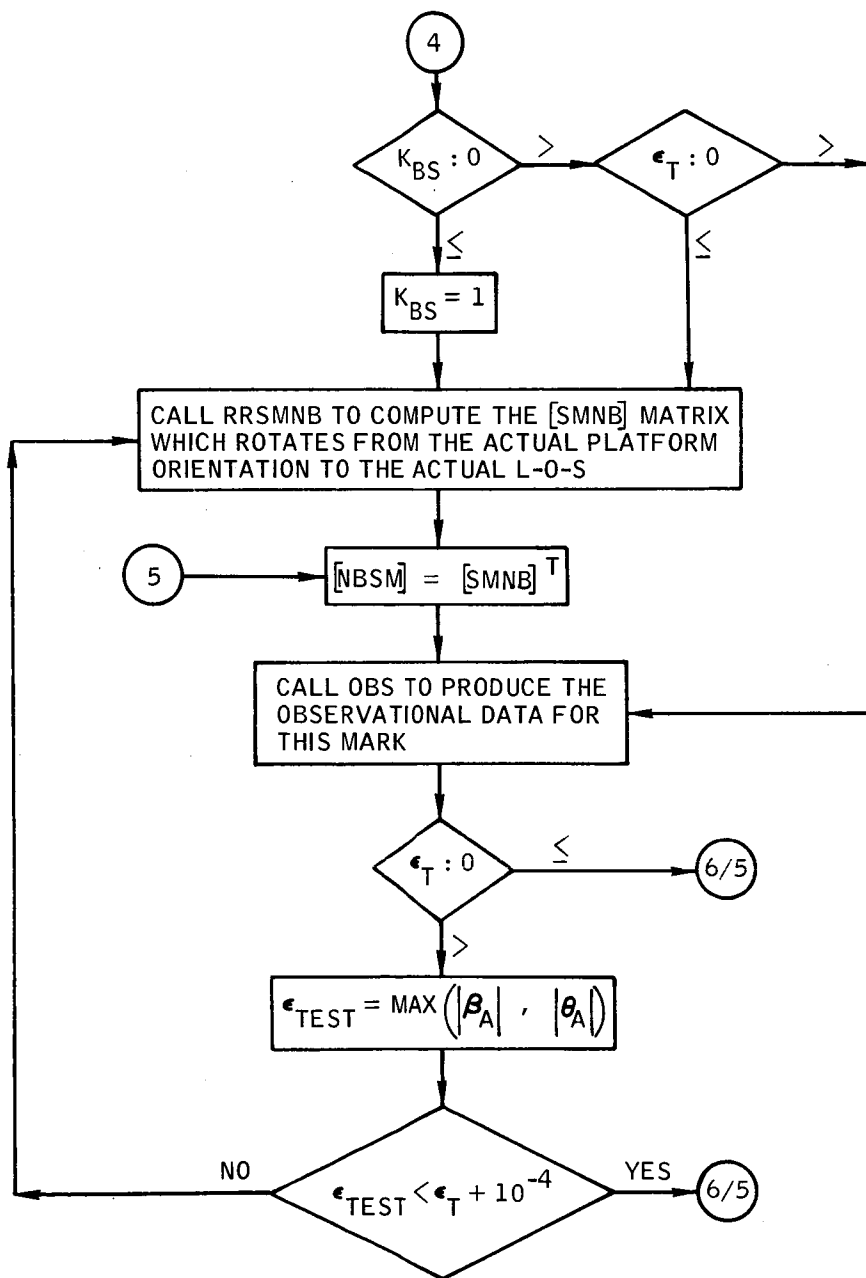


Figure B-109.- Continued.

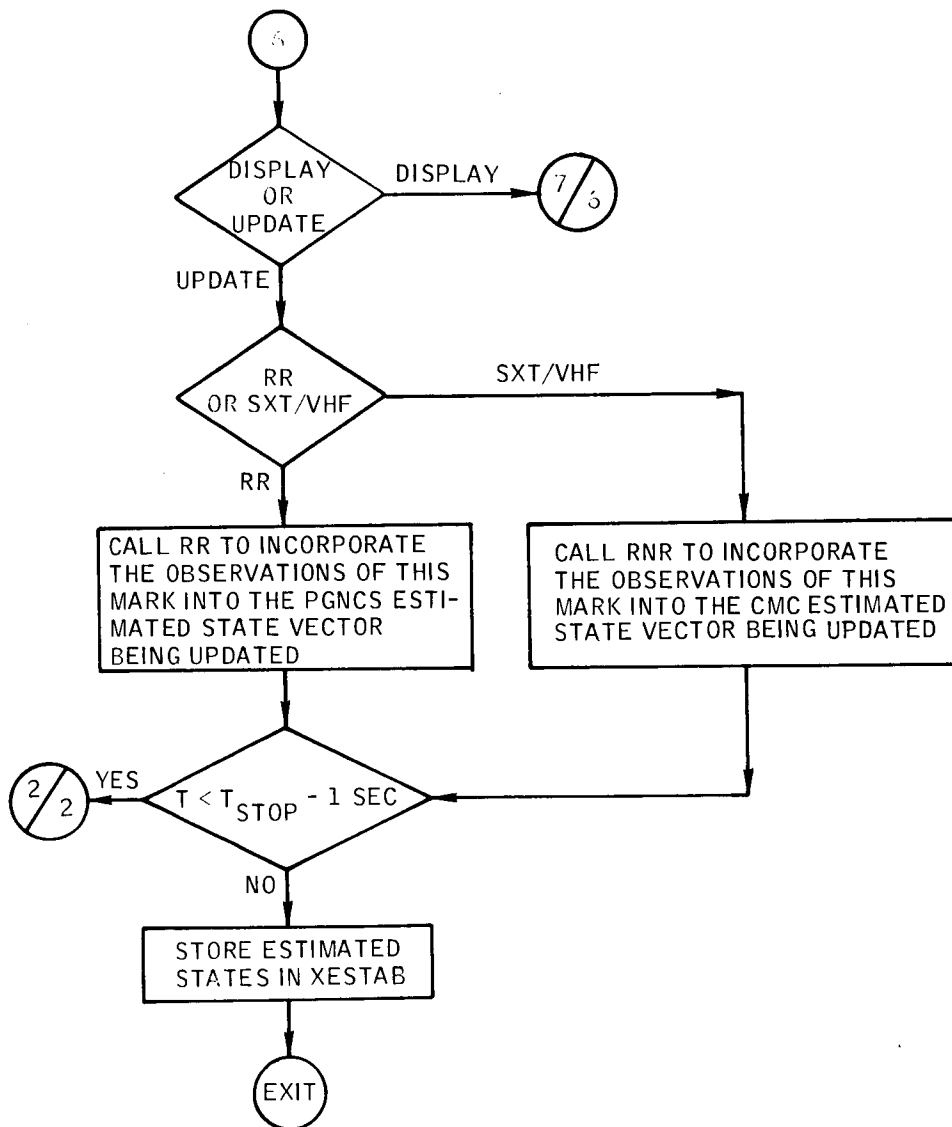


Figure B-109.- Continued.

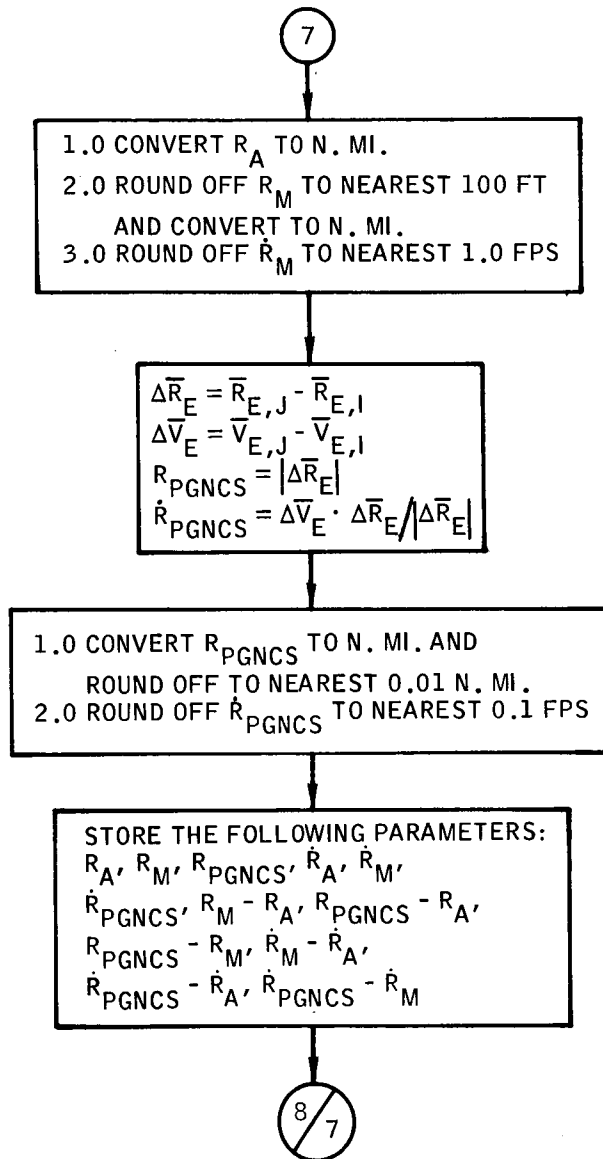


Figure B-109.- Continued.

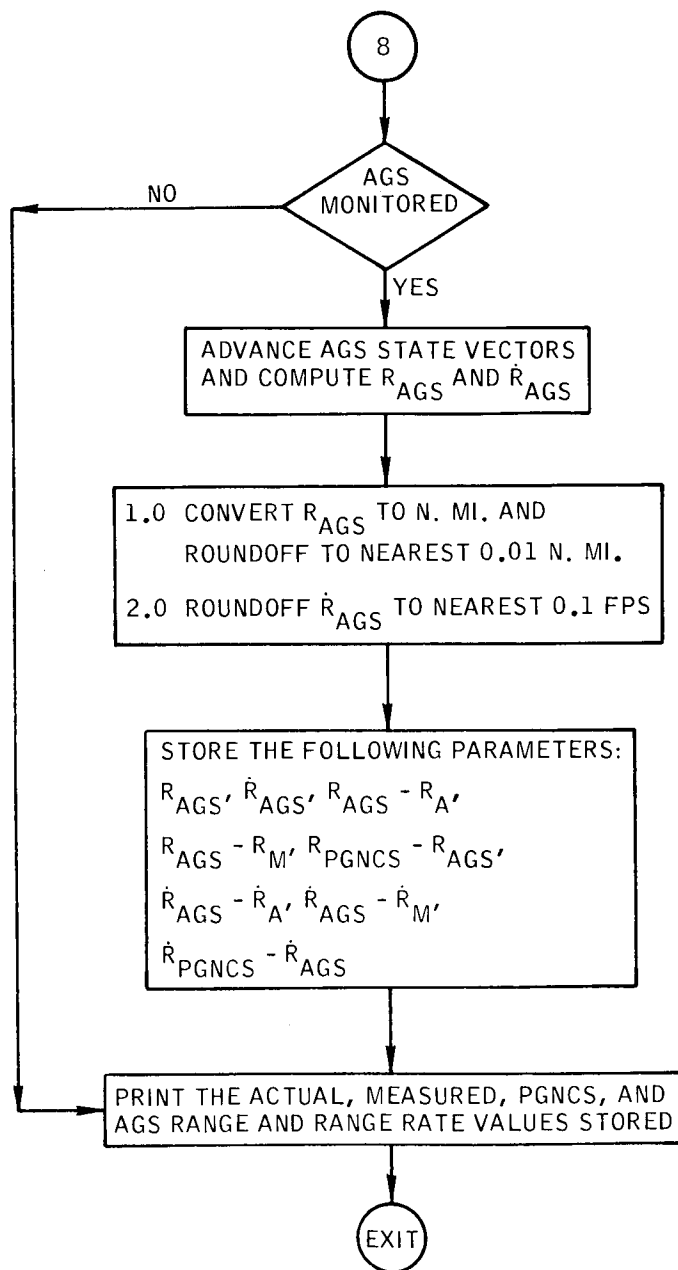


Figure B-109.- Continued.

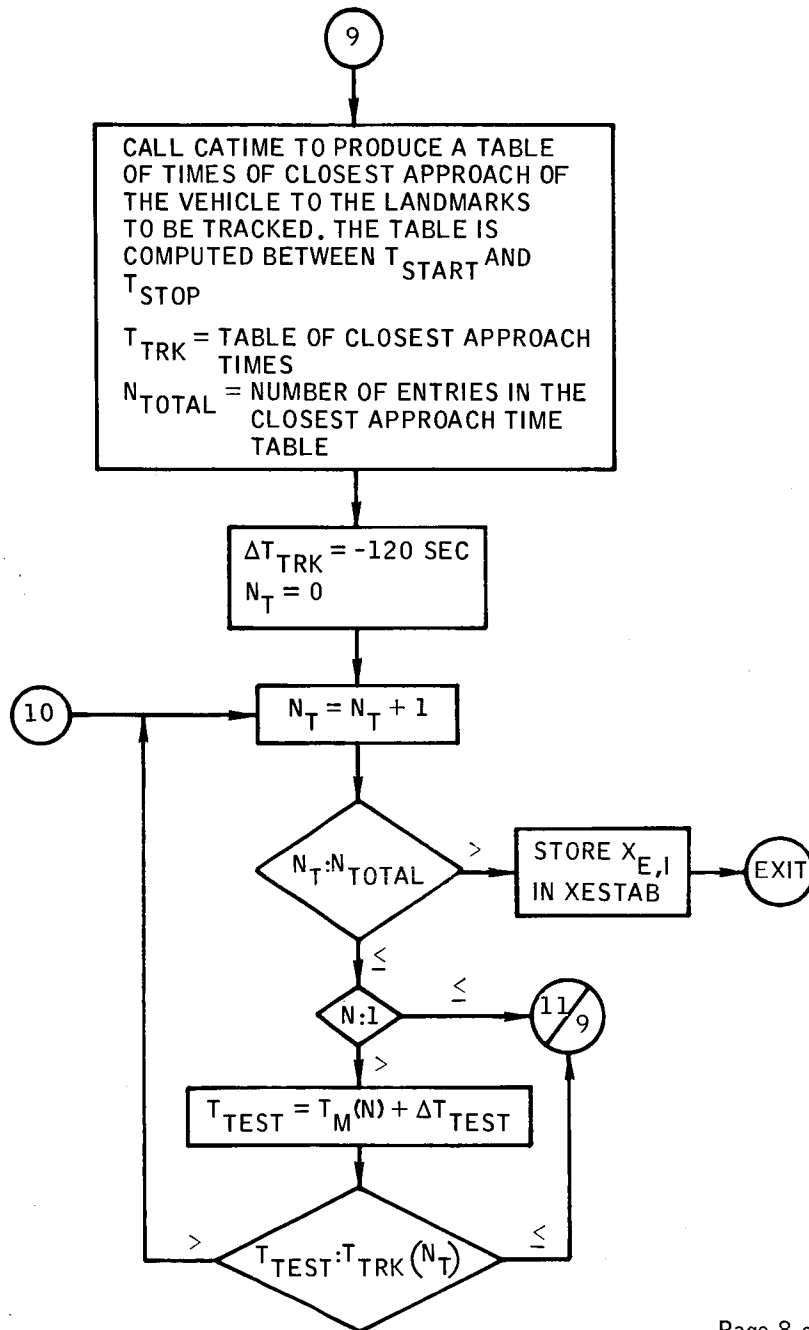


Figure B-109.- Continued.

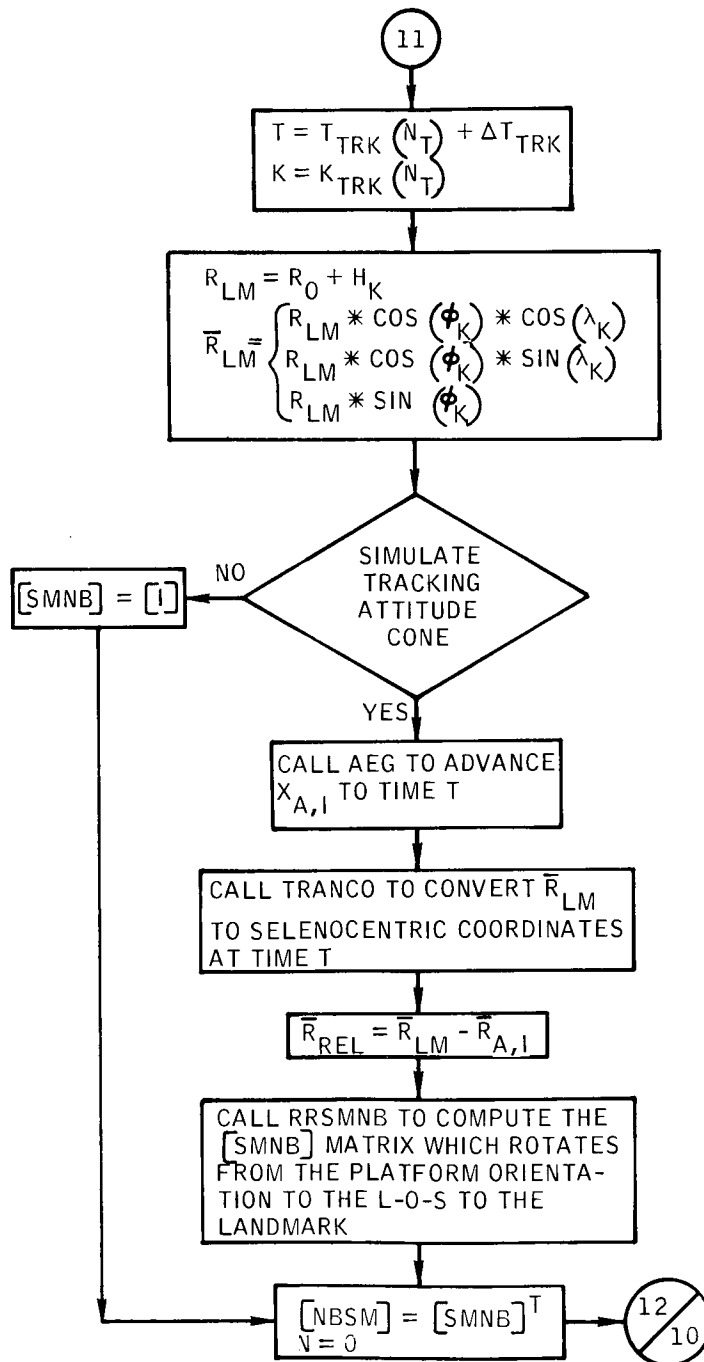


Figure B-109.- Continued.

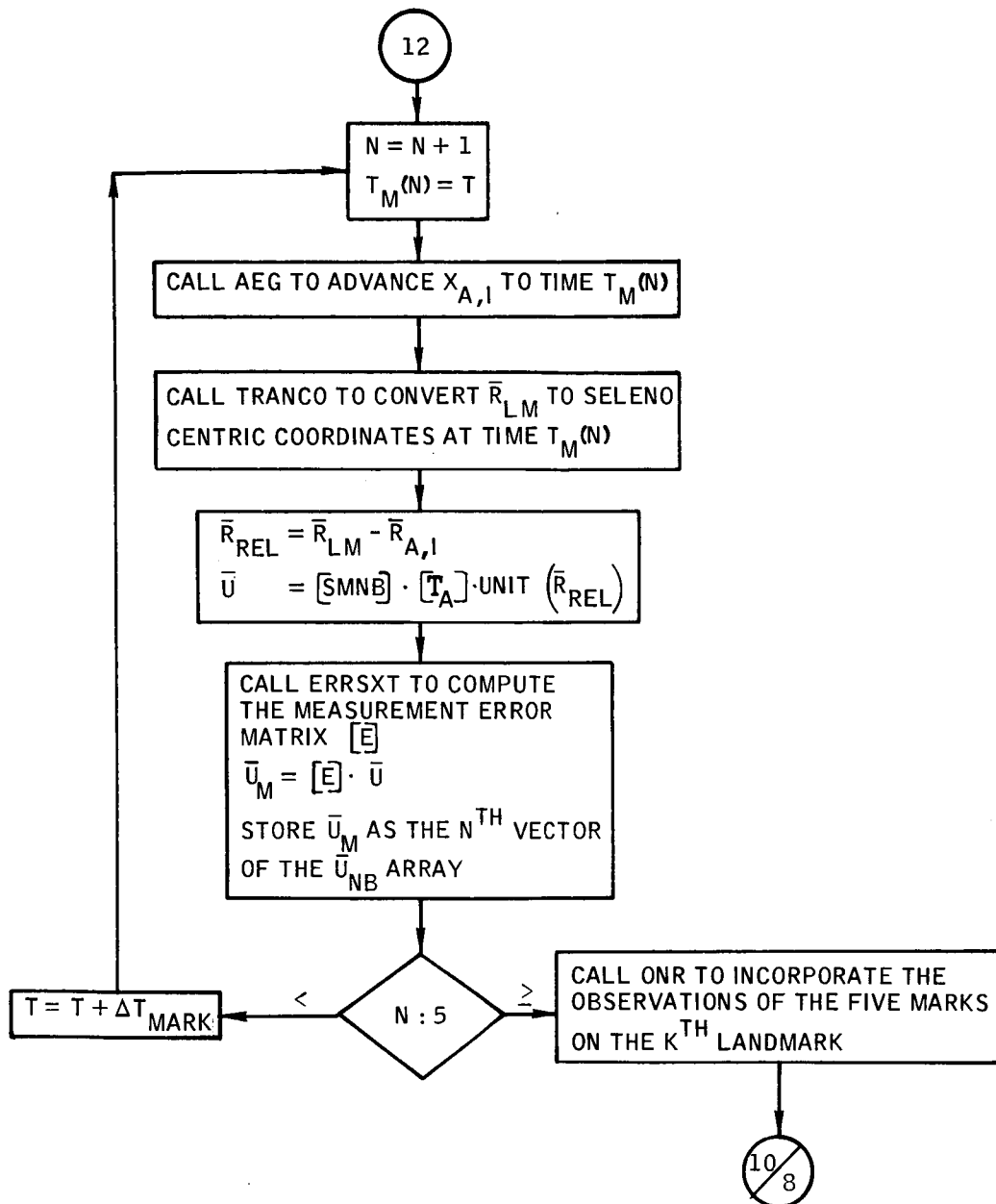


Figure B-109.- Concluded.



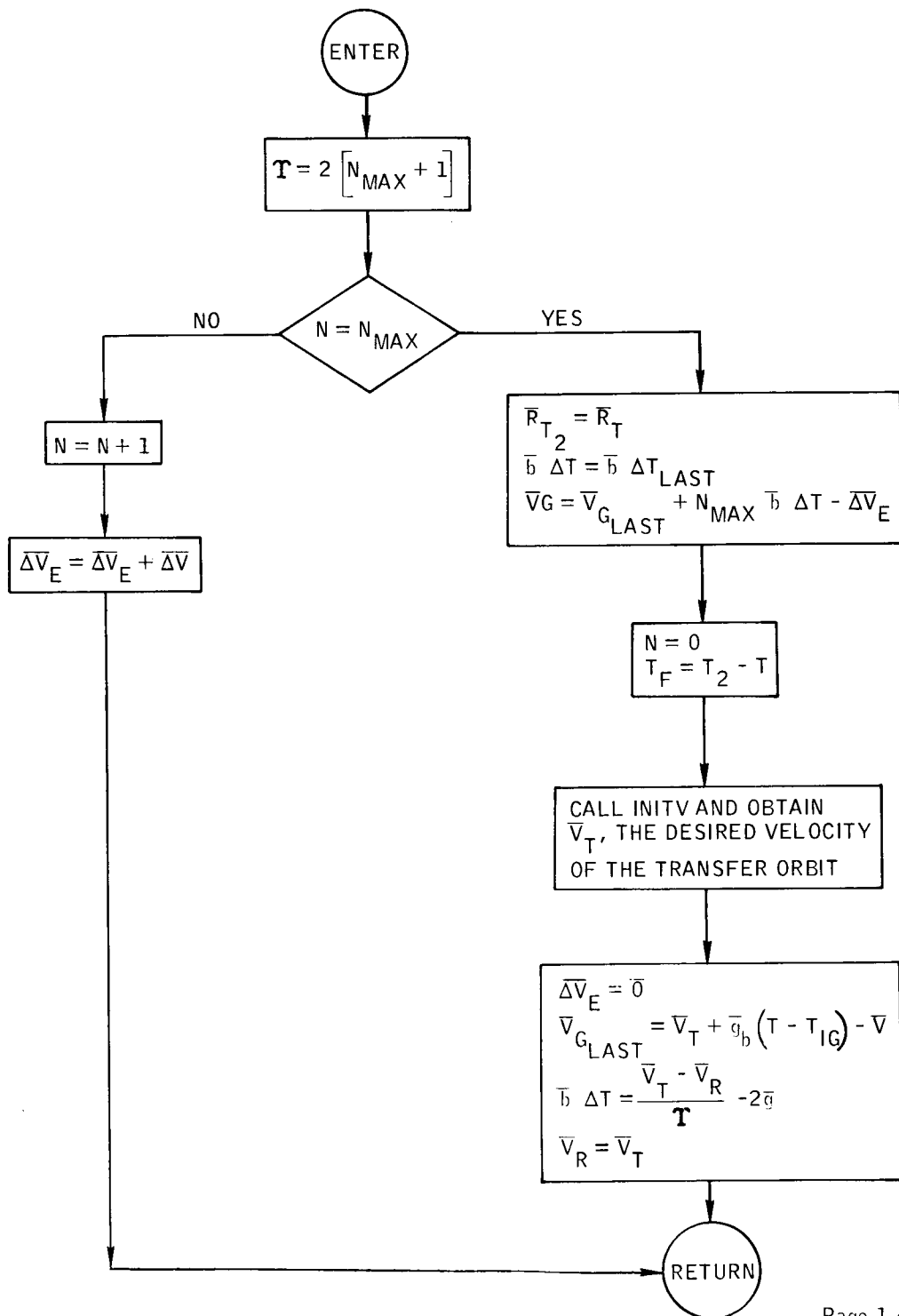


Figure B-110.- Flow chart of subroutine VTBG.

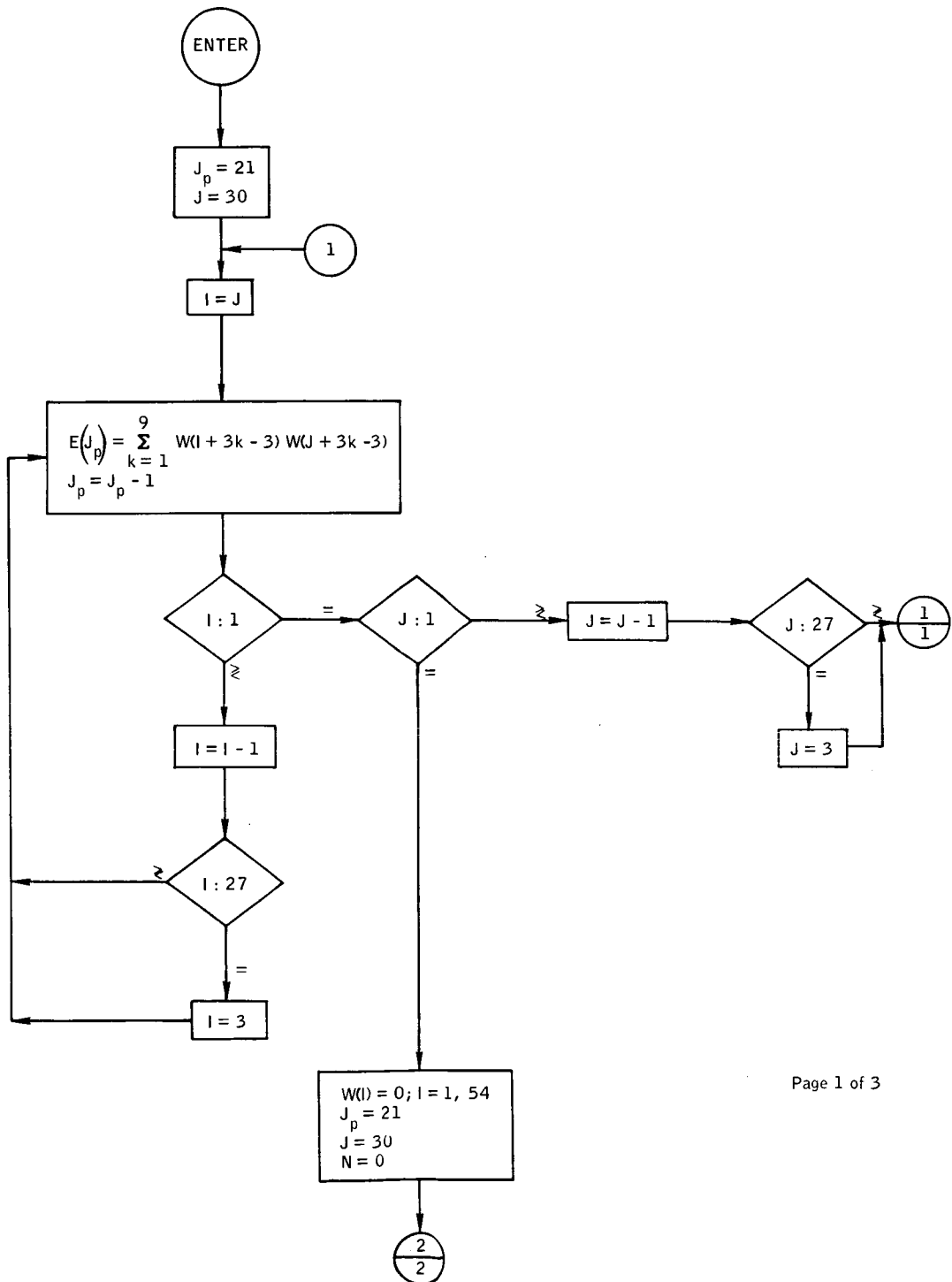


Figure B-111. - Flow chart of subroutine WMATCN.

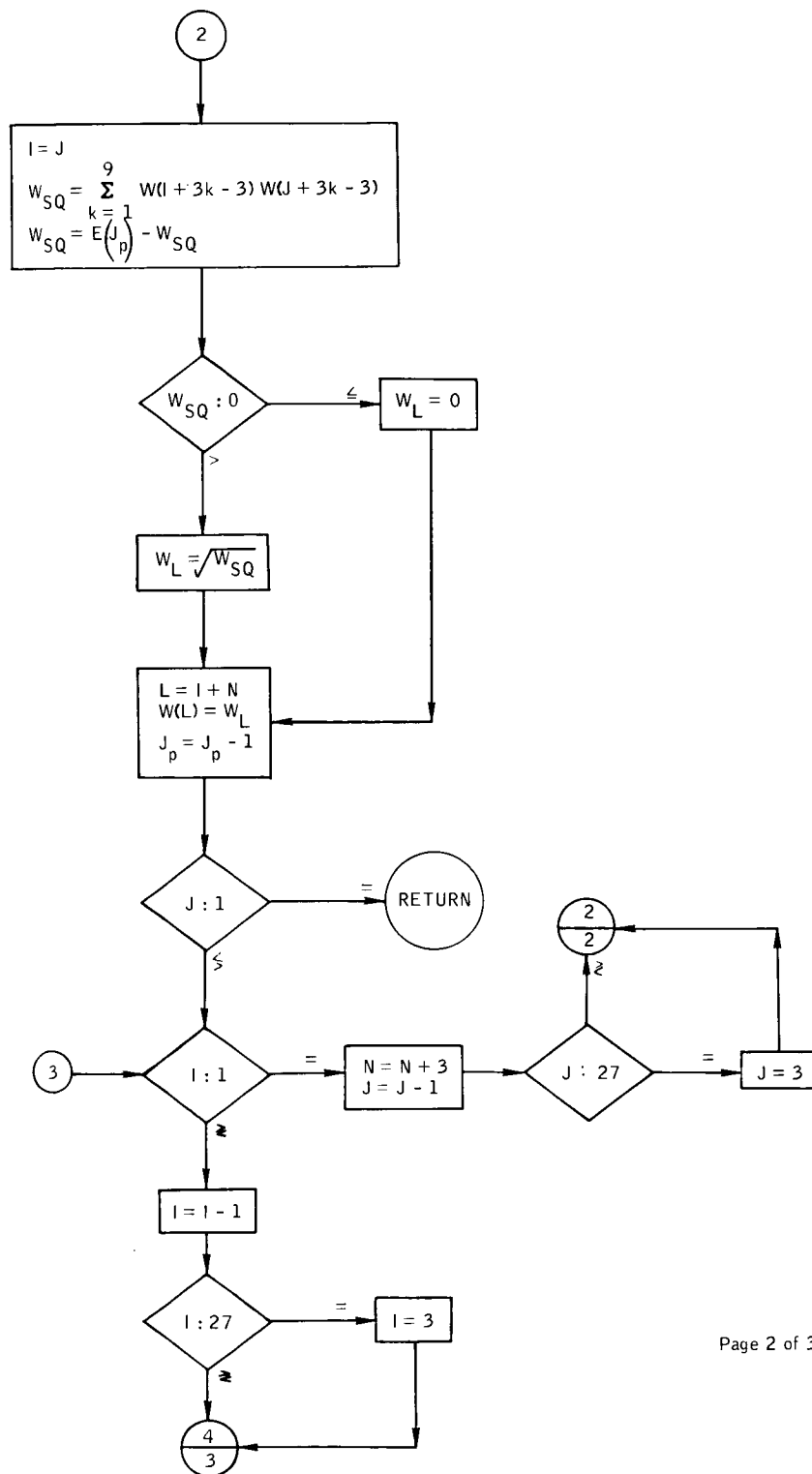


Figure B-111. - Continued.

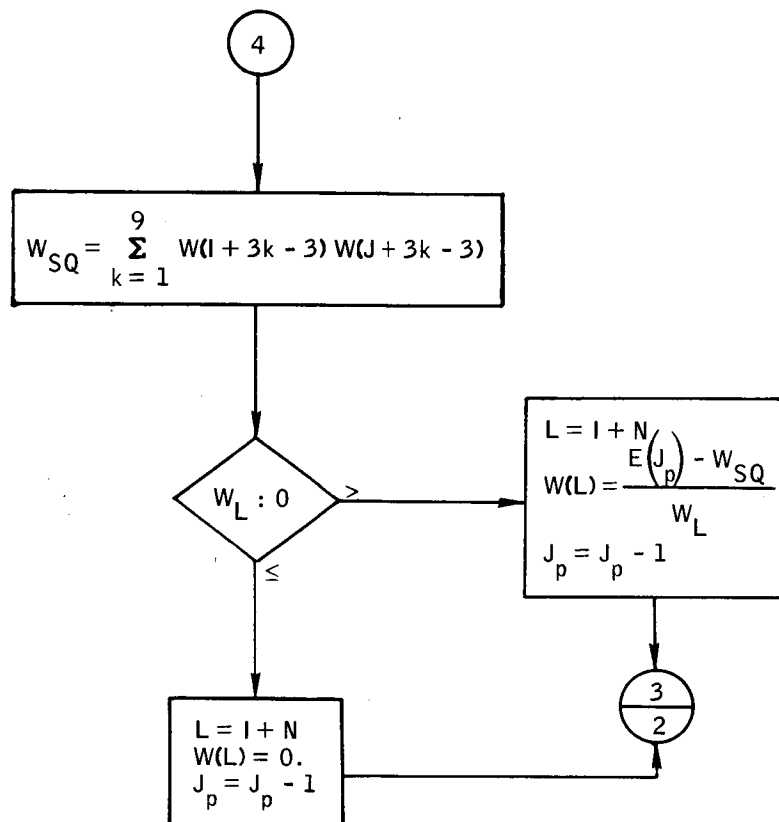


Figure B-111.- Concluded.

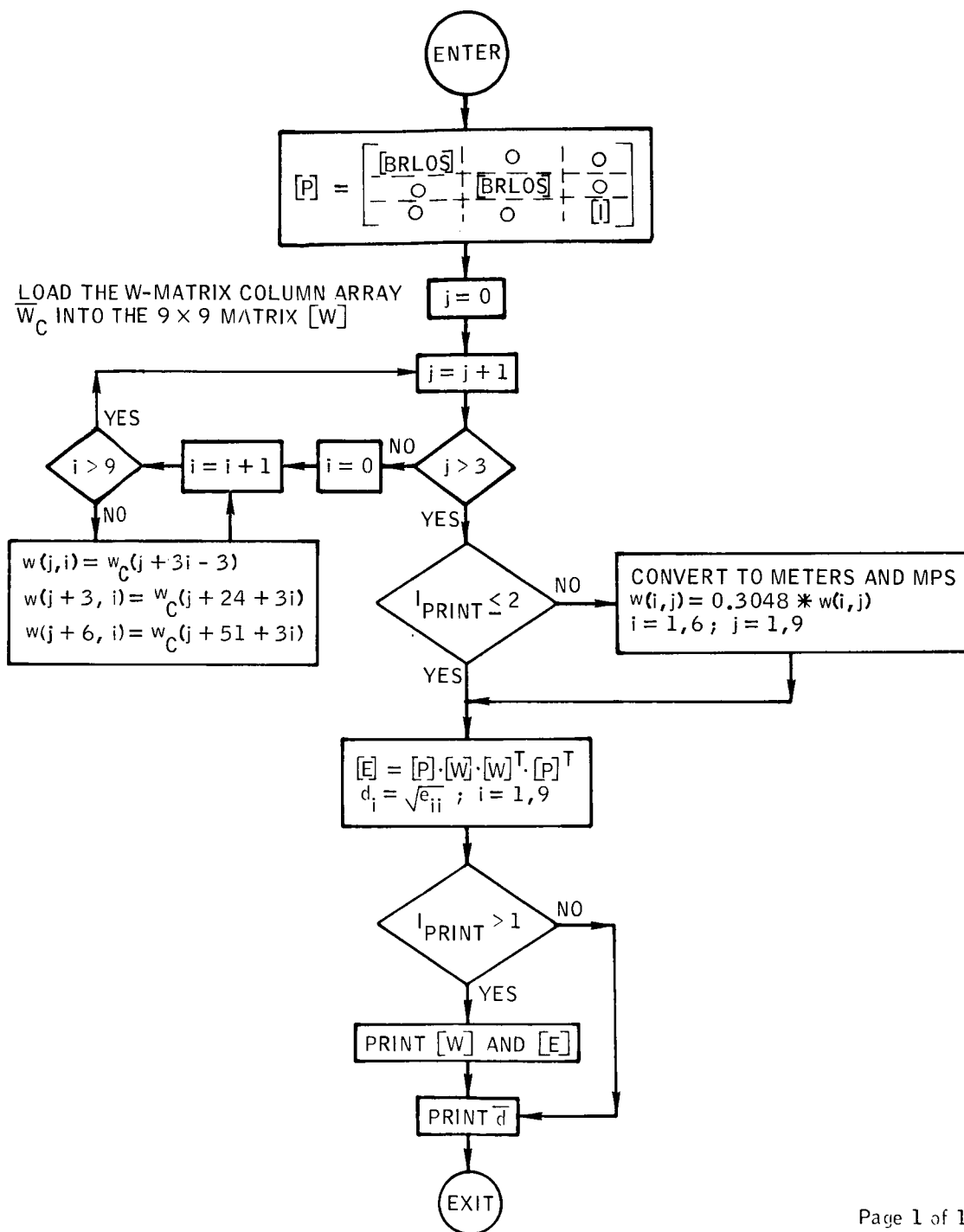


Figure B-112.- Flow chart of subroutine WMT.

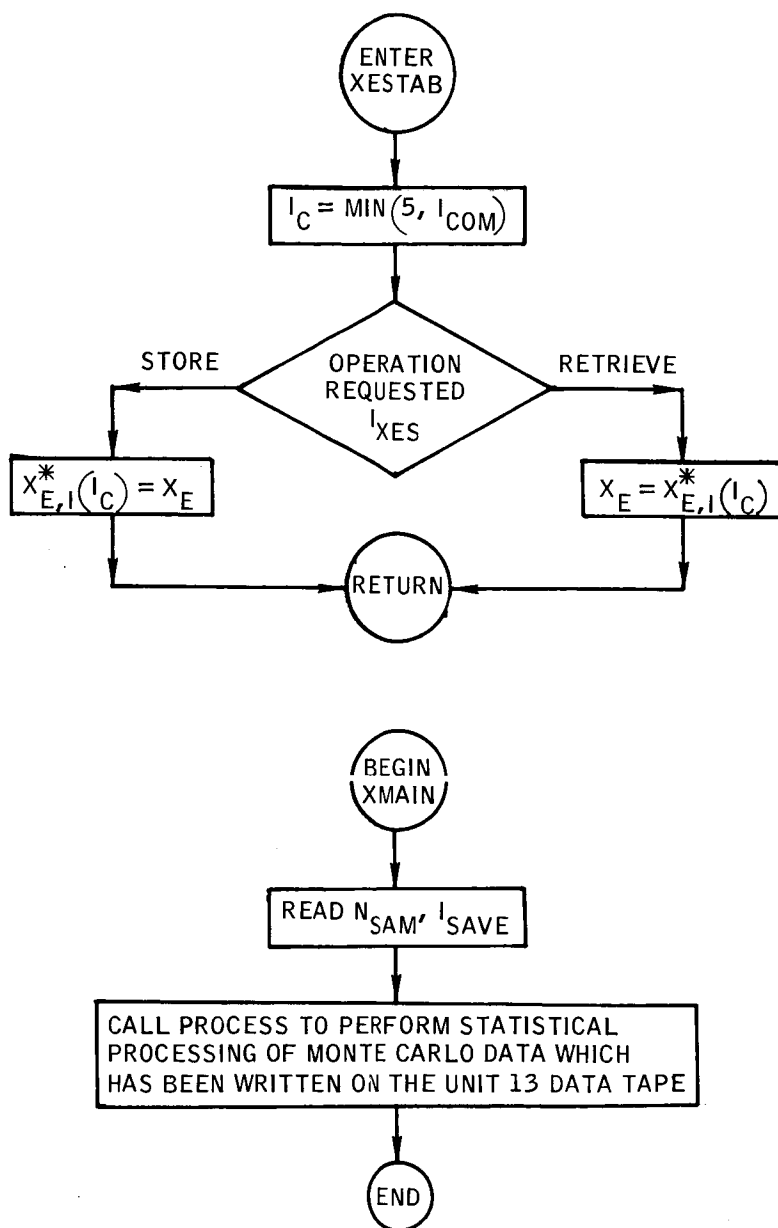


Figure B-113.- Flow charts of subroutine XESTAB and XMAIN.

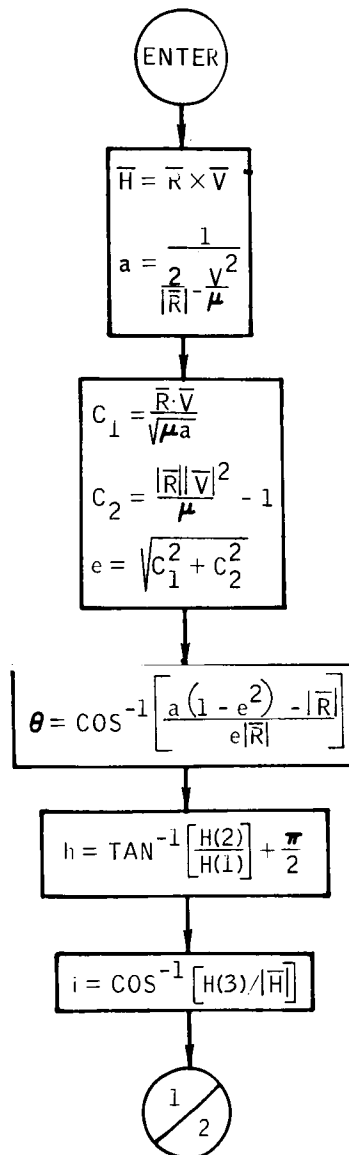


Figure B-114.- Flow chart of subroutine XYZTOE.

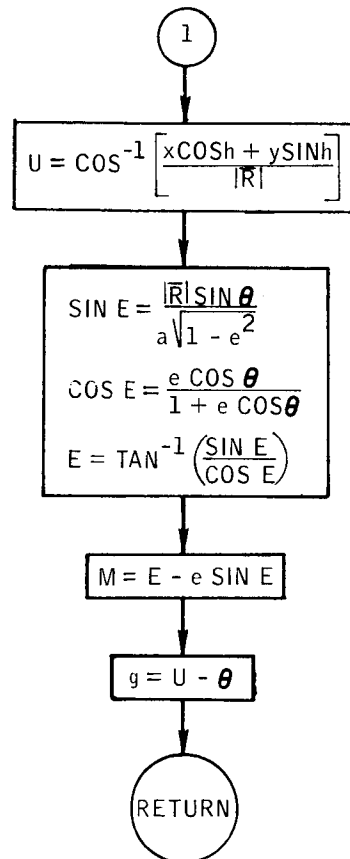


Figure B-114.- Concluded.



APPENDIX C  
DEFINITIONS OF SYMBOLS USED IN  
SUBROUTINES OF AGAST

## APPENDIX C

## DEFINITIONS OF SYMBOLS USED IN SUBROUTINES OF AGAST

APS	ascent propulsion system
$A_{LIM}$	limiting acceleration used for rate limiting in LM descent guidance
$A_{N1}$	initial maneuver line number
$A_{N2}$	final maneuver line number
$A_{TM}$	magnitude of the expected acceleration vector
$A_{TRIM}$	prestored value of the acceleration during the trim phase of LM descent
$A_{ZLIM}$	limiting value on the Z component of the thrust vector
$\bar{A}_C$	commanded thrust vector in LM ascent guidance
$\bar{A}_{CG}$	total commanded acceleration in guidance coordinates; includes thrust and gravity acceleration
$\bar{A}_{CP}$	total commanded acceleration in platform coordinates
$\bar{A}_D$	acceleration vector caused by gravity
$\bar{A}_{DG}$	desired target acceleration vector in LM descent guidance
$\bar{A}_F$	unitized thrust vector, selenocentric coordinates
$\bar{A}_{FP}$	thrust vector desired, platform coordinates
$\bar{A}_T$	desired thrust vector

[A]	<p>a. rotation matrix that relates the AGS strapped down platform to the AGS reference frame</p> <p>b. rotation matrix from basic reference coordinates to planetary coordinates in the state vector propagation routines</p>
[AT]	rotation matrix that relates the AGS strapped down platform to the BR frame
[A <sub>0</sub> ]	same as [AT]
a	<p>a. general symbol for semimajor axis</p> <p>b. rendezvous navigation parameter in DINCP1 and DINCP2</p>
a <sub>I</sub>	semimajor axis of the active vehicle
a <sub>J</sub>	semimajor axis of the passive vehicle
a <sub>M</sub>	magnitude of thrust acceleration in LM ascent guidance
a <sub>N</sub>	mean motion
$\bar{a}_{PERT}$	acceleration caused by gravitational perturbations of the potential
$\bar{a}_T$	thrust vector in LM ascent guidance
BR	abbreviation for basic reference
BTM	measured RR shaft angle
B <sub>DAY</sub>	base day
B <sub>MONTH</sub>	base month
B <sub>YEAR</sub>	base year
$\bar{B}_1, \bar{B}_2, \bar{B}_3$	geometry vectors used in the navigational update scheme of subroutine ONR

$[B]$	accelerometer misalignment rotation matrix
$[BRLOS]$	rotation matrix that relates the basic reference frame to a line-of-sight frame
$[BRLOS]_A$	actual $[BRLOS]$
$[BRLV]$	rotation matrix that relates the basic reference frame to a local vertical frame
$[BRLV]_A$	actual $[BRLV]$
$[BRLV]_E$	estimated $[BRLV]$ based on estimated onboard states
$[BRNB]$	rotation matrix that relates the basic reference frame to the navigation base frame
$[B_A]$	$[B]$ -matrix for AGS
$[B_C]$	$[B]$ -matrix for CMC
$[B_P]$	$[B]$ -matrix for LM PGNCs.
$b$	argument of latitude of closest approach to a landmark (in subroutine TPASS)
$\bar{b}\Delta t$	incremental change of the velocity-to-be-gained vector for the time interval $\Delta t$
$\bar{b}_1, \bar{b}_2, \bar{b}_3$	geometry vectors used in the navigational update routines
$[b]$	range or range rate RR filter weights
$C$	steering constant
CANT	cant angle
CART	Cartesian state vector
CARTL	Cartesian state vector (in subroutine AGSKEP)
$C_E$	product of eccentricity and cosine of the eccentric anomaly

$C_{\Delta E}$	cosine of the difference between the present and final eccentric anomalies
$[C]$	decomposition matrix for a covariance matrix $\Sigma$
$[C_{GP}]$	rotation matrix that relates the guidance frame to the platform coordinate system
$c_i$	product of eccentricity and cosine of the eccentric anomaly (in subroutine OPS)
$c_{ij}$	representative element of the decomposition matrix $[C]$
$c_k$	input to subroutine SENSOR which designates the method used to simulate the current guidance cycle
DAYS	number of days from the beginning of the year to the base date
DPS	descent propulsion system
$DT_{MARK}$	time between marks in the AGS RR update simulation
$D_{CA}$	distance of closest approach between the CSM and LM
$\bar{D}$	vector perpendicular to the plane in which the radius, velocity, and acceleration vectors should lie at the end of the current descent phase
$\bar{D}_{IG}$	integrated gravity acceleration vector per 2-second computer cycle
E	a. eccentric anomaly (subroutine TA) b. desired elevation angle (subroutine PRETPI)
ELE	classical orbital elements
$E_A$	actual elevation angle
$E_L$	desired elevation angle
$E_{NO}$	number of RCS quads to be used

[E]	SXT unit vector error matrix
e	orbital eccentricity
F	thrust magnitude
F <sub>A</sub>	actual thrust magnitude
F <sub>C</sub>	commanded thrust magnitude
F <sub>CMIN</sub>	minimum DPS thrust level
F <sub>D</sub>	thrust level commanded by the descent guidance
F <sub>ENG</sub>	thrust level passed to subroutine START
F <sub>LIM</sub>	thrust level value used to limit the down-range componant of the thrust acceleration vector
F <sub>MAX</sub>	initial DPS full thrust magnitude
F <sub>NOM</sub>	nominal thrust profile
F <sub>P</sub>	value of the commanded thrust on the previous guidance cycle
F <sub>SLP</sub>	rate of change of the thrust level as a function of burn time
F <sub>TAB</sub>	table of thrust magnitudes used to determine specific impulse values
F <sub>TRIM</sub>	constant that is representative of the DPS thrust during the trim phase
F <sub>1</sub>	thrust level at the beginning of each thrust phase (subroutine RUNGA)
F <sub>2</sub>	thrust level at the end of each thrust phase (subroutine RUNGA)
F <sub>6</sub>	flag that indicates whether or not subroutine TIMEP is to advance the state vector through the time interval T <sub>21</sub>

$F_{57}$	thrust level representative of 57 percent of DPS full-rated thrust
$F_{63}$	thrust level representative of 63 percent of DPS full-rated thrust
$F_A^*$	save table of actual thrust profiles
$F', F''$	coefficients of polynomial used to calculate LM thrust level at full throttle as a function of burn time
$f$	coefficient used in Keplerian orbit prediction equations
$f(x)$	value of dependent variable in the regula-falsi iteration
$f_3$	flag set to 0 or 1 according to whether the iterator should use the regula falsi or bias method
$f_4$	flag set to 0 or 1 according to whether the iterator is to act as a first order or a second order iterator
$f_7$	flag set to 1 if the input requires the conic trajectory to close through infinity
$f$	coefficient used in Keplerian orbit prediction equations
$G_{EFF}$	effective gravity
$\overline{G}_N$	gravity vector computed in present 2-second computer cycle
$\overline{G}$	gravity vector computed in previous 2-second computer cycle
$\overline{GRAV}$	same as $\overline{G}$
$g$	a. acceleration caused by gravity at the earth's surface b. argument of latitude of pericenter c. coefficient used in Keplerian prediction equations
$g_e$	acceleration caused by gravity at the earth's surface
$g_n$	orbital rotation rate of the pericenter
$\dot{g}$	coefficient used in Keplerian orbit prediction equations

$\bar{g}$	acceleration vector caused by gravity
$\bar{g}_{AGS}$	same as $\overline{GRAV}$
$\bar{g}_b$	gravity acceleration perturbation caused by oblateness of the central body
$\bar{g}_p$	gravity acceleration vector used on the previous guidance cycle
H	a. altitude of a landmark above the reference sphere b. magnitude of the angular momentum vector
$H_{ALT}$	current altitude in the LM ascent guidance equations
$H_a$	altitude of the apocenter
$H_k$	altitude of the kth landmark above the reference sphere
$H_p$	altitude of the pericenter
$\bar{H}$	angular momentum vector
h	a. current altitude in the LM descent guidance equations b. argument of the ascending node of the orbital plane
$h_{LS}$	altitude of the landing site referenced from the mean lunar radius
$h_n$	rotation rate of ascending node of the orbital plane
$h_{p1}$	pericenter altitude on the pre-CDH orbit
$h_{p2}$	pericenter altitude on the pre-TPI orbit
$\bar{h}_c$	unit angular momentum vector of the CSM
I	a. index of the active vehicle b. general iteration counter



INC	orbital inclination
INIT	flag that indicates whether the current guidance cycle is the initial one or not
INITRR	flag that indicates whether the current entry to the AGS RR logic is the first entry or not
I <sub>ABORT</sub>	flag that indicates whether or not one abort from powered descent is to occur
	-1 nominal descent
	0 an abort is to occur
	1 abort has occurred
I <sub>AC</sub>	alarm flag that indicates the reason for convergence failure in the CSI and TPI iterations
I <sub>ANGLE</sub>	control flag that indicates the type of tracking data to be simulated
	0 use both range and angle data
	1 use range data only
	2 use angle data only
I <sub>C</sub>	computer flag
I <sub>COM</sub>	flag that indicates the controlling computer on the current event
	1 CMC
	2 LGC
	3 AGS
I <sup>*</sup> <sub>COM</sub>	saved value of I <sub>COM</sub>
I <sub>CON</sub>	flag that designates the units on the input reference state
I <sub>COUNT</sub>	general symbol for an iteration counter

$I_{COV}$  storage/retrieval flag for the covariance matrix  
storage routine COVTAB

- 0 store
- 1 retrieve

$I_{DIF}$  flag that indicates type of state vector to be processed

- 1  $\delta X_A$
- 2  $\delta X_E$
- 3  $\Delta X_A$
- 4  $\Delta X_E$
- 5  $\delta \Delta X_E$

$I_{DISPLAY}$  flag that controls print of  $\Delta \Delta h$  data and closest approach data

$I_{DPS}$  flag that indicates whether DPS engine is being used

$I_{DV}$  flag that indicates route to be used in the  
subroutine LVLHDX

- 0 convert from LV to BR
- 1 convert from BR to LV

$I_{ENG}$  flag that indicates engine to be used to perform a maneuver

- 1 RCS
- 2 DPS (or SPS for CSM)
- 3 APS

$I_{EX}$  maneuver simulation control flag

- 0 execute and trim residuals to zero
- 1 execute and model trim

	2	execute with no trim
	3	execute with no trim and add pointing errors
	4	do not execute
	5	impulsive simulation
$I_{FLAG}$		maneuver guidance control flag
	1	impulsive guidance
	2	external $\Delta V$ guidance
	3	Lambert guidance
	4	descent guidance
	5	ascent guidance
	6	AGS guidance
$I_{FLQGO}$		flag that routes the logic to set the LM descent braking phase targets
$I_{FLQG1}$		flag that routes the logic to set the LM descent approach phase targets
$I_{FLVF}$		flag which when set to 1 routes logic to the velocity-following mode in the LM descent guidance
$I_{FLVF2}$		flag that routes the logic to set the targets used by the velocity-following mode of the LM descent guidance
$I_{FLVP}$		ascent vertical rise control flag
	0	nominal ascent
	1	vertical rise phase
$I_{FPC}$		ascent targeting control
	0	target for altitude and velocity
	1	target for velocity only

$I_{\text{GUESS}}$  regula-falsi iteration control  
     0 do not attempt to guess at solution until solution has  
       been bounded  
     >0 make a guess at the solution even if the solution has  
       not been bounded  
  
 $I_{\text{KNOWN}}$  optical tracking flag that indicates whether the tracked  
           landmark is categorized as known or unknown  
  
 $I_{\text{MAIN}}$  index of the main thrust phase  
  
 $I_{\text{MDC}}$  index of the current descent guidance phase  
  
 $I_{\text{ME}}$  index of the main thrust phase  
  
 $I_{\text{MEDPS}}$  index of the DPS main thrust phase  
  
 $I_{\text{MON}}$  flag that indicates whether a computer is to be monitored  
  
 $I_{\text{MOVE}}$  flag that indicates to the state vector propagation logic  
           which time value is to be used  
  
 $I_{\text{NOMT}}$  flag that indicates whether AGAST is currently generating  
           a reference trajectory or a sample trajectory  
  
 $I_{\text{ONOFF}}$  initialization flag for the guidance equations  
  
 $I_{\text{ORB}}$  flag that indicates whether the LM is in orbit or not  
  
 $I_{\text{P}}$  print flag  
  
 $I_{\text{PASS}}$  index that indicates which solution is being computed in the  
           targeting  
         1 CMC  
         2 LGC  
         3 AGS

- 4 MSFN
- 5 ACT/CMC
- 6 ACT/LGC
- 7 ACT/AGS
- 8 ACT/ACT

$I_{PE}$  flag that indicates whether platform errors are to be simulated or not

$I_{PE}^*$  saved value of  $I_{PE}$

$I_{PERTA}$  flag that controls the option to perturb the initial actual state vectors

$I_{PERTE}$  flag that controls the option to perturb the initial estimated state vectors

$I_{PH}$  index of thrust phase

$I_{PH}'$  index of thrust phase on the previous guidance cycle

$I_{PHASE}$  index of the current descent phase

$I_{PLTN}$  flag that specifies whether the platform errors have been initialized or not

$I_{PLTSG}$  flag that controls the setting of platform errors

- 0 use input errors
- 1 compute platform errors from  $\sigma$ 's

$I_{PRINT}$  print flag

$I_R$  flag that designates how the AEG is to output U and M

- 0 output U and M in the interval  $[0, 2\pi]$
- 1 output U and M in the proper revolution

$I_{\text{RAN}}$  controls the logic routing of the random number generator  
     1 output zeros only  
     0 initial call to RANNO  
     1 subsequent call to RANNO

$I_{\text{RBIAS}}$  RR bias control flag

$I_{\text{ROT}}$  indicates whether an input covariance matrix is to be rotated or not

$I_{\text{SAM}}$  flag that indicates whether a mission event is to be a reference point and what kind of statistical processing is to be performed

$I_{\text{SAVE}}$  reference point counter

$I_{\text{SET}}$  indicates whether the input vector is in classical, Cartesian, or spherical elements

$I_{\text{SP}}$  specific impulse

$I_{\text{SP}_A}$  actual specific impulse of the current thrust phase

$I_{\text{SP}_A}^*$  stored values of specific impulse for each thrust phase

$I_{\text{SP}_D}$  specific impulse that corresponds to the commanded DPS thrust level

$I_{\text{SP}_{\text{NOM}}}$  nominal specific impulse

$I_{\text{SP}}', I_{\text{SP}}''$  first and second degree time derivatives of the specific impulse used in the polynomial in the descent guidance

$I_{\text{SPNP}}$  specific impulse of the tail-off phase

$I_{\text{SPLIT}}$  flag that indicates if the burn ignition time and the  $\Delta V$  of an external  $\Delta V$  maneuver are to be biased by subroutine SPLIT to account for the finite burn effects

0 do not bias the burn

1 bias the burn

$I_{SPTAB}$  table of specific impulse values used to calculate DPS specific impulse as a function of the commanded thrust

$I_{STAGE}$  flag that defines the status of the DPS stage during powered ascent

1 nominal ascent with APS or DPS ascent without staging the DPS

0 DPS staging is to occur

1 DPS staging is to occur on the current guidance cycle

2 staging has occurred and the burn is being completed with the APS

$I_{STATE}$  flag set to 1 or 0 depending upon whether or not the initial state vectors for ascent have been computed by AFLPN

$I_{STBRN}$  flag that initializes the  $T_{GO}$  calculations by calling SHORTB

$I_{STOP}$  flag to control the logic which sets the time to end onboard tracking

$I_{SXTB}$  SXT bias control flag

$I_{TDV}$  flag set to 0 or 1 depending upon whether or not the automatic target  $\Delta V$  option is desired on all monitored computers after a burn

$I_{TEV}$  flag that controls the setting of an event time

$I_{THR}$  flag to control the logic which sets up a model of the actual thrust profile

$I_{THR}^*$  flag for each engine which designates whether a constant or linearly varying thrust model is to be used for the main engine phase of a burn

$I_{THROT}$  flag that indicates if the DPS engine is to throttle up despite the short burn logic constraints

$I_{TIME}$  flag that indicates the form of the input reference state time  
 $I_{TYPE}$  flag that indicates whether an input covariance matrix represents actual state vector uncertainties or estimated state vector uncertainties  
 $I_{UPDATE}$  flag that indicates if the state vectors which result from a MSFN update are to be transferred to the monitoring computers  
 $I_V$  vehicle flag used in subroutine PERRO  
 $I_{VEH}$  index of active vehicle; in subroutine ONR, it indicates the state vector being updated  
 $I_{VR}$  vehicle index of the state vector which is to be transferred from one computer to update another computer  
 $I_{WMATRIX}$  W-matrix initialization control flag  
 $I_{WRITE}$  flag that indicates if the out-of-plane velocity at a maneuver point is to be nulled  
 $I_{2PH}$  flag that indicates whether or not two-phase descent is to be used  
 $[I]$  the  $n$  by  $n$  identity matrix  
 $i$  orbital inclination  
 $J$  index of passive vehicle  
 $J_D$  dimension of the W-matrix (may be either 6 by 6 or 9 by 9)  
 $J_{DFLAG}$  flags that indicate which of the maneuver targeting differences are to be produced  
 $J_{DGZ}$  the desired Z-component of the target jerk vector in the LM descent guidance  
 $J_{ENTER}$  flag that indicates a reentry condition in ENCKE  
 $J_F$  routing flag for the print logic of the onboard tracking routines



- $J_{FLAG}$       a. internal routing flag for the logic of subroutine RNR
- b. in descent, this flag determines which set of target vectors will be used for the current phase
- $J_{KT,PHASE}$     the Z-component of the target jerk vector for each phase of LM descent
- $J_{LOOP}$         flag that controls the cycle iteration during the preignition phase
- $J_{MFLAG}$        flag that designates which sections of the LM ascent insertion covariance matrix are to be entered as input
- $J_{NEXT}$         flag that indicates whether or not a  $T_{NEXT}$  time is to be computed in TARGET
- $J_{PASS}$         first value of  $I_{PASS}$  in the maneuver targeting loop in subroutine TARGET
- $J_{PHASE}$        flag that indicates current descent guidance phase
- 1   braking phase
- 2   approach phase
- $J_{SFLAG}$        flags that designate which of the maneuver targeting solutions are desired
- $J_{SKIP}$         increment by which  $I_{PASS}$  is increased in TARGET after each targeting solution has been obtained
- $J_V$            flag that indicates which vehicle's state vector is to propagate the W-matrix in ENCKE
- $J_1$            index input to SETTHR that indicates the first engine to be modeled in the thrust setting logic
- $J_1^{28}$         component of external  $\Delta V$  in down-range direction
- $J_2$            a. index input to SETTHR that indicates the last engine to be modeled in the thrust setting logic
- b. in the state vector propagation routines,  $J_2$  designates a constant in the gravitational potential function

$J_2^{28}$	component of external $\Delta V$ in cross-range direction
$J_{2E}$	the $J_2$ constant for the earth gravitational potential function
$J_3$	constant in the gravitational potential function
$J_3^{28}$	component of external $\Delta V$ in negative radial direction
$J_4, J_{22}, J_{31}$	constant in gravitational potential function
$J_{1900}$	Julian date of January 1, 1900
$J_{1964}$	Julian date of January 1, 1964
$J^1$	desired TPI time
$J^2$	cotangent of desired LOS angle at TPI time
$J^5$	nominal landing site radius
$J^6$	desired LM transfer time for direct intercept transfer routine
$J^7$	term in LM semimajor axis $\alpha_L$ in orbit insertion route
$J^8$	lower limit of $\alpha_L$ in orbit insertion route
$J^9$	upper limit of $\alpha_L$ in orbit insertion route
$J^{16}$	orbit insertion targeted injection altitude
$J^{17}$	radar range rate
$J^{18}$	radar range
$J^{21}$	vertical pitch steering altitude threshold
$J^{22}$	vertical pitch steering altitude rate threshold
$J^{23}$	orbit insertion targeted injection radial rate

J<sup>25</sup> altitude above lunar surface for an altitude update

J<sup>26</sup> radar filter update time initialization value

K a. in subroutine SAMSIG, this flag indicates the number of variables to be processed  
b. in subroutine COMDKI, this flag is an iteration counter

KA AGSKEP initialization flag

KI initialization flag in subroutine AGSKEP

KORIN flag that indicates the coordinate system of a state vector being entered into a propagation routine

KOROUT flag that indicates the desired coordinate system of a state vector to be output from a propagation routine

KRNDFG flag that indicates whether or not the onboard tracking equations have been initialized

K<sub>BS</sub> flag that indicates whether or not the tracking vehicle is to boresight along the line of sight

K<sub>D</sub> a. in AMAIN and INCOV, this parameter is the index of a covariance matrix  
b. in the tracking incorporation routines, this parameter is the index of the update matrix

K<sub>DIR</sub> flag used to determine the thrust direction in the ascent guidance

K<sub>ENTER</sub> routing option for subroutine START

K<sub>EPOCH</sub> initialization parameter for JPLEPH

K<sub>EST</sub> flag that indicates whether the estimated states are to be propagated with the AEG or with the onboard integrator

K<sub>EVENT</sub> event counter

{K<sub>i</sub>}<sub>i=0</sub><sup>3</sup> powered descent abort constants

$K_{MODE}$  flag that indicates whether or not subroutine SAMPLE is to output a perturbed state vector X

$K_{NSR}$  iteration counter in subroutine JOCDH

$K_{STBRN}$  flag that indicates if the burn is less than 6 seconds in length

$K_{STEER}$  flag that indicates if steering is allowed on the current guidance cycle

$K_{STBURN}$  same as  $K_{STBRN}$

$K_{S10}$  guidance selection flag

- 0 orbit insertion
- 1 CSI
- 2 CDH
- 3 TPI search
- 4 TPI execute
- 5 external  $\Delta V$

$K_{TARG}$  flag that controls the routing logic of DKI maneuver computations

$K_{TGO}$  flag in the ascent guidance equations which prohibits the cycling of the  $T_{GO}$  equation after  $T_{GO}$  becomes less than 4 seconds

$K_{THR}$  flag that indicates whether or not the thrust model is to be changed for the current maneuver event

$K_{TOFF}$  flag that indicates whether the burn is in the tail-off phase or is complete

$K_{TRK}$  code associated with the  $T_{TRK}$  table and consisting of a table of indicies for the landmarks to be tracked

$K_{UL}$  ullage phase indicator

$K'_{UL}$	value of $K_{UL}$ on previous cycle through the integrator
$K_{UTA}$	flag that controls the routing of the platform error model logic of subroutine MANEUV
$K_{VR}$	vertical rise indicator in the LM ascent guidance logic 0    steer in the commanded direction 1    steer along the radius vector
$K_X$	coefficient of the x term of the equation used to solve for powered descent initiation
$K_Y$	coefficient of the y term of the equation used to solve for powered descent initiation
$K_V$	coefficient of the velocity term of the equation used to solve for powered descent initiation
$K_{XTRA}$	counter which indicates how many variables have been loaded into the XTRA array
$K_1$	a.    initialization flag for the state vector propagation routines b.    index input to SETTHR which indicates the first vehicle to be modeled in the thrust setting logic c.    engine constant in subroutine SHORTB
$K_2$	a.    index input to SETTHR which indicates the last vehicle to be modeled in the thrust setting logic b.    engine constant in subroutine SHORTB
$K_6$	counter that indicates the index of the 6 by 6 covariance matrix to be used on the current event
$K_{12}$	counter that indicates the index of the 12 by 12 covariance matrix to be used on the current event
$K_1^2$	AGS gravitational constant
$K_2^2$	reciprocal of $K_1^2$

$K_3^2$	value of $g$ in AGS if overflow occurs in $e^2$
$K_4^2$	$-K_1^2 \Delta t$ ( $\Delta t = 2$ sec)
$K_4^4$	coefficient in linear expression for $\dot{r}_f$ as a function of $r_f$
$K_5^4$	constant in linear expression for $\dot{r}_f$ as a function of $r_f$
$K_6^4$	upper limit on $\dot{r}_f$
$K_{11}^2$	value to which $V_T$ is set if overflow occurs in $V_T$
$K_{12}^4$	acceleration check for $\ddot{R}_{DTL}$
$K_{14}^5$	upper limit on $\ddot{r}_d$
$K_{17}^2$	controls iterations of p-iterator
$K_{17}^5$	lower limit on $\ddot{y}_d$
$K_{18}^5$	lower limit of $r_d$
$K_{19}^2$	$\Delta p$ limiter in p-iterator
$K_{20}^2$	p-iterator convergence check
$K_{20}^5$	lower limit of $\ddot{r}_d$
$K_{26}^5$	velocity-to-be-gained threshold
$\bar{K}_{XL}$	constants associated with the landmark and used in landmark tracking
$k_Q$	flag that indicates the type of rendezvous navigation parameter for which print is desired
$L$	a. vehicle index b. intermediate matrix for range and range rate updates in AGS

$LM_{UP}$	rendezvous navigation flag that indicates whether the state vector being updated is that of the LM or that of the CSM
LOS	line of sight
LV	local vertical
$L_{EC}$	primary flag for event category <ol style="list-style-type: none"> <li>1 maneuver</li> <li>2 platform alinement</li> <li>3 update event (using a covariance matrix)</li> <li>4 update event (model onboard tracking)</li> </ol>
$L_{EN}$	secondary flag for event category; e.g., this flag is used to differentiate between the different maneuver types
$L_{SA}$	flag that indicates how the actual landing site position is to be calculated
$L_{SE}$	flag that indicates how the estimated landing site position is to be calculated
$L_1$	index that indicates the first state vector to be propagated in the AEG and in ENCKE
$L_2$	index that indicates the last state vector to be propagated in the AEG and in ENCKE
[LVBR]	rotation matrix that relates the Apollo local vertical frame to the basic reference frame
$[LVBR]_A$	actual [LVBR]
[LVLOS]	rotation matrix that relates the Apollo local vertical frame to the rendezvous navigation line-of-sight frame
$[LVLOS]_A$	actual [LVLOS]
$\ell_{MAX}$	upper bound of general independent variable
$\ell_{MIN}$	lower bound of general independent variable

$\ell_1, \ell_2$  indices that indicate which computer platforms are to be modeled in SETPLT

M mean anomaly

$M_{AGS}$  burn monitor flag for the AGS computer

$M_O$  array that contains the number of days in each month of the year

$M_{PGNCS}$  burn monitor flag for the LGC and CMC computers

$M_{PT}$  counter that indicates the number of maneuvers stored in the mission plan table

m a. vehicle mass  
b. matrix of partial derivatives of the computed range rate with respect to inplane position and velocity component

$\dot{m}$  vehicular mass flow

N a. mark counter for the tracking routines  
b. number of Monte Carlo samples in the statistical processing routines  
c. counter that indicates the number of guidance cycles which have passed since the last Lambert solution in a Lambert guided maneuver

$N_{DEL}$  0 for range rate radar update in AGS  
1 for range radar update in AGS

$N_l$  flag that indicates the number of offsets to be computed in subroutine INITV

$N_c$  counter used in the thrust sensing logic in MANEUV

$N_{CASE}$  Monte Carlo loop counter

$N'_{CASE}$  counter that indicates number of cycles of the AGAST logic, including the cycle for generation of the reference trajectory



$N_{CDH}$       apsis indicator for the CDH maneuver  
 $N_F$         maneuver line counter to be advanced to in subroutine COMDKI  
 $N_I$         initial maneuver line counter in subroutine COMDKI  
 $N_{LM}$       number of landmarks to be tracked  
 $N_{MAX}$      number of guidance cycles in a Lambert guided maneuver  
              between each Lambert solution  
 $N_P$         index of the tail-off phase  
 $N_{PASS}$     iteration counter for the  $T_{GO}$  calculation of the descent  
              guidance  
 $N_{PH}$       burn simulator control flag that keeps  $I'_{PH}$  from being  
              set until all logic required for initialization of a  
              new thrust phase has been processed  
 $N_{SAM}$      number of Monte Carlo cycles requested  
 $N_{THROT}$    flag that indicates whether or not the DPS is to be  
              throttled up  
 $N_{TOTAL}$    counter for the  $T_{TRK}$  table  
 $N_1$         a. maneuver line number of the first maneuver of a  
              DKI sequence  
              b. otherwise equivalent to  $N_1$   
 $N_2$         a. maneuver line number of the second maneuver of a  
              DKI sequence  
              b. otherwise equivalent to  $N_F$   
 $N_3$         a. maneuver line number of the third maneuver of a  
              DKI sequence  
              b. in subroutine START, this parameter is the index of  
              the main thrust phase

$N_4$	index of the main engine ignition thrust phase in subroutine START
$N_5$	index of the tail-off thrust phase in subroutine START
[NBSM]	rotation matrix that relates the navigation base coordinate frame to the stable member (IMU) frame
$n$	variable that indicates which actual solution is to be used for computation of the maneuver targeting error
$n_{CSM}$	mean motion of the CSM
$n_E$	mean motion of CSM in AGS
$n_I$	mean motion of the $i$ th vehicle
$n_i$	mean motion output by orbit parameters subroutine
$P$	a. orbital period in subroutine COMDKI b. LM state vector error covariance matrix in AGS c. semilatus rectum of LM transfer orbit in AGS
PDI	a. powered descent initiation b. time of powered descent initiation
PEM	platform error matrix in subroutine AGSRR
$P_F$	thrust dispersion percentage desired
$P_{HT}$	equivalent to $\Delta T_{BP}$
$P_I$	specific impulse dispersion percentage desired
$P_N$	ratio of the semilatus rectum to the position vector magnitude
$P'$	previous value of $p$ in $p$ -iterator portion of AGS
[P]	rotation matrix output from subroutine PMATRIX

$[P(t)]$	platform error matrix
$[P_A(t)]$	AGS platform error matrix
$[P_E(t)]$	platform error matrix output from subroutine PERRO
$[PNL]$	lunar libration matrix which is output from subroutine JPLEPH; see the second definition of $[A]$
$[P_T]$	PGNCS platform error matrix at the time of AGS-to-PGNCS alinement
$p_i$	probability table generated in the cumulative distribution function routine CDFUNC
$Q$	intermediate computation matrix for radar update equations
$q$	present LM perigee
$q_a$	same as $q$
$q_1$	perigee of LM transfer orbit
$R$	radius vector magnitude
$RR$	rendezvous radar
$R_A$	a. actual relative range in tracking routines b. radius of apogee in CONVRT
$R_{AGS}$	estimated relative range in the AGS
$R_a$	radius of apogee
$R_{BIAS}$	bias to RR range measurement
$R_{DD}$	desired LM insertion radius
$R_E$	earth equatorial radius magnitude
$R_{EPH}$	conversion factor from er/hr to fps

$R_{IGX}, R_{IGZ}$	desired x and z components of the LM position vector at the full throttle point of descent
$R_J$	target radius vector magnitude
$R_L$	chaser radius vector magnitude
$R_{LS}$	radius magnitude of the landing site
$R_{LSM}$	same as $R_{LS}$
$R_M$	measured relative range
$R_{MOON}$	mean lunar radius
$R_O$	equivalent to $R_{MOON}$
$R_P$	radius of perigee
$R_{PGNCS}$	estimated relative range in the PGNCS
$R_{REF}$	mean radius of the central body
$R_{TA}$	CSM state vector in the AGS
$R_x, R_z$	components of $\bar{R}$ along local vertical and local horizontal axes, respectively
$\dot{R}$	a. radical velocity component b. relative range rate
$\dot{R}_A$	actual relative range rate
$\dot{R}_{AGS}$	estimated relative range rate in the AGS
$\dot{R}_M$	measured relative range rate
$\dot{R}_{PGNCS}$	estimated relative range rate in the PGNCS

$\bar{R}^{**}$	computed range rate saved when subroutine FILTER is initialized
$R_{DTL}$	lower limit of $r_d$ , computed as a function of vehicle configuration
$\bar{R}$	a. position vector b. relative position vector of CSM with respect to the LM
$\bar{R}^{**}$	computed inertial range vector in subroutine FILTER
$\bar{R}_{AGS}$	AGS estimated LM position vector
$\bar{R}_{A,I}$	actual position vector of the active vehicle
$\bar{R}_{A,J}$	actual position vector of the passive vehicle
$\bar{R}_{AVG}$	position vector to be integrated by subroutine AGSAG (input and output)
$\bar{R}_C$	position vector used in the ascent guidance
$\bar{R}_{CL}$	range vector directed from the CSM to a landmark
$\bar{R}_{CON}$	conic position vector in ENCKE
$\bar{R}_{CSM}$	position vector of the CSM
$\bar{R}_{DG}$	desired target position vector
$\bar{R}_{E,I}$	estimated position vector of the active vehicle
$\bar{R}_{E,J}$	estimated position vector of the passive vehicle
$\bar{R}_G$	position vector in LM descent guidance coordinates
$\bar{R}_I$	position vector of the active vehicle
$\bar{R}_{IG}$	position vector at ignition time

$\bar{R}_{I1}$	position vector of the active vehicle at CSI
$\bar{R}_{I2}$	position vector of the active vehicle at CDH
$\bar{R}_J$	position vector of the passive vehicle
$\bar{R}_{JC}$	passive vehicle position at CDH phase match
$\bar{R}_{J1}$	position vector of passive vehicle at CSI
$\bar{R}_{J2}$	position vector of passive vehicle at CDH
$\bar{R}_{J3}$	position vector of passive vehicle at TPI
$\bar{R}_J^*$	position vector of the passive vehicle at phase match with the desired position of the chaser at TPI
$\bar{R}_L$	a. position vector of a landmark in subroutine ONR b. magnitude of position vector in TCONE
$\bar{R}_{LC}$	vector from the active vehicle to the passive vehicle
$\bar{R}_{LM}$	position vector of the LM
$\bar{R}_{LS}$	landing site position vector
$\bar{R}_{LSA}$	actual landing site position vector
$\bar{R}_M$	position vector at the midpoint of a burn
$\bar{R}_N$	new value of position vector integrated by subroutine AGSAG
$\bar{R}_0$	a. position vector input to subroutines LVLHDX and PMATRX b. rectified state vector in ENCKE
$\bar{R}_0^*$	saved value of $\bar{R}_0$ in ENCKE

$\bar{R}_P$	a. position vector in platform coordinates in the LM descent guidance  b. landmark position vector in selenocentric coordinates in subroutine ONR
$\bar{R}_{PGS}$	PGNCS estimated LM position vector
$\bar{R}_{PP}$	range vector in platform coordinates directed from the LM to the landing site
$\bar{R}_{REL}$	actual relative range vector
$\bar{R}_S$	position vector of the landmark to be tracked
$\bar{R}_{SG}$	landmark position vector in selenographic coordinates
$\bar{R}_T$	target vector for Lambert maneuver
$\bar{R}_{T,JPHASE}$	input target position vector for each descent guidance phase
$\bar{R}_{T2}$	offset target vector in a Lambert maneuver
$\dot{\bar{R}}$	computed range rate vector between LM and CSM
[R]	a. see [P]  b. rotation matrix from first point of Aries to Greenwich coordinates in AMATRX
[ROT <sub>RR</sub> ]	matrix that defines the actual orientation of the LM Z-body axis
[R <sub>0</sub> ]	matrix that defines the vehicle attitude during a burn
r	a. position vector magnitude  b. range in PCA
$r_b$	predicted LM burnout radius saved from previous 2-second cycle
$r_f$	predicted LM radial distance at $t_{ig}$ , current for orbit insertion

$r_i$	inertial position vector magnitude output by subroutine OPS
$r_T$	predicted radial distance of CSM as it crosses the vector $\bar{r}_5$ in the direction of the LM at $t_{ig}$
$\dot{r}$	range rate
$\dot{r}_A$	predicted LM altitude rate at $t_{ig}$ for CSI and CDH
$\dot{r}_f$	predicted radial rate for the following <ol style="list-style-type: none"> <li>CSM as it crossed the vector <math>\bar{r}_s</math> in the direction of the LM at <math>t_{ig}</math> for CDH</li> <li>LM in orbit insertion mode</li> <li>LM at <math>t_{ig}</math> for CSI</li> </ol>
$\ddot{r}_d$	desired radial acceleration
$\ddot{\ddot{r}}_d$	desired derivative of the radial acceleration
$\bar{r}$	<ol style="list-style-type: none"> <li>LM position vector</li> <li>position vector to be advanced by subroutine CONIC</li> </ol>
$\bar{r}_C$	predicted CSM inertial position vector at $t_{ig}$ for CSI, CDH, or TPI modes; at present time for orbit insertion mode
$\bar{r}_0$	position vector input to subroutines OPS and ELPRE
$\bar{r}_5$	predicted LM inertial position vector at $t_{ig}$ ; current LM position vector for orbit insertion
$\dot{\bar{r}}_F$	LM velocity vector just prior to the second impulse in the transfer orbit
$\dot{\bar{r}}_I$	LM velocity vector after first impulse for the transfer orbit
S	intermediate symbol for a sum



SAVMAN      array that contains the following data for each solution targeted

- a.  $T_{EX}$
- b.  $\Delta V_{EX}$
- c.  $\dot{y}$
- d.  $h_a$
- e.  $h_p$
- f.  $E_A$

SOM          stable orbit midcourse maneuver

SOR          stable orbit rendezvous maneuver

SPHERE      six-dimensional array of spherical orbital elements

$S_E$           product of the orbital eccentricity and the sine of the eccentric anomaly

$S_i$           product of eccentricity and sine of eccentric anomaly

$S_{\Delta E}$       sine of the difference in the present and final eccentric anomalies

$S_{07}$       1    if velocity-to-be-gained vector is to be frozen in AGS inertial coordinates and sensed velocity;  
              0    otherwise

$S_{10}$       same as  $K_{S10}$

$S_{16}$       1    compute CDH at one-half LM orbital period after CSI  
              3    compute CDH at 1.5 LM orbital periods after CSI

[SMNB]      rotation matrix that relates the stable member (IMU) frame to the navigation base coordinate frame

$S_j$           accelerometer scale factor in subroutine SETPLT

T            current mission time referenced from the base time

$T_{CL}^{TH}$	threshold time for the maneuver line logic
TIME	a. clock time read from the UNIVAC 1108 system clock b. time to which a state vector is to be advanced in ENCKE
$T_A$	time of alinement
$T_{ABORT}$	time at which an abort from descent is to occur
$T_{AGS}$	time associated with the AGS state vector
$T_{AO}$	time from CSI to CDH in AGS
$T_{ASCENT}$	nominal ascent powered flight time
$T_B$	time of burn
$T_{BIAS}$	time bias added to the CDH or TPI maneuver time
$T_{CA}$	time of closest approach of the LM and CSM
$T_{CDH}$	time of the CDH maneuver
$T_{CSI}$	time of the CSI maneuver
$T_{COMP}$	time between each Lambert solution in a Lambert guided burn
$T_D$	direct transfer time through which the conic update of the state vector is to be made
$T_{DV}$	time used in the target $\Delta V$ logic
$T_E$	time associated with an estimated state vector
$T_E^*$	saved value of $T_E$
$T_{ENDAPR}$	the $\Delta T$ , referenced from the LM descent approach phase target point, at which the approach phase is terminated
$T_{ENDBRK}$	the $\Delta T$ , referenced from the LM descent braking phase target point, at which the braking phase is terminated

$T_{ERR}$	error in the transfer time in subroutine LAMBERT
$T_{EVENT}$	time of the current event
$T_{EX}$	time of an external $\Delta V$ maneuver
$T_F$	a. time of the final maneuver in a Lambert sequence b. mark time in the optical tracking routines
$T_{FA}$	time of the first apsis crossing after a threshold time
$T_{FTP}$	time at which DPS full throttle position is to be achieved
$T_{GO}$	a. in the LM descent guidance logic, this parameter represents the time to go until the end of the current descent guidance phase b. in all other guidance logic, this parameter represents the time to go until the main engine cut off.
$T'_{GO}$	time to go until end of tail-off
$T''_{GO}$	time to go until end of the current thrust phase
$T^*_{GO}$	stored $T_{GO}$ which was calculated during the current guidance cycle
$T_{GOAUG}$	first guess at the approach phase duration
$T_I$	time of the first maneuver in a Lambert sequence
$T_{IG}$	time of burn initiation
$T_{IM}$	table of the $\Delta T$ 's of each thrust phase used in subroutine START
$T_{IMN4}$	ullage phase $\Delta T$
$T_i$	time input to ELPRE which represents one of the following a. time from CSM epoch to rendezvous b. time from CSM epoch to rendezvous retarded by $J^4$ in TPI mode

	c. time from CSM epoch to CSM crossing vector in $\bar{r}_5$ direction in CSI and CDH modes
$T_{ig}$	desired time of next AGS maneuver
$T_{iga}$	time of CSI in AGS
$T_{igb}$	time of CDH in AGS
$T_{JC}$	time in Julian centuries from January 1, 1900, to the base date
$T_{JD}$	Julian date of the base date
$T_{LAST}$	a. time of the last event b. time of the last initial state vector in the AEG
$T_{LO}$	lift-off time
$T_M$	table of five mark times for a pass over a landmark
$T_{MARK}$	vector of tracking sequence times in subroutine AGSRR
$T_{MOVE}$	time to which the state vectors are to be propagated
$T_{NEXT}$	time of the next event
$T_{NEXTTE}$	estimated $T_{NEST}$ values for each monitored computer
$T_{NSR}$	time of the NSR maneuver
$T_{N1}$	time of the first maneuver of a DKI sequence
$T_{N2}$	time of the second maneuver of a DKI sequence
$T_{N3}$	time of the third maneuver of a DKI sequence
$T_P$	a. orbital period b. time from TPI to rendezvous

$T_P'$	previous value of $T_p$ in p-iterator portion of AGS
$T_{perg}$	time of LM to perilune
$T_R$	a. time of the initial reference state vector b. predicted time from present to rendezvous (valid only for TPI mode)
$T_{SAVE}$	table of closest approach times of the CSM a landmark
$T_{SEC}$	time to which a state vector is to be advanced
$T_{SEC}^*$	saved value of $T_{SEC}$
$T_{START}$	start time for onboard tracking
$T_{STOP}$	stop time for onboard tracking
$T_T$	time at which the passive vehicle is at phase match with the desired SOR target
$T_{TPF}$	time of rendezvous
$T_{TPI}$	time of terminal phase initiation
$T_{TRK}$	table of closest approach times of the CSM to a set of landmarks
$T_{XUS}$	average-g integration time interval left before burn ignition
$T_{\Delta}$	time from present to next maneuver
$T_1$	a. time of the first maneuver of a Lambert sequence b. time of last radar range update
$T_2$	time of the second maneuver of a Lambert sequence
$T_4$	time since the DPS went to the full throttle position
$T_{21}$	computed transfer time from Kepler's equation

$T'_{21}$	previous value of $T_{21}$
$T'$	time of the last guidance cycle
$[T]$	REFSMAT; rotation matrix that relates the basic reference system to the estimated IMU orientation
$[T_A]$	rotation matrix that relates the basic reference system to the actual IMU orientation
$t$	time of LM state vector in AGS
$t_E$	time of CSM state vector in AGS
$t_{ig}$	desired time of next maneuver
$t'_{21}$	previous value of $t_{21}$ in iteration
$U$	vehicle's argument of latitude
$U_{AP}$	argument of latitude of the apoapsis
$U_{CSI}$	argument of latitude of the CSI maneuver
$U_I$	argument of latitude of the active vehicle
$U_J$	argument of latitude of the passive vehicle
$U_{OC}$	argument of latitude of the maneuver line
$U_{1X}$	x-component of vector $\bar{U}_1$
$U_{1Z}$	Z-component of vector $\bar{U}_1$
$U^*$	saved value at $U$
$\bar{U}$	general symbol for a unit vector
$\bar{U}_B$	burn residual
$\bar{U}_{CL}$	unit vector along $\bar{R}_{CL}$
$\bar{U}_M$	unit vector along the line of sight of the SXT to an object

$\bar{U}_{NB}$	SXT navigation base unit vector directed along the line of sight to an object being tracked
$\bar{U}_Q$	unit vector in the LM ascent guidance along the negative CSM angular momentum vector
$\bar{U}_R$	unit vector along the radius vector
$\bar{U}_{REL}$	unit vector along the relative range vector
$\bar{U}_{r_1}$	unit vector of $\bar{r}_1$ in subroutine CONIC
$\bar{U}_{SM}$	unit vector in stable member coordinates along the line of sight to a landmark being tracked
$\bar{U}_{SXT}$	unit vector produced by the alinement of the SXT to an object to be tracked
$\bar{U}_{TA}$	unit vector along the actual thrust direction
$\bar{U}_{TD}$	unit vector along the desired thrust direction
$\bar{U}_y$	unit vector in the LM ascent guidance which is perpendicular to the LM radius vector
$\bar{U}_Z$	down-range unit vector at LM insertion
$\bar{U}_{ZR}$	vector through the central body north pole
$\bar{U}_1$	unit LM position vector
$\bar{U}_2$	CSI and CDH: unit vector pointing toward the CSM at $t_{ig}$  TPI: unit vector pointing toward either rendezvous point or toward rendezvous point retarded by $J^4$
[UVWXYZ]	rotation matrix that relates the uvw local vertical coordinate system to the xyz Apollo local vertical coordinate system
V	general symbol for velocity

VAR <sub>IMU</sub>	onboard constant that represents the a priori estimate of the IMU angular error variances per axis
VAR <sub>INT</sub>	onboard constant that represents the a priori estimate of the relative range error variance caused by coasting integration inaccuracies
VAR <sub>R</sub>	onboard constant that represents the a priori estimate of the RR measured range error variance corresponding to a percentage error
VAR <sub>RMIN</sub>	onboard constant that represents the minimum RR measured range error variance
VAR <sub>SCT</sub>	onboard constant that represents the a priori estimate of the scanning telescope angular error variance per axis
VAR <sub>SXT</sub>	onboard constant that represents the a priori estimate of the sextant angular error variance per axis
VAR <sub>V</sub>	onboard constant that represents the a priori estimate of the RR measured range rate error variance corresponding to a percentage error
VAR <sub>VMIN</sub>	onboard constant that represents the minimum RR measured range rate error variance
VAR <sub>VHF</sub>	onboard constant that represents the a priori estimate of the VHF measured range error variance corresponding to a percentage error
VAR <sub>VHFMIN</sub>	onboard constant that represents the minimum VHF measured range error variance
VAR <sub><math>\beta</math></sub>	onboard constant that represents the a priori estimate of the RR measured shaft angle error variance
VAR <sub><math>\theta</math></sub>	onboard constant that represents the a priori estimate of the RR measured trunnion angle error variance
VHF <sub>BIAS</sub>	bias on VHF range measurement
V <sub>CON</sub>	array that contains conversion factors needed to convert various velocity units to fps



$V_E, V_e$	thrust exhaust velocity
$V_G$	magnitude of velocity-to-be-gained vector
$V_{GX}, V_{GY}, V_{GZ}$	components along the LM X-, Y-, and Z-body axes, respectively, of the velocity to be gained
$V_{gx}, V_{gy}, V_{gz}$	components along the LM X-, Y-, and Z-body axes, respectively, of the total LM velocity to be gained during the burn
$V_H$	a. horizontal velocity component b. desired horizontal velocity at insertion
$V_{H,I}$	horizontal velocity component of the active vehicle
$V_R$	horizontal component of the present LM velocity
$V_{Ra}$	horizontal component of LM velocity vector parallel to the CSM orbit, at present time in orbit insertion mode, at $t_{ig}$ in CSI or CDH mode
$V_{hf}$	required horizontal component of LM velocity parallel to CSM plane for the current guidance mode
$V_{IGV}$	desired velocity magnitude at the DPS full throttle position
$V_{IH}$	desired horizontal velocity of active vehicle at CDH
$V_{IV}$	desired radial velocity of the active vehicle at CDH
$V_{Il}$	velocity of the active vehicle CSI
$V_{po}$	predicted velocity to be gained at CDH; computed in the CSI mode only in AGS
$V_{py}$	predicted LM out-of-CSM plane velocity at $t_{ig}$ for CSI, CDH, and TPI; current for orbit insertion
$V_t$	total change in velocity required for a direct transfer

$V_{TRIM}$	magnitude of the trim maneuver
$V_{v,I}$	vertical velocity component of the active vehicle
$V_{v,J}$	vertical velocity component of the passive vehicle
$V_Y$	component of LM velocity in direction perpendicular to the CSM orbit
$V_{Y0}$	same as $V_Y$
$V_1$	$\Delta V$ of CSI maneuver
$V_{10}$	$\Delta V$ of previous guess at the $\Delta V$ of CSI
$V_{2FG}$	desired target velocity for the velocity-following mode
$\bar{V}$	general symbol for velocity vector
$\bar{V}_A$	actual velocity vector
$\bar{V}_{A,I}$	actual velocity vector of active vehicle
$\bar{V}_{A,J}$	actual velocity vector of passive vehicle
$\bar{V}_{AGS}$	AGS estimated LM velocity vector
$\bar{V}_{AVG}$	velocity input to subroutine AGSAG to be integrated
$\bar{V}_C$	CSM velocity vector
$\bar{V}_{CON}$	velocity of the conic vector in ENCKE
$\bar{V}_{CSM}$	CSM velocity vector
$\bar{V}_{DG}$	desired velocity target vector in the descent guidance
$\bar{V}_E$	estimated state velocity

$\bar{V}_{E,I}$	estimated velocity vector for the active vehicle
$\bar{V}_{E,J}$	estimated velocity vector for the passive vehicle
$\bar{V}_F$	predicted braking velocity for direct transfer
$\bar{V}_G$	velocity to be gained
$\bar{V}_I$	velocity of the active vehicle at the point of the first maneuver of a Lambert sequence
$\bar{V}'_I$	see $\bar{V}_t$
$\bar{V}_{IG}$	velocity vector at ignition time
$\bar{V}_{I1}$	active vehicle velocity at CSI
$\bar{V}_{I2}$	active vehicle velocity at CDH
$\bar{V}'_{I2}$	desired active vehicle velocity after CDH
$\bar{V}_i$	updated velocity vector in subroutine ELPRE
$\bar{V}_J$	velocity vector of the passive vehicle
$\bar{V}_{JC}$	velocity vector of the passive vehicle at CDH phase match
$\bar{V}_{J1}$	velocity vector of the passive vehicle at CSI
$\bar{V}_{J2}$	velocity vector of the passive vehicle at CDH
$\bar{V}_{J3}$	velocity vector of the passive vehicle at TPI
$\bar{V}_{LC}$	relative velocity vector of LM with respect to the CSM
$\bar{V}_M$	velocity vector of the monitoring computer's state
$\bar{V}_N$	present velocity vector in subroutine AGSAG

$\bar{V}_0$	a. input velocity vector to the routines LVLHDX and PMATRIX
	b. initial velocity vector in ENCKE
	c. velocity vector to be updated by subroutines OPS and ELPRE
$\bar{V}_0^*$	saved value of $\bar{V}_0$ in ENCKE
$\bar{V}_P$	velocity vector in platform coordinator
$\bar{V}_{PGS}$	velocity vector of the PGNCS state vector
$\bar{V}_{PP}$	velocity vector in platform coordinates which has a magnitude equal to the ground speed
$\bar{V}_R$	rotated velocity vector
$\bar{V}_{REL}$	actual velocity vector of CSM relative to the LM
$\bar{V}_{ROT}$	velocity of the spacecraft in selenocentric coordinates caused by lunar rotation
$\bar{V}_T$	desired vector after the first maneuver in a Lambert transfer
$\bar{V}_T'$	same as $\bar{V}_T$
$\bar{V}_{T,JPHASE}$	input velocity target vector for each phase of descent
$\bar{V}_1$	horizontal unit vector in transfer plane
$\bar{V}_1'$	unit vector normal to $\bar{U}$ , and parallel to the CSM orbital plane at $t_{ig}$ in CSI, CDH, and TPI; at present in orbit insertion
$\bar{V}_2$	a. unit vector horizontal at rendezvous point and in transfer orbital plane
	b. also as above except retarded by $J^4$ in transfer orbital plane
$\bar{V}_5$	predicted LM velocity vector at TPI

$W_{\text{AFTER}}$	vehicle weight after a maneuver
$W_{\text{A,I}}$	actual weight of active vehicle
$W_{\text{AT}}$	table of vehicle weight at each thrust phase
$W_{\text{BO}}$	vehicle weight at main engine burn out
$W_{\text{E}}$	estimated vehicle weight
$W_{\text{LM}}$	LM weight
$W_{\text{O}}$	vehicle weight at the beginning of a maneuver
$W_{\text{T}}$	vehicle weight at the beginning of each thrust phase
$\dot{W}$	weight flow
$\dot{W}_{\text{ENG}}$	weight flow used in subroutines SPLIT and START
$[W]$	navigation filter W-matrix
$[W_{\text{B}}]$	partitioned W-matrix used in the propagation routine ENCKE
$[W_{\text{ICOM}}]$	W-matrix of the $I_{\text{COM}}$ computer
$[W_{\ell}]$	$\ell$ th 3 by 3 matrix generated by partitioning the 9 by 9 W-matrix and indexing the partition by rows
$[W_{\text{UNL}}]$	initial W-matrix for an unknown landmark
$W_{\text{CY}}$	Y-component of $\bar{W}_{\text{C}}$
$W_{\text{LY}}$	Y-component of $\bar{W}_{\text{L}}$
$\dot{W}$	weight flow table for the thrust profile
$\bar{W}_{\text{C}}$	unit vector normal to CSM orbital plane
$\bar{W}_{\text{D}}$	$K_{\text{D}}$ dimensional vector of the initial diagonal values of the W-matrix

$\bar{W}_\ell$	$\ell$ th three-dimensional column vector of the W-matrix; the column vectors are indexed by rows
$\bar{W}_1$	unit vector perpendicular to transfer orbital plane
X	general symbol for a six-dimensional state vector
XREAD1	first record format on data unit 13; consists of flags that define the type of maneuver statistics that are to be produced
XREAD2	second record format on data unit 13; consists of reference states and comments to be printed
XREAD3	third record format on data unit 13; consists of sample event time, sample actual stater, sample estimated stater, targeted $\Delta V$ , and burn statistics
XREAD4	fourth record format on data unit 13; consists of total burned $\Delta V$ , braking $\Delta \bar{V}$ , and extra orbital parameters for processing
XTRA	an array of ten orbital parameters for which statistical processing is desired
$X_A$	actual state vector
$X_{AGS}$	AGS estimated LM state vector
$X_E$	estimated state vector
$X_{E,I}$	estimated state vector of the active vehicle
$X_{ES}$	estimated state vectors that result from sampling of MSFN and onboard tracking uncertainty matrices
$X_{J6}$	same as $J^6$
$X_{LS}$	landing site position vector
$X_{LSA}$	actual landing site position vector
$X_{LSE}$	estimated landing site position vector

$X_{LSR}$	reference landing site vector
$X_R$	reference state vector
$\bar{X}$	symbol used in subroutine INPUT to represent the input state vector; it may lie in Cartesian coordinates, classical elements, or spherical elements
$\bar{X}_{DD}$	target LM insertion velocity vector
$\bar{X}_R$	rotated state vector in TRANCO
$x$	a. independent variable in the regula-falsi iteration in REGFAL b. universal variable in subroutine UNIVAR
$x_i$	a. array of samples of the parameter $X$ for which a cumulative distribution table is desired b. array of random numbers generated by subroutine RANNO
$X_{NOM}$	nominal value of the variable $X$
$X_{K12}$	same as $K_1^2$
$X_N$	the $n$ th value for the quotient of the universal variable $X$ and the position vector magnitude
$\bar{X}_b$	unit vector along LM $X$ -body axis
$\bar{X}_{bD}$	unit vector along desired pointing direction in steering
$y$	a. out-of-plane position component b. yaw angle in subroutine START c. component of LM vector in the direction perpendicular to the CSM vector in AGS
$Y_{DD}$	desired out-of-plane position at insertion
$Y_{ERR}$	error in the dependent variable $y$ in subroutine ITRATE

$Y_i$	array of random numbers uniformly distributed on the interval $[0, 1]$
$Y'$	previous value of $Y$
$\dot{Y}$	out-of-plane velocity component
$\ddot{Y}_d$	desired out-of-plane acceleration
$\ddot{\bar{Y}}_d$	desired derivative of the out-of-plane acceleration
$\bar{Y}_b$	unit vector along LM $Y$ -body axis
$\bar{Z}_b$	unit vector along LM $Z$ -body axis
$\bar{Z}_{bD}$	unit vector along range vector which commands desired pointing direction in $Z$ -axis steering
$\bar{Z}_{bX}$	actual $Z$ -body direction in inertial reference frame
$\bar{Z}_i$	navigation filter vector used in the intermediate computations
$[Z]$	matrix formed by the three $\bar{Z}_i$ vectors
$\alpha$	reciprocal of the semimajor axis in subroutine CONIC
$\bar{\alpha}^2$	navigation filter variance
$\alpha_E$	semimajor axis of CSM orbit
$\alpha_i$	semimajor axis of LM orbit
$\alpha_L$	desired semimajor axis of LM orbit after burn
$\alpha_N$	ratio of magnitude of initial position vector to semimajor axis
$\alpha_{TOL}$	tolerance on the phase angle convergence in COMDKI
$\beta_A$	actual RR shaft angle
$\beta_E$	estimated RR shaft angle



$\beta_M$	measured RR shaft angle
$\gamma$	a. flight-path angle in subroutine OUTPUT b. error in phase angle convergence in CFP c. intermediate variable in the W-matrix update routine DINCP2 d. inertial flight-path angle as measured from vertical in subroutine UNIVAR
$\gamma_0$	value of CFP phase angle convergence error on the previous iteration
$\Delta E_i$	difference in the final and initial eccentric anomalies in subroutine ELPRE
$\Delta H_{CDH}$	differential height at CDH
$\Delta H_D$	desired differential height at the second maneuver of the modified SOR logic
$\Delta H_{TPI}$	desired differential height at TPI
$\Delta h$	differential height
$\Delta h_D$	desired differential height at CDH
$\Delta h_{MAX}$	maximum differential height between two orbits
$\Delta h_{MIN}$	minimum differential height between two orbits
$\Delta M_i$	difference in the final and initial mean anomalies
$\Delta P$	change in P for next iteration in p-iterator portion of AGS
$\Delta R_M$	measured relative range
$\dot{\Delta R}_E$	estimated relative range rate
$\dot{\Delta R}_M$	measured relative range rate

$\Delta r$	difference in the radial distances of the CSM and LM at phase match at CDH
$\Delta r_1$	a. difference between the X-components of measured range and the computed range b. the difference between the measured range rate and the computed range rate
$\Delta T$	a. integration step size b. guidance cycle length
$\Delta T_B$	burn time for a maneuver
$\Delta T_{BI}$	half the burn time for a maneuver
$\Delta T_{BP}$	table of phase times for the thrust profile
$\Delta T_{BP}^*$	stored table of thrust profile phase times
$\Delta T_{BPA}^*$	equivalent to $\Delta T_{BP}^*$
$\Delta T_{BRAKE}$	first guess at the braking phase duration
$\Delta T_{BURN}$	time spent in a thrusting maneuver; includes ullage
$\Delta T'_{BURN}$	$\Delta T$ of the current thrust maneuver from ullage ignition to the current guidance cycle
$\Delta T_{BURN}^*$	$\Delta T$ between ullage ignition and main engine cutoff
$\Delta T_{CA}$	time tolerance used to define convergence of the closest approach iteration of TPASS
$\Delta T_{CL}$	desired maneuver line time bias from the apsidal crossing
$\Delta T_{ENG}$	thrust profile phase timer set in subroutine SPLIT and input to subroutine START
$\Delta T_{GO}$	incremental adjustment to $T_{GO}$ in the descent guidance logic
$\Delta T_{IG}$	incremental adjustment to the PDI calculation of the preignition phase

$\Delta T_{INT}$	integration step size
$\Delta T_{MARK}$	time increment between marks
$\Delta T_{MAX}$	maximum time step allowed in elevation angle search
$\Delta T_P$	$\Delta T$ of the current thrust phase
$\Delta T_{PASS}$	minimum acceptable $\Delta T$ of a CSM pass over a landmark
$\Delta T_{SAVE}$	table of $\Delta T$ 's of CSM passes over the landmark to be tracked
$\Delta T_{TAIL-OFF}$	duration of burn tail-off phase
$\Delta T_{TAIL-OFF}^*$	stored value for $\Delta T_{TAIL-OFF}$
$\Delta T_{TEST}$	minimum acceptable time between the optical tracking of two landmarks
$\Delta T_{TO}$	duration of burn tail-off phase
$\Delta T_{TOL}$	minimum time between the maneuver line threshold time and the initial maneuver line
$\Delta V$	magnitude of velocity vector increment
$\{\Delta V_k\}_{k=1}^N$	table of samples of total $\Delta V$ required for the mission profile
$\Delta V_{MAN}$	total $\Delta V$ of a maneuver
$\Delta V_{MIN}$	minimum $\Delta V$ required during a guidance cycle for the guidance to consider the engine to be burning
$\Delta V_{REF}$	reference value for the total $\Delta V$ required for the mission profile
$\Delta V_{TO}$	tail-off $\Delta V$
$\Delta V_{TOT}$	total $\Delta V$ of a maneuver

$\Delta V_{TOTAL}$	total $\Delta V$ of a maneuver
$\Delta V_1$	$\Delta V$ remaining to be burned by the main engine before cutoff
$\Delta X_A$	actual relative state vector
$\Delta X_E$	estimated relative state vector
$\Delta x$	a. step size in the computations of the cumulative distribution table of subroutine CDFUNC b. increment in the independent variable $x$ computed in REGFAL c. increment in the universal variable $x$ in subroutine CONIC
$\Delta Z$	increment in the general independent variable in subroutine ITRATE
$\Delta \Delta h$	maximum variation in the differential height between two orbits
$\Delta \alpha$	phase error at TPI in subroutine COMDKI
$\Delta \theta$	phase error at TPI in subroutine PMISS
$\overline{\Delta IG}$	integrated gravity acceleration vector per 2-second computer cycle
$\overline{\Delta Q}_S$	sum of sensed velocity increments $\overline{\Delta q}_p$
$\overline{\Delta q}_p$	sensed velocity increments
$\overline{\Delta q}_s$	identical with $\overline{\Delta Q}_s$
$\overline{\Delta R}$	vector increment to a radius vector
$\overline{\Delta R}_A$	actual relative position vector
$\overline{\Delta R}_E$	estimated relative position vector
$\overline{\Delta V}$	incremental velocity vector

$\Delta \bar{V}_A$	a. actual incremental velocity vector b. actual relative velocity vector
$\Delta \bar{V}_{AGS}$	incremental velocity sensed by the AGS accelerometers
$\Delta \bar{V}_B$	accelerometer $\Delta V$ read bias
$\Delta \bar{V}_{BR}$	incremental velocity vector in basic reference coordinates
$\Delta \bar{V}_{CDH}(LV)$	required CDH $\Delta V$ in local vertical coordinates
$\Delta \bar{V}_{CSI}(LV)$	required CSI $\Delta V$ in local vertical coordinates
$\Delta \bar{V}_E$	a. estimated incremental velocity vector b. estimated relative velocity vector
$\Delta \bar{V}_{EX}$	incremental velocity for an external $\Delta V$ maneuver
$\Delta \bar{V}(LV)$	incremental velocity in local vertical coordinates
$\Delta \bar{V}_{LV}$	equivalent to $\Delta \bar{V}(LV)$
$\Delta \bar{V}_{N1}$	the $\Delta \bar{V}$ of the first maneuver of a DKI sequence
$\Delta \bar{V}_{N2}$	the $\Delta \bar{V}$ of the second maneuver of a DKI sequence
$\Delta \bar{V}_{N3}$	the $\Delta \bar{V}$ of the third maneuver of a DKI sequence
$\Delta \bar{V}_P$	accelerometer sensed $\Delta \bar{V}$ in platform coordinates
$\Delta \bar{V}_{PGS}$	incremental velocity sensed by the PGNCS accelerometers
$\Delta \bar{V}_S$	sensed $\Delta V$ during a guidance cycle
$\Delta \bar{V}_{TPF}$	incremental velocity required for velocity match at rendezvous
$\Delta \bar{V}_u$	unit vector directed along $\Delta \bar{V}_{VEC}$

$\Delta \bar{V}_{VEC}$	incremental velocity targeted for a maneuver
$\Delta \bar{V}_1$	$\Delta V$ of the first maneuver in a maneuver sequence
$\Delta \bar{V}_2$	$\Delta V$ of the second maneuver in a maneuver sequence
$\Delta \bar{X}_3$	correction vector to a landmark position vector
$\delta$	minimum central angle between the radius vector of the spacecraft and that of a landmark
$\delta Q$	discrepancy between the measured value and estimated value of a tracking parameter
$\delta R$	measurement bias on range
$\delta R_{VHF}$	VHF measurement bias on range
$\dot{\delta R}$	measurement bias on range rate
$\delta \bar{R}_A$	error in the estimated relative range vector after a tracking mark has been incorporated
$\delta \bar{R}_B$	error in the estimated relative range vector before a tracking mark has been incorporated
$\delta \bar{R}_C$	correction to the estimated relative range vector
$\delta r$	a. stable orbit displacement distance b. difference in the CSM and LM radial distances at phase match at $t_{ig}$ in AGS
$\delta T$	a. time lag between the target vehicle and the desired chaser position at the time of the second maneuver of the stable orbit sequence b. guidance cycle increment in the burn simulation routine RUNGA c. general variable for a time step increment
$\delta T_{ABORT}$	time from powered descent ignition at which an abort is to occur

$\delta T_{INC}$	integration interval in the burn simulation routine RUNGA
$\delta T_{STAGE}$	maximum time from powered descent ignition at which staging is to occur
$\delta T_{START}$	time increment from the last event to the start of onboard tracking
$\delta T_{US}$	integration step size during ullage
$\delta T_4$	time increment remaining until the end of the current guidance cycle
$\delta U$	tolerance on U used in placing U in the proper quadrant in the AEG
$\delta V_X$	current iteration on the $N_{C1}$ maneuver in subroutine COMDKI
$\delta V_1$	previous iteration on the $N_{C1}$ maneuver in subroutine COMDKI
$\delta V_2$	current iteration on the $N_{C1}$ maneuver in subroutine COMDKI
$\delta X$	state vector dispersion
$\delta X_E$	dispersion of the estimated state vector from the actual state vector
$\{\delta X_k\}_{k=1}^N$	table of state vector dispersion in the subroutine SAMDIF
$\delta X_{LA}$	dispersions obtained from sampling the lunar ascent insertion matrix
$\delta X_{LSA}$	dispersion of the actual landing site off the reference landing site
$\delta X_{LSE}$	dispersion of the estimated landing site off the actual landing site
$\delta X_S$	sum of the entries in the table $\{\delta X_k\}_{k=1}^N$
$\delta_A$	maximum acceptable central angle between the radius vector of the spacecraft and that of a landmark which is to be tracked

$\delta_{SXT_x}, \delta_{SXT_y}, \delta_{SXT_z}$	angular bias error for each axis of the unit vector produced by sextant tracking
$\delta\alpha_1$	phase angle error on the previous $N_{Cl}$ iteration in subroutine COMDKI
$\delta\alpha_2$	phase angle error on the current $N_{Cl}$ iteration in subroutine COMDKI
$\delta\beta$	RR shaft angle measurement bias
$\delta\beta_E$	onboard navigation filter estimate of $\delta\beta$
$\delta\Delta X_E$	difference between $\Delta X_A$ in local vertical coordinates and $\Delta X_E$ in local vertical coordinates
$\delta\theta$	RR trunnion angle measurement bias
$\delta\theta_E$	onboard navigation filter estimate of $\delta\theta$
$\delta\mu_i$	sample mean of the differences between the reference value of the parameter $x$ and the sample values of $x$
$\delta_2$	staying flag in AGS
$\bar{\delta}$	position vector deviation from $\bar{R}_{CON}$ , which is the conic position vector in subroutine ENCKE
$\bar{\delta}^*$	saved value of $\bar{\delta}$
$\bar{\delta}_i$	equivalent to $\bar{\delta}$ indexed by vehicle number
$\bar{\delta}_S$	saved value of $\bar{\delta}$
$\delta\bar{V}_A$	error in the estimated relative velocity vector after a tracking mark has been incorporated
$\delta\bar{V}_B$	error in the estimated relative velocity vector before a tracking mark has been incorporated
$\delta\bar{V}_C$	correction to the estimated relative velocity vector



$\delta \bar{X}_i$	correction to the estimated state vector being updated
$\epsilon_x, \epsilon_y, \epsilon_z$	angular error for each axis of the unit vector produced by sextant tracking
$\epsilon_D$	desired elevation angle at TPI
$\epsilon_{ij}$	element of the $\epsilon$ -matrix which consists of the error angles for the accelerometer mounting
$\epsilon_{MIN}$	minimum acceptable tracking visibility angle from a landmark to an orbiting spacecraft
$\epsilon_T$	tracking attitude deadband
$\bar{n}$	random vector of variable dimension; the vector is generated in such a way that each component has a mean of zero and a standard deviation of 1
$\theta$	<ul style="list-style-type: none"> <li>a. phase angle</li> <li>b. true anomaly</li> <li>c. half the orbital arc traveled by the spacecraft while visible to a landmark (subroutine TPASS)</li> </ul>
$\theta_A$	actual RR trunnion angle
$\theta_{CANT}$	engine cant angle
$\theta_D$	desired phase angle at TPI
$\theta_f$	central angle between CSM and LM at $t_{ig}$ in CSI mode of AGS; at present in orbit insertion mode
$\theta_{INS}$	desired true anomaly at insertion
$\theta_{LOS}$	line-of-sight angle of CSM relative to the LM
$\theta_M$	measured RR trunnion angle
$\theta_T$	orbital arc traveled by the spacecraft during a burn

$\theta_{TPI}$	phase angle at TPI
$\theta_x, \theta_y, \theta_z$	platform misalignment angles
$\theta_{x,0}; \theta_{y,0}; \theta_{z,0}$	initial platform misalignment angles
$\dot{\theta}_x, \dot{\theta}_y, \dot{\theta}_z$	platform gyro drift rates
$\lambda$	a. longitude of the spacecraft b. longitude of a landmark
$\lambda_K$	longitude of the kth landmark
$\lambda_R$	longitude of the landmark for which visibility data are to be computed in subroutine TPASS
$\lambda_{R,0}$	input $\lambda_R$ in selenographic coordinates (subroutine TPASS)
$\mu$	a. gravitational constant of the central body b. mean of a random variable
$\mu_E$	gravitational constant of the earth
$\mu_i$	sample mean of the ith parameter table processed by subroutine SAMSIG
$\mu_R$	mean of the radius vector dispersions
$\mu_V$	mean of the velocity vector dispersions
$\mu_2$	iteration control counter in subroutine ELPRE
$\mu_3$	p-iteration control counter in AGS
$\mu_8$	ullage counter
$\bar{\mu}$	mean of a random vector
$\bar{v}$	deviation of the velocity vector from $\bar{v}_{CON}$ , which is the conic velocity vector of subroutine ENCKE

$\bar{v}_i$	vector $\bar{v}_i$ indexed by vehicle number
$\bar{v}^*$	same value as $\bar{v}$
$\rho_{ij}$	correlation coefficient for the $i$ th and $j$ th components of a state vector
$\Sigma$	covariance matrix
$\Sigma_A$	covariance matrix of actual state vector dispersions from the reference state vector
$\Sigma_{A,I}$	$\Sigma_A$ for the $i$ th vehicle
$\Sigma_{LA}$	covariance matrix that represents the dispersions of the actual and estimated states at insertion caused by powered ascent
$\Sigma_{LSA}$	covariance matrix that represents the dispersions of the actual landing site from the reference landing site
$\Sigma_{LSE}$	covariance matrix that represents dispersions of the estimated landing site off the actual landing site
$\Sigma_{r,c}$	the 6 by 6 matrix in the $r$ th row and $c$ th column of a square partitioning of a 12 by 12 covariance matrix
$\Sigma_{REL}$	covariance matrix of dispersions to the estimated relative state vector
$\Sigma_{R,K6}$	storage array for 6 by 6 tracking covariance matrices
$\Sigma_T$	a 12 by 12 covariance matrix of MSFN tracking uncertainties for two vehicles
$\Sigma_{T,K12}$	storage array for 12 by 12 tracking covariance matrices
$\sigma$	standard deviation

$\left. \begin{array}{l} \sigma_{\text{B}_{\text{SXT}_x}} \\ \sigma_{\text{B}_{\text{SXT}_y}} \\ \sigma_{\text{B}_{\text{SXT}_z}} \end{array} \right\}$	standard deviation of the angular bias in each axis of the unit vector produced by sextant tracking
$\sigma_{\text{B}_{\text{VHF}}}$	standard deviation of the VHF range measurement bias
$\sigma_{\text{AAL}}$	standard deviation of the angular accelerometer misalignment for each axis
$\sigma_{\text{ALN}}$	standard deviation of the initial platform misalignment angles for each axis
$\sigma_{\text{DFT}}$	standard deviation of the platform gyro drift rate for each axis
$\sigma_{\text{DVB}}$	standard deviation of the accelerometer read bias for each axis
$\sigma_{\text{F}}$	standard deviation of the thrust magnitude
$\sigma_{\text{I}}$	standard deviation of the specific impulse
$\sigma_i$	standard deviation of the $i$ th parameter of an array
$\sigma_{ij}$	element of the $i$ th row and $j$ th column of the covariance matrix $\Sigma$
$\sigma_{\text{N}_R}$	standard deviation of the RR noise on the range measurement
$\sigma_{\text{N}_R^{\cdot}}$	standard deviation of the RR noise on the range rate measurement
$\sigma_{\text{N}_\beta}$	standard deviation of the RR noise on the shaft angle measurement
$\sigma_{\text{N}_\Theta}$	standard deviation of the RR noise on the trunnion angle measurement
$\sigma_{\text{R}}$	standard deviation of the radius vector dispersions

$\left. \begin{array}{l} \sigma_{\text{SXT}_x} \\ \sigma_{\text{SXT}_y} \\ \sigma_{\text{SXT}_z} \end{array} \right\}$	standard deviation of the angle noise in each axis of the unit vector produced by sextant tracking
$\sigma_V$	standard deviation of the velocity vector dispersions
$\sigma_{\text{SR}}$	standard deviation of the bias in the RR range measurement
$\sigma_{\dot{\text{SR}}}$	standard deviation of the bias in the RR range rate measurement
$\sigma_{\delta\beta}$	standard deviation of the bias in the RR shaft angle measurement
$\sigma_{\delta\theta}$	standard deviation of the bias in the RR trunnion angle measurement
$\tau$	a. time since last rectification in ENCKE b. ratio of vehicle weight to weight flow in the LM ascent guidance logic
$\tau_G$	time increment, in LM descent guidance, during which velocity errors are to be damped out during the velocity-following mode
$\tau_S$	time increment to the termination of the current guidance phase in LM descent guidance
$\tau^*$	saved value of $\tau$ at insertion
$\phi$	latitude
$\phi_{\text{ASCENT}}$	powered flight arc of ascent
$\phi_{\text{CSM}}$	travel angle of the CSM during powered ascent
$\phi_D$	desired phase angle at insertion in a powered ascent
$\phi_K$	latitude of the kth landmark
$\phi_R$	latitude of the landmark for which visibility data are to be computed in subroutine TPASS

$\phi_{R,0}$	input $\phi_R$ in selenographic coordinates (subroutine TPASS)
$\phi_{TLO}$	desired phase angle at lift-off in a lunar ascent
$\psi$	heading angle from north
$\psi_P$	sine of LM pitch attitude
$\psi_Y$	sine of desired LM out-of-plane attitude
$\omega$	magnitude of the vector $\overline{\omega}_C$
$\omega_A$	mean motion of the passive vehicle
$\omega_E$	rotation rate of the earth about its polar axis
$\omega_{MOON}$	rotation rate of the moon about its polar axis
$\omega_P$	mean motion of the passive vehicle
$\omega_t$	target travel angle during a chaser two-impulse sequence
$\omega_I$	apsidal rotation rate of the active vehicle
$\overline{\omega}$	thrust turning rate vector
$\overline{\omega}_C$	commanded thrust turning rate vector
$\overline{\omega}_i$	Kalman filter weighting vector used in the onboard tracking routines
$\overline{\omega}_P$	angular rotation rate vector of the moon in spacecraft platform coordinates
$\overline{\omega}_{SC}$	angular rotation rate vector of the moon in selenocentric coordinates
$\overline{\omega}_{SG}$	angular rotation rate vector of the moon in selenographic coordinates

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